Birzeit University

Department of Mathematics

Quiz 8

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December 13, 2018

Number:.....

Q1 [10 points]. Consider the following integral

$$I = \int_{1}^{2} \int_{0}^{\sqrt{2x - x^{2}}} \frac{1}{(x^{2} + y^{2})^{2}} dy dx.$$

Convert the integral I into an equivalent polar integral. Then evaluate the polar integral.

$$0 \le y \le \sqrt{2x-x^2}$$
 $y = 0, y = \sqrt{2x-x^2}$
 $y = 0, y = \sqrt{2x-x^2}$
 $y = 0 + y^2 = 1$
 $y = 0 + y^2 = 0 + y^2 = 1$

$$I = \iint_{0}^{2 \cos \theta} \frac{1}{(\Upsilon^{2})^{2}} \cdot \Upsilon d\Upsilon d\theta$$

$$= \int_{8}^{\frac{\pi}{4}} \left[\frac{-1}{8} \sec^{2}\theta + \frac{1}{2} \left(\frac{1 + \cos^{2}\theta}{2} \right) \right] d\theta$$

$$= \left[\frac{1}{8} + \frac{1}{4} \left(0 + \frac{5 \ln 2\theta}{2}\right)\right] \frac{\pi}{4}$$

$$= \left[\frac{1}{8} + \frac{1}{4} \left(0 + \frac{5 \ln 2\theta}{2}\right)\right] \frac{\pi}{4}$$
Good Luck

Good Luck

$$= -\frac{1}{8}(1) + \frac{1}{4}(\frac{\pi}{4} + \frac{1}{2}) - 0 = \frac{\pi}{16}$$

$$y = \sqrt{2x - x}$$

$$x^2 + y^2 = 2x$$

$$\chi^2 = 2x$$

$$\chi^2 = 2\sqrt{\xi}$$

Birzeit University Department of Mathematics

Quiz 9

Math	2311	١
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December 13, 2018

Name:

Number:....

Q1 [10 points]. Let D be the region lies in the first octant bounded by the coordinate planes, the plane x + y = 4 and the cylinder $y^2 + 4z^2 = 16$. Write triple integral in the order dxdydz that give the volume of D. Evaluate the integral.

