# COMP2421—DATA STRUCTURES

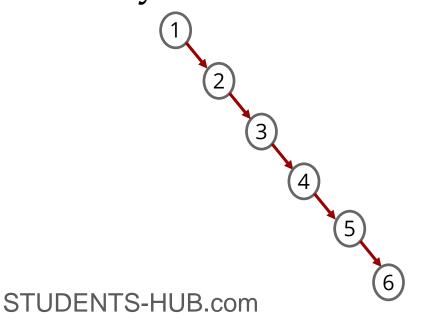
#### **AVL Trees**

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#### **AVL**

- AVL (Adelson-Velskii and Landis) tree is a binary search tree with additional balance property.
- It actually ensures that the depth of the tree is O(log n).
- Why do we need balance?



#### **AVL (2)**

- Height of the left subtree and height of the right subtree differ by at most 1.
- For a tree to be balanced, the value has to only be -1, 0, 1 at each node.
- Balance( tree ) = height of (tree.left) height of (tree.right) (height of the root's left branch and the height of the root's right branch).

#### **AVL (3)**

• This means that all elements in the tree can be ordered in some consistent manner.

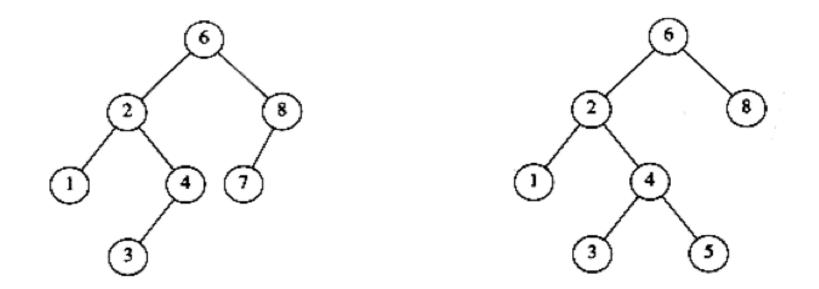


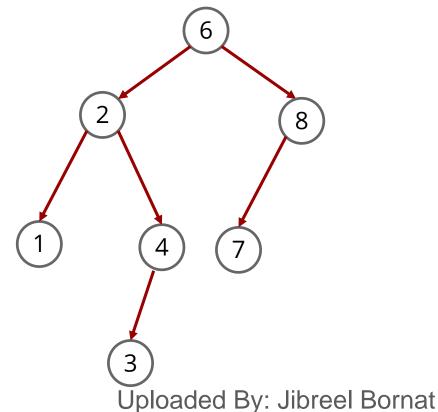
Figure 4.29 Two binary search trees. Only the left tree is AVL.

#### Rotations

- The balance of an AVL-tree is made via rotations.
- The algorithm: start at the node inserted and travel up the tree, updating the balance information at every node on the path.
- If we get to the root without having found any badly balanced nodes, then nothing to update.
- Otherwise, we do rotation at the first badly balanced node found, adjust the balance, and we are done.

• If the insertion causes some node in the AVL tree to lose balance, perform rotation at that node. In most cases, this is sufficient to rebalance the tree.

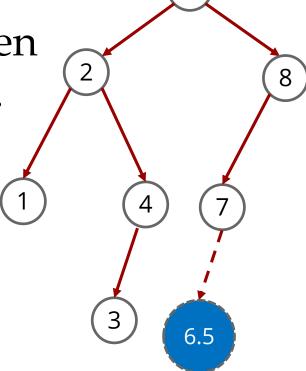
- There are two types of rotations
  - Single Rotation
  - Double Rotation
- Example: Insert the node 6.5 to the following tree



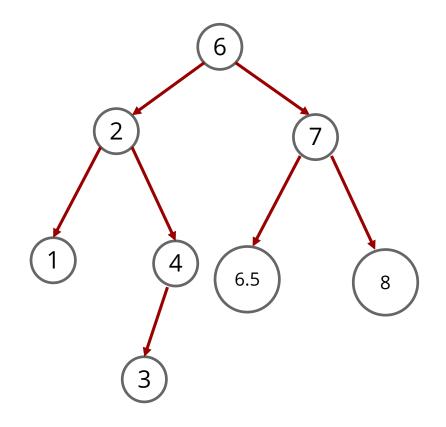
• After inserting 6.5, the original AVL tree on the

left, node 8 becomes unbalanced.

• Thus, we do a single rotation between 7 & 8 obtaining the tree on the right.



After rotation the tree becomes

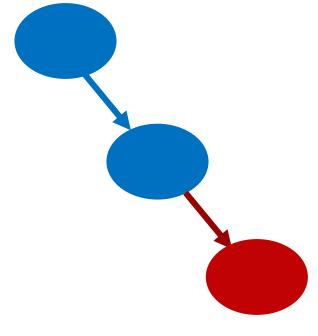


- To re-balance a tree there are 4 different situations:
- 1. insert into the left sub-tree of the left child (Right single rotation)

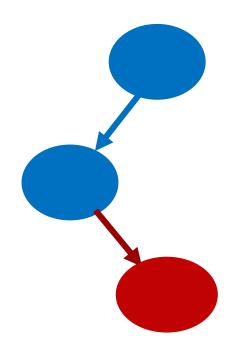
• To re-balance a tree there are 4 different situations:

2. insert into the right sub-tree of the right child (Left single

rotation)



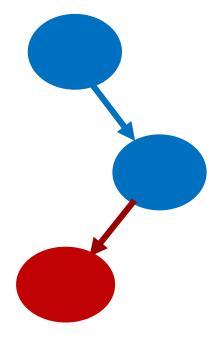
- To re-balance a tree there are 4 different situations:
- 3. insert into the right of the left sub-tree (LR double rotation)



• To re-balance a tree there are 4 different situations:

4. insert into the left of the right sub-tree (RL – double

rotation)



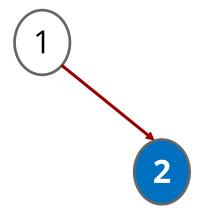
- Create an AVL tree and insert the values from 1 to 7.
- Insert( **1** )

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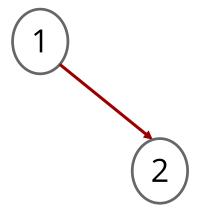
- Create an AVL tree and insert the values from 1 to 7.
- Insert( **2** )

1

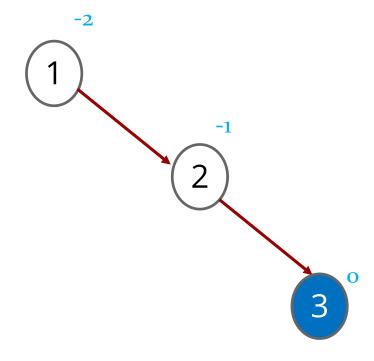
- Create an AVL tree and insert the values from 1 to 7.
- Insert( **2** )



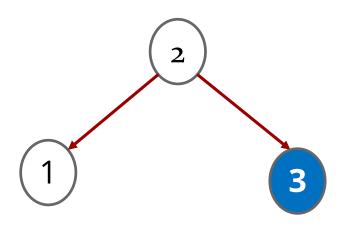
- Create an AVL tree and insert the values from 1 to 7.
- Insert( **3** )



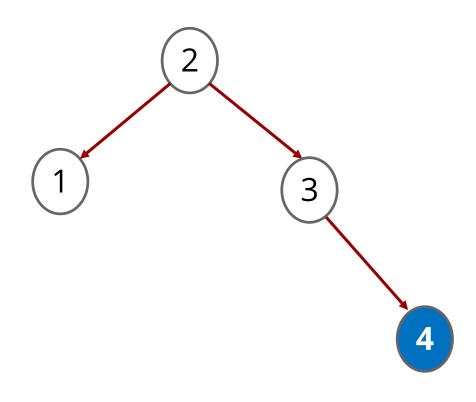
- Create an AVL tree and insert the values from 1 to 7.
- Insert( **3** )



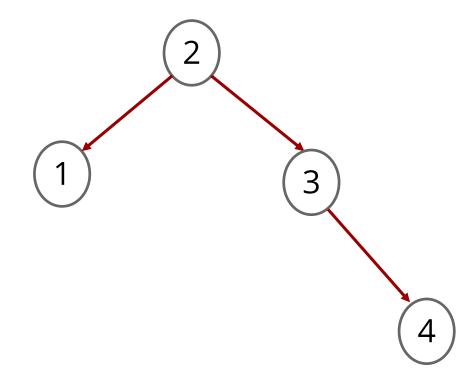
• Insert( **4** )



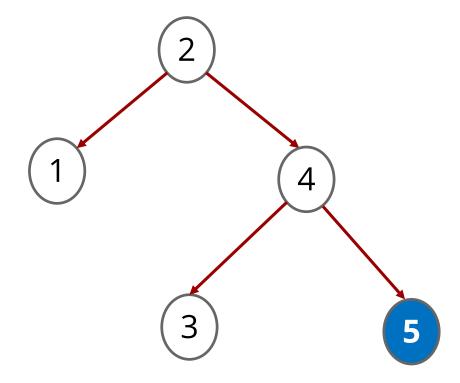
• Insert( **4** )



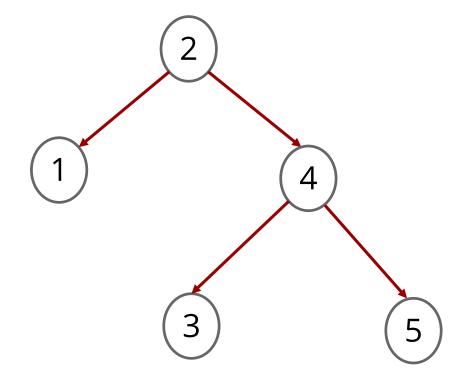
• Insert( **5** )

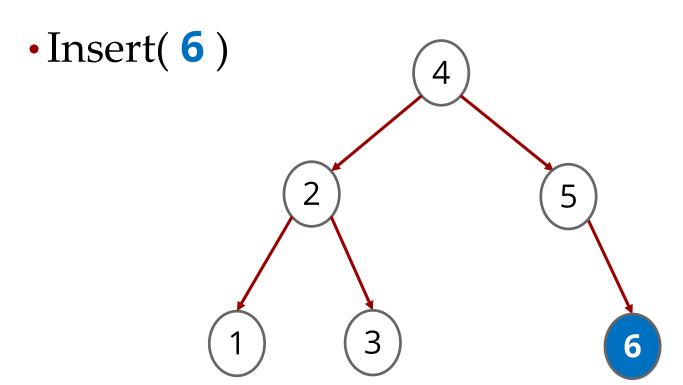


• Insert( **5** )



• Insert( **6** )

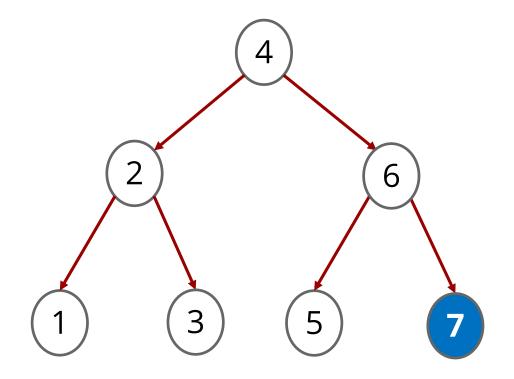




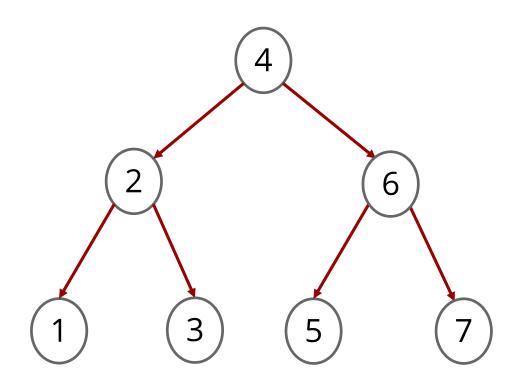
• Insert( **7** ) 4 5

• Insert( **7** ) 4 6

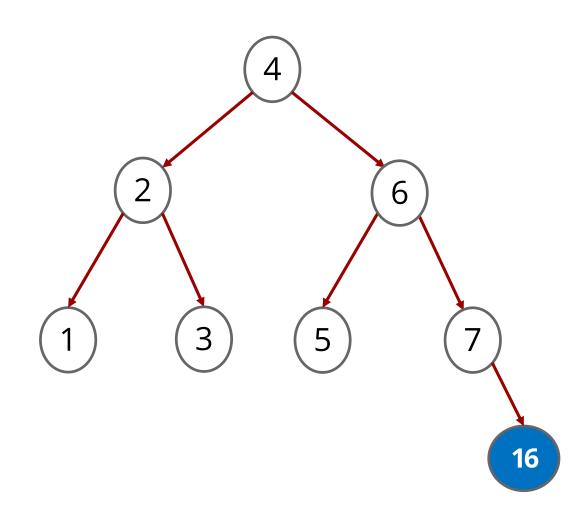
• Now insert the numbers 10 – 16 backward to the tree

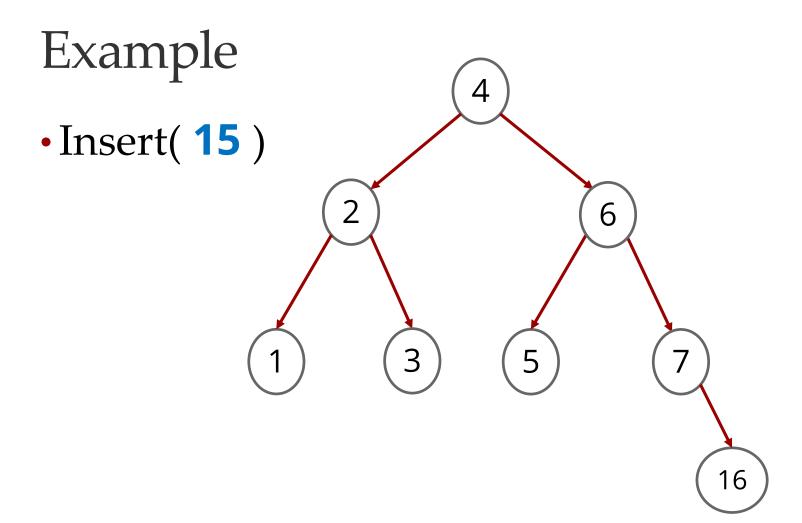


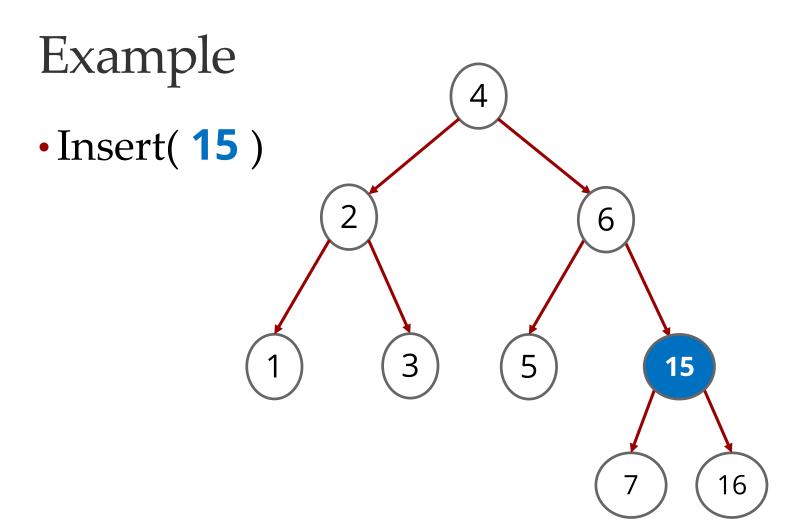
• Insert( **16** )

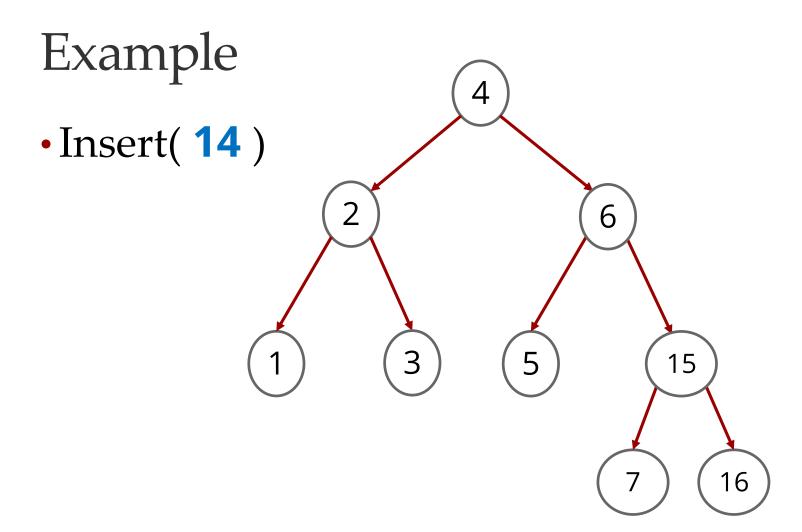


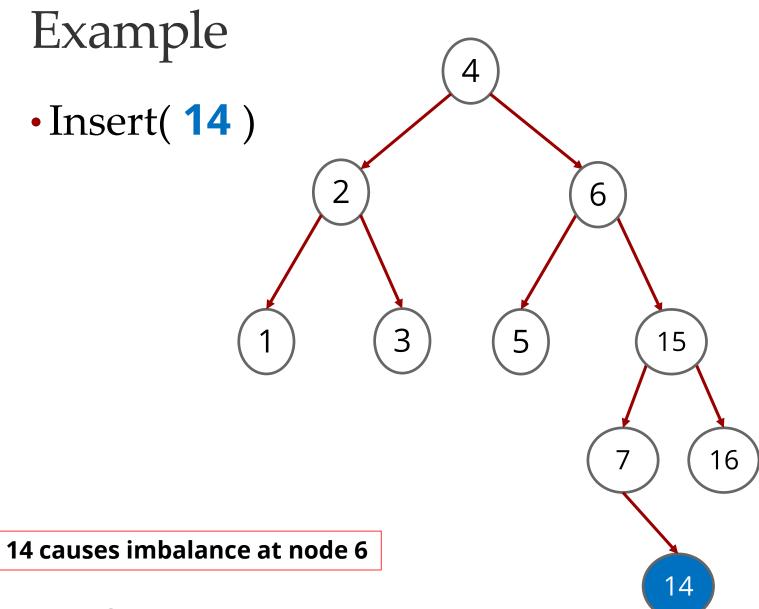
• Insert( **16** )

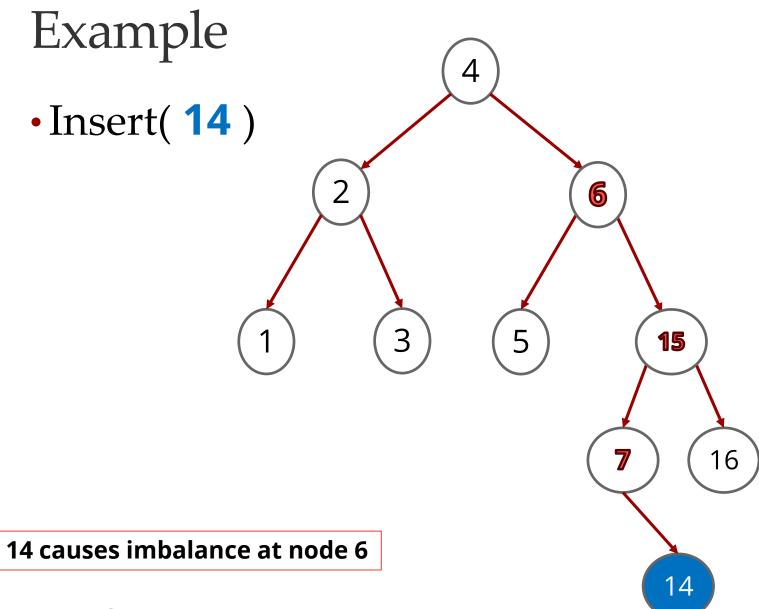


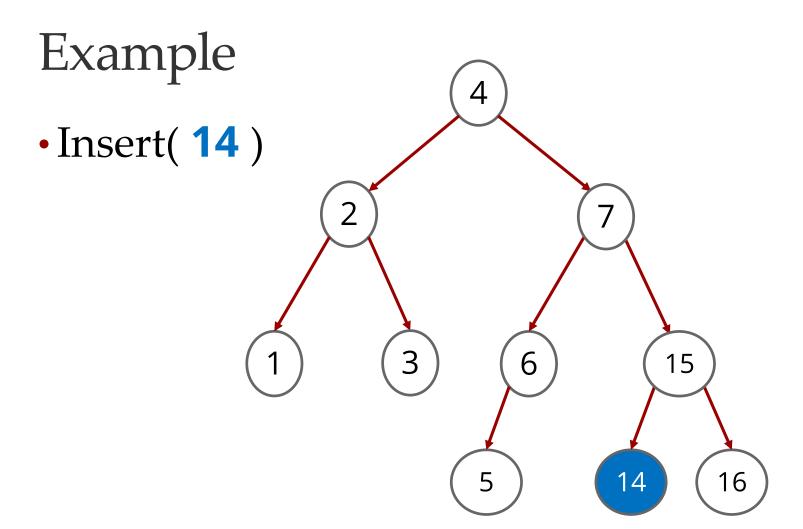


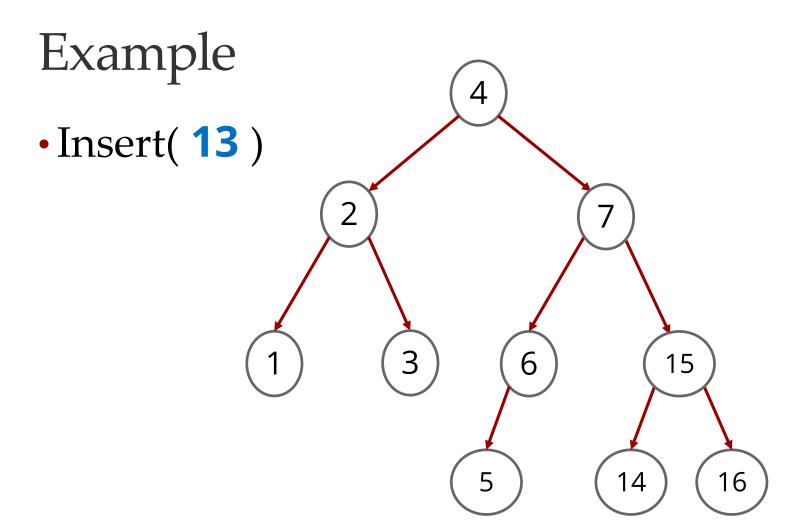


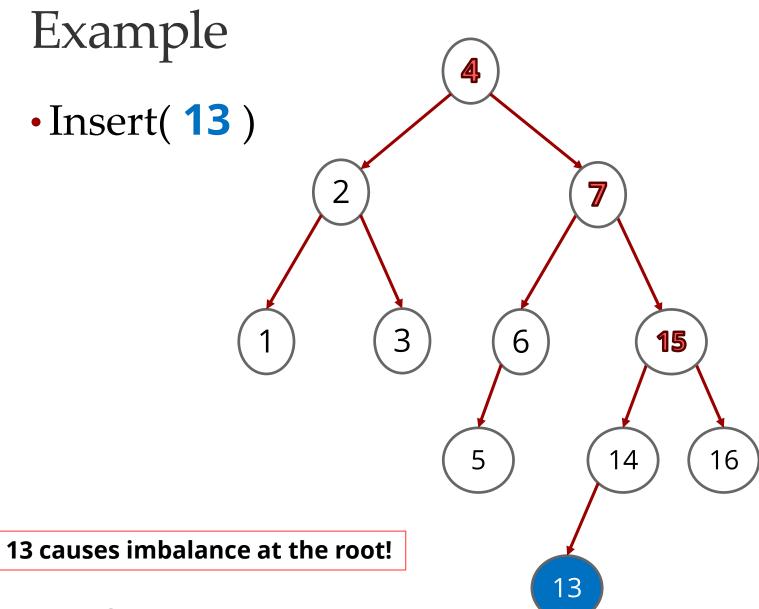


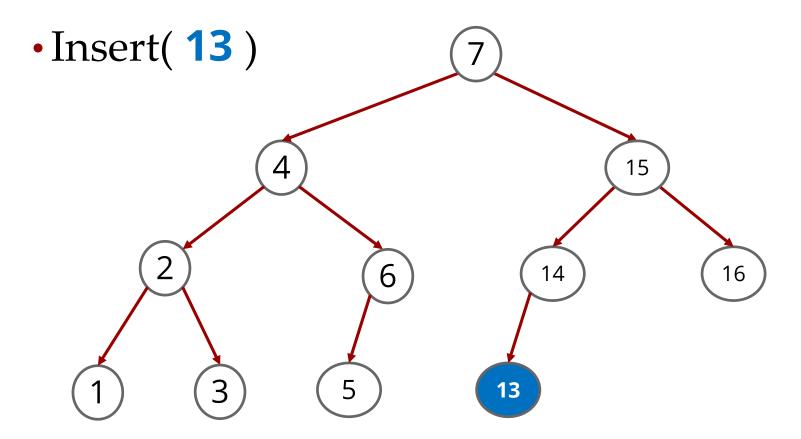


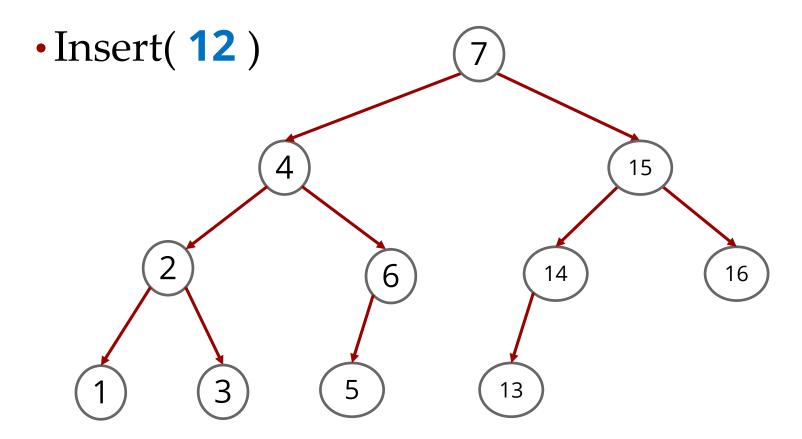


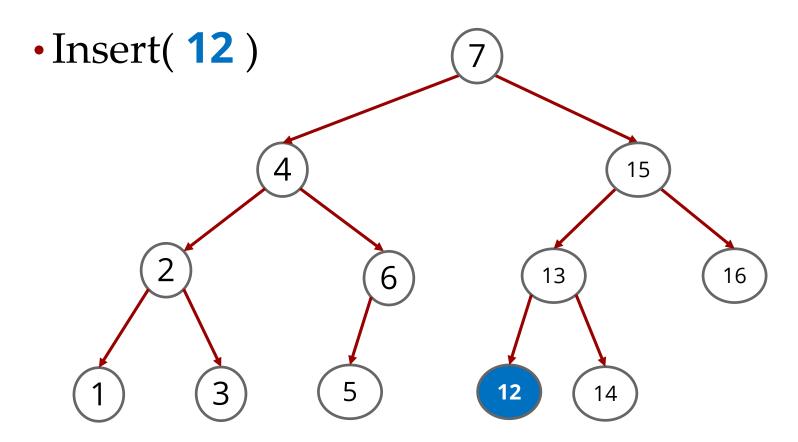


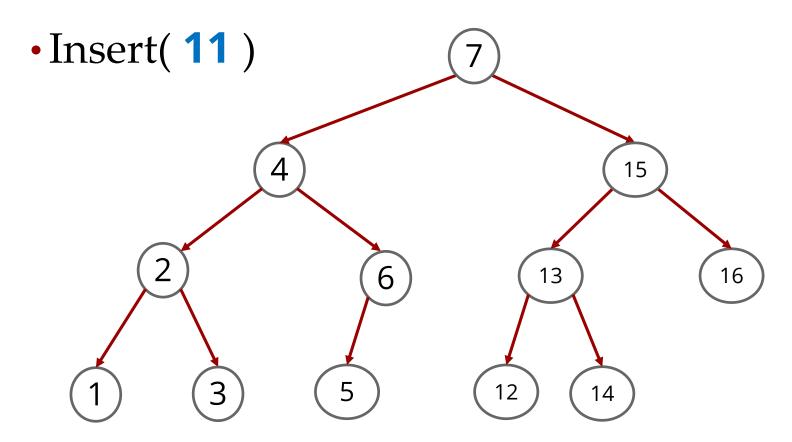


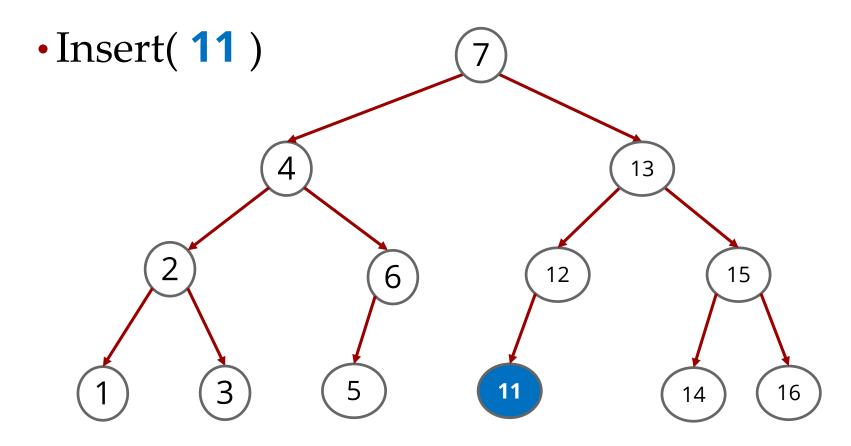


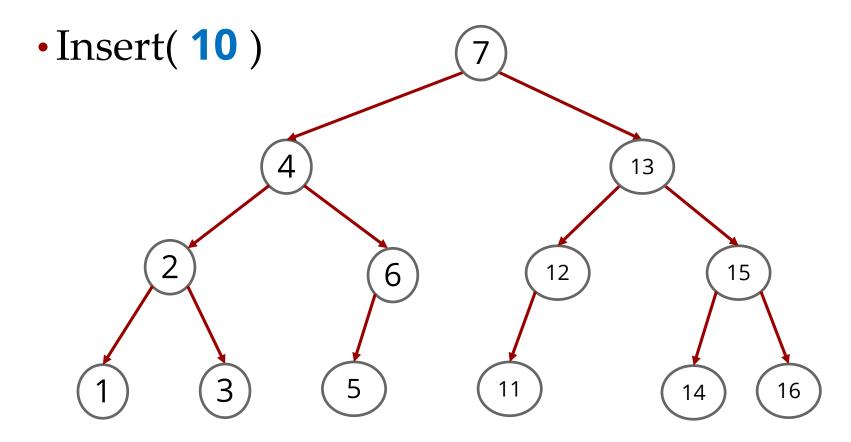


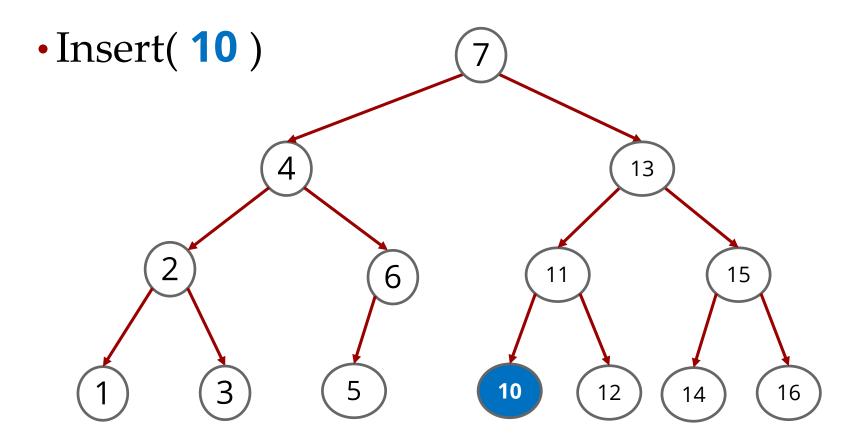


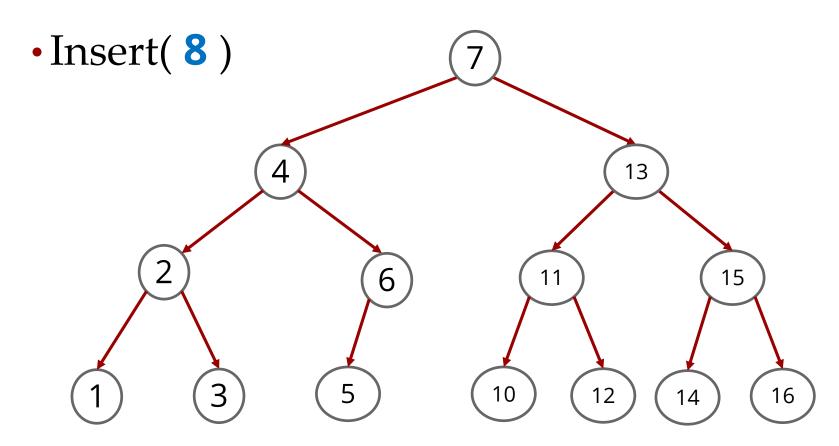


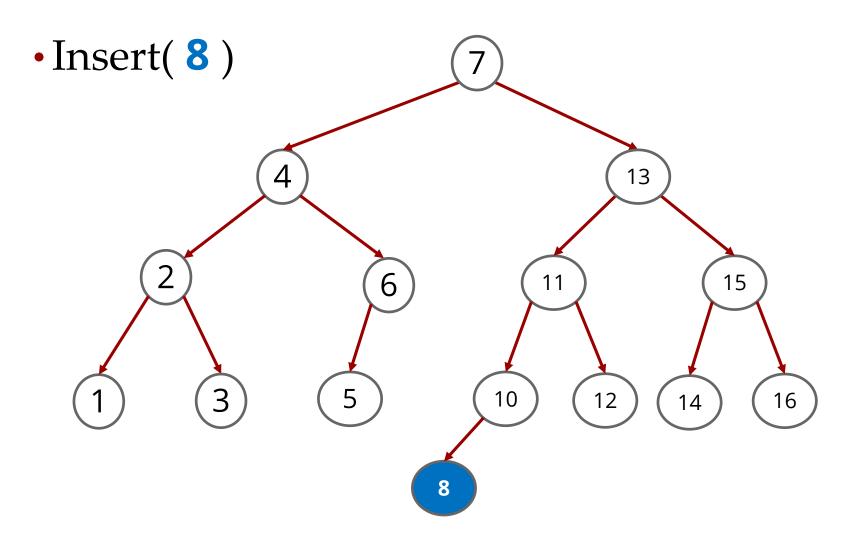


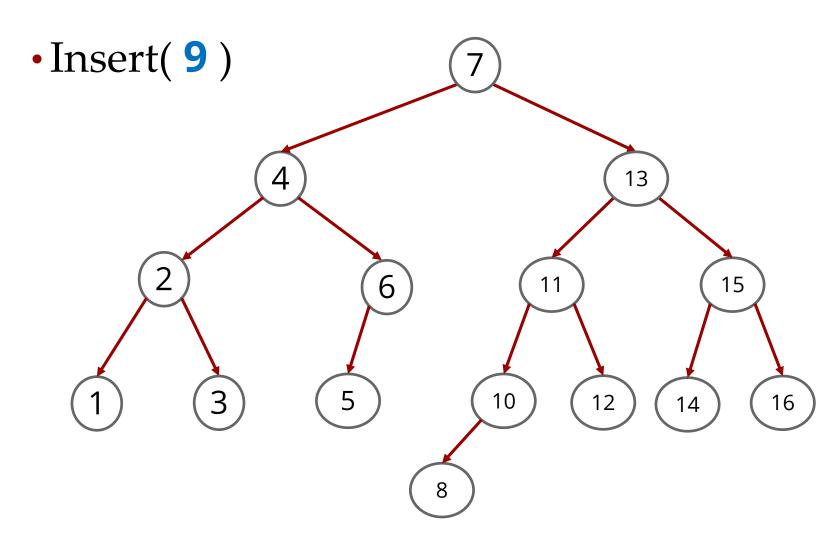


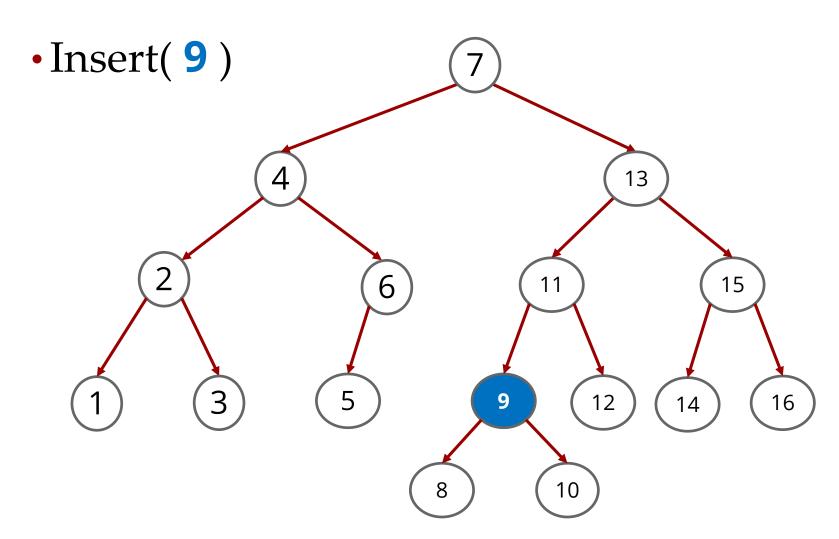












#### **AVL Tree Implementation**

- The main structure is the same as the BST
- Differs in adding the Rotations methods
  - SingleRotateWithLeft
  - SingleRotateWithRight
  - DoubleRotateWithRight
  - DoubleRotateWithLeft
- Code will be sent (the textbook author's implementation)

#### Applications of AVL Trees

- Used frequently for quick searching as it takes O(log n) because the tree is balanced
- Used in <u>Databases</u>
  - Intensive look-up applications where insertion & deletion are not that frequent but search for items is performed frequently
  - The large cost of rebalancing is a limitation!
- Used for in-memory collections such as sets and dictionaries