

### RC Filteres

\* Filteres: is an electrical circuit that allows signals with a defined frequency range to pass while blocking others with different frequency ranges.

\* Filters are useful units in many electrical and electronic devices such as radio, TV, etc

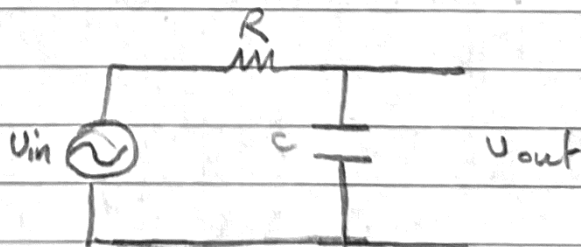
\* There are three typer of filters: high pass, low pass and band pass filters

\* Attenuation is the decrease in amplitude

\* In filters unwanted signals are highly attenuated through the circuit while required signals are passed with almost no attenuation.

#### ① Low-pass RC filter

\* The circuit equivalent impedance  $Z_{eq} = R + X_c$



$$\Rightarrow Z_{eq} = R - \frac{j}{\omega c}$$

$$I(t) = \frac{U_{in}(t)}{Z_{eq}} \Rightarrow I(t) = \frac{U_{in0} \cos(\omega t)}{R - j/\omega c}$$

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$$V_{out}(t) = V_c(t) = I(t) Z_c$$

$$= \frac{V_{in0} \cos(\omega t)}{R - \frac{j}{\omega C}} \times \frac{-j}{\omega C}$$

$$= \frac{V_{in0} \cos(\omega t)}{(R - \frac{j}{\omega C}) \frac{\omega C}{-j}}$$

$$= \frac{V_{in0} \cos(\omega t)}{j \times \frac{R\omega C}{-j} + 1}$$

$$\begin{aligned} \sqrt{-1} \times \sqrt{-1} \times -1 \\ = -1 \times -1 \\ = 1 \end{aligned}$$

$$V_{out}(t) = \frac{V_{in0} \cos(\omega t)}{1 + jR\omega C}$$

$$\Rightarrow V_c(t) = \frac{V_{in0} \cos(\omega t)}{1 + j\omega RC}$$

$$V_{co} = \frac{V_{in0}}{\sqrt{1 + \omega^2 C^2 R^2}}$$

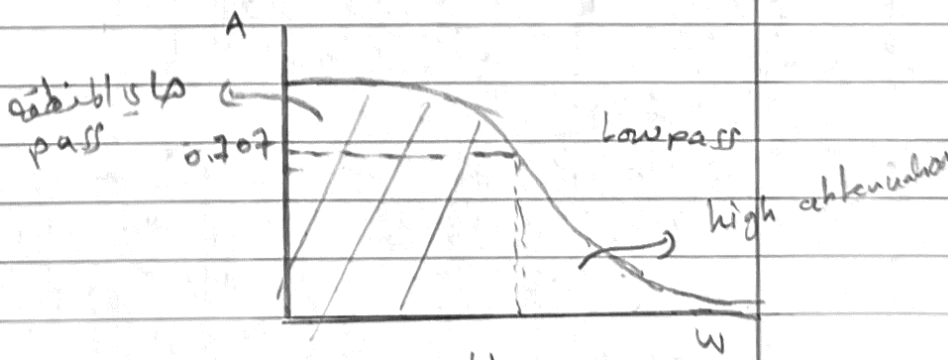
$V_{in0}$ : the amplitude of  $V_{in}(t)$  (input)

$V_{co}$ : the amplitude of  $V_c(t)$  (output)

\* The attenuation factor  $A = \frac{V_{co}}{V_{in0}} = \frac{1}{\sqrt{1 + \omega^2 C^2 R^2}}$

$$\omega_{-3dB} = \frac{1}{RC}$$

$$A = \frac{1}{\sqrt{1 + \left(\frac{\omega}{\omega_{-3dB}}\right)^2}}$$



③

low pass

$$\textcircled{1} \text{ if } \omega \ll \omega_{-3dB} \Rightarrow A = \frac{1}{\sqrt{1+0}} = 1 \Rightarrow \text{pass}$$

The amplitude of the output signal is equal to that of the input signal  $\Rightarrow$  in other word the signal passed without attenuation

$$\textcircled{2} \text{ if } \omega \gg \omega_{-3dB} \Rightarrow A = \frac{1}{\sqrt{1+\infty}} = 0 \Rightarrow \text{Attenuated}$$

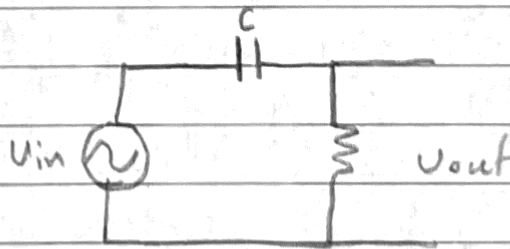
A is extremely small and the output signal is highly attenuated

$$\textcircled{3} \text{ if } \omega = \omega_{-3dB} \Rightarrow A = \frac{1}{\sqrt{1+1}} = \frac{1}{\sqrt{2}} = 0.707$$

The amplitude of the output signal is 0.707 of the amplitude of the input amplitude. This value set a practical boundary between passed signals and highly attenuated ones

### ⑧ High-pass RC filter

Using exactly the same procedure used in case A this lead to



$$A = \frac{V_{out} = IR}{1} \Rightarrow \left( A = \frac{R}{\sqrt{R^2 + X_C^2}} \right)$$

$$\sqrt{1 + \left( \frac{\omega_{-3dB}}{\omega} \right)^2}$$

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①  $\omega \ll \omega_{-3dB}$   $\Rightarrow A = \frac{1}{\sqrt{1+\infty}} = 0$  (Attenuated)

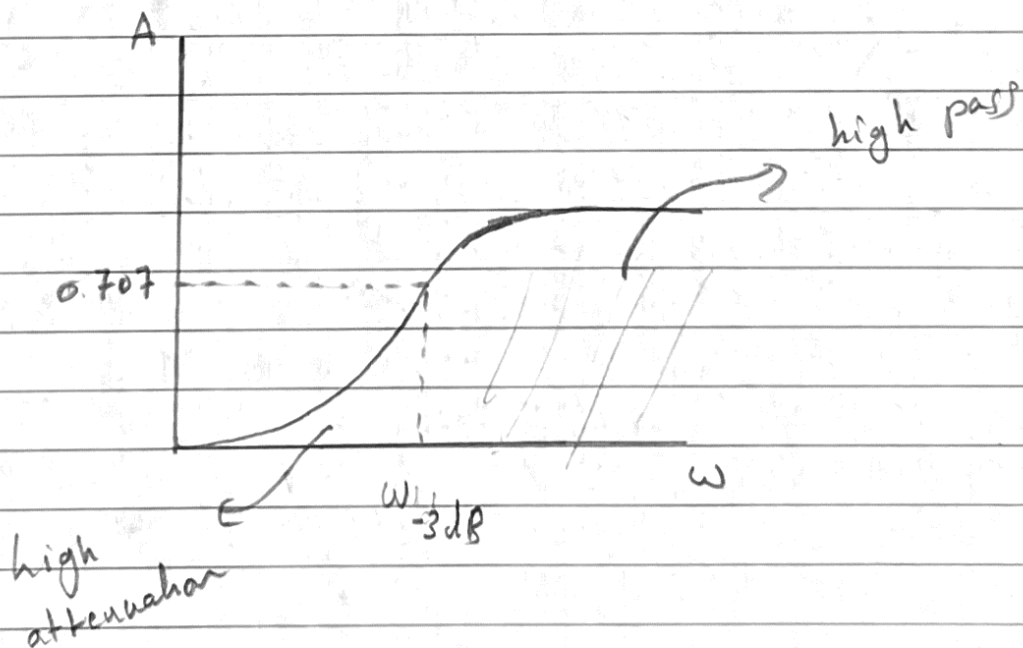
A is extremely small and the output signal is highly attenuated.

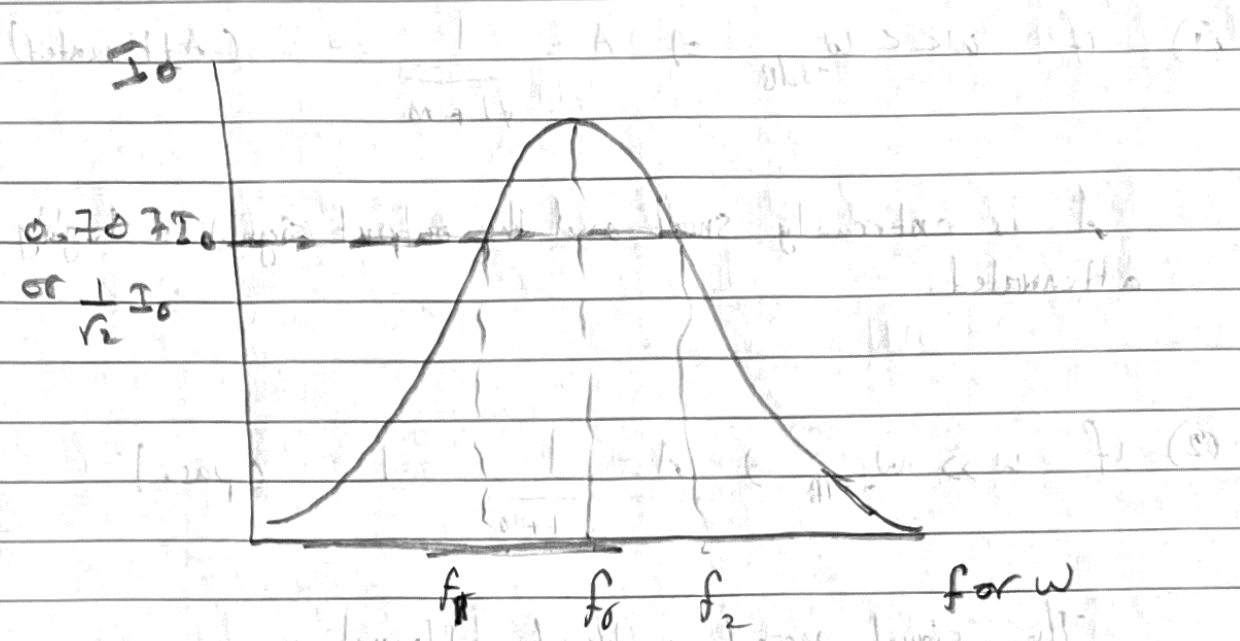
② if  $\omega \gg \omega_{-3dB} \Rightarrow A = \frac{1}{\sqrt{1+0}} = 1$  (pass)

The signal passed without attenuation

③ if  $\omega = \omega_{-3dB} \Rightarrow \frac{1}{\sqrt{1+1}} = \frac{1}{\sqrt{2}} = 0.707$

boundary between passed signals and highly attenuated ones.





band pass filter

# Differentiators and Integrators

## (A) Low pass filter

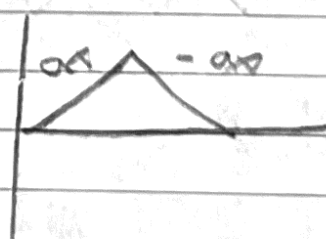
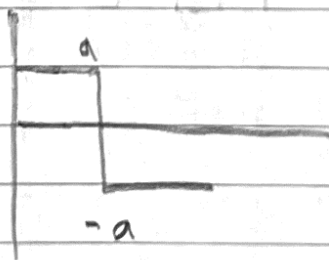
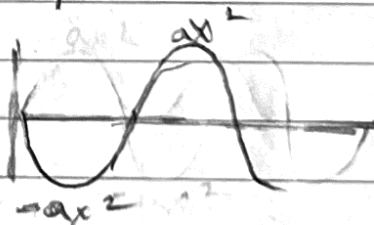
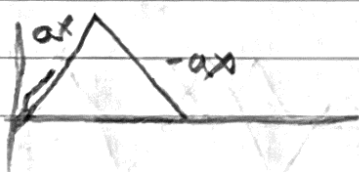
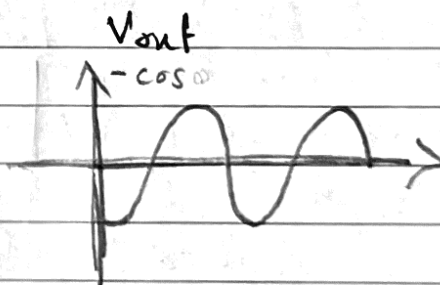
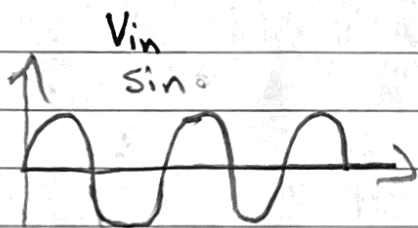
\* For  $\omega \gg \omega_{-3dB}$   $V_{out}(t)$  is extremely small

\* For  $\omega \gg \omega_{-3dB}$   $V_{in}(t) \approx V_R(t)$

\* For  $\omega \gg \omega_{-3dB}$  The output voltage is just the integral of input voltage ( $V_R$ )

$\Rightarrow$  under such conditions this circuit acts as an integrator

$\omega \gg \omega_{-3dB}$



Ⓑ High pass filter

\* For  $\omega \ll \omega_{-3dB}$   $V_{out}(t)$  is extremely small

\* For  $\omega \ll \omega_{-3dB}$   $V_{in}(t) \approx V_c(t)$

\* For  $\omega \gg \omega_{-3dB}$  The output voltage is just the derivative of the input voltage ( $V_c(t)$ )

⇒ under such conditions this circuit acts as a differentiator

