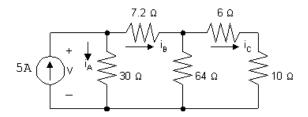
Simple Resistive Circuits

Assessment Problems

AP 3.1



Start from the right hand side of the circuit and make series and parallel combinations of the resistors until one equivalent resistor remains. Begin by combining the 6Ω resistor and the 10Ω resistor in series:

 $6\,\Omega + 10\,\Omega = 16\,\Omega$

Now combine this 16Ω resistor in parallel with the 64Ω resistor:

$$16\,\Omega \| 64\,\Omega = \frac{(16)(64)}{16+64} = \frac{1024}{80} = 12.8\,\Omega$$

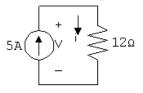
This equivalent 12.8Ω resistor is in series with the 7.2Ω resistor:

 $12.8\,\Omega+7.2\,\Omega=20\,\Omega$

Finally, this equivalent 20Ω resistor is in parallel with the 30Ω resistor:

$$20\,\Omega \| 30\,\Omega = \frac{(20)(30)}{20+30} = \frac{600}{50} = 12\,\Omega$$

Thus, the simplified circuit is as shown:



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[a] With the simplified circuit we can use Ohm's law to find the voltage across both the current source and the 12Ω equivalent resistor:

 $v = (12 \Omega)(5 A) = 60 V$

[b] Now that we know the value of the voltage drop across the current source, we can use the formula p = -vi to find the power associated with the source:

p = -(60 V)(5 A) = -300 W

Thus, the source delivers 300 W of power to the circuit.

[c] We now can return to the original circuit, shown in the first figure. In this circuit, v = 60 V, as calculated in part (a). This is also the voltage drop across the 30 Ω resistor, so we can use Ohm's law to calculate the current through this resistor:

$$i_A = \frac{60 \text{ V}}{30 \Omega} = 2 \text{ A}$$

Now write a KCL equation at the upper left node to find the current i_B :

$$-5 \text{ A} + i_A + i_B = 0$$
 so $i_B = 5 \text{ A} - i_A = 5 \text{ A} - 2 \text{ A} = 3 \text{ A}$

Next, write a KVL equation around the outer loop of the circuit, using Ohm's law to express the voltage drop across the resistors in terms of the current through the resistors:

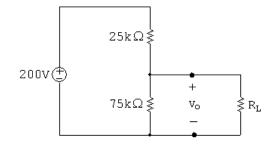
$$-v + 7.2i_B + 6i_C + 10i_C = 0$$

So $16i_C = v - 7.2i_B = 60 \text{ V} - (7.2)(3) = 38.4 \text{ V}$
Thus $i_C = \frac{38.4}{16} = 2.4 \text{ A}$

Now that we have the current through the 10Ω resistor we can use the formula $p = Ri^2$ to find the power:

$$p_{10\Omega} = (10)(2.4)^2 = 57.6 \text{ W}$$

AP 3.2



[a] We can use voltage division to calculate the voltage v_o across the 75 k Ω resistor:

$$v_o(\text{no load}) = \frac{75,000}{75,000 + 25,000}(200 \text{ V}) = 150 \text{ V}$$

[b] When we have a load resistance of 150 k Ω then the voltage v_o is across the parallel combination of the 75 k Ω resistor and the 150 k Ω resistor. First, calculate the equivalent resistance of the parallel combination:

75 k
$$\Omega \| 150 \ k\Omega = \frac{(75,000)(150,000)}{75,000 + 150,000} = 50,000 \ \Omega = 50 \ k\Omega$$

Now use voltage division to find v_o across this equivalent resistance:

$$v_o = \frac{50,000}{50,000 + 25,000} (200 \text{ V}) = 133.3 \text{ V}$$

[c] If the load terminals are short-circuited, the 75 k Ω resistor is effectively removed from the circuit, leaving only the voltage source and the 25 k Ω resistor. We can calculate the current in the resistor using Ohm's law:

$$i = \frac{200 \text{ V}}{25 \text{ k}\Omega} = 8 \text{ mA}$$

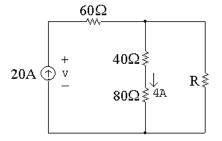
Now we can use the formula $p = Ri^2$ to find the power dissipated in the 25 k Ω resistor:

$$p_{25k} = (25,000)(0.008)^2 = 1.6 \text{ W}$$

[d] The power dissipated in the 75 k Ω resistor will be maximum at no load since v_o is maximum. In part (a) we determined that the no-load voltage is 150 V, so be can use the formula $p = v^2/R$ to calculate the power:

$$p_{75k}(\max) = \frac{(150)^2}{75,000} = 0.3 \text{ W}$$

AP 3.3



[a] We will write a current division equation for the current throught the 80Ω resistor and use this equation to solve for R:

$$i_{80\Omega} = \frac{R}{R + 40\,\Omega + 80\,\Omega} (20 \text{ A}) = 4 \text{ A}$$
 so $20R = 4(R + 120)$
Thus $16R = 480$ and $R = \frac{480}{16} = 30\,\Omega$

STU transference Education, Inc., Upper Saddle River, NJ. All rights reserved. This publication is protected by Copyright and written permission should be obtained transference prior any productive reproduction, storage in a retrieval system, or transmission in any form or by any hears dectronic mechanical protocopying Ornat recording, or likewise. For information regarding permission(s), write to: Rights and Permissions Department, Pearson Education, Inc., Upper Saddle River, NJ 07458. [b] With $R = 30 \Omega$ we can calculate the current through R using current division, and then use this current to find the power dissipated by R, using the formula $p = Ri^2$:

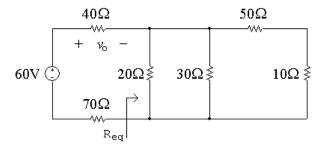
$$i_R = \frac{40 + 80}{40 + 80 + 30} (20 \text{ A}) = 16 \text{ A}$$
 so $p_R = (30)(16)^2 = 7680 \text{ W}$

[c] Write a KVL equation around the outer loop to solve for the voltage v, and then use the formula p = -vi to calculate the power delivered by the current source:

 $-v + (60 \Omega)(20 A) + (30 \Omega)(16 A) = 0 \quad \text{so} \quad v = 1200 + 480 = 1680 V$ Thus, $p_{\text{source}} = -(1680 V)(20 A) = -33,600 W$

Thus, the current source generates 33,600 W of power.





[a] First we need to determine the equivalent resistance to the right of the 40Ω and 70Ω resistors:

$$R_{\rm eq} = 20\,\Omega \|30\,\Omega\| (50\,\Omega + 10\,\Omega) \qquad \text{so} \qquad \frac{1}{R_{\rm eq}} = \frac{1}{20\,\Omega} + \frac{1}{30\,\Omega} + \frac{1}{60\,\Omega} = \frac{1}{10\,\Omega}$$

Thus, $R_{\rm eq} = 10\,\Omega$

Now we can use voltage division to find the voltage v_o :

$$v_o = \frac{40}{40 + 10 + 70} (60 \text{ V}) = 20 \text{ V}$$

[b] The current through the 40Ω resistor can be found using Ohm's law:

$$i_{40\Omega} = \frac{v_o}{40} = \frac{20 \text{ V}}{40 \Omega} = 0.5 \text{ A}$$

This current flows from left to right through the $40 \,\Omega$ resistor. To use current division, we need to find the equivalent resistance of the two parallel branches containing the $20 \,\Omega$ resistor and the $50 \,\Omega$ and $10 \,\Omega$ resistors:

$$20\,\Omega \| (50\,\Omega + 10\,\Omega) = \frac{(20)(60)}{20 + 60} = 15\,\Omega$$

Now we use current division to find the current in the 30Ω branch:

$$i_{30\Omega} = \frac{15}{15+30}(0.5 \text{ A}) = 0.16667 \text{ A} = 166.67 \text{ mA}$$

[c] We can find the power dissipated by the 50Ω resistor if we can find the current in this resistor. We can use current division to find this current from the current in the 40Ω resistor, but first we need to calculate the equivalent resistance of the 20Ω branch and the 30Ω branch:

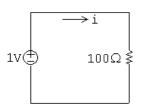
$$20\,\Omega \| 30\,\Omega = \frac{(20)(30)}{20+30} = 12\,\Omega$$

Current division gives:

$$i_{50\Omega} = \frac{12}{12 + 50 + 10} (0.5 \text{ A}) = 0.08333 \text{ A}$$

Thus, $p_{50\Omega} = (50)(0.08333)^2 = 0.34722 \text{ W} = 347.22 \text{ mW}$

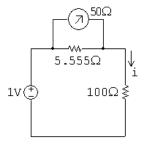
AP 3.5 [a]



We can find the current i using Ohm's law:

$$i = \frac{1 \text{ V}}{100 \Omega} = 0.01 \text{ A} = 10 \text{ mA}$$

[b]

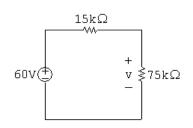


 $R_m = 50\,\Omega \| 5.555\,\Omega = 5\,\Omega$

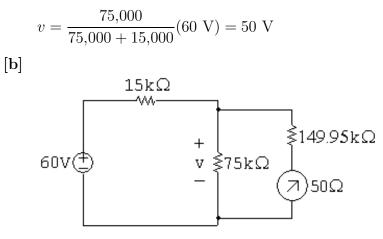
We can use the meter resistance to find the current using Ohm's law:

$$i_{\text{meas}} = \frac{1 \text{ V}}{100 \Omega + 5 \Omega} = 0.009524 = 9.524 \text{ mA}$$

AP 3.6 [a]



Use voltage division to find the voltage v:



The meter resistance is a series combination of resistances:

 $R_m = 149,950 + 50 = 150,000\,\Omega$

We can use voltage division to find v, but first we must calculate the equivalent resistance of the parallel combination of the 75 k Ω resistor and the voltmeter:

$$75,000 \,\Omega \| 150,000 \,\Omega = \frac{(75,000)(150,000)}{75,000 + 150,000} = 50 \,\mathrm{k\Omega}$$

Thus,
$$v_{\text{meas}} = \frac{50,000}{50,000 + 15,000} (60 \text{ V}) = 46.15 \text{ V}$$

AP 3.7 [a] Using the condition for a balanced bridge, the products of the opposite resistors must be equal. Therefore,

$$100R_x = (1000)(150)$$
 so $R_x = \frac{(1000)(150)}{100} = 1500 \,\Omega = 1.5 \,\mathrm{k\Omega}$

[b] When the bridge is balanced, there is no current flowing through the meter, so the meter acts like an open circuit. This places the following branches in parallel: The branch with the voltage source, the branch with the series combination R_1 and R_3 and the branch with the series combination of R_2 and R_x . We can find the current in the latter two branches using Ohm's law:

$$i_{R_1,R_3} = \frac{5 \text{ V}}{100 \Omega + 150 \Omega} = 20 \text{ mA};$$
 $i_{R_2,R_x} = \frac{5 \text{ V}}{1000 + 1500} = 2 \text{ mA}$

We can calculate the power dissipated by each resistor using the formula $p = Ri^2$:

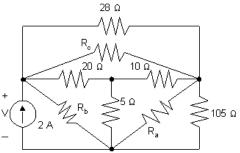
 $p_{100\Omega} = (100 \,\Omega)(0.02 \,\mathrm{A})^2 = 40 \,\mathrm{mW}$

$$p_{150\Omega} = (150 \,\Omega)(0.02 \,\mathrm{A})^2 = 60 \,\mathrm{mW}$$

 $p_{1000\Omega} = (1000 \,\Omega)(0.002 \,\text{A})^2 = 4 \,\text{mW}$ $p_{1500\Omega} = (1500 \,\Omega)(0.002 \,\text{A})^2 = 6 \,\text{mW}$

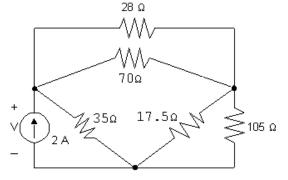
Since none of the power dissipation values exceeds 250 mW, the bridge can be left in the balanced state without exceeding the power-dissipating capacity of the resistors.

AP 3.8 Convert the three Y-connected resistors, 20Ω , 10Ω , and 5Ω to three Δ -connected resistors $R_{\rm a}, R_{\rm b}$, and $R_{\rm c}$. To assist you the figure below has both the Y-connected resistors and the Δ -connected resistors



$$R_{\rm a} = \frac{(5)(10) + (5)(20) + (10)(20)}{20} = 17.5\,\Omega$$
$$R_{\rm b} = \frac{(5)(10) + (5)(20) + (10)(20)}{10} = 35\,\Omega$$
$$R_{\rm c} = \frac{(5)(10) + (5)(20) + (10)(20)}{5} = 70\,\Omega$$

The circuit with these new Δ -connected resistors is shown below:



From this circuit we see that the 70 Ω resistor is parallel to the 28 Ω resistor:

$$70\,\Omega \|28\,\Omega = \frac{(70)(28)}{70+28} = 20\,\Omega$$

Also, the 17.5Ω resistor is parallel to the 105Ω resistor:

$$17.5\,\Omega \| 105\,\Omega = \frac{(17.5)(105)}{17.5+105} = 15\,\Omega$$

Once the parallel combinations are made, we can see that the equivalent 20Ω resistor is in series with the equivalent 15Ω resistor, giving an equivalent resistance of $20 \Omega + 15 \Omega = 35 \Omega$. Finally, this equivalent 35Ω resistor is in parallel with the other 35Ω resistor:

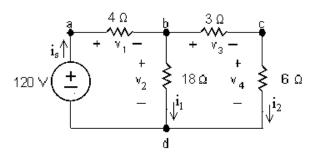
$$35\,\Omega \| 35\,\Omega = \frac{(35)(35)}{35+35} = 17.5\,\Omega$$

Thus, the resistance seen by the 2 A source is 17.5Ω , and the voltage can be calculated using Ohm's law:

 $v = (17.5 \,\Omega)(2 \,\mathrm{A}) = 35 \,\mathrm{V}$

Problems

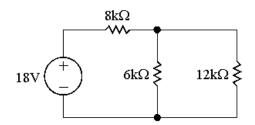
P 3.1 [a] From Ex. 3-1: $i_1 = 4$ A, $i_2 = 8$ A, $i_s = 12$ A at node b: -12 + 4 + 8 = 0, at node d: 12 - 4 - 8 = 0



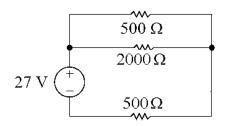
- [b] $v_1 = 4i_s = 48 \text{ V}$ $v_3 = 3i_2 = 24 \text{ V}$ $v_2 = 18i_1 = 72 \text{ V}$ $v_4 = 6i_2 = 48 \text{ V}$ loop abda: -120 + 48 + 72 = 0, loop bcdb: -72 + 24 + 48 = 0, loop abcda: -120 + 48 + 24 + 48 = 0
- P 3.2 [a] $p_{4\Omega} = i_s^2 4 = (12)^2 4 = 576 \text{ W}$ $p_{18\Omega} = (4)^2 18 = 288 \text{ W}$ $p_{3\Omega} = (8)^2 3 = 192 \text{ W}$ $p_{6\Omega} = (8)^2 6 = 384 \text{ W}$
 - [b] p_{120V} (delivered) = $120i_s = 120(12) = 1440$ W

$$[\mathbf{c}] p_{\text{diss}} = 576 + 288 + 192 + 384 = 1440 \text{ W}$$

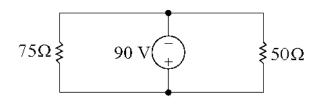
P 3.3 [a] The 5 k Ω and 7 k Ω resistors are in series. The simplified circuit is shown below:



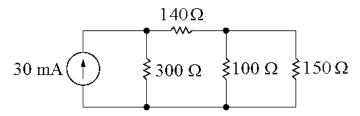
[b] The 800Ω and 1200Ω resistors are in series, as are the 300Ω and 200Ω resistors. The simplified circuit is shown below:



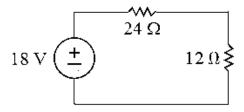
[c] The 35Ω , 15Ω , and 25Ω resistors are in series. as are the 10Ω and 40Ω resistors. The simplified circuit is shown below:



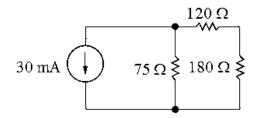
[d] The 50 Ω and 90 Ω resistors are in series, as are the 80 Ω and 70 Ω resistors. The simplified circuit is shown below:



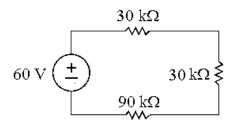
P 3.4 [a] The 36 Ω and 18 Ω resistors are in parallel. The simplified circuit is shown below:



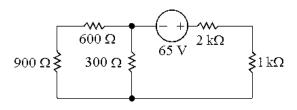
[b] The 200 Ω and 120 Ω resistors are in parallel, as are the 210 Ω and 280 Ω resistors. The simplified circuit is shown below:



[c] The 100 k Ω , 150 k Ω , and 60 k Ω resistors are in parallel, as are the 75 k Ω and 50 k Ω resistors. The simplified circuit is shown below:



[d] The 750Ω and 500Ω resistors are in parallel, as are the 1.5 k Ω and 3 k Ω resistors. The simplified circuit is shown below:



- P 3.5 Always work from the side of the circuit furthest from the source. Remember that the current in all series-connected circuits is the same, and that the voltage drop across all parallel-connected resistors is the same.
 - [a] Circuit in Fig. P3.3(a):

 $R_{\rm eq} = [(7000 + 5000) \| 6000] + 8000 = 12,000 \| 6000 + 8000$

 $= 4000 + 8000 = 12 \ \mathrm{k}\Omega$

Circuit in Fig. P3.3(b):

$$R_{\rm eq} = [500||(800 + 1200)] + 300 + 200 = (500||2000) + 300 + 200$$
$$= 400 + 300 + 200 = 900 \,\Omega$$

Circuit in Fig. P3.3(c):

 $R_{\rm eq} = (35 + 15 + 25) \| (10 + 40) = 75 \| 50 = 30 \,\Omega$

Circuit in Fig. P3.3(d):

$$R_{eq} = ([(70+80)||100] + 50 + 90)||300 = [(150||100) + 50 + 90]||300$$
$$= (60+50+90)||300 = 200||300 = 120 \Omega$$

[b] Note that in every case, the power delivered by the source must equal the power absorbed by the equivalent resistance in the circuit. For the circuit in Fig. P3.3(a):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{18^2}{12,000} = 0.027 = 27 \text{ mW}$$

For the circuit in Fig. P3.3(b):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{27^2}{900} = 0.81 = 810 \text{ mW}$$

For the circuit in Fig. P3.3(c):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{90^2}{30} = 270 \ {\rm W}$$

For the circuit in Fig. P3.3(d):

$$P = I_s^2(R_{eq}) = (0.03)^2(120) = 0.108 = 108 \text{ mW}$$

- P 3.6 Always work from the side of the circuit furthest from the source. Remember that the current in all series-connected circuits is the same, and that the voltage drop across all parallel-connected resistors is the same.
 - [a] Circuit in Fig. P3.4(a):

 $R_{\rm eq} = (36||18) + 24 = 12 + 24 = 36\,\Omega$

Circuit in Fig. P3.4(b):

 $R_{\rm eq} = 200 ||120||[(210||280) + 180] = 200 ||120||(120 + 180) = 200 ||120||300 = 60 \,\Omega$ Circuit in Fig. P3.4(c):

 $R_{\rm eq} = (75 \text{ k} \| 50 \text{ k}) + (100 \text{ k} \| 150 \text{ k} \| 60 \text{ k}) + 90 \text{ k} = 30 \text{ k} + 30 \text{ k} + 90 \text{ k} = 150 \text{ k}\Omega$

Circuit in Fig. P3.4(d):

$$R_{eq} = [(600 + 900) ||750||500] + (1500 ||3000) + 2000 = (1500 ||750||500) + 1000 + 2000$$
$$= 250 + 1000 + 2000 = 3250 = 3.25 \text{ k}\Omega$$

[b] Note that in every case, the power delivered by the source must equal the power absorbed by the equivalent resistance in the circuit. For the circuit in Fig. P3.4(a):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{18^2}{36} = 9 \ {\rm W}$$

For the circuit in Fig. P3.4(b):

$$P = I_s^2(R_{eq}) = (0.03)^2(60) = 0.054 = 54 \text{ mW}$$

For the circuit in Fig. P3.4(c):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{60^2}{150,000} = 0.024 = 24 \text{ mW}$$

For the circuit in Fig. P3.4(d):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{65^2}{3250} = 1.3 \text{ W}$$

P 3.7 [a] Circuit in Fig. P3.7(a):

$$R_{eq} = ([(15||60) + (30||45) + 20]||50) + 25 + 10 = [(12 + 18 + 20)||50] + 25 + 10$$
$$= (50||50) + 25 + 10 = 25 + 25 + 10 = 60 \Omega$$

Circuit in Fig. P3.7(b) – begin by simplifying the 75Ω resistor and all resistors to its right:

$$[(18+12)\|60+30]\|75 = (30\|60+30)\|75 = (20+30)\|75 = 50\|75 = 30 \Omega$$

Now simplify the remainder of the circuit:

$$R_{eq} = ([(30+20)||50] + (20||60))||40 = [(50||50) + 15]||40 = (25+15)||40$$
$$= 40||40 = 20 \Omega$$

Circuit in Fig. P3.7(c) – begin by simplifying the left and right sides of the circuit:

$$R_{\text{left}} = [(1800 + 1200) \| 2000] + 300 = (3000 \| 2000) + 300 = 1200 + 300 = 1500 \Omega$$
$$R_{\text{right}} = [(500 + 2500) \| 1000] + 750 = (3000 \| 1000) + 750 = 750 + 750 = 1500 \Omega$$
Now find the equivalent resistance seen by the source:

$$R_{\rm eq} = (R_{\rm left} || R_{\rm right}) + 250 + 3000 = (1500 || 1500) + 250 + 3000$$
$$= 750 + 250 + 3000 = 4000 = 4 \ \mathrm{k}\Omega$$

Circuit in Fig. P3.7(d):

$$R_{eq} = ([(750 + 250)||1000] + 100)||([(150 + 600)||500] + 300)$$

= [(1000||1000) + 100]||[(750||500) + 300] = (500 + 100)||(300 + 300)
= 600||600 = 300 \Omega

[b] Note that in every case, the power delivered by the source must equal the power absorbed by the equivalent resistance in the circuit. For the circuit in Fig. P3.7(a):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{30^2}{60} = 15 \ {\rm W}$$

For the circuit in Fig. P3.7(b):

$$P = I_s^2(R_{eq}) = (0.08)^2(20) = 0.128 = 128 \text{ mW}$$

For the circuit in Fig. P3.7(c):

$$P = \frac{V_s^2}{R_{\rm eq}} = \frac{20^2}{4000} = 0.1 = 100 \text{ mW}$$

For the circuit in Fig. P3.7(d):

$$P = I_s^2(R_{eq}) = (0.05)^2(300) = 0.75 = 750 \text{ mW}$$

- P 3.8 [a] $R_{ab} = 24 + (90\|60) + 12 = 24 + 36 + 12 = 72 \Omega$ [b] $R_{ab} = [(4 \text{ k} + 6 \text{ k} + 2 \text{ k})\|8 \text{ k}] + 5.2 \text{ k} = (12 \text{ k}\|8 \text{ k}) + 5.2 \text{ k} = 4.8 \text{ k} + 5.2 \text{ k} = 10 \text{ k}\Omega$ [c] $R_{ab} = 1200\|720\|(320 + 480) = 1200\|720\|800 = 288 \Omega$
- P 3.9 Write an expression for the resistors in series and parallel from the right side of the circuit to the left. Then simplify the resulting expression from left to right to find the equivalent resistance.
 - [a] $R_{ab} = [(26+10)||18+6]||36 = (36||18+6)||36 = (12+6)||36 = 18||36 = 12\Omega$

[b]
$$R_{\rm ab} = [(12+18)||10||15||20+16]||30+4+14 = (30||10||15||20+16)||30+4+14$$

 $= (4+16)||30+4+14 = 20||30+4+14 = 12+4+14 = 30\,\Omega$

[c] $R_{\rm ab} = (500 \| 1500 \| 750 + 250) \| 2000 + 1000 = (250 + 250) \| 2000 + 1000$

$$= 500 \|2000 + 1000 = 400 + 1000 = 1400 \,\Omega$$

[d] Note that the wire on the far right of the circuit effectively removes the 60Ω resistor!

$$R_{ab} = [([(30 + 18)||16 + 28]||40 + 20)||24 + 25 + 10]||50$$

= ([(48||16 + 28)||40 + 20]||24 + 25 + 10)||50
= ([(12 + 28)||40 + 20]||24 + 25 + 10)||50 = [(40||40 + 20)||24 + 25 + 10]||50
= [(20 + 20)||24 + 25 + 10]||50 = (40||24 + 25 + 10)||50 = (15 + 25 + 10)||50
= 50||50 = 25 \Omega

P 3.10 [a] R + R = 2R

- $[\mathbf{b}] \ R + R + R + \dots + R = nR$
- [c] R + R = 2R = 3000 so R = 1500 = 1.5 k Ω This is a resistor from Appendix H.
- [d] nR = 4000; so if n = 4, R = 1 k Ω This is a resistor from Appendix H.

P 3.11 [a]
$$R_{eq} = R ||R = \frac{R^2}{2R} = \frac{R}{2}$$

[b] $R_{eq} = R ||R||R|| \cdots ||R$ (*n R's*)
 $= R ||\frac{R}{n-1}$
 $= \frac{R^2/(n-1)}{R+R/(n-1)} = \frac{R^2}{nR} = \frac{R}{n}$
[c] $\frac{R}{2} = 5000$ so $R = 10$ k Ω
This is a resistor from Appendix H.

[d]
$$\frac{R}{n} = 4000$$
 so $R = 4000n$
If $n = 3$ $r = 4000(3) = 12 \text{ k}\Omega$
This is a resistor from Appendix H. So put three 12k resistors in parallel
to get $4k\Omega$.

P 3.12 [a]
$$v_o = \frac{160(3300)}{(4700 + 3300)} = 66 \text{ V}$$

[b] $i = 160/8000 = 20 \text{ mA}$
 $P_{R_1} = (400 \times 10^{-6})(4.7 \times 10^3) = 1.88 \text{ W}$
 $P_{R_2} = (400 \times 10^{-6})(3.3 \times 10^3) = 1.32 \text{ W}$

[c] Since R_1 and R_2 carry the same current and $R_1 > R_2$ to satisfy the voltage requirement, first pick R_1 to meet the 0.5 W specification

 Ω

$$i_{R_1} = \frac{160 - 66}{R_1}$$
, Therefore, $\left(\frac{94}{R_1}\right)^2 R_1 \le 0.5$
Thus, $R_1 \ge \frac{94^2}{0.5}$ or $R_1 \ge 17,672 \,\Omega$

Now use the voltage specification:

$$\frac{R_2}{R_2 + 17,672}(160) = 66$$

Thus, $R_2 = 12,408 \,\Omega$

P 3.13
$$4 = \frac{20R_2}{R_2 + 40}$$
 so $R_2 = 10 \Omega$
 $3 = \frac{20R_e}{40 + R_e}$ so $R_e = \frac{120}{17} \Omega$
Thus, $\frac{120}{17} = \frac{10R_L}{10 + R_L}$ so $R_L = 24$
P 3.14 [a] $v_o = \frac{40R_2}{R_c + R_c} = 8$ so $R_1 = 4R_2$

$$\begin{aligned} \|\mathbf{R}\| &= \|\mathbf{R}\| + R_2 &= \mathbf{C} &= \mathbf{S} \mathbf{C} &= \mathbf{R}_1 + \mathbf{R}_2 \\ \text{Let } &R_{\text{e}} = R_2 \|R_{\text{L}} = \frac{R_2 R_{\text{L}}}{R_2 + R_{\text{L}}} \\ &v_o = \frac{40 R_{\text{e}}}{R_1 + R_{\text{e}}} = 7.5 \quad \text{so} \quad R_1 = 4.33 R_{\text{e}} \\ \text{Then, } &4R_2 = 4.33 R_{\text{e}} = \frac{4.33(3600 R_2)}{3600 + R_2} \\ \text{Thus, } &R_2 = 300 \,\Omega \quad \text{and} \quad R_1 = 4(300) = 1200 \,\Omega \end{aligned}$$

[b] The resistor that must dissipate the most power is R_1 , as it has the largest resistance and carries the same current as the parallel combination of R_2 and the load resistor. The power dissipated in R_1 will be maximum when the voltage across R_1 is maximum. This will occur when the voltage divider has a resistive load. Thus,

$$v_{R_1} = 40 - 7.5 = 32.5 \text{ V}$$

 $p_{R_1} = \frac{32.5^2}{1200} = 880.2 \text{ m W}$

Thus the minimum power rating for all resistors should be 1 W.

P 3.15 Refer to the solution to Problem 3.16. The voltage divider will reach the maximum power it can safely dissipate when the power dissipated in R_1 equals 1 W. Thus,

$$\frac{v_{R_1}^2}{1200} = 1$$
 so $v_{R_1} = 34.64$ V

$$v_o = 40 - 34.64 = 5.36$$
 V

So,
$$\frac{40R_{\rm e}}{1200 + R_{\rm e}} = 5.36$$
 and $R_{\rm e} = 185.68\,\Omega$

Thus,
$$\frac{(300)R_{\rm L}}{300 + R_{\rm L}} = 185.68$$
 and $R_{\rm L} = 487.26\,\Omega$

The minimum value for $R_{\rm L}$ from Appendix H is 560 Ω .

P 3.16
$$R_{eq} = 10 \| [6+5\|(8+12)] = 10 \| (6+5\|20) = 10 \| (6+4) = 5 \Omega$$

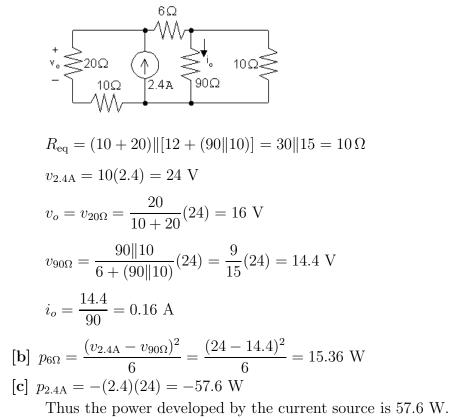
 $v_{10A} = v_{10\Omega} = (10 \text{ A})(5 \Omega) = 50 \text{ V}$

Using voltage division:

$$v_{5\Omega} = \frac{5\|(8+12)}{6+5\|(8+12)}(50) = \frac{4}{6+4}(50) = 20 \text{ V}$$

Thus,
$$p_{5\Omega} = \frac{v_{5\Omega}^2}{5} = \frac{20^2}{5} = 80$$
 W

P 3.17 [a]



P 3.18 Begin by using KCL at the top node to relate the branch currents to the current supplied by the source. Then use the relationships among the branch currents to express every term in the KCL equation using just i_2 :

 $0.05 = i_1 + i_2 + i_3 + i_4 = 0.6i_2 + i_2 + 2i_2 + 4i_1 = 0.6i_2 + i_2 + 2i_2 + 4(0.6i_2) = 6i_2$

Therefore,

 $i_2 = 0.05/6 = 0.00833 = 8.33 \text{ mA}$

Find the remaining currents using the value of i_2 :

$$i_1 = 0.6i_2 = 0.6(0.00833) = 0.005 = 5 \text{ mA}$$

$$i_3 = 2i_2 = 2(0.00833) = 0.01667 = 16.67 \text{ mA}$$

$$i_4 = 4i_1 = 4(0.005) = 0.02 = 20 \text{ mA}$$

Since the resistors are in parallel, the same voltage, 25 V, appears across each of them. We know the current and the voltage for every resistor so we can use Ohm's law to calculate the values of the resistors:

$$R_1 = 25/i_1 = 25/0.005 = 5000 = 5 \ \mathrm{k}\Omega$$

$$R_2 = 25/i_2 = 25/0.00833 = 3000 = 3 \text{ k}\Omega$$

 $R_3 = 25/i_3 = 25/0.01667 = 1500 = 1.5 \text{ k}\Omega$
 $R_4 = 25/i_4 = 25/0.02 = 1250 = 1.25 \text{ k}\Omega$

The resulting circuit is shown below:

$$50\text{mA} \stackrel{+}{\underbrace{}} 25\text{V} \stackrel{+}{\leq} 5\text{k}\Omega \stackrel{-}{\leq} 3\text{k}\Omega \stackrel{-}{\leq} 1.5\text{k}\Omega \stackrel{+}{\leq} 1.25\text{k}\Omega$$

P 3.19
$$\frac{(24)^2}{R_1 + R_2 + R_3} = 80$$
, Therefore, $R_1 + R_2 + R_3 = 7.2 \Omega$
 $\frac{(R_1 + R_2)24}{(R_1 + R_2 + R_3)} = 12$
Therefore, $2(R_1 + R_2) = R_1 + R_2 + R_3$

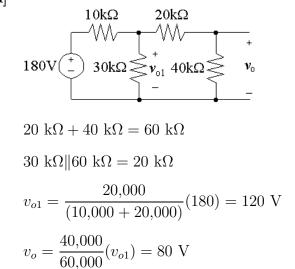
Thus, $R_1 + R_2 = R_3$; $2R_3 = 7.2$; $R_3 = 3.6 \Omega$

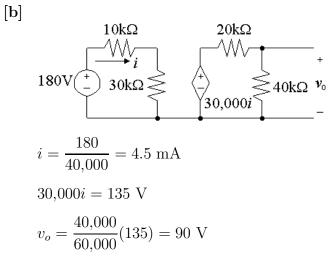
$$\frac{R_2(24)}{R_1 + R_2 + R_3} = 5$$

 $4.8R_2 = R_1 + R_2 + 3.6 = 7.2$

Thus, $R_2 = 1.5 \Omega$; $R_1 = 7.2 - R_2 - R_3 = 2.1 \Omega$

P 3.20 [a]



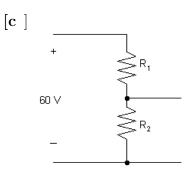


[c] It removes the loading effect of the second voltage divider on the first voltage divider. Observe that the open circuit voltage of the first divider is

$$v_{o1}' = \frac{30,000}{40,000}(180) = 135 \text{ V}$$

Now note this is the input voltage to the second voltage divider when the current-controlled voltage source is used.

P 3.21 [a] At no load:
$$v_o = kv_s = \frac{R_2}{R_1 + R_2}v_s$$
.
At full load: $v_o = \alpha v_s = \frac{R_e}{R_1 + R_e}v_s$, where $R_e = \frac{R_oR_2}{R_o + R_2}$.
Therefore $k = \frac{R_2}{R_1 + R_2}$ and $R_1 = \frac{(1-k)}{k}R_2$
 $\alpha = \frac{R_e}{R_1 + R_e}$ and $R_1 = \frac{(1-\alpha)}{\alpha}R_e$
Thus $\left(\frac{1-\alpha}{\alpha}\right)\left[\frac{R_2R_o}{R_o + R_2}\right] = \frac{(1-k)}{k}R_2$
Solving for R_2 yields $R_2 = \frac{(k-\alpha)}{\alpha(1-k)}R_o$
Also, $R_1 = \frac{(1-k)}{k}R_2$ \therefore $R_1 = \frac{(k-\alpha)}{\alpha k}R_o$
[b] $R_1 = \left(\frac{0.05}{0.68}\right)R_o = 2.5 \text{ k}\Omega$
 $R_2 = \left(\frac{0.05}{0.12}\right)R_o = 14.167 \text{ k}\Omega$



Maximum dissipation in R_2 occurs at no load, therefore,

$$P_{R_2(\text{max})} = \frac{[(60)(0.85)]^2}{14,167} = 183.6 \text{ mW}$$

Maximum dissipation in R_1 occurs at full load.

$$P_{R_1(\text{max})} = \frac{[60 - 0.80(60)]^2}{2500} = 57.60 \text{ mW}$$

$$P_{R_{1}} = \frac{(60)^{2}}{2500} = 1.44 \text{ W} = 1440 \text{ mW}$$

$$P_{R_{2}} = \frac{(0)^{2}}{14,167} = 0 \text{ W}$$

P 3.22 [a] Let v_o be the voltage across the parallel branches, positive at the upper terminal, then

$$i_g = v_o G_1 + v_o G_2 + \dots + v_o G_N = v_o (G_1 + G_2 + \dots + G_N)$$

It follows that $v_o = \frac{i_g}{(G_1 + G_2 + \dots + G_N)}$

The current in the k^{th} branch is $i_k = v_o G_k$; Thus,

$$i_k = \frac{i_g G_k}{[G_1 + G_2 + \dots + G_N]}$$

[b] $i_5 = \frac{40(0.2)}{2 + 0.2 + 0.125 + 0.1 + 0.05 + 0.025} = 3.2$ A

P 3.23 [a] The equivalent resistance of the 6 k Ω resistor and the resistors to its right is

$$6 k \| (5 k + 7 k) = 6 k \| 12 k = 4 k \Omega$$

Using voltage division,

$$v_{6k} = \frac{4000}{8000 + 4000} (18) = 6 \text{ V}$$

[b] $v_{5k} = \frac{5000}{5000 + 7000} (6) = 2.5 \text{ V}$

P 3.24 [a] The equivalent resistance of the 100Ω resistor and the resistors to its right is

 $100||(80+70) = 100||150 = 60\,\Omega$

Using current division,

$$i_{50} = \frac{(50+90+60)||300}{50+90+60}(0.03) = \frac{120}{200}(0.03) = 0.018 = 18 \text{ mA}$$

[b] $v_{70} = \frac{(80+70)||100}{80+70}(0.018) = \frac{60}{150}(0.018) = 0.0072 = 7.2 \text{ mA}$

P 3.25 [a] The equivalent resistance of the circuit to the right of, and including, the 50Ω resistor is

 $[(60||15) + (45||30) + 20]||50 = 25\,\Omega$

Thus by voltage division,

$$v_{25} = \frac{25}{25 + 25 + 10}(30) = 12.5 \text{ V}$$

[b] The current in the 25Ω resistor can be found from its voltage using Ohm's law:

$$i_{25} = \frac{12.5}{25} = 0.5 \text{ A}$$

[c] The current in the 25Ω resistor divides between two branches – one containing 50Ω and one containing $(45||30) + (15||60) + 20 = 50\Omega$. Using current division,

$$i_{50} = \frac{50||50}{50}(i_{25}) = \frac{25}{50}(0.5) = 0.25$$
 A

[d] The voltage drop across the 50Ω resistor can be found using Ohm's law:

$$v_{50} = 50i_{50} = 50(0.25) = 12.5 \text{ V}$$

[e] The voltage v_{50} divides across the equivalent resistance $(45||30) \Omega$, the equivalent resistance $(15||60) \Omega$, and the 20Ω resistor. Using voltage division,

$$v_{60} = v_{15||60} = \frac{15||60}{(15||60) + (30||45) + 20}(12.5) = \frac{12}{12 + 18 + 20}(12.5) = 3 \text{ V}$$

P 3.26 [a] The equivalent resistance to the right of the 36Ω resistor is

 $6 + [18||(26 + 10)] = 18 \Omega$

By current division,

$$i_{36} = \frac{36||18}{36}(0.45) = 0.15 = 150 \text{ mA}$$

[b] Using Ohm's law,

 $v_{36} = 36i_{36} = 36(0.15) = 5.4 \text{ V}$

[c] Before using voltage division, find the equivalent resistance of the 18Ω resistor and the resistors to its right:

$$18\|(26+10) = 12\,\Omega$$

Now use voltage division:

$$v_{18} = \frac{12}{12+6}(5.4) = 3.6 \text{ V}$$

[d]
$$v_{10} = \frac{10}{10 + 26} (3.6) = 1 \text{ V}$$

P 3.27 [a] Begin by finding the equivalent resistance of the 30Ω resistor and all resistors to its right:

$$([(12+18)||10||15||20]+16)||30 = 12\Omega$$

Now use voltage division to find the voltage across the 4Ω resistor:

$$v_4 = \frac{4}{4+12+14}(6) = 0.8 \text{ V}$$

[b] Use Ohm's law to find the current in the 4Ω resistor:

 $i_4 = v_4/4 = 0.8/4 = 0.2$ A

[c] Begin by finding the equivalent resistance of all resistors to the right of the 30Ω resistor:

 $[(12+18)||10||15||20] + 16 = 20\,\Omega$

Now use current division:

$$i_{16} = \frac{30||20}{20}(0.2) = 0.12 = 120 \text{ mA}$$

[d] Note that the current in the 16Ω resistor divides among four branches – $20 \Omega, 15 \Omega, 10 \Omega$, and $(12 + 18) \Omega$:

$$i_{10} = \frac{20||15||10||(12+18)}{10}(0.12) = 0.048 = 48 \text{ mA}$$

[e] Use Ohm's law to find the voltage across the 10Ω resistor:

$$v_{10} = 10i_{10} = 10(0.048) = 0.48 \text{ V}$$

$$[\mathbf{f}] \ v_{18} = \frac{18}{12 + 18} (0.48) = 0.288 = 288 \text{ mV}$$

$$P \ 3.28 \quad [\mathbf{a}] \ v_{6k} = \frac{6}{6 + 2} (18) = 13.5 \text{ V}$$

$$v_{3k} = \frac{3}{3 + 9} (18) = 4.5 \text{ V}$$

$$v_x = v_{6k} - v_{3k} = 13.5 - 4.5 = 9 \text{ V}$$

$$[\mathbf{b}] \ v_{6k} = \frac{6}{8} (V_s) = 0.75 V_s$$

$$v_{3k} = \frac{3}{12} (V_s) = 0.25 V_s$$

$$v_x = (0.75 V_s) - (0.25 V_s) = 0.5 V_s$$

P 3.29 Use current division to find the current in the branch containing the 10 k and 15 k resistors, from bottom to top

$$i_{10k+15k} = \frac{(10 \text{ k} + 15 \text{ k}) \| (3 \text{ k} + 12 \text{ k})}{10 \text{ k} + 15 \text{ k}} (18) = 6.75 \text{ mA}$$

Use Ohm's law to find the voltage drop across the 15 k resistor, positive at the top:

$$v_{15k} = -(6.75 \text{ m})(15 \text{ k}) = -101.25 \text{ V}$$

Find the current in the branch containing the 3 k and 12 k resistors, from bottom to top

$$i_{10k+15k} = \frac{(10 \text{ k} + 15 \text{ k}) \| (3 \text{ k} + 12 \text{ k})}{3 \text{ k} + 12 \text{ k}} (18) = 11.25 \text{ mA}$$

Use Ohm's law to find the voltage drop across the 12 k resistor, positive at the top:

$$v_{12k} = -(12 \text{ k})(11.25 \text{ m}) = -135 \text{ V}$$

$$v_o = v_{15k} - v_{12k} = -101.25 - (-135) = 33.75 \text{ V}$$

P 3.30 The equivalent resistance of the circuit to the right of the 90 Ω resistor is

$$R_{\rm eq} = [(150||75) + 40]||(30 + 60) = 90||90 = 45\,\Omega$$

Use voltage division to find the voltage drop between the top and bottom nodes:

$$v_{\rm Req} = \frac{45}{45 + 90}(3) = 1 \,\,{\rm V}$$

Use voltage division again to find v_1 from v_{Req} :

$$v_1 = \frac{150||75}{150||75+40}(1) = \frac{50}{90}(1) = \frac{5}{9} V$$

Use voltage division one more time to find v_2 from v_{Req} :

$$v_2 = \frac{30}{30+60}(1) = \frac{1}{3} \text{ V}$$

P 3.31 Find the equivalent resistance of all the resistors except the 2Ω :

 $5\Omega \| 20\Omega = 4\Omega;$ $4\Omega + 6\Omega = 10\Omega;$ $10 \| (15 + 12 + 13) = 8\Omega = R_{eq}$

Use Ohm's law to find the current i_q :

$$i_g = \frac{125}{2 + R_{eq}} = \frac{125}{2 + 8} = 12.5 \text{ A}$$

Use current division to find the current in the 6Ω resistor:

$$i_{6\Omega} = \frac{8}{6+4}(12.5) = 10$$
 A

Use current division again to find i_o :

$$i_o = \frac{5\|20}{20}i_{6\Omega} = \frac{5\|20}{20}(10) = 2$$
 A

P 3.32 Use current division to find the current in the 8Ω resistor. Begin by finding the equivalent resistance of the 8Ω resistor and all resistors to its right:

$$R_{\rm eq} = ([(20||80) + 4]||30) + 8 = 20\,\Omega$$

$$i_8 = \frac{60 \|R_{eq}}{R_{eq}}(0.25) = \frac{60 \|20}{20}(0.25) = 0.1875 = 187.5 \text{ mA}$$

Use current division to find i_1 from i_8 :

$$i_1 = \frac{30 \| [4 + (80 \| 20)]}{30} (i_8) = \frac{30 \| 20}{30} (0.1875) = 0.075 = 75 \text{ mA}$$

STU control by Copyright and written permission should be obtained recording, or likewise. For information regarding permission(s), write to: Rights and Permissions Department, Pearson Education, Inc., Upper Saddle River, NJ 07458. Use current division to find $i_{4\Omega}$ from i_8 :

$$i_{4\Omega} = \frac{30\|[4 + (80\|20)]}{4 + (80\|20)}(i_8) = \frac{30\|20}{20}(0.1875) = 0.1125 = 112.5 \text{ mA}$$

Finally, use current division to find i_2 from $i_{4\Omega}$:

$$i_2 = \frac{80||20}{20}(i_{4\Omega}) = \frac{80||20}{20}(0.1125) = 0.09 = 90 \text{ mA}$$

P 3.33 The current in the shunt resistor at full-scale deflection is $i_{\rm A} = i_{\rm fullscale} - 3 \times 10^{-3}$ A. The voltage across $R_{\rm A}$ at full-scale deflection is always 150 mV; therefore,

$$R_{\rm A} = \frac{150 \times 10^{-3}}{i_{\rm fullscale} - 3 \times 10^{-3}} = \frac{150}{1000i_{\rm fullscale} - 3}$$

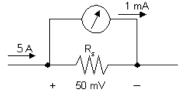
$$[\mathbf{a}] \ R_{\rm A} = \frac{150}{5000 - 3} = 30.018 \ {\rm m}\Omega$$

[b] Let R_m be the equivalent ammeter resistance:

$$R_m = \frac{0.15}{5} = 0.03 = 30 \text{ m}\Omega$$

[c] $R_A = \frac{150}{100 - 3} = 1.546 \Omega$
[d] $R_m = \frac{0.15}{0.1} = 1.5 \Omega$

P 3.34



Original meter:	$R_{\rm e} = \frac{50 \times 10^{-3}}{5} = 0.01 \Omega$
Modified meter:	$R_{\rm e} = \frac{(0.02)(0.01)}{0.03} = 0.00667\Omega$
$\therefore (I_{\rm fs})(0.00667) = 50 \times 10^{-3}$	
: $I_{\rm fs} = 7.5 \ {\rm A}$	

P 3.35 At full scale the voltage across the shunt resistor will be 200 mV; therefore the power dissipated will be

$$P_{\rm A} = \frac{(200 \times 10^{-3})^2}{R_{\rm A}}$$

Therefore
$$R_{\rm A} \ge \frac{(200 \times 10^{-3})^2}{1.0} = 40 \text{ m}\Omega$$

Otherwise the power dissipated in R_A will exceed its power rating of 1 W When $R_A = 40 \text{ m}\Omega$, the shunt current will be

$$i_{\rm A} = \frac{200 \times 10^{-3}}{40 \times 10^{-3}} = 5 \text{ A}$$

The measured current will be $i_{\text{meas}} = 5 + 0.002 = 5.002$ A \therefore Full-scale reading for practical purposes is 5 A.

P 3.36 [a] The model of the ammeter is an ideal ammeter in parallel with a resistor whose resistance is given by

$$R_m = \frac{100 \,\mathrm{mV}}{2 \,\mathrm{mA}} = 50 \,\Omega.$$

We can calculate the current through the real meter using current division:

$$i_m = \frac{(25/12)}{50 + (25/12)}(i_{\text{meas}}) = \frac{25}{625}(i_{\text{meas}}) = \frac{1}{25}i_{\text{meas}}$$

[b] At full scale, $i_{\text{meas}} = 5$ A and $i_{\text{m}} = 2$ mA so 5 - 0.002 = 4998 mA flows through the resistor R_{A} :

$$R_{\rm A} = \frac{100 \text{ mV}}{4998 \text{ mA}} = \frac{100}{4998} \Omega$$
$$i_m = \frac{(100/4998)}{50 + (100/4998)} (i_{\rm meas}) = \frac{1}{2500} (i_{\rm meas})$$

[c] Yes

P 3.37 For all full-scale readings the total resistance is

$$R_V + R_{\rm movement} = \frac{\text{full-scale reading}}{10^{-3}}$$

We can calculate the resistance of the movement as follows:

$$R_{\rm movement} = \frac{20 \text{ mV}}{1 \text{ mA}} = 20 \,\Omega$$

Therefore, $R_V = 1000$ (full-scale reading) -20

$$[\mathbf{a}] \ R_V = 1000(50) - 20 = 49,980 \,\Omega$$
$$[\mathbf{b}] \ R_V = 1000(5) - 20 = 4980 \,\Omega$$
$$[\mathbf{c}] \ R_V = 1000(0.25) - 20 = 230 \,\Omega$$
$$[\mathbf{d}] \ R_V = 1000(0.025) - 20 = 5 \,\Omega$$

P 3.38 [a]
$$v_{\text{meas}} = (50 \times 10^{-3})[15||45||(4980 + 20)] = 0.5612 \text{ V}$$

[b] $v_{\text{true}} = (50 \times 10^{-3})(15||45) = 0.5625 \text{ V}$
% error $= \left(\frac{0.5612}{0.5625} - 1\right) \times 100 = -0.224\%$

P 3.39 The measured value is $60||20.1 = 15.05618 \Omega$.

$$i_g = \frac{50}{(15.05618 + 10)} = 1.995526 \text{ A};$$
 $i_{\text{meas}} = \frac{60}{80.1}(1.996) = 1.494768 \text{ A}$

The true value is $60||20 = 15 \Omega$.

$$i_g = \frac{50}{(15+10)} = 2$$
 A; $i_{true} = \frac{60}{80}(2) = 1.5$ A
%error $= \left[\frac{1.494768}{1.5} - 1\right] \times 100 = -0.34878\% \approx -0.35\%$

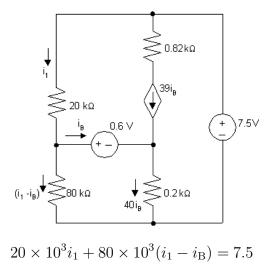
P 3.40 Begin by using current division to find the actual value of the current i_o :

$$i_{\text{true}} = \frac{15}{15 + 45} (50 \text{ mA}) = 12.5 \text{ mA}$$

$$i_{\text{meas}} = \frac{15}{15 + 45 + 0.1} (50 \text{ mA}) = 12.4792 \text{ mA}$$

% error $= \left[\frac{12.4792}{12.5} - 1\right] 100 = -0.166389\% \approx -0.17\%$

P 3.41 [a]



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$$80 \times 10^3 (i_1 - i_B) = 0.6 + 40 i_B (0.2 \times 10^3)$$

$$100i_1 - 80i_{\rm B} = 7.5 \times 10^{-3}$$

 $80i_1 - 88i_B = 0.6 \times 10^{-3}$

Calculator solution yields $i_{\rm B} = 225\,\mu{\rm A}$

[b] With the insertion of the ammeter the equations become

 $100i_1 - 80i_B = 7.5 \times 10^{-3}$ (no change) $80 \times 10^3(i_1 - i_B) = 10^3i_B + 0.6 + 40i_B(200)$

 $80i_1 - 89i_{\rm B} = 0.6 \times 10^{-3}$

Calculator solution yields $i_{\rm B} = 216 \,\mu {\rm A}$

[c] % error
$$= \left(\frac{216}{225} - 1\right) 100 = -4\%$$

P 3.42 [a] Since the unknown voltage is greater than either voltmeter's maximum reading, the only possible way to use the voltmeters would be to connect them in series.

 $R_{m1} = (300)(900) = 270 \text{ k}\Omega;$ $R_{m2} = (150)(1200) = 180 \text{ k}\Omega$

 $R_{m1} + R_{m2} = 450 \text{ k}\Omega$

(100)(1200) = 100 MJ

 $i_{1 \text{ max}} = \frac{300}{270} \times 10^{-3} = 1.11 \text{ mA}; \qquad i_{2 \text{ max}} = \frac{150}{180} \times 10^{-3} = 0.833 \text{ mA}$

 \therefore $i_{\text{max}} = 0.833 \text{ mA}$ since meters are in series

$$v_{\rm max} = (0.833 \times 10^{-3})(270 + 180)10^3 = 375 \text{ V}$$

Thus the meters can be used to measure the voltage.

[c]
$$i_m = \frac{320}{450 \times 10^3} = 0.711 \text{ mA}$$

 $v_{m1} = (0.711)(270) = 192 \text{ V}; \qquad v_{m2} = (0.711)(180) = 128 \text{ V}$

P 3.43 The current in the series-connected voltmeters is

$$\begin{split} i_m &= \frac{205.2}{270,000} = \frac{136.8}{180,000} = 0.76 \text{ mA} \\ v_{50 \text{ } \text{k}\Omega} &= (0.76 \times 10^{-3})(50,000) = 38 \text{ V} \\ V_{\text{power supply}} &= 205.2 + 136.8 + 38 = 380 \text{ V} \\ \text{P } 3.44 \quad R_{\text{meter}} &= R_m + R_{\text{movement}} = \frac{500 \text{ V}}{1 \text{ mA}} = 1000 \text{ k}\Omega \\ v_{\text{meas}} &= (50 \text{ k}\Omega \| 250 \text{ k}\Omega \| 1000 \text{ k}\Omega)(10 \text{ mA}) = (40 \text{ k}\Omega)(10 \text{ mA}) = 400 \text{ V} \\ v_{\text{true}} &= (50 \text{ k}\Omega \| 250 \text{ k}\Omega \| 1000 \text{ k}\Omega)(10 \text{ mA}) = (40 \text{ k}\Omega)(10 \text{ mA}) = 400 \text{ V} \\ \psi_{\text{true}} &= (50 \text{ k}\Omega \| 250 \text{ k}\Omega)(10 \text{ mA}) = (41.67 \text{ k}\Omega)(10 \text{ mA}) = 416.67 \text{ V} \\ \% \text{ error } &= \left(\frac{400}{416.67} - 1\right) 100 = -4\% \\ \text{P } 3.45 \quad [\textbf{a}] \quad v_{\text{meter}} = 180 \text{ V} \\ [\textbf{b}] \quad R_{\text{meter}} = (100)(200) = 20 \text{ k}\Omega \\ 20 \| 70 = 15.55556 \text{ k}\Omega \\ v_{\text{meter}} = \frac{180}{35.55556} \times 15.55556 = 78.75 \text{ V} \\ [\textbf{c}] \quad 20 \| 20 = 10 \text{ k}\Omega \\ v_{\text{meter}} = \frac{180}{80}(10) = 22.5 \text{ V} \\ [\textbf{d}] \quad v_{\text{meter}} = 180 \text{ V} \\ v_{\text{meter}} = 180 \text{ V} \\ v_{\text{meter}} = b \text{ V} \text{ volume } v_{\text{meter}} = 101.26 \text{ V} \\ \text{ No, because of the loading effect.} \\ \text{P } 3.46 \quad [\textbf{a}] \quad R_1 = (100/2)10^3 = 50 \text{ k}\Omega \\ R_2 = (10/2)10^3 = 50 \text{ k}\Omega \\ R_3 = (1/2)10^3 = 500 \Omega \end{split}$$

[b] Let $i_{\rm a}$ = actual current in the movement $i_{\rm d}$ = design current in the movement Then % error $= \left(\frac{i_a}{i_a} - 1\right) 100$ For the 100 V scale: $i_{\rm a} = \frac{100}{50.000 + 25} = \frac{100}{50.025}, \qquad i_{\rm d} = \frac{100}{50.000}$ $\frac{i_{\rm a}}{i_{\rm a}} = \frac{50,000}{50,025} = 0.9995$ % error = (0.9995 - 1)100 = -0.05%For the 10 V scale: $\frac{i_a}{i_d} = \frac{5000}{5025} = 0.995$ % error = (0.995 - 1.0)100 = -0.4975%For the 1 V scale: $\frac{i_{\rm a}}{i_{\rm c}} = \frac{500}{525} = 0.9524$ % error = (0.9524 - 1.0)100 = -4.76%P 3.47 From the problem statement we have $50 = \frac{V_s(10)}{10 + R_s}$ (1) V_s in mV; R_s in MΩ $48.75 = \frac{V_s(6)}{6+R} \quad (2)$ [a] From Eq (1) $10 + R_s = 0.2V_s$ $R_{s} = 0.2V_{s} - 10$ Substituting into Eq (2) yields $48.75 = \frac{6V_s}{0.2V - 4}$ or $V_s = 52 \text{ mV}$ **[b]** From Eq (1) $50 = \frac{520}{10 + R_{\circ}}$ or $50R_s = 20$ So $R_s = 400 \text{ k}\Omega$ P 3.48 [a] $R_{\text{movement}} = 50 \,\Omega$ $R_1 + R_{\text{movement}} = \frac{30}{1 \times 10^{-3}} = 30 \text{ k}\Omega$ \therefore $R_1 = 29,950 \Omega$ $R_2 + R_1 + R_{\text{movement}} = \frac{150}{1 \times 10^{-3}} = 150 \text{ k}\Omega$ \therefore $R_2 = 120 \text{ k}\Omega$ 300 $0 \ k\Omega$

$$R_3 + R_2 + R_1 + R_{\text{movement}} = \frac{1}{1 \times 10^{-3}} = 300$$

$$\therefore R_3 = 150 \text{ k}\Omega$$

[b]

$$v_{1} = (0.96 \text{ m})(150 \text{ k}) = 144 \text{ V}$$

$$i_{\text{move}} = \frac{144}{120 + 29.95 + 0.05} = 0.96 \text{ mA}$$

$$i_{1} = \frac{144}{750 \text{ k}} = 0.192 \text{ mA}$$

$$i_{2} = i_{\text{move}} + i_{1} = 0.96 \text{ m} + 0.192 \text{ m} = 1.152 \text{ mA}$$

$$v_{\text{meas}} = v_{x} = 144 + 150i_{2} = 316.8 \text{ V}$$
[c] $v_{1} = 150 \text{ V};$ $i_{2} = 1 \text{ m} + 0.20 \text{ m} = 1.20 \text{ mA}$

$$i_{1} = 150/750,000 = 0.20 \text{ mA}$$

$$\therefore v_{\text{meas}} = v_{x} = 150 + (150 \text{ k})(1.20 \text{ m}) = 330 \text{ V}$$
3.49 [a] $R_{\text{meter}} = 300 \text{ k}\Omega + 600 \text{ k}\Omega ||200 \text{ k}\Omega = 450 \text{ k}\Omega$

$$450 ||360 = 200 \text{ k}\Omega$$

$$V_{\text{meter}} = \frac{200}{240}(600) = 500 \text{ V}$$

[b] What is the percent error in the measured voltage?

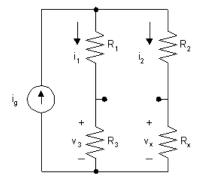
True value
$$=\frac{360}{400}(600) = 540 \text{ V}$$

% error $=\left(\frac{500}{540} - 1\right)100 = -7.41\%$

Р

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P 3.50 Since the bridge is balanced, we can remove the detector without disturbing the voltages and currents in the circuit.



It follows that

$$i_{1} = \frac{i_{g}(R_{2} + R_{x})}{R_{1} + R_{2} + R_{3} + R_{x}} = \frac{i_{g}(R_{2} + R_{x})}{\sum R}$$

$$i_{2} = \frac{i_{g}(R_{1} + R_{3})}{R_{1} + R_{2} + R_{3} + R_{x}} = \frac{i_{g}(R_{1} + R_{3})}{\sum R}$$

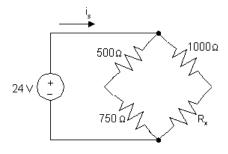
$$v_{3} = R_{3}i_{1} = v_{x} = i_{2}R_{x}$$

$$\therefore \frac{R_{3}i_{g}(R_{2} + R_{x})}{\sum R} = \frac{R_{x}i_{g}(R_{1} + R_{3})}{\sum R}$$

$$\therefore R_{3}(R_{2} + R_{x}) = R_{x}(R_{1} + R_{3})$$

From which
$$R_x = \frac{R_2 R_3}{R_1}$$

P 3.51 [a]



The condition for a balanced bridge is that the product of the opposite resistors must be equal:

(500)(
$$R_x$$
) = (1000)(750) so $R_x = \frac{(1000)(750)}{500} = 1500 \,\Omega$

[b] The source current is the sum of the two branch currents. Each branch current can be determined using Ohm's law, since the resistors in each branch are in series and the voltage drop across each branch is 24 V:

$$i_s = \frac{24 \text{ V}}{500 \Omega + 750 \Omega} + \frac{24 \text{ V}}{1000 \Omega + 1500 \Omega} = 28.8 \text{ mA}$$

[c] We can use Ohm's law to find the current in each branch:

$$i_{\text{left}} = \frac{24}{500 + 750} = 19.2 \text{ mA}$$

 $i_{\text{right}} = \frac{24}{1000 + 1500} = 9.6 \text{ mA}$

Now we can use the formula $p = Ri^2$ to find the power dissipated by each resistor:

$$p_{500} = (500)(0.0192)^2 = 184.32 \text{ mW}$$
 $p_{750} = (750)(0.0192)^2 = 276.18 \text{ mW}$
 $p_{1000} = (1000)(0.0096)^2 = 92.16 \text{ mW}$ $p_{1500} = (1500)(0.0096)^2 = 138.24 \text{ mW}$

Thus, the $750\,\Omega$ resistor absorbs the most power; it absorbs 276.48 mW of power.

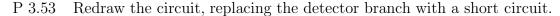
- [d] From the analysis in part (c), the 1000Ω resistor absorbs the least power; it absorbs 92.16 mW of power.
- P 3.52 Note the bridge structure is balanced, that is $15 \times 5 = 3 \times 25$, hence there is no current in the 5 k Ω resistor. It follows that the equivalent resistance of the circuit is

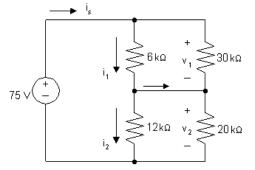
$$R_{\rm eq} = 750 + (15,000 + 3000) ||(25,000 + 5000) = 750 + 11,250 = 12 \ \mathrm{k}\Omega$$

The source current is 192/12,000 = 16 mA. The current down through the branch containing the 15 k Ω and 3 k Ω resistors is

$$i_{3k} = \frac{11,250}{18,000}(0.016) = 10 \text{ mA}$$

$$\therefore p_{3k} = 3000(0.01)^2 = 0.3 \text{ W}$$





 $6 \text{ k}\Omega \parallel 30 \text{ k}\Omega = 5 \text{ k}\Omega$

12 k $\Omega \| 20 \ k\Omega = 7.5 \ k\Omega$

$$i_s = \frac{75}{12,500} = 6 \text{ mA}$$

$$v_1 = 0.006(5000) = 30 \text{ V}$$

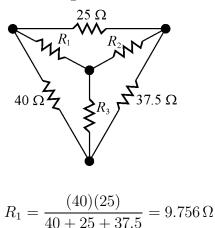
 $v_2 = 0.006(7500) = 45 \text{ V}$

$$i_1 = \frac{30}{6000} = 5 \text{ mA}$$

 $i_2 = \frac{45}{12,000} = 3.75 \text{ mA}$

 $i_{\rm d} = i_1 - i_2 = 1.25~{\rm mA}$

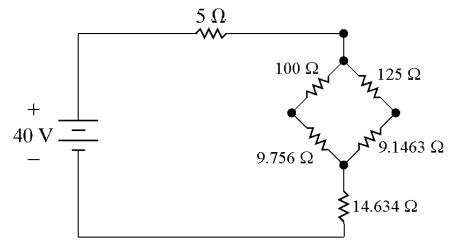
- P 3.54 In order that all four decades (1, 10, 100, 1000) that are used to set R_3 contribute to the balance of the bridge, the ratio R_2/R_1 should be set to 0.001.
- P 3.55 Use the figure below to transform the Δ to an equivalent Y:



$$R_2 = \frac{(25)(37.5)}{40 + 25 + 37.5} = 9.1463\,\Omega$$

$$R_3 = \frac{(40)(37.5)}{40 + 25 + 37.5} = 14.634\,\Omega$$

Replace the Δ with its equivalent Y in the circuit to get the figure below:



Find the equivalent resistance to the right of the $5\,\Omega$ resistor:

 $(100 + 9.756) ||(125 + 9.1463) + 14.634 = 75 \Omega$

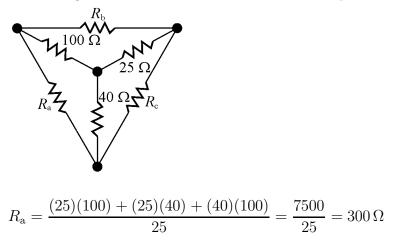
The equivalent resistance seen by the source is thus $5 + 75 = 80 \Omega$. Use Ohm's law to find the current provided by the source:

$$i_{\rm s} = \frac{40}{80} = 0.5$$
 A

Thus, the power associated with the source is

$$P_{\rm s} = -(40)(0.5) = -20$$
 W

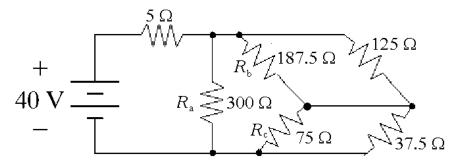
P 3.56 Use the figure below to transform the Y to an equivalent Δ :



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$$R_{\rm b} = \frac{(25)(100) + (25)(40) + (40)(100)}{40} = \frac{7500}{40} = 187.5\,\Omega$$
$$R_{\rm c} = \frac{(25)(100) + (25)(40) + (40)(100)}{100} = \frac{7500}{100} = 75\,\Omega$$

Replace the Y with its equivalent Δ in the circuit to get the figure below:



Find the equivalent resistance to the right of the $5\,\Omega$ resistor:

 $300\|[(125||187.5) + (37.5||75)] = 75\,\Omega$

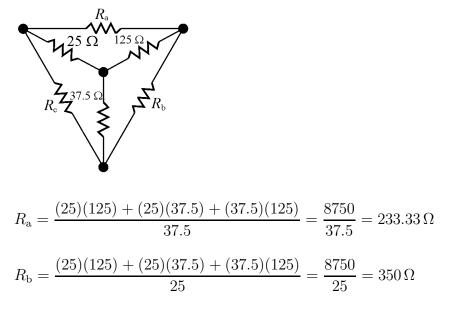
The equivalent resistance seen by the source is thus $5 + 75 = 80 \Omega$. Use Ohm's law to find the current provided by the source:

$$i_{\rm s} = \frac{40}{80} = 0.5$$
 A

Thus, the power associated with the source is

$$P_{\rm s} = -(40)(0.5) = -20$$
 W

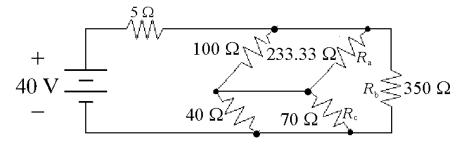
P 3.57 Use the figure below to transform the Y to an equivalent Δ :



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$$R_{\rm c} = \frac{(25)(125) + (25)(37.5) + (37.5)(125)}{125} = \frac{8750}{125} = 70\,\Omega$$

Replace the Y with its equivalent Δ in the circuit to get the figure below:



Find the equivalent resistance to the right of the $5\,\Omega$ resistor:

$$350\|[(100\|233.33) + (40\|70)] = 75\,\Omega$$

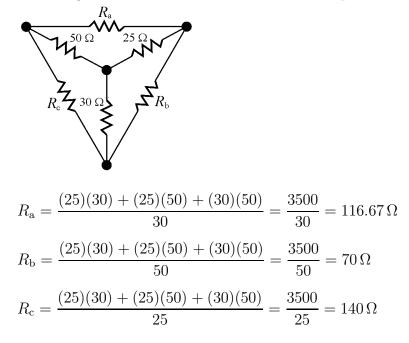
The equivalent resistance seen by the source is thus $5 + 75 = 80 \Omega$. Use Ohm's law to find the current provided by the source:

$$i_{\rm s} = \frac{40}{80} = 0.5$$
 A

Thus, the power associated with the source is

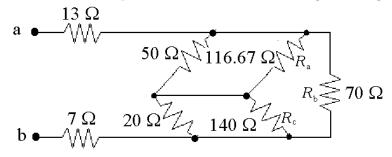
$$P_{\rm s} = -(40)(0.5) = -20 \text{ W}$$

P 3.58 [a] Use the figure below to transform the Y to an equivalent Δ :



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Replace the Y with its equivalent Δ in the circuit to get the figure below:



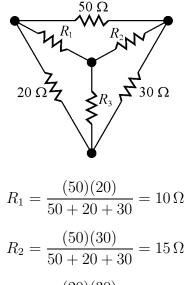
Find the equivalent resistance to the right of the $13\,\Omega$ and $7\,\Omega$ resistors:

 $70\|[(50\|116.67) + (20\|140)] = 30\,\Omega$

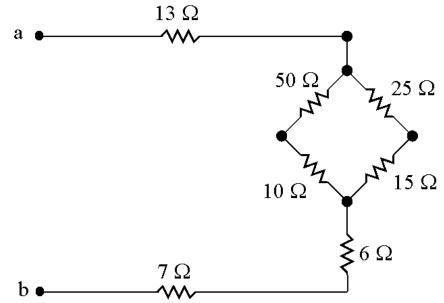
Thus, the equivalent resistance seen from the terminals a-b is:

$$R_{\rm ab} = 13 + 30 + 7 = 50\,\Omega$$

[b] Use the figure below to transform the Δ to an equivalent Y:



$$R_3 = \frac{(20)(30)}{50 + 20 + 30} = 6\,\Omega$$



Replace the Δ with its equivalent Y in the circuit to get the figure below:

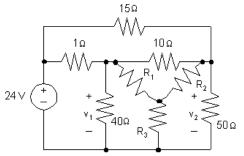
Find the equivalent resistance to the right of the $13\,\Omega$ and $7\,\Omega$ resistors:

 $(50+10) \| (25+15) + 6 = 30 \,\Omega$

Thus, the equivalent resistance seen from the terminals a-b is:

 $R_{\rm ab} = 13 + 30 + 7 = 50\,\Omega$

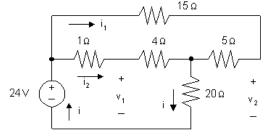
- [c] Convert the delta connection $R_1 R_2 R_3$ to its equivalent wye. Convert the wye connection $R_1 - R_3 - R_4$ to its equivalent delta.
- P 3.59 Begin by transforming the Δ -connected resistors $(10\,\Omega, 40\,\Omega, 50\,\Omega)$ to Y-connected resistors. Both the Y-connected and Δ -connected resistors are shown below to assist in using Eqs. 3.44 – 3.46:



Now use Eqs. 3.44 - 3.46 to calculate the values of the Y-connected resistors:

$$R_1 = \frac{(40)(10)}{10 + 40 + 50} = 4\,\Omega; \quad R_2 = \frac{(10)(50)}{10 + 40 + 50} = 5\,\Omega; \quad R_3 = \frac{(40)(50)}{10 + 40 + 50} = 20\,\Omega$$

STU transfer Education, Inc., Upper Saddle River, NJ. All rights reserved. This publication is protected by Copyright and written permission should be obtained transfer prior bay productient reproduction, storage in a retrieval system, or transmission in any form or by apy means Ceterronic mechanical) proceeding, or likewise. For information regarding permission(s), write to: Rights and Permissions Department, Pearson Education, Inc., Upper Saddle River, NJ 07458. The transformed circuit is shown below:



The equivalent resistance seen by the 24 V source can be calculated by making series and parallel combinations of the resistors to the right of the 24 V source:

$$R_{\rm eq} = (15+5) \| (1+4) + 20 = 20 \| 5+20 = 4+20 = 24 \,\Omega$$

Therefore, the current i in the 24 V source is given by

$$i = \frac{24 \text{ V}}{24 \Omega} = 1 \text{ A}$$

Use current division to calculate the currents i_1 and i_2 . Note that the current i_1 flows in the branch containing the 15Ω and 5Ω series connected resistors, while the current i_2 flows in the parallel branch that contains the series connection of the 1Ω and 4Ω resistors:

$$i_1 = \frac{4}{15+5}(i) = \frac{4}{20}(1 \text{ A}) = 0.2 \text{ A}, \quad \text{and} \quad i_2 = 1 \text{ A} - 0.2 \text{ A} = 0.8 \text{ A}$$

Now use KVL and Ohm's law to calculate v_1 . Note that v_1 is the sum of the voltage drop across the 4Ω resistor, $4i_2$, and the voltage drop across the 20Ω resistor, 20i:

$$v_1 = 4i_2 + 20i = 4(0.8 \text{ A}) + 20(1 \text{ A}) = 3.2 + 20 = 23.2 \text{ V}$$

Finally, use KVL and Ohm's law to calculate v_2 . Note that v_2 is the sum of the voltage drop across the 5Ω resistor, $5i_1$, and the voltage drop across the 20Ω resistor, 20i:

$$v_2 = 5i_1 + 20i = 5(0.2 \text{ A}) + 20(1 \text{ A}) = 1 + 20 = 21 \text{ V}$$

P 3.60 [a] Convert the upper delta to a wye.

$$R_{1} = \frac{(50)(50)}{200} = 12.5 \,\Omega$$
$$R_{2} = \frac{(50)(100)}{200} = 25 \,\Omega$$
$$R_{3} = \frac{(100)(50)}{200} = 25 \,\Omega$$

Convert the lower delta to a wye.

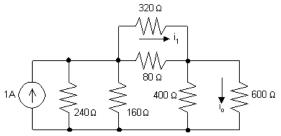
$$R_4 = \frac{(60)(80)}{200} = 24 \,\Omega$$
$$R_5 = \frac{(60)(60)}{200} = 18 \,\Omega$$
$$R_6 = \frac{(80)(60)}{200} = 24 \,\Omega$$

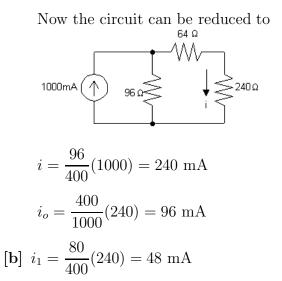
Now redraw the circuit using the wye equivalents.

*
$$1.5 \Omega$$

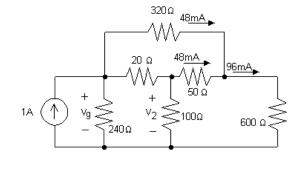
 12.5Ω
 12.5Ω
 25Ω
 25Ω
 25Ω
 25Ω
 24Ω
 24Ω
 24Ω
 24Ω
 18Ω
 $R_{ab} = 1.5 + 12.5 + \frac{(120)(80)}{200} + 18 = 14 + 48 + 18 = 80 \Omega$
[b] When $v_{ab} = 400 \text{ V}$
 $i_g = \frac{400}{80} = 5 \text{ A}$
 $i_{31} = \frac{48}{80}(5) = 3 \text{ A}$
 $p_{31\Omega} = (31)(3)^2 = 279 \text{ W}$

P 3.61 [a] After the 20Ω — 100Ω — 50Ω wye is replaced by its equivalent delta, the circuit reduces to





 $[\mathbf{c}]$ Now that i_o and i_1 are known return to the original circuit



$$v_2 = (50)(0.048) + (600)(0.096) = 60$$
 V
 $i_2 = \frac{v_2}{100} = \frac{60}{100} = 600$ mA

 $[\mathbf{d}] \ v_g = v_2 + 20(0.6 + 0.048) = 60 + 12.96 = 72.96 \text{ V}$

$$p_q = -(v_q)(1) = -72.96 \text{ W}$$

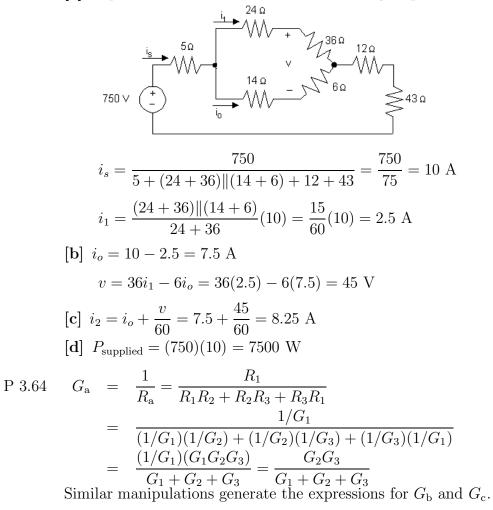
Thus the current source delivers 72.96 W.

P 3.62
$$8 + 12 = 20 \Omega$$

$$20 \| 60 = 15 \Omega$$
$$15 + 20 = 35 \Omega$$
$$35 \| 140 = 28 \Omega$$
$$28 + 22 = 50 \Omega$$

 $30 + 10 = 40 \Omega$ $i_g = 240/40 = 6 \text{ A}$ $i_o = (6)(50)/125 = 2.4 \text{ A}$ $i_{140\Omega} = (6 - 2.4)(35)/175 = 0.72 \text{ A}$ $p_{140\Omega} = (0.72)^2(140) = 72.576 \text{ W}$

P 3.63 [a] Replace the 60–120–20 Ω delta with a wye equivalent to get



P 3.65 [a] Subtracting Eq. 3.42 from Eq. 3.43 gives

$$R_1 - R_2 = (R_c R_b - R_c R_a)/(R_a + R_b + R_c).$$

Adding this expression to Eq. 3.41 and solving for R_1 gives

$$R_1 = R_{\rm c} R_{\rm b} / (R_{\rm a} + R_{\rm b} + R_{\rm c})$$

To find R_2 , subtract Eq. 3.43 from Eq. 3.41 and add this result to Eq. 3.42. To find R_3 , subtract Eq. 3.41 from Eq. 3.42 and add this result to Eq. 3.43.

[b] Using the hint, Eq. 3.43 becomes

$$R_1 + R_3 = \frac{R_{\rm b}[(R_2/R_3)R_{\rm b} + (R_2/R_1)R_{\rm b}]}{(R_2/R_1)R_{\rm b} + R_{\rm b} + (R_2/R_3)R_{\rm b}} = \frac{R_{\rm b}(R_1 + R_3)R_2}{(R_1R_2 + R_2R_3 + R_3R_1)}$$

Solving for $R_{\rm b}$ gives $R_{\rm b} = (R_1R_2 + R_2R_3 + R_3R_1)/R_2$. To find $R_{\rm a}$: First use Eqs. 3.44–3.46 to obtain the ratios $(R_1/R_3) = (R_{\rm c}/R_{\rm a})$ or $R_{\rm c} = (R_1/R_3)R_{\rm a}$ and $(R_1/R_2) = (R_{\rm b}/R_{\rm a})$ or $R_{\rm b} = (R_1/R_2)R_{\rm a}$. Now use these relationships to eliminate $R_{\rm b}$ and $R_{\rm c}$ from Eq. 3.42. To find $R_{\rm c}$, use Eqs. 3.44–3.46 to obtain the ratios $R_{\rm b} = (R_3/R_2)R_{\rm c}$ and $R_{\rm a} = (R_3/R_1)R_{\rm c}$. Now use the relationships to eliminate $R_{\rm b}$ and $R_{\rm a}$ from Eq. 3.41.

P 3.66 [a]
$$R_{\rm ab} = 2R_1 + \frac{R_2(2R_1 + R_{\rm L})}{2R_1 + R_2 + R_{\rm L}} = R_{\rm L}$$

Therefore
$$2R_1 - R_L + \frac{R_2(2R_1 + R_L)}{2R_1 + R_2 + R_L} = 0$$

Thus
$$R_{\rm L}^2 = 4R_1^2 + 4R_1R_2 = 4R_1(R_1 + R_2)$$

When $R_{\rm ab} = R_{\rm L}$, the current into terminal a of the attenuator will be $v_i/R_{\rm L}$.

Using current division, the current in the $R_{\rm L}$ branch will be

$$\frac{v_i}{R_L} \cdot \frac{R_2}{2R_1 + R_2 + R_L}$$
Therefore $v_o = \frac{v_i}{R_L} \cdot \frac{R_2}{2R_1 + R_2 + R_L} R_L$
and $\frac{v_o}{v_i} = \frac{R_2}{2R_1 + R_2 + R_L}$
[b] $(300)^2 = 4(R_1 + R_2)R_1$
 $22,500 = R_1^2 + R_1R_2$
 $\frac{v_o}{v_i} = 0.5 = \frac{R_2}{2R_1 + R_2 + 300}$
 $\therefore R_1 + 0.5R_2 + 150 = R_2$
 $0.5R_2 = R_1 + 150$
 $R_2 = 2R_1 + 300$
 $\therefore 22,500 = R_1^2 + R_1(2R_1 + 300) = 3R_1^2 + 300R_1$
 $\therefore R_1^2 + 100R_1 - 7500 = 0$

Solving,

 $R_1 = 50\,\Omega$

 $R_2 = 2(50) + 300 = 400\,\Omega$

[c] From Appendix H, choose $R_1 = 47 \Omega$ and $R_2 = 390 \Omega$. For these values, $R_{\rm ab} \neq R_{\rm L}$, so the equations given in part (a) cannot be used. Instead

$$R_{ab} = 2R_1 + [R_2 || (2R_1 + R_L)] = 2(47) + 390 || (2(47) + 300)$$
$$= 94 + 390 || 394 = 290 \Omega$$

% error =
$$\left(\frac{290}{300} - 1\right) 100 = -3.33\%$$

Now calculate the ratio of the output voltage to the input voltage. Begin by finding the current through the top left R_1 resistor, called i_a :

$$i_{\rm a} = \frac{v_i}{R_{\rm ab}}$$

Now use current division to find the current through the $R_{\rm L}$ resistor, called $i_{\rm L}$:

$$i_{\rm L} = \frac{R_2}{R_2 + 2R_1 + R_{\rm L}} i_{\rm a}$$

Therefore, the output voltage, v_o , is equal to $R_{\rm L}i_{\rm L}$:

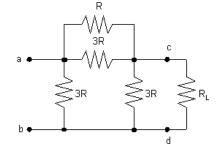
$$v_o = \frac{R_2 R_{\rm L} v_i}{R_{\rm ab} (R_2 + 2R_1 + R_{\rm L})}$$

Thus,

$$\frac{v_o}{v_i} = \frac{R_2 R_L}{R_{ab}(R_2 + 2R_1 + R_L)} = \frac{390(300)}{290(390 + 2(47) + 300)} = 0.5146$$

% error = $\left(\frac{0.5146}{0.5} - 1\right) 100 = 2.92\%$

P 3.67 [a] After making the Y-to- Δ transformation, the circuit reduces to



Therefore $R_{\rm ab} = R_{\rm L}$

[b] When $R = R_{\rm L}$, the circuit reduces to

$$i_{o} = \frac{i_{i}(3R_{L})}{4.5R_{L}} = \frac{1}{1.5}i_{i} = \frac{1}{1.5}\frac{v_{i}}{R_{L}}, \quad v_{o} = 0.75R_{L}i_{o} = \frac{1}{2}v_{i},$$

Therefore $\frac{v_{o}}{v_{i}} = 0.5$

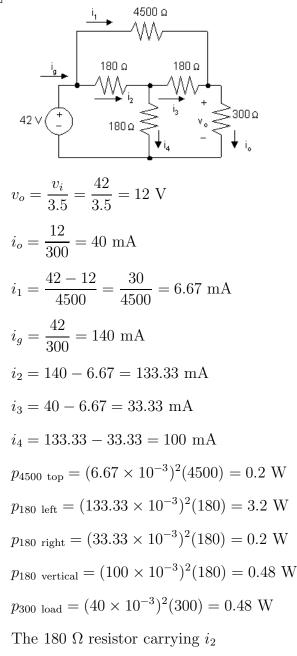
P 3.68 [a] $3.5(3R - R_L) = 3R + R_L$

10.5R - 1050 = 3R + 300 $7.5R = 1350, \qquad R = 180 \,\Omega$ $2(180)(200)^2$

$$R_2 = \frac{2(180)(300)^2}{3(180)^2 - (300)^2} = 4500\,\Omega$$

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[b]



- [c] $p_{180 \text{ left}} = 3.2 \text{ W}$
- [d] Two resistors dissipate minimum power the 4500 Ω resistor and the 180 Ω resistor carrying i_3 .
- [e] They both dissipate 0.2 W.

P 3.69 [a] R₀+ΔR + + + v₀ - $v_{\rm a} = \frac{v_{\rm in}R_4}{R_2 + R_4 + \Delta R}$ $v_{\rm b} = \frac{R_3}{R_2 + R_3} v_{\rm in}$ $v_o = v_{\rm a} - v_{\rm b} = \frac{R_4 v_{\rm in}}{R_o + R_4 + \Delta R} - \frac{R_3}{R_2 + R_3} v_{\rm in}$ When the bridge is balanced, $\frac{R_4}{R_2 + R_4} v_{\rm in} = \frac{R_3}{R_2 + R_3} v_{\rm in}$ $\therefore \quad \frac{R_4}{R_2 + R_4} = \frac{R_3}{R_2 + R_3}$ $v_{o} = \frac{R_{4}v_{in}}{R_{o} + R_{4} + \Delta R} - \frac{R_{4}v_{in}}{R_{o} + R_{4}}$ $= R_{4}v_{in} \left[\frac{1}{R_{o} + R_{4} + \Delta R} - \frac{1}{R_{o} + R_{4}}\right]$ Thus, $= \frac{R_4 v_{\rm in}(-\Delta R)}{(R_o + R_4 + \Delta R)(R_o + R_4)}$ $\approx \frac{-(\Delta R)R_4 v_{\rm in}}{(R_2 + R_4)^2}, \qquad \text{since } \Delta R << R_4$ **[b]** $\Delta R = 0.03 R_o$ $R_o = \frac{R_2 R_4}{R_2} = \frac{(1000)(5000)}{500} = 10,000\,\Omega$ $\Delta R = (0.03)(10^4) = 300\,\Omega$ $\therefore v_o \approx \frac{-300(5000)(6)}{(15\ 000)^2} = -40 \text{ mV}$ $[\mathbf{c}] \quad v_o = \frac{-(\Delta R)R_4 v_{\rm in}}{(R_o + R_4 + \Delta R)(R_o + R_4)} \\ = \frac{-300(5000)(6)}{(15,300)(15,000)}$ = -39.2157 mV

P 3.70 [a] approx value
$$= \frac{-(\Delta R)R_4 v_{in}}{(R_o + R_4)^2}$$

true value $= \frac{-(\Delta R)R_4 v_{in}}{(R_o + R_4 + \Delta R)(R_o + R_4)}$
 $\therefore \frac{\text{approx value}}{\text{true value}} = \frac{(R_o + R_4 + \Delta R)}{(R_o + R_4)}$
 $\therefore \% \text{ error } = \left[\frac{R_o + R_4}{R_o + R_4 + \Delta R} - 1\right] \times 100 = \frac{-\Delta R}{R_o + R_4} \times 100$

Note that in the above expression, we take the ratio of the true value to the approximate value because both values are negative.

But
$$R_o = \frac{R_2 R_4}{R_3}$$

 $\therefore \% \text{ error } = \frac{-R_3 \Delta R}{R_4 (R_2 + R_3)}$
[b] % error $= \frac{-(500)(300)}{(5000)(1500)} \times 100 = -2\%$
P 3.71 $\frac{\Delta R(R_3)(100)}{(R_2 + R_3)R_4} = 0.5$
 $\frac{\Delta R(500)(100)}{(1500)(5000)} = 0.5$
 $\therefore \Delta R = 75 \Omega$
% change $= \frac{75}{10,000} \times 100 = 0.75\%$

P 3.72 [a] Using the equation for voltage division,

$$V_y = \frac{\beta R_y}{\beta R_y + (1 - \beta) R_y} V_S = \frac{\beta R_y}{R_y} V_S = \beta V_S$$

[b] Since β represents the touch point with respect to the bottom of the screen, $(1 - \beta)$ represents the location of the touch point with respect to the top of the screen. Therefore, the *y*-coordinate of the pixel corresponding to the touch point is

$$y = (1 - \beta)p_y$$

Remember that the value of y is capped at $(p_y - 1)$.

P 3.73 [a] Use the equations developed in the Practical Perspective and in Problem 3.72:

$$V_x = \alpha V_S \qquad \text{so} \qquad \alpha = \frac{V_x}{V_S} = \frac{1}{5} = 0.2$$
$$V_y = \beta V_S \qquad \text{so} \qquad \beta = \frac{V_y}{V_S} = \frac{3.75}{5} = 0.75$$

[b] Use the equations developed in the Practical Perspective and in Problem 3.72:

$$x = (1 - \alpha)p_x = (1 - 0.2)(480) = 384$$
$$y = (1 - \beta)p_y = (1 - 0.75)(800) = 200$$

Therefore, the touch occurred in the upper right corner of the screen.

P 3.74 Use the equations developed in the Practical Perspective and in Problem 3.72:

$$x = (1 - \alpha)p_x \quad \text{so} \quad \alpha = 1 - \frac{x}{p_x} = 1 - \frac{480}{640} = 0.25$$
$$V_x = \alpha V_S = (0.25)(8) = 2 \text{ V}$$
$$y = (1 - \beta)p_y \quad \text{so} \quad \beta = 1 - \frac{y}{p_y} = 1 - \frac{192}{1024} = 0.8125$$
$$V_y = \beta V_S = (0.8125)(8) = 6.5 \text{ V}$$

P 3.75 From the results of Problem 3.74, the voltages corresponding to the touch point (480, 192) are

 $V_{x1} = 2 \text{ V}; \qquad V_{y1} = 6.5 \text{ V}$

Now calculate the voltages corresponding to the touch point (240, 384):

$$x = (1 - \alpha)p_x \quad \text{so} \quad \alpha = 1 - \frac{x}{p_x} = 1 - \frac{240}{640} = 0.625$$
$$V_{x2} = \alpha V_S = (0.625)(8) = 5 \text{ V}$$
$$y = (1 - \beta)p_y \quad \text{so} \quad \beta = 1 - \frac{y}{p_y} = 1 - \frac{384}{1024} = 0.625$$
$$V_{y2} = \beta V_S = (0.625)(8) = 5 \text{ V}$$

When the screen is touched at two points simultaneously, only the smaller of the two voltages in the x direction is sensed. The same is true in the y direction. Therefore, the voltages actually sensed are

$$V_x = 2 \text{ V}; \qquad V_y = 5 \text{ V}$$

These two voltages identify the touch point as (480, 384), which does not correspond to either of the points actually touched! Therefore, the resistive touch screen is appropriate only for single point touches.