Chapter - 1

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System converting

① Binary to decimal ($2 \rightarrow 10$):-

Decimal value = $(d_{(n-1)} \times 2^{(n-1)}) + (d_{(n-2)} \times 2^{(n-2)}) + + (d_1 \times 2^1) + (d_0 \times 2^0)$

By Putting the onswers above of each bit

\bigcirc Decimal to Binary (10 \rightarrow 2):-

We make a table then divide by 2

Exp: Convert (157), to Binary

157	2	_	Inswer: (10011101),
78	1		
39	0		طريقة المل 8-
19	1		 نعمل جدول \$ 2 على الجيب والمرقم عهم البيار
9	1		د قالما کے دسما دلا ہ ک دلا ہما کی ھ
Ч	1		وی الیاد ہط النائج
2	0		 لا بصیر النالج عفر بوقف
ı	0		(و بلتب المجواب من تعت لفوق ا
0	1		•

(3) Anything to Decimal :-

(1) find the radix

Radix is the number of the system: Decimal _____ Radix = 10

Binary -> Radix = 2 Octal Radix = 8

Hexadecimal => Radix = 16

(2) Use this way to convert to decimal:

How to convert any system to decimal?

Decimal value = $(d_{(a-1)} \times r^{(a-1)}) + (d_{(a-2)} \times r^{(a-2)}) + + (d_1 \times r^2) + (d_0 \times r^2)$

* Since: r is the "radix"

n is the "bit number" d is the "number"

Exp: -

(11011) $_{\scriptscriptstyle 2} = (1+2^4) + (1\times 2^3) + (1\times 2^1) + (1\times 2^0) = 27$

(2107)₈ = $(2 \times 8^3) + (1 \times 8^2) + (7 \times 8^0) = 1095$

 $(B2)_{16} = (11 \times 16) + (2 \times 16^{0}) = 178$ STUDENTS-HUB.com Uploaded By: anonymous

① Decimal to Anything:— 1095 136

2

🛈 بعمل جدول ۴ عمى الجيب و الموقم عهماليلا حقالها کے دیں ادلا ہ ۳ دلا ہتا المن (۵)

 $2^{3} + 2^{2} + 1 + \frac{1}{2} + \frac{1}{16} = 13.5625$

 $16 \times 16^{2} + 2 \times 16 + 2 + 3 \times 16^{1} + 5 \times 16^{2} = 6088.1875$

(1101.1001)2=

 $(F22.35)_{16} =$

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لما بهیں النائج صفر ہو قفے

طريقة الحل 8-

Answer = 0.64

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0.8125 × 8 66

4.0

N x r

0.5 x 8

لحا أومل مض 🔿

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EXP:-

- ❖ Convert N = 0.6875 to Radix 2
- ❖ Solution: Multiply N by 2 repeatedly & collect integer bits

Multiplication	New Fraction	Bit	
0.6875 × 2 = 1.375	0.375	1 -	→ First fraction bit
$0.375 \times 2 = 0.75$	0.75	0	
0.75 × 2 = 1.5	0.5	1	
0.5 × 2 = 1.0	0.0	1 -	→ Last fraction bit

- ❖ Stop when new fraction = 0.0, or when enough fraction bits are obtained
- **.** Therefore, $N = 0.6875 = (0.1011)_2$

EXP:

- ❖ Convert *N* = 139.6875 to Octal (Radix 8)
- ❖ Solution: *N* = 139 + 0.6875 (split integer from fraction)
- The integer and fraction parts are converted separately

Division	Quotient	Remainder		
139 / 8	17	3		
17 / 8	2	1		
2/8	0	2		

Multiplication	New Fraction	Digit
$0.6875 \times 8 = 5.5$	0.5	5
$0.5 \times 8 = 4.0$	0.0	4

- **.** Therefore, $139 = (213)_8$ and $0.6875 = (0.54)_8$
- ❖ Now, join the integer and fraction parts with radix point

$$N = 139.6875 = (213.54)_8$$

Complement Numbers

الهدف: تبسيط عمليات الطرح وبعض العمليات المنطقية

N Complement :- "n-digits number" 10's complement: 1000 --- n times

9's complement: 9999 n times

8's complement: 8888 --- n times

N's complement: NNNN --- n times

The rule :-

Base - N Since &- Base : This One الوقم الذع نويو متممت : N

Examples:-1) 10's complement of 546700 = 1000000 - 546700 = 453300

- 2 10's complement of 012398 = 1000000 012398 = 987602
- ③ 9's complement of 546700 = 999999 546700 = 453299 49 9's complement of 012398 = 999999 - 012398 = 987601
- (5) 8's complement of 546700 = 888888- 546700 = 342188
- @ 8's complement of 012398 = 888888 0123980 = 87649 Qonymous

Examples:-

① Using 10's comp do 72532 - 3250 4

first: find the Comp of the negative number 10000 -3250 = 6750

Second: Add it to the first number 72532 + 6750 = 169282

finally: if there is Overflow we discard it and the answer is positive.

Final Answer = 69282

2 Using 10's comp do 3250 - 72532

100000 - 72532 = 27468

3250 + 27468 = 30,718 No overflow ==> Negative

Since it's negative !-

Answer = - (10's comp for 30718)

= - (100000 - 30718)

= - 69282

Convert 1 to 0 and 0 to 1 Example 11 011000 becomes 00100111 (3) 2's complement 1's complement + 1 Example 11 011000 becomes 15 Complement كويل الرقم إلى D 00100111 اكفاف 1 للناتج 00101000 اً في الأدقام تموس بعضها ا أجد Comp كالم المطووع (الاسب)) Example 🕹 ا جمعه ر ۱۱۱ تان غي زيادة يعني الرخم موجب Find 13-6 by 2's comp 300001101 (1) 000001101 - 00000110 2) Twos comp of 6 is 11111001 1)00000111 11111010 Corry => Positive Answer Ansyptoated By anothimouts STUDENTS-HUB.com

(2) 1's complement

Difference between carry and over flow

1) carry:-

Happen when we add / subtract un signed numbers their sum was out of range (dealing with 4-bit and the answer was 5-bit)

(2) overflow:-

Happen when dealing with signed numbers

- * When we add two positive integers the answer is negative
- * When we add two negative integers the answer is positive
- They are alike => NO overflow
- 00001111 15
- 00001000 11111000
- 00010111 00000111 Yes Corry, No overflow No Carry, No overslow
- They are different => Overflow (4) 3
- -38 01001111 10011101 -99 01000000 64
- -137 101110111 10001111 143 No Corry, Yes Overflow Yes Carry, Yes overflow

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How to know if the number is negative on positive?

I have to check it its signed (2's complement) or unsigned

Signed:-

1000 = -8 not 8, why?

When it says to me signed I have to look at the mostleft bit

if it's 1 → negative number حديد 1 => الما يلثى الاقم بـ 1 => الحديد الحا يبلش الاحم د 0 => موجب (= 0 عليه الاحم د الاحم د الاحم الاحم

Examples:-

	Signed	Unsigned
0011	3	3
1000	- 8	8
1001	-7	9
1100	-4	12
1111	-1	15
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```
1100 = -4
          1001 = -7
        +0101 = 5
                                   +0100 = 4
                                   10000 = 0
          1110 = -2
           (a) (-7) + (+5)
                                     (b) (-4) + (+4)
           Corry
                                Corrs
                                   1.1
         00
         0011 = 3
                                    1100 = -4
        +0100 = 4
                                   +11111 = -1
                                   11011 = -5
          0111 = 7
           (c)(+3)+(+4)
                                     (d)(-4)+(-1)
                                Corry, No overflow
      Comy
                                   10
        0 1
         0101 = 5
                                   1001 = -7
                                   +1010 = -6
        +0100 = 4
         1001 = Overflow
                                   10011 = Overflow
            (e) (+5) + (+4)
                                      (f)(-7) + (-6)
                                       0101 = 5
            0010 = 2
           +1001 = -7
                                      +1110 = -2
            1011 = -5
                                      10011 = 3
                               (b) M = 5 = 0101
    (a) M = 2 = 0010
        s = 7 = 0111
                                   s = 2 = 0010
                                  -s = 1110
       -s = 1001
            1011 = -5
                                       0101 = 5
           +1110 = -2
                                      +0010 = 2
           11001 = -7
                                       0111 = 7
    (c) M = -5 = 1011
                               (d) M = 5 = 0101
        s = 2 = 0010
                                   s = -2 = 1110
       -s = 1110
                                  -s = 0010
            0111 = 7
                                       1010 = -6
           +0111 = 7
                                      +1100 = -4
            1110 = Overflow
                                      10110 = Overflow
    (e) M = 7 = 0111
                               (f) M = -6 = 1010
STUDENTS HOBE
                                   s = 4 \overline{U}ploaded By: anonymous
                 0111
```

Minimum number of bits required

$$2^{n-1} < M < 2^n \implies M: The worked number$$

Example :-How many bits do you need to represent 10 decimal digits

Solution:
$$log^{10} = Answer => log^{10} = 4$$

$$Log^{10} = Answer \implies log_2^{10} = 4$$

$$\implies to represent 10 we need 2^4 Bit = 16$$

① To simplify conversions, decimal codes can be used

Decimal codes

- ② Define a binary code for each decimal digit
- 3 Since 10 decimal digits exit, a 4-bit code is used

Binary coded decimal (BCD)

BCD is a weighted code like binary (8, 4, 2, 1)

There are six invalid codes (1010, 1011, 1100, 1101, 1110, 1111)

Coding:

1310 = (0001 0011)BCD

30710= (0011 0000 0111)BCD

Conversion:

 $|3_{10} = (1101)_{2}$ 307,0= (100110011)2

BCD Arithmetic:-

(1) write the representation of each number

(2) add each digit with the digit below it

3 if the answer is more than "9" (Num > 9) add "1" carry in the next set of numbers

(4) after finishing, if the answer of the set is

STUDENTS-HUB.commore than "9", add 6 to it "0110" loaded By: anonymous

Example 1:-

Example 2:-





	Corny Because >	9
5789	0101 0111 1000 1001	
⁺ 3901	0011 1001 0000 0001	
Follow the colours	1001(10000) 1001(1010) Add 6 Because 7	9
to understand	0000 0110 0000 0110	
	1001 10110 1001 10000 Delete Any corry	

Find Answer :- 1001 0110 1001 0000 = 9690

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Gray Code

Used to detect if there is any error occurred during any process in the computer

From	binary	to	Gray	cod	e:-
	_				

(1) put the most left bit

(2) compare each digit with the digit beside it

Same (00, 11): put 0

Different (01, 10): put 1

Example 2:-Example 1:-

Convent 0 1) 12 to Gray code Convent 110010 to Gray code

Answer = 0 1 0 Answer = 101011

(1) put the most left bit ② compare each digit with the digit

next to its above

Example 2:-Convent 0/1000 to Binary Convent 1/0/1/0/1/13 to Binary

> Answer = 1/1 Uploaded By: anonymous

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Example 1:-

Always

Answer = (

From Gray code to binary:–

Binary Logic

$$\begin{array}{c|ccccc}
\hline
1 & AND & & & & & & & & \\
& & Z = X & and Y & & & & & \\
& & Z = X & Y & & & & & \\
& & Z = XY & & & & & \\
\end{array}$$

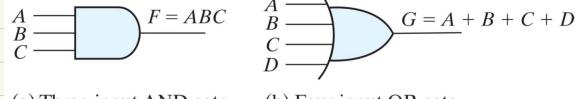
	Χ	Υ	Z=XY
	0	0	0
Y —	0	1	0
A Z	1	0	0
	1	1	1

2 OR		Χ	Υ	Z=X+Y
Z = X or Y		0	0	0
Z = X + Y	V	0	1	1
	$\frac{X}{Y}$ Z	1	0	1
		1	1	1

C UK				- 1	ムー 人士 I
Z = X or Y			0	0	0
Z = X + Y	v		0	1	1
	<u>X</u> Y	$\sum Z$	1	0	1
	1		1	1	1
③ NOT				Χ	Z=X′
$Z = \overline{X}$ or $Z = X$				0	1
				1	0
		X	>)-	Z	

Examples

$$x = 0 = 1 = 1 = 0 = 0$$
 $y = 0 = 0 = 1 = 1 = 0$
 $AND: x \cdot y = 0 = 0 = 1 = 0 = 0$
 $OR: x + y = 0 = 1 = 1 = 1 = 0$
 $NOT: x' = 1 = 0 = 0 = 1 = 1$



(a) Three-input AND gate (b) Four-input OR gate

YOURSELF

Believe

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