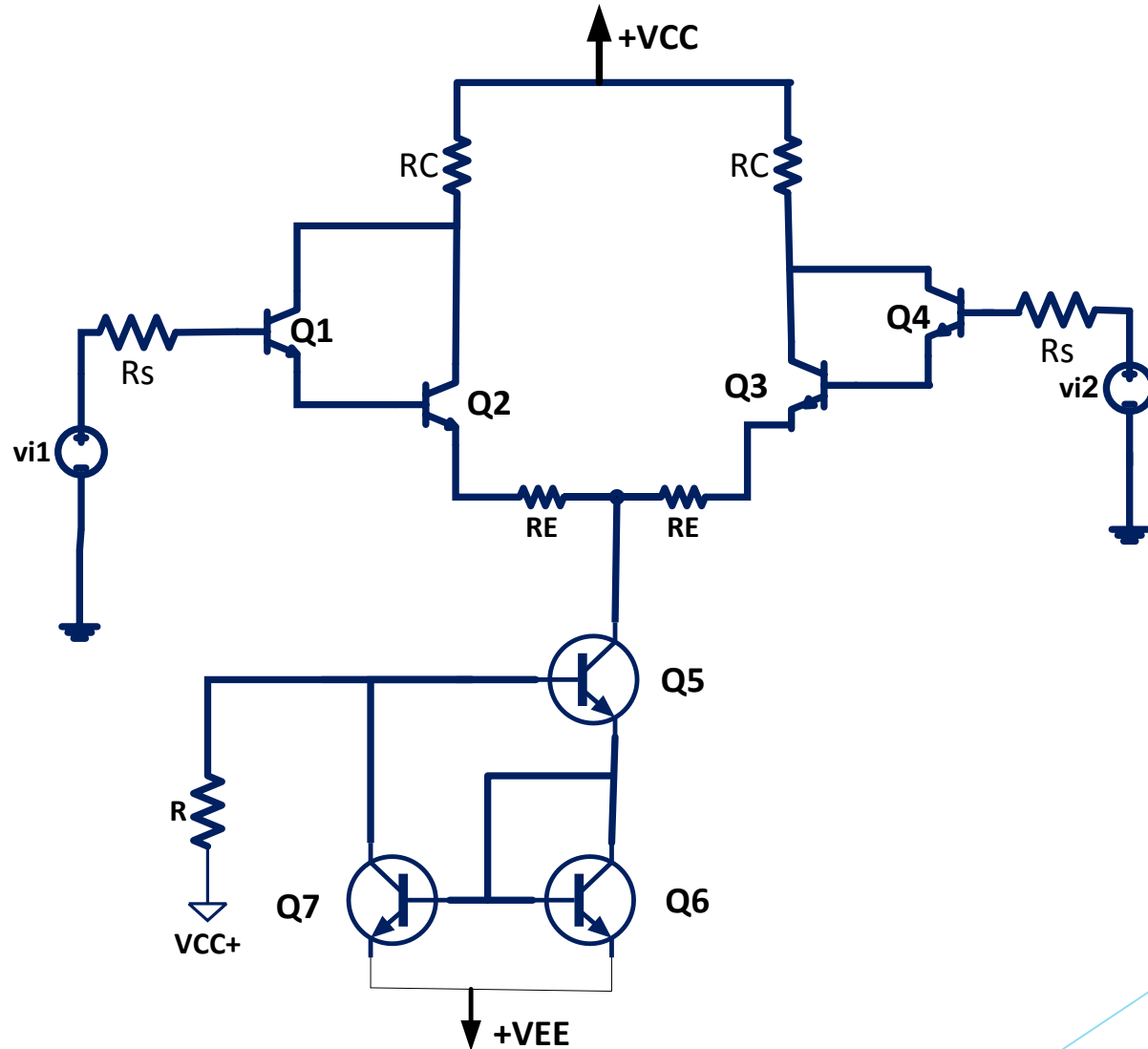
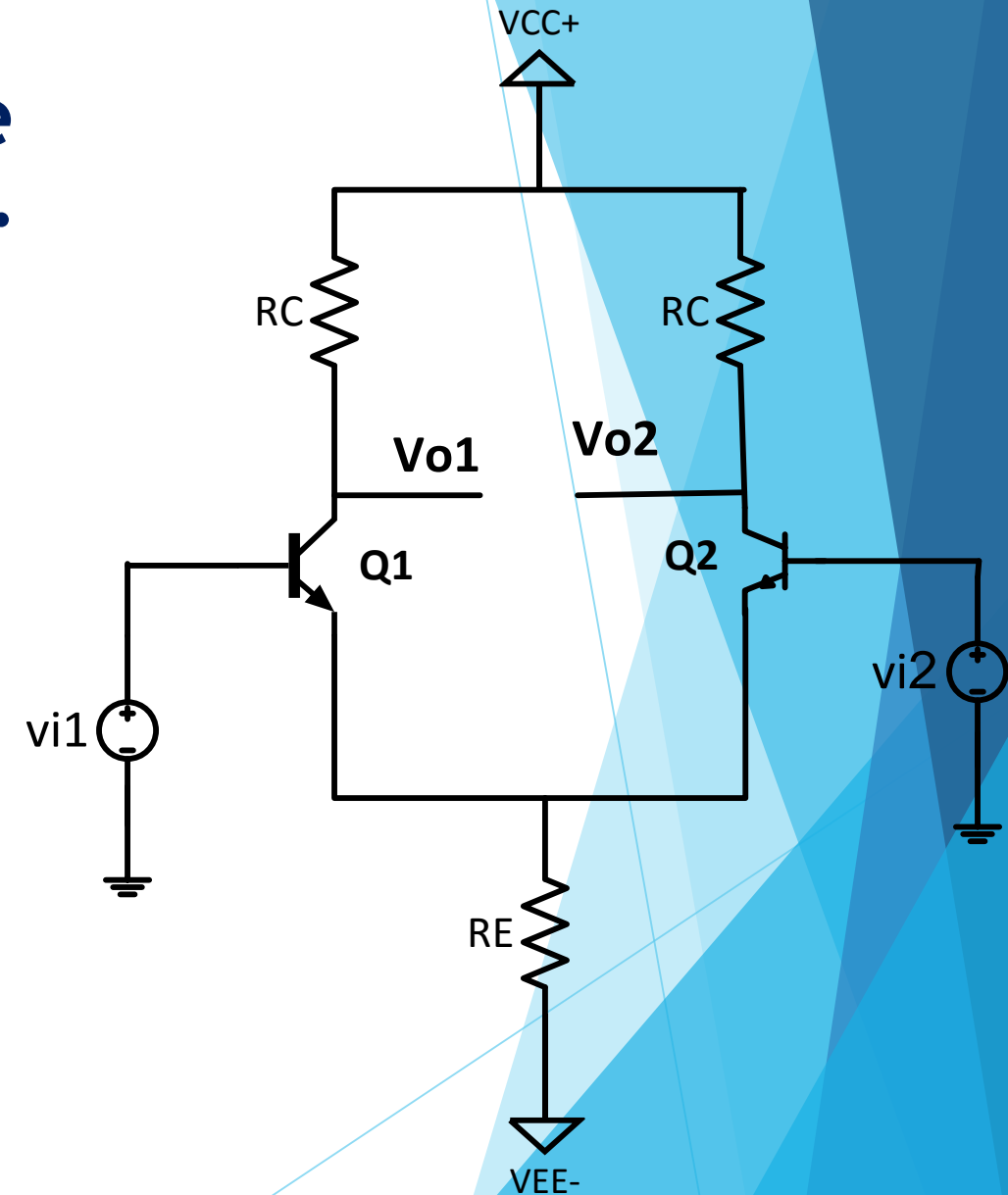


Differential Amplifiers



Differential Amplifiers

- ▶ Designed to amplify the difference between two input signal voltages.
- ▶ Found in many electronic circuits, including low and high frequency amplifiers.
- ▶ Almost always used as the input stage inside an IC operational amplifier to provide :
 - ▶ **Large input impedance** .
 - ▶ **Rejection of the noise** .



Differential Amplifiers

Simple Differential Amplifier

DC Analysis:

$$V_{B1} = V_{B2} = 0 \quad \text{since } v_{i1} = v_{i2} = 0$$

$$V_{E1} = V_{E2} = -0.7 \text{ V}$$

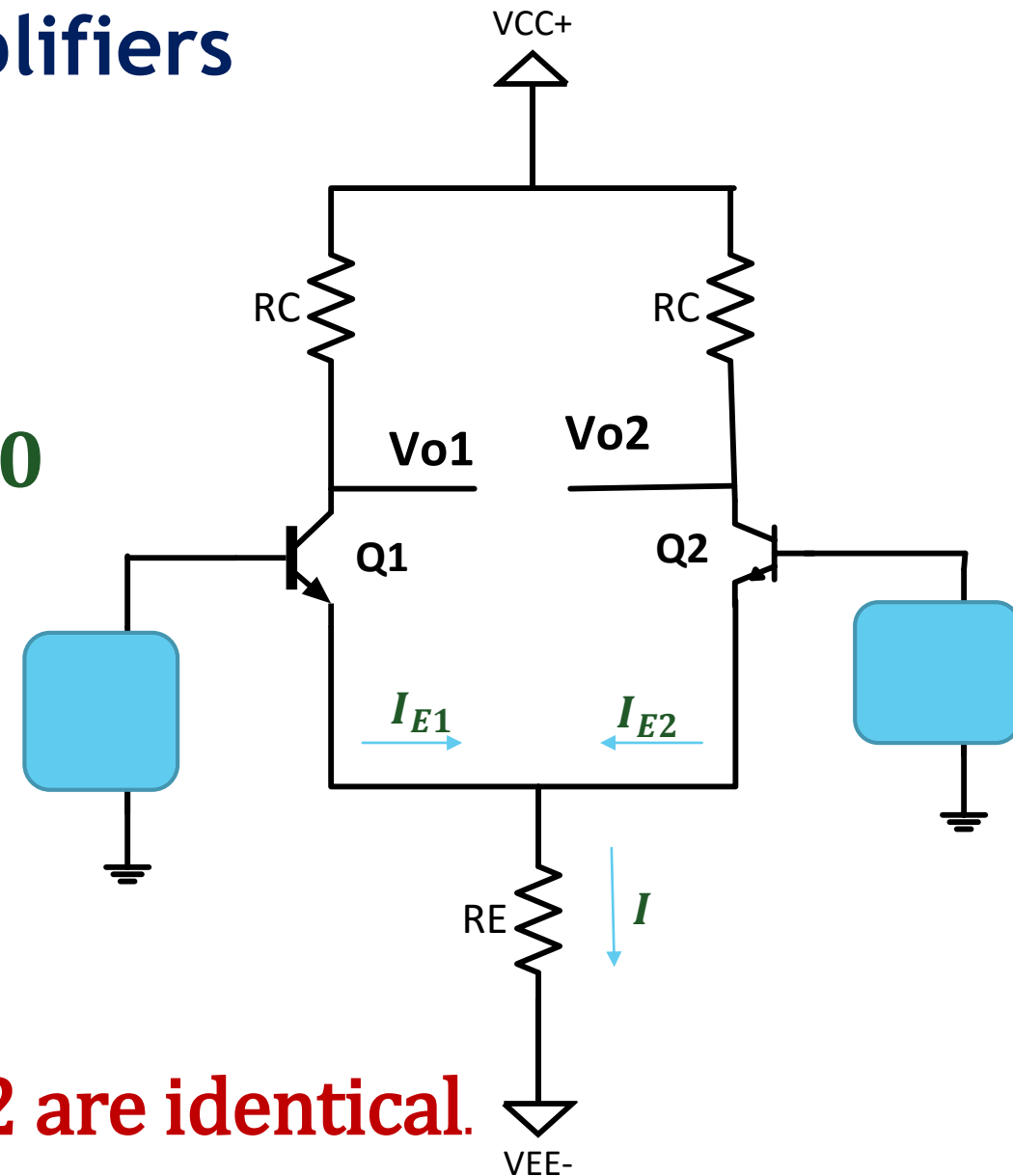
$$I = \frac{-0.7 + V_{EE}}{R_E}$$

$$I_{E1} = I_{E2} = \frac{1}{2} I$$

symmetry

Q1 & Q2 are identical.

$$\therefore \beta_1 = \beta_2$$



Differential Amplifiers

Simple Differential Amplifier

Ac small Signal Analysis:

Calculate and sketch $V_{o1}(t)$ and $V_{o2}(t)$ if $V_{i1}(t) = V_{i2}(t) = 100\text{mV}$ Peak sinusoidal

assuming

$$\beta_1 = \beta_2$$

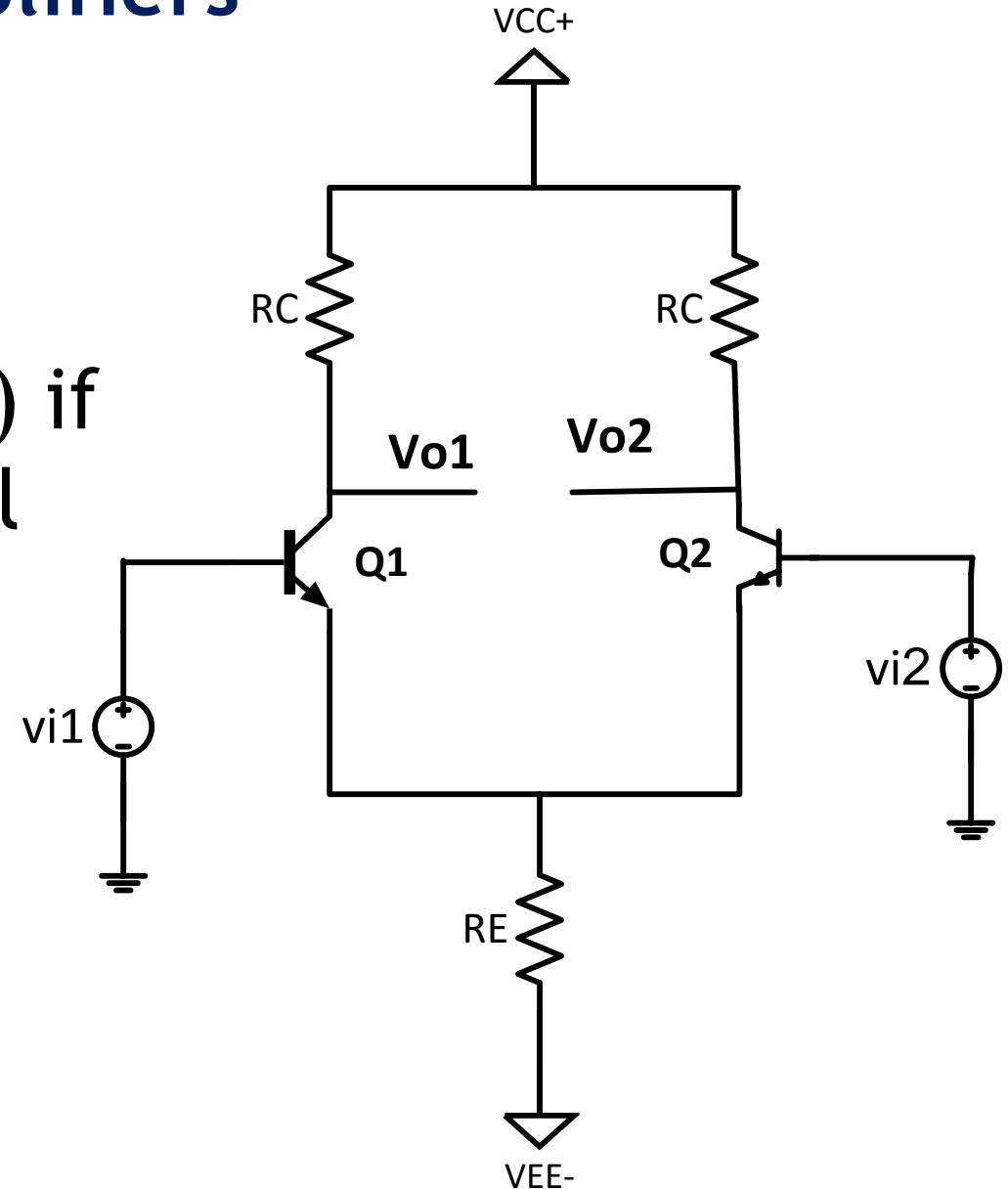
and

$$\frac{v_{c1}}{v_{be1}} = \frac{v_{c2}}{v_{be2}} = -100$$

$$\frac{v_{o1}}{v_{be1}} = \frac{v_{o2}}{v_{be2}} = -100$$

$$\frac{v_{o1}}{v_{be1}} = \frac{v_{o2}}{v_{be2}} = -100$$

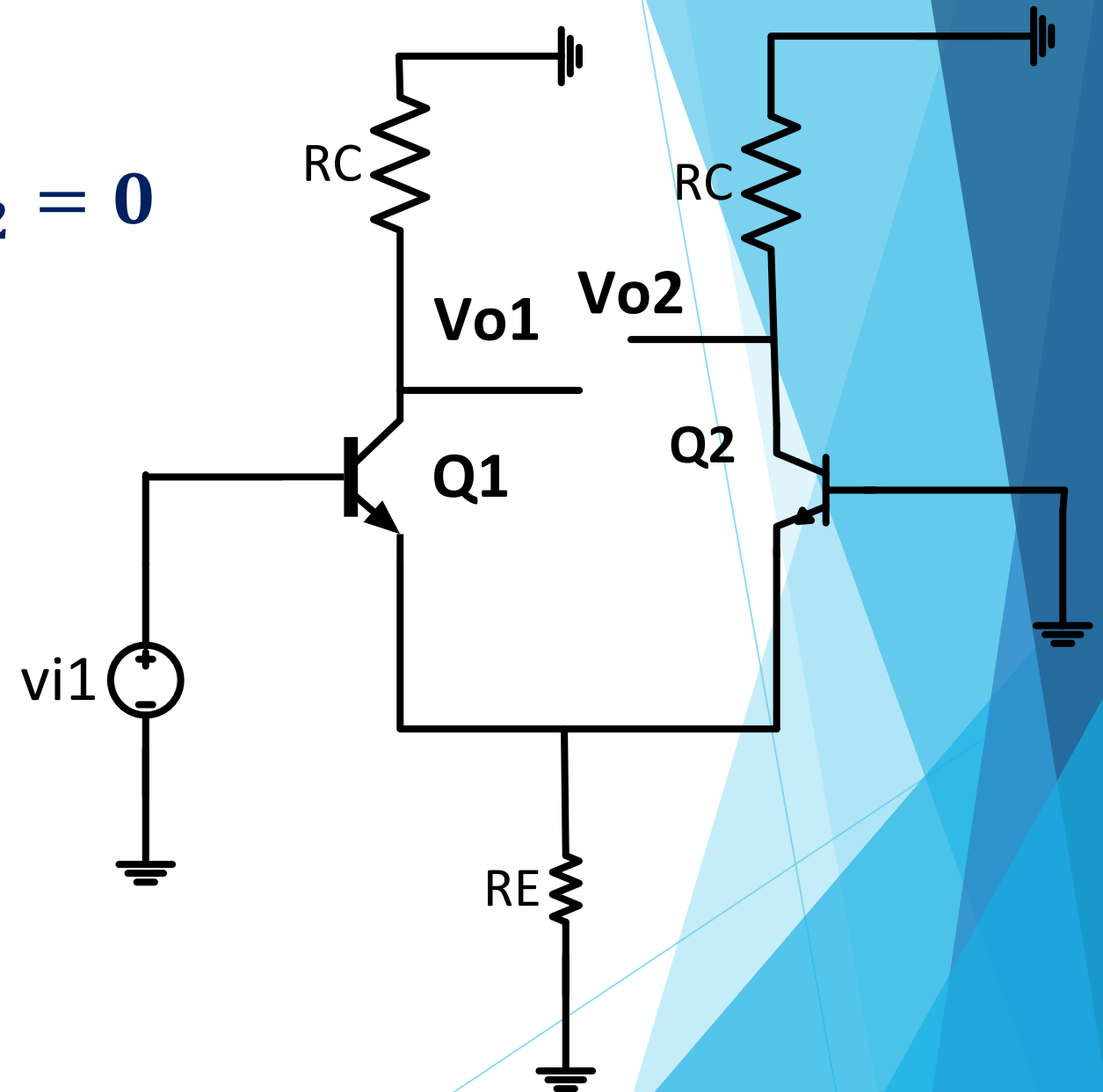
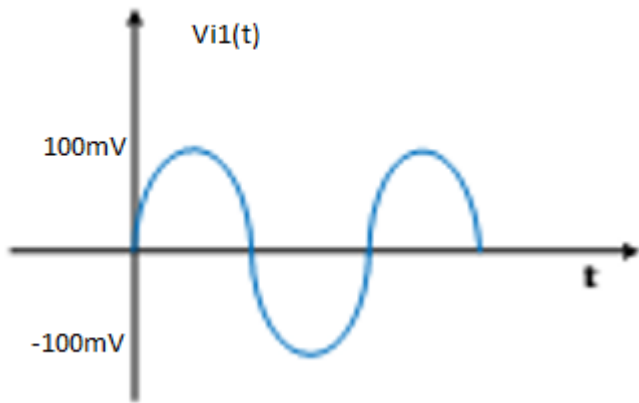
STUDENTS-HUB.COM



Uploaded By: anonymous

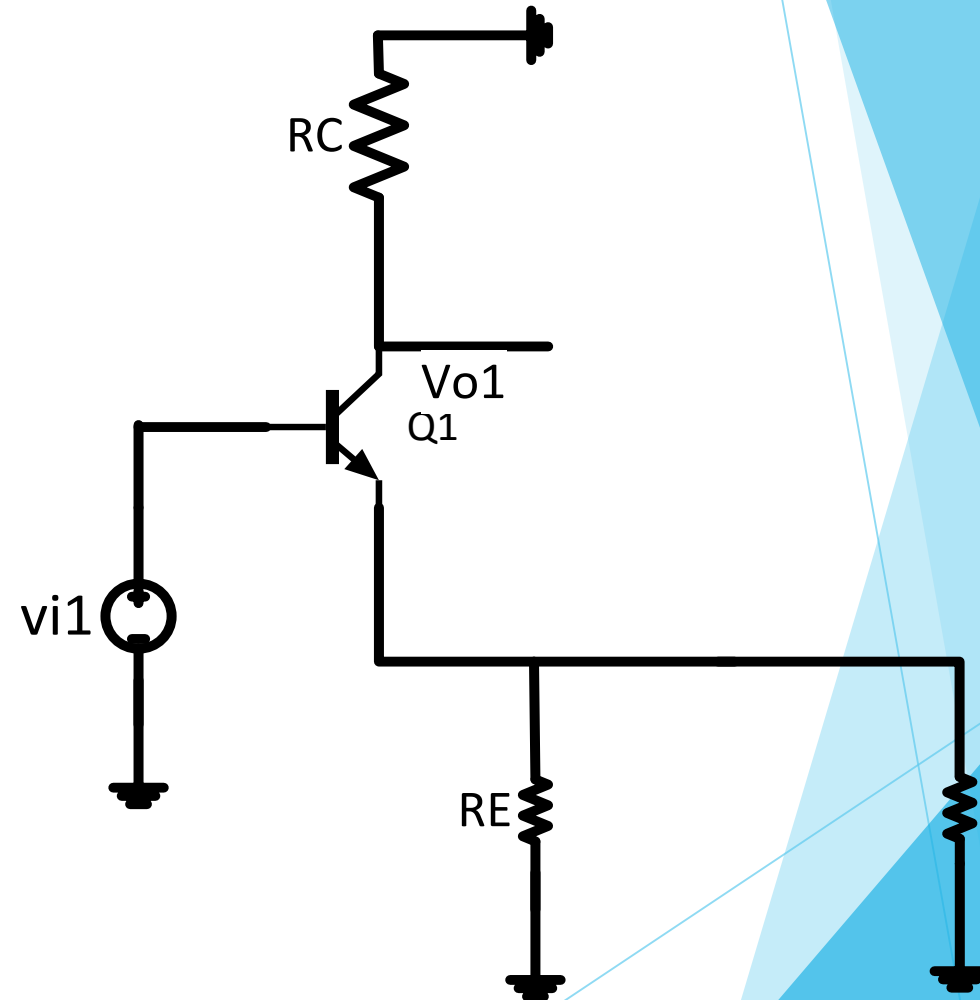
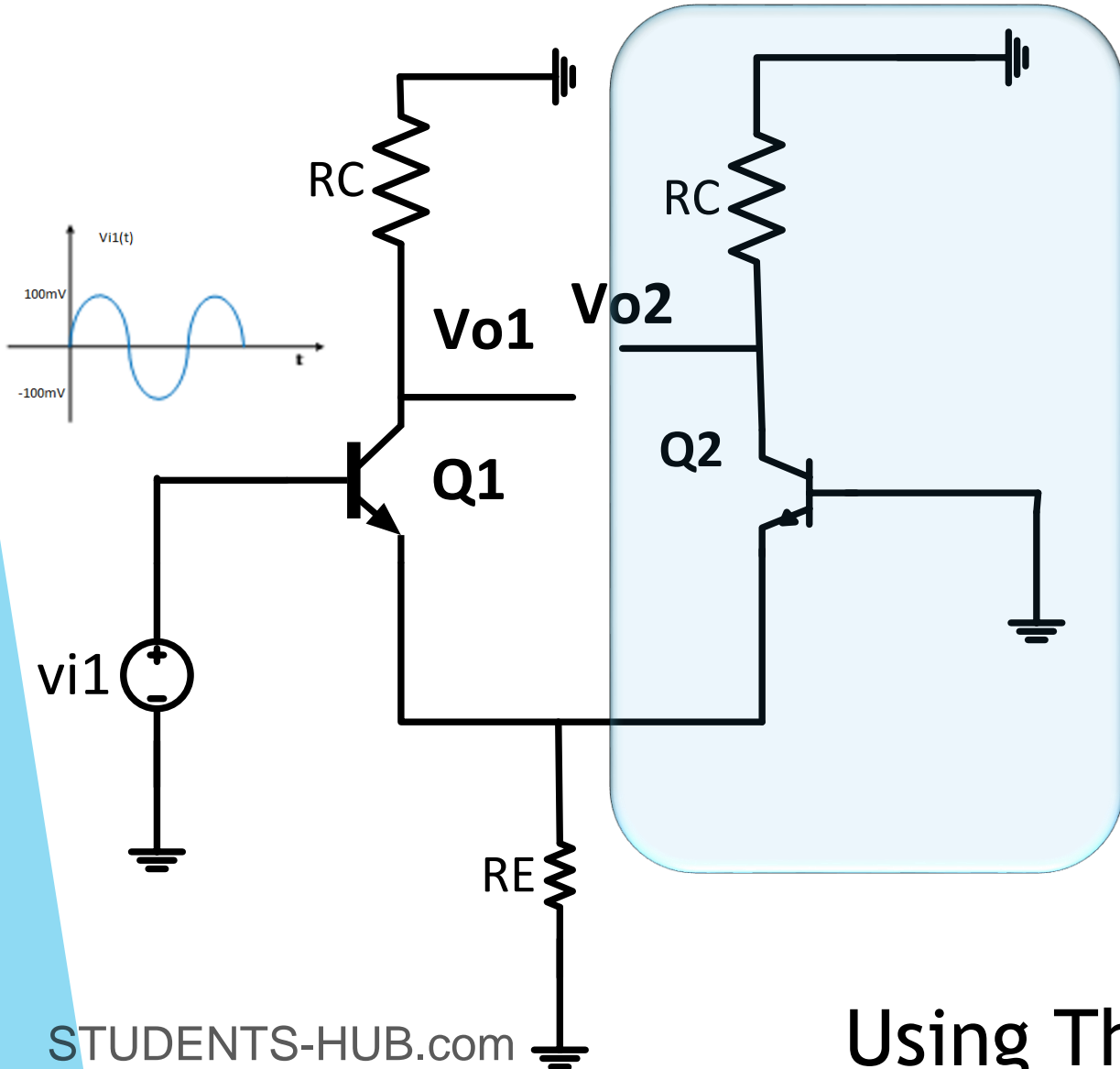
Using superposition

1) *let $v_{i1} = 100\text{ mV peak}$, $v_{i2} = 0$*



Simple Differential Amplifier

1) let $v_{i1} = 100 \text{ mV peak}$, $v_{i2} = 0$

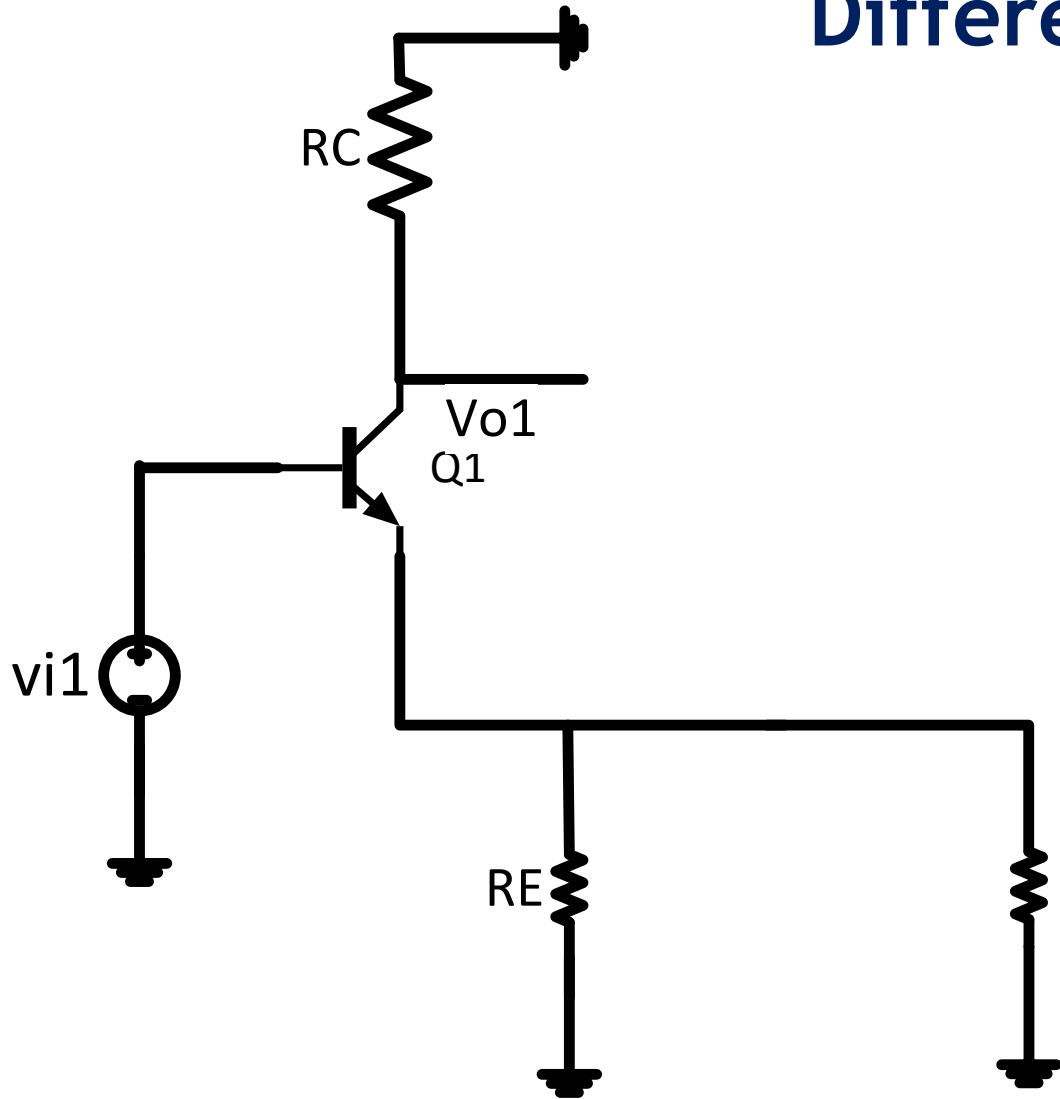


$$\frac{h_{ie2}}{h_{fe+1}} = h_{ib2}$$

Using Thevenin theorem

Uploaded By: anonymous

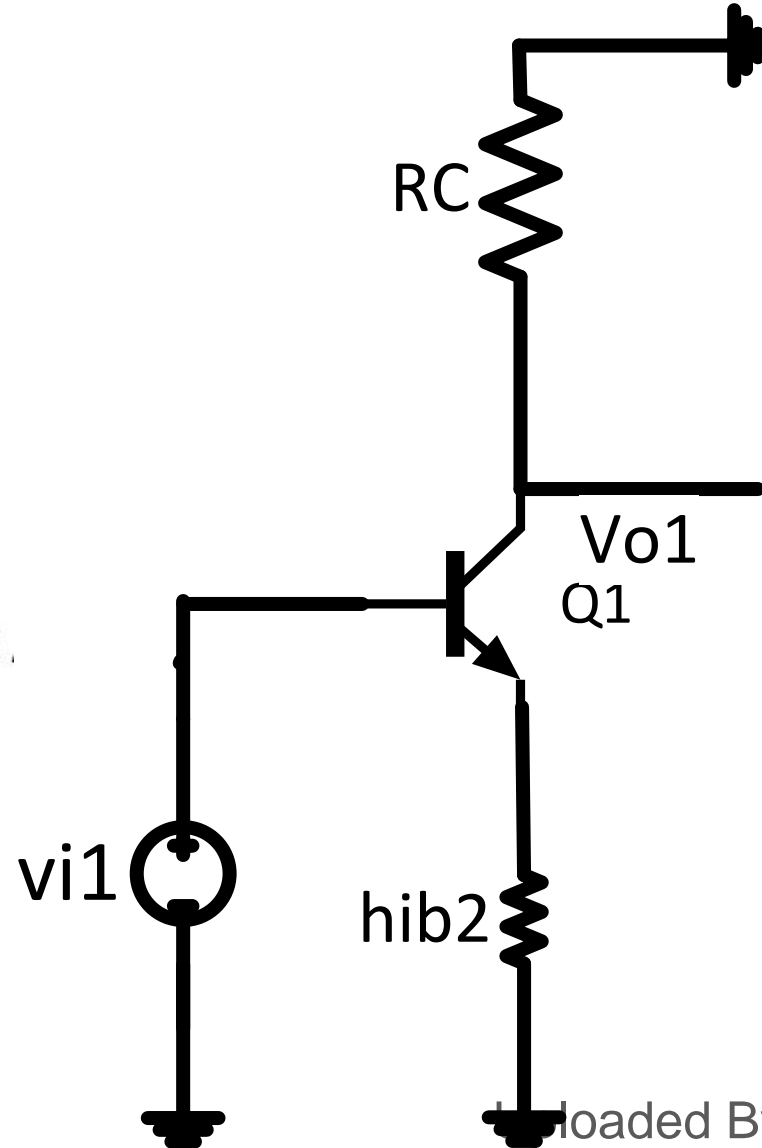
Differential Amplifiers



$$\frac{h_{ie2}}{h_{fe}+1} = h_{ib2}$$

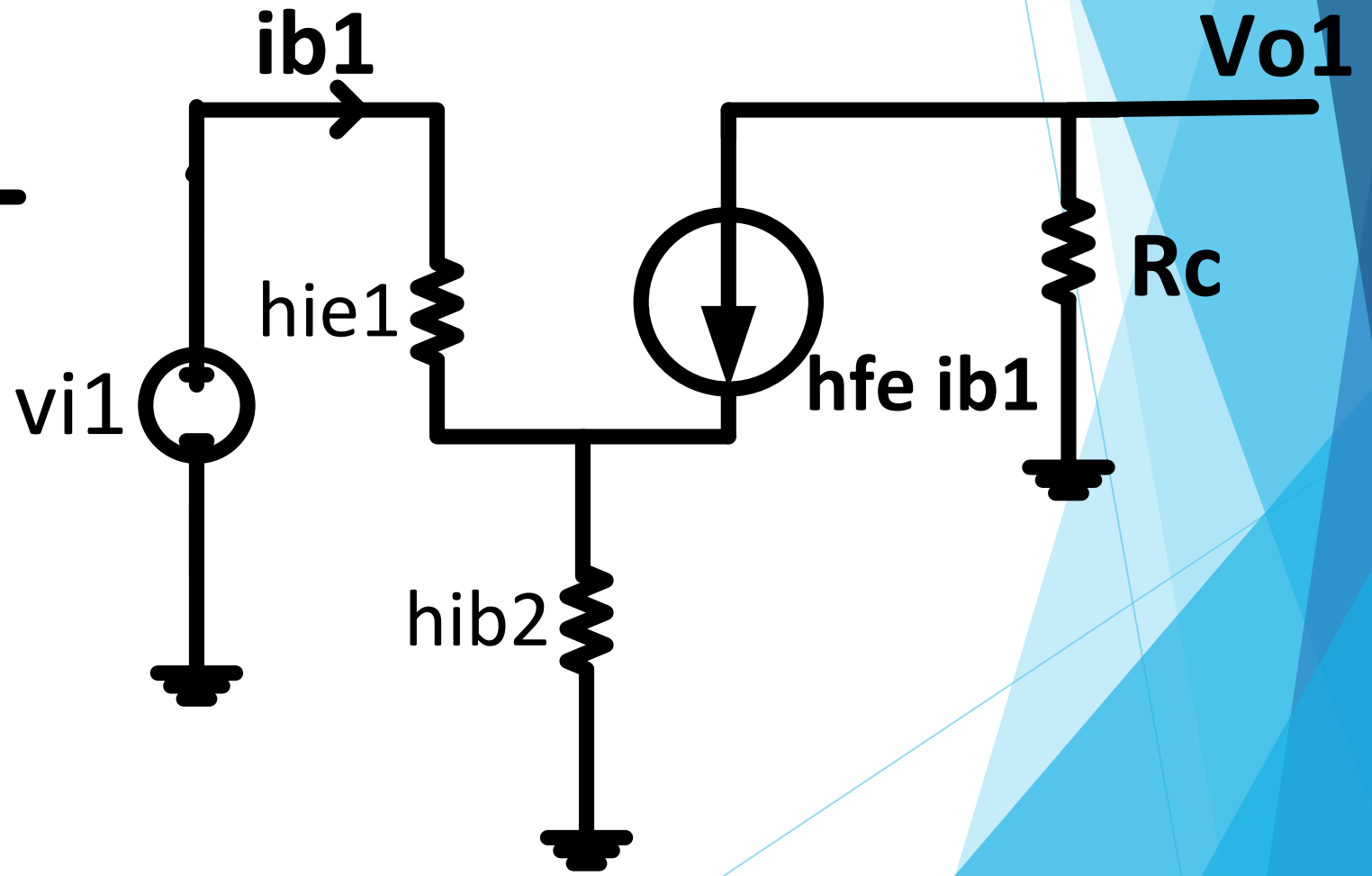
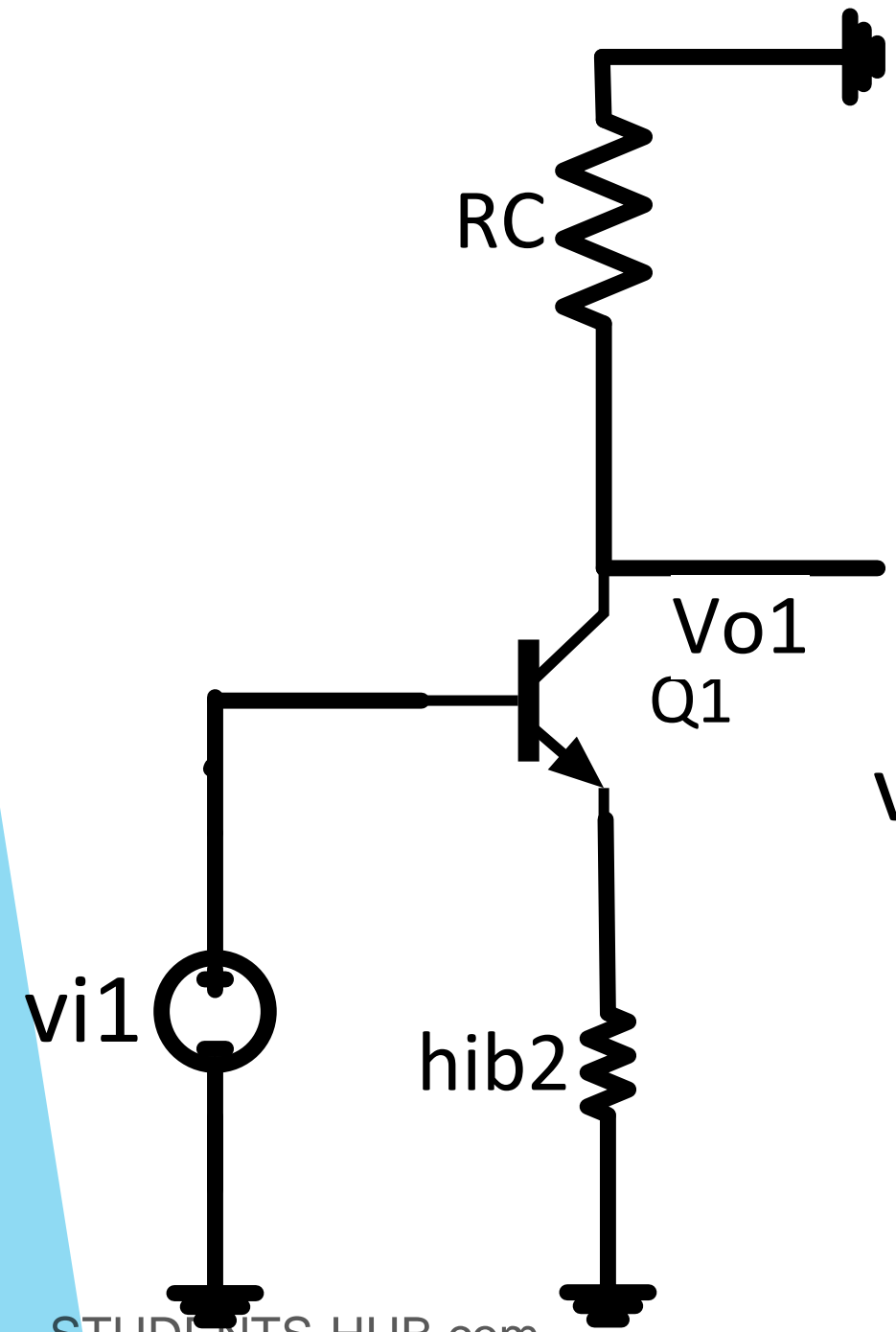
if $R_E \gg h_{ib2}$

$\therefore R_E \parallel h_{ib2} \approx h_{ib2}$



$$\frac{v_{o1}}{v_{be1}} = \frac{v_{o2}}{v_{be2}} = -100$$

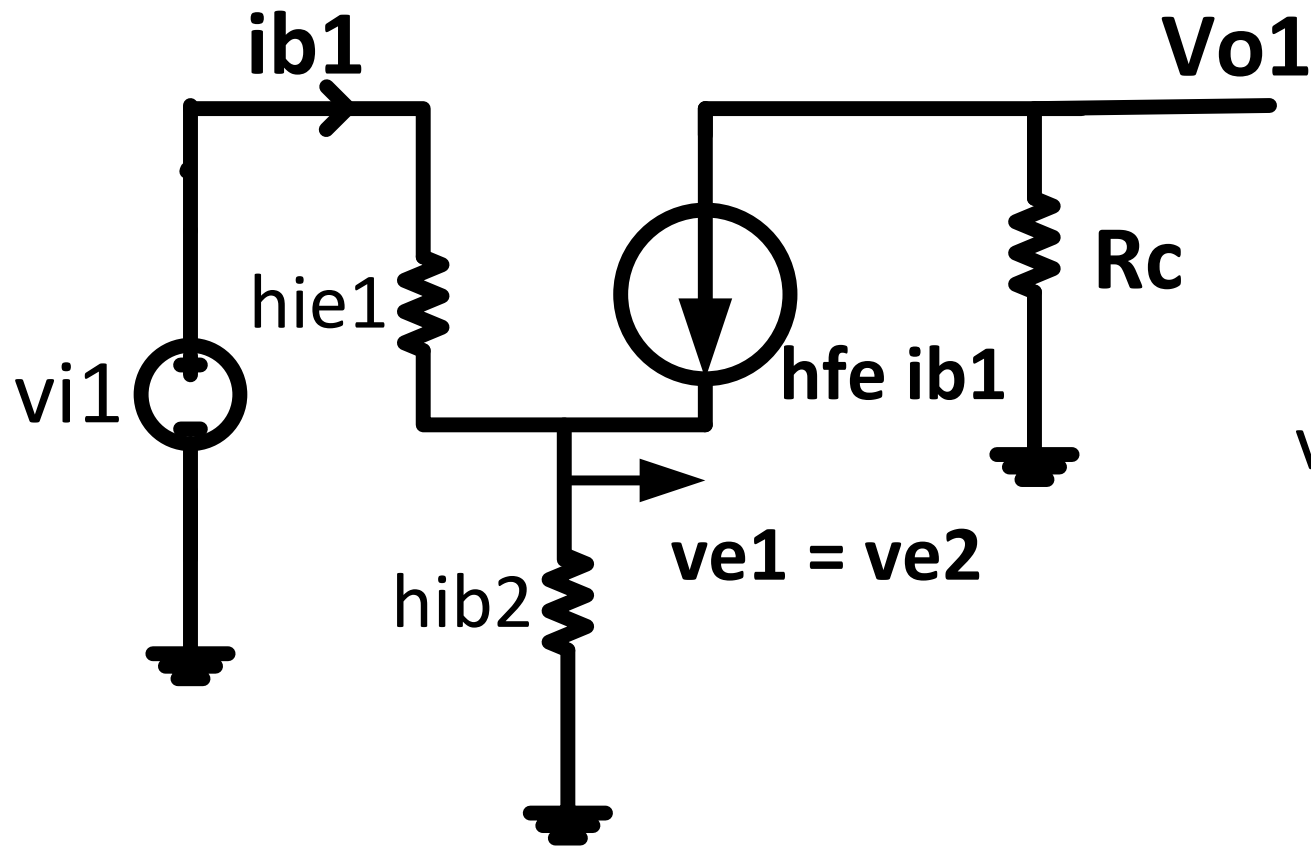
Ac small signal equivalent circuit




Differential Amplifiers

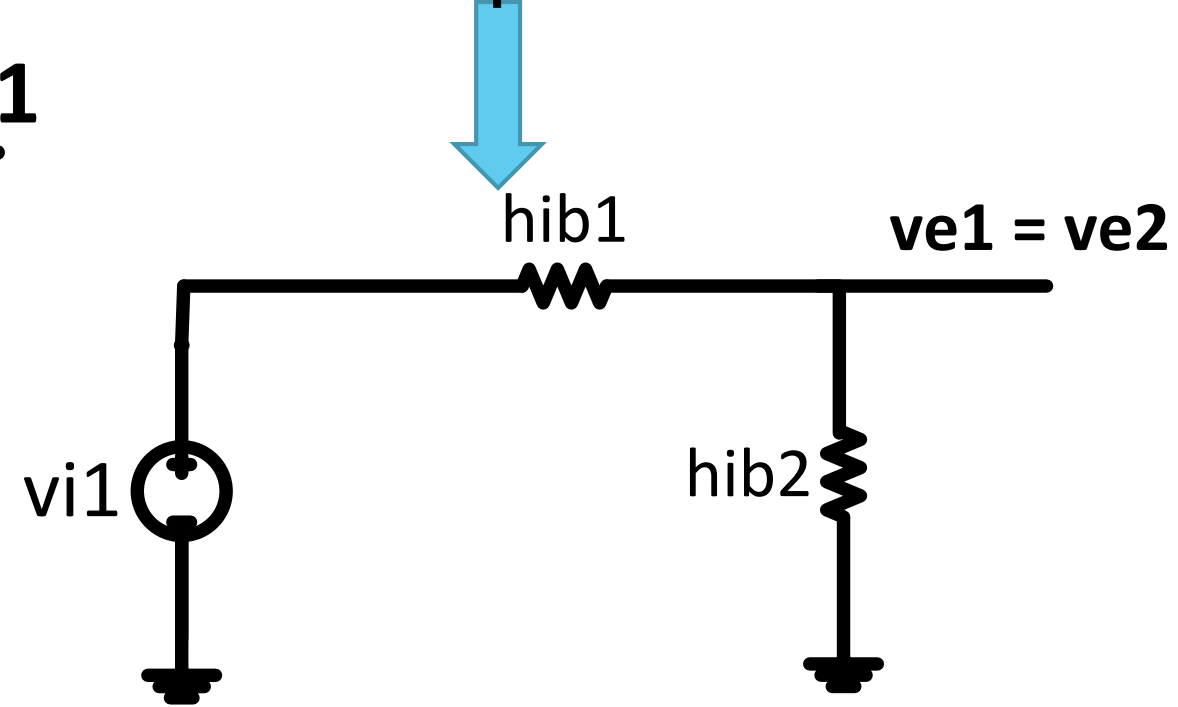
Simple Differential Amplifier

AC Small Signal Analysis:



To find $v_{e1} = v_{e2}$ 

Emitter equivalent circuit



$$v_{e1} = \frac{1}{2} v_{i1} = 50 \text{ mV peak}$$

Differential Amplifiers

$$\frac{v_{o1}}{v_{be1}} = \frac{v_{o2}}{v_{be2}} = -100$$

AC Small Signal Analysis:

$$v_{e1} = v_{e2} = \frac{1}{2} v_{i1} = 50 \text{ mV peak}$$

$$v_{be1} = v_{b1} - v_{e1}$$

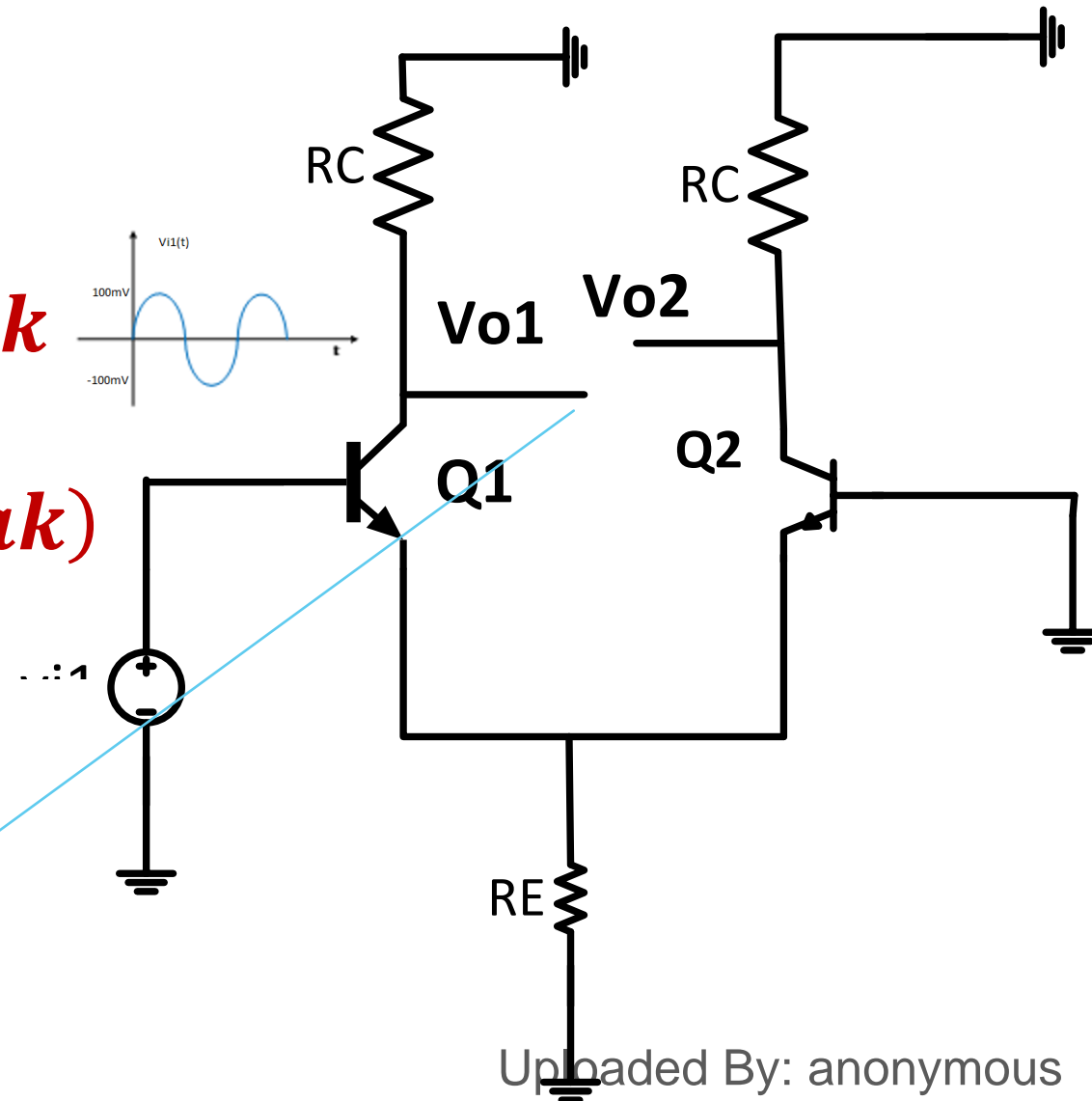
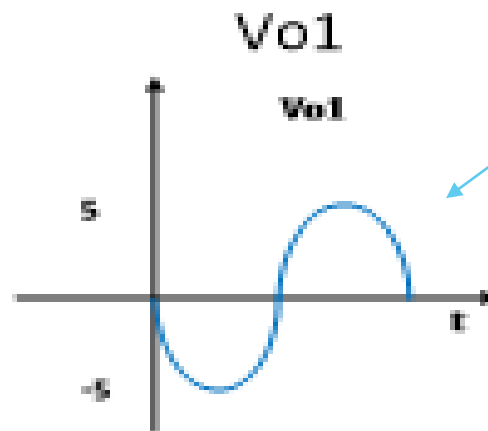
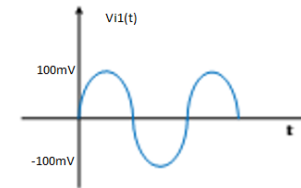
$$v_{be1} = 100 \text{ mV peak} - 50 \text{ mV peak}$$

$$v_{be1} = 50 \text{ mV peak}$$

$$\therefore v_{c1} = v_{o1} = (-100)(50 \text{ mV peak})$$

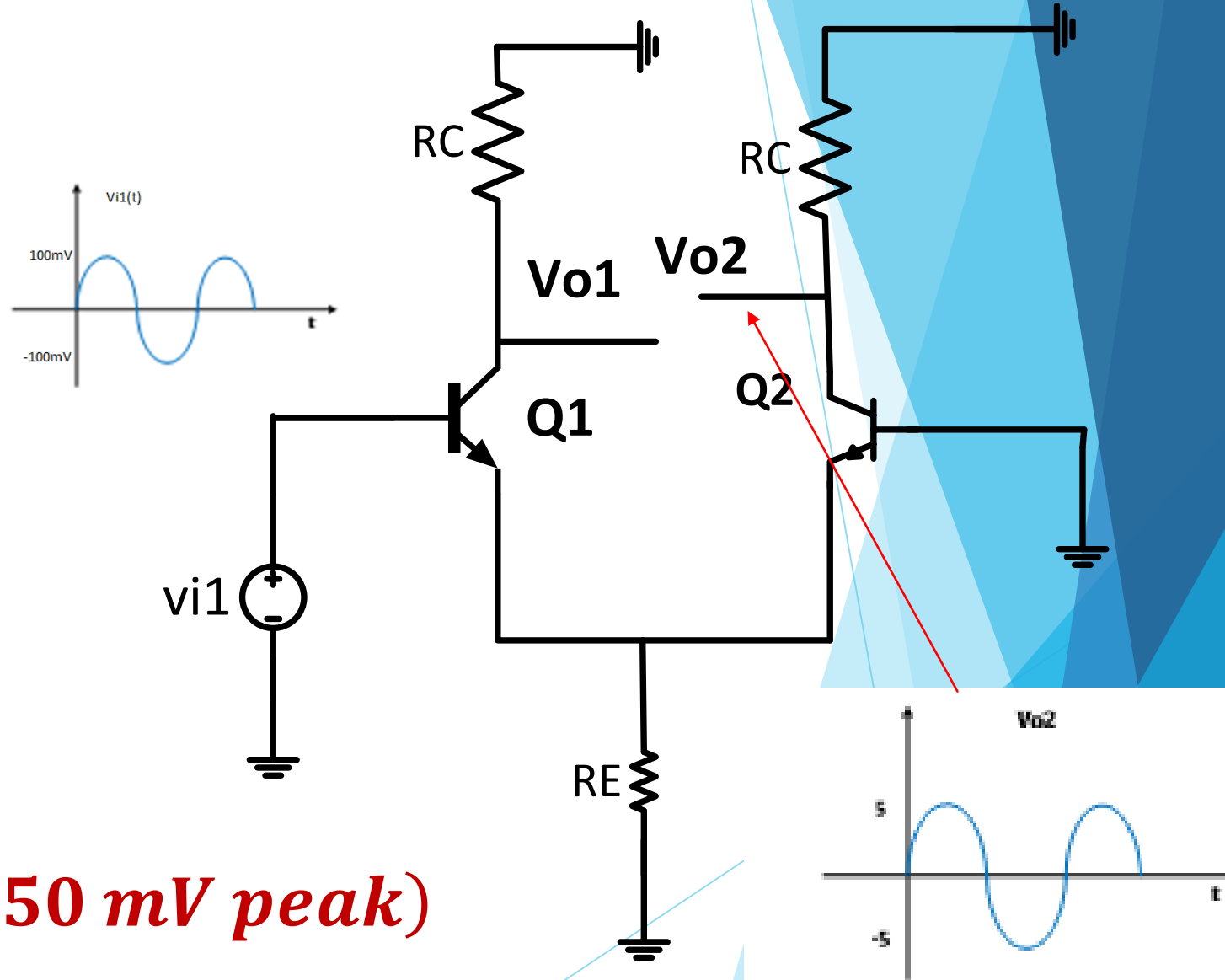
$$\therefore v_{c1} = -5 \text{ V peak}$$

$$v_{o1} = -5 \text{ V peak}$$



$$\frac{v_{o2}}{v_{be2}} = -100$$

- ▶ *to find $v_{c2} = v_{o2}$,*
- ▶ *we need to find v_{be2}*
- ▶ *$v_{be2} = v_{b2} - v_{e2}$*
- ▶ *$= v_{b2} - v_{e2}$*
- ▶ *$v_{be2} = 0 - 50 \text{ mV peak}$*
- ▶ *$v_{be2} = -50 \text{ mV peak}$*
- ▶ *$\therefore v_{o2} = v_{c2} = (-100)(-50 \text{ mV peak})$*
- ▶ *$v_{o2} = +5 \text{ V peak}$*



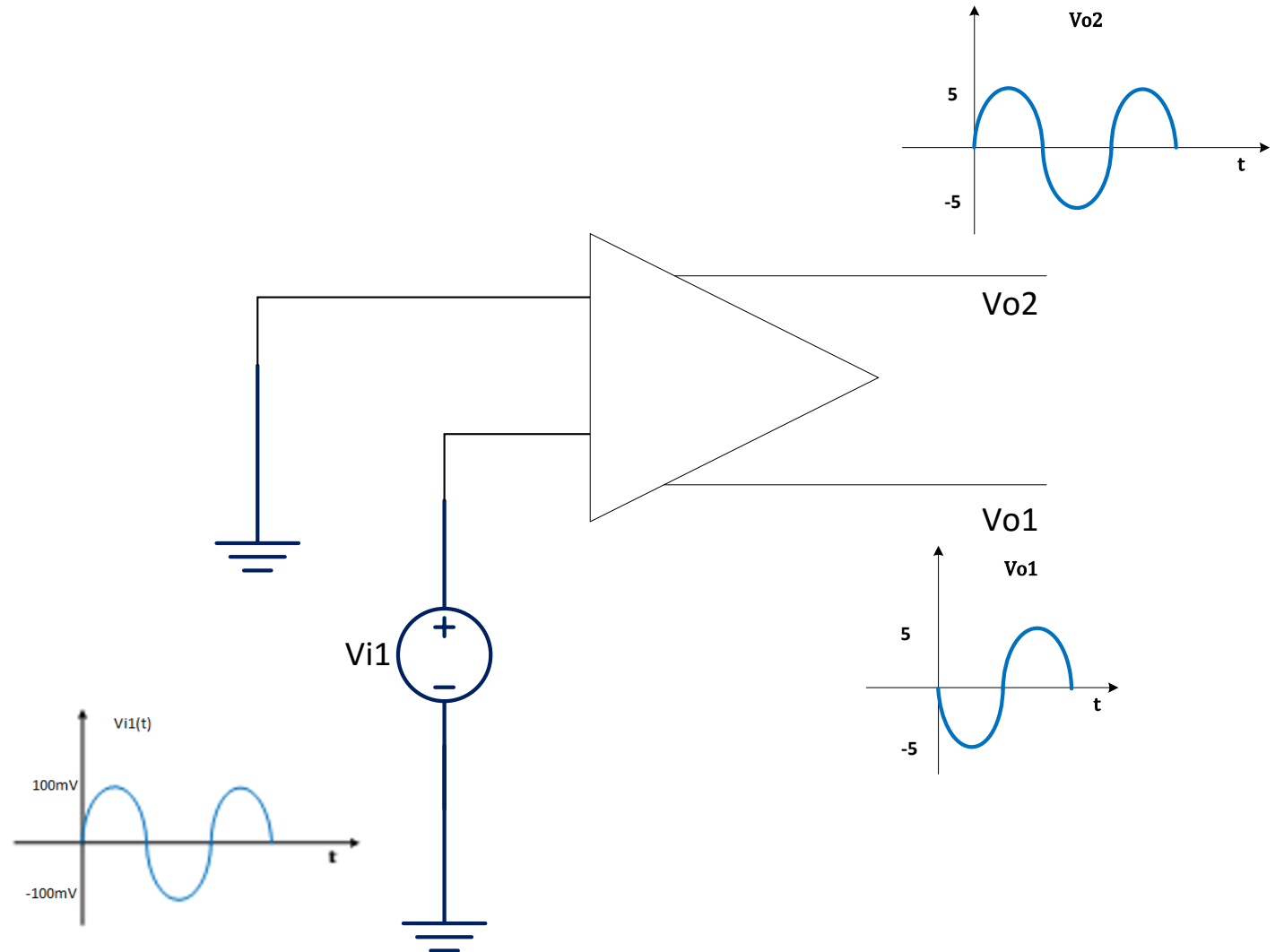
Differential Amplifiers

Simple Differential Amplifier

AC Small Signal Analysis:

$$v_{o1} = -5 V \text{ peak}$$

$$v_{o2} = +5 V \text{ peak}$$



Differential Amplifiers

AC Small Signal Analysis:

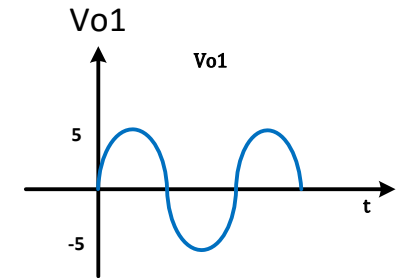
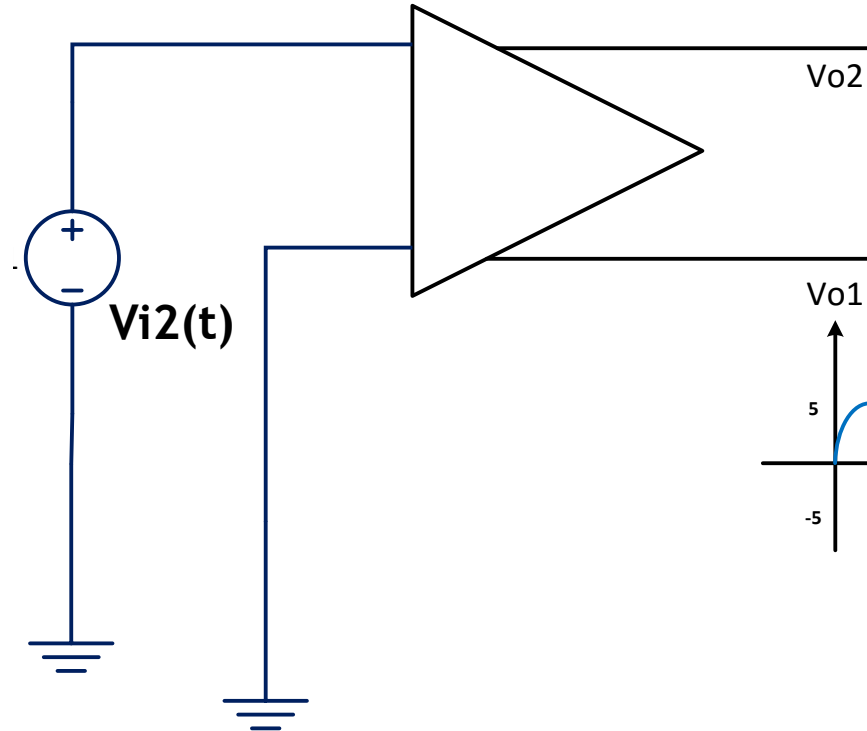
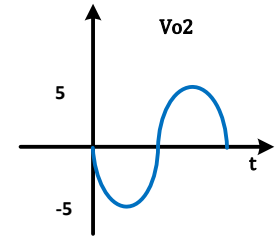
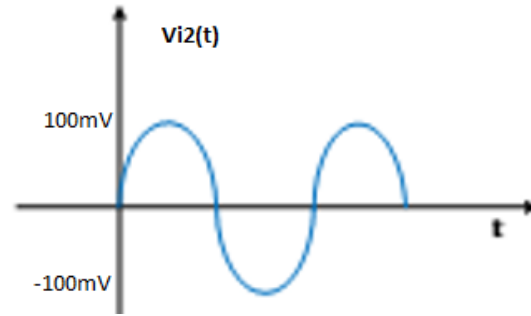
Using same steps for

$$v_{i2} = 100 \text{ mV peak}$$

$$v_{i1} = 0$$

$$v_{o1} = +5 \text{ V peak}$$

$$v_{o2} = -5 \text{ V peak}$$



Differential Amplifiers

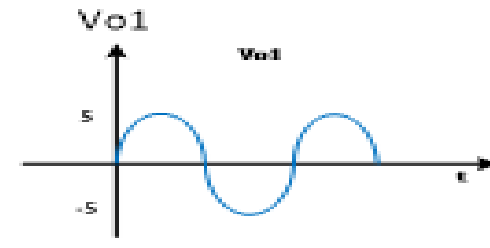
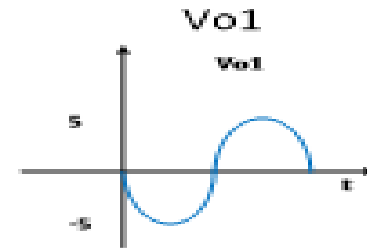
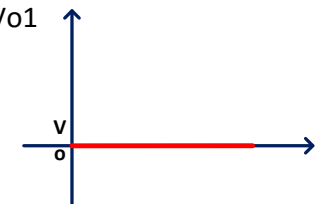
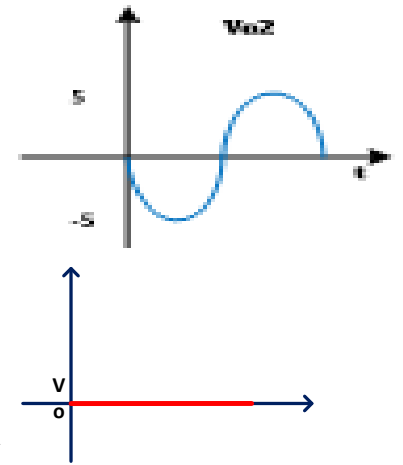
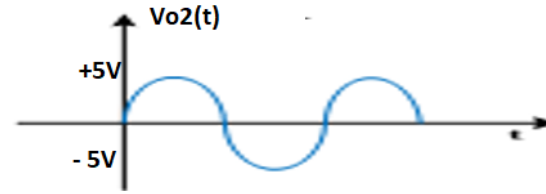
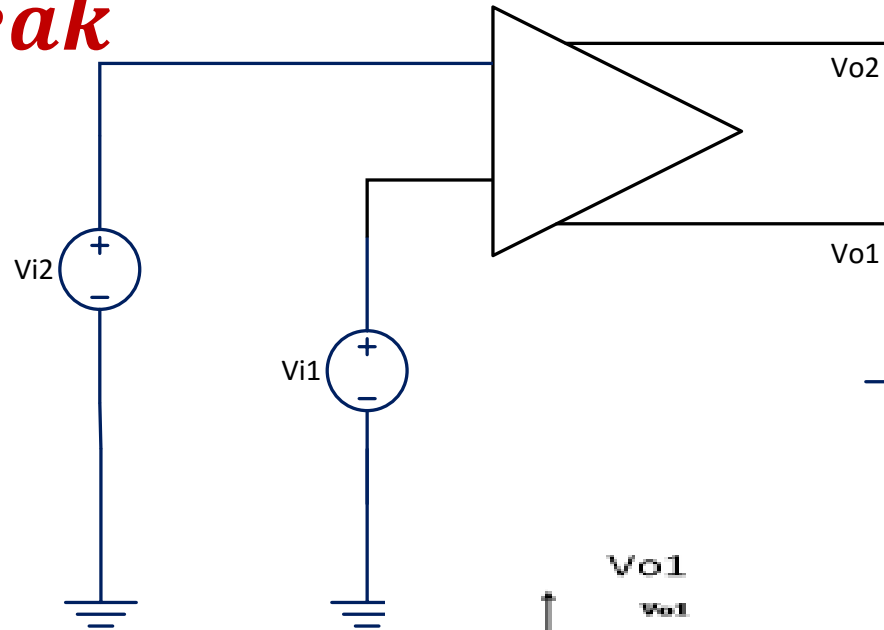
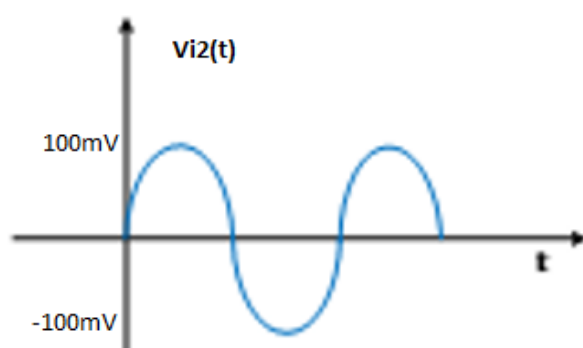
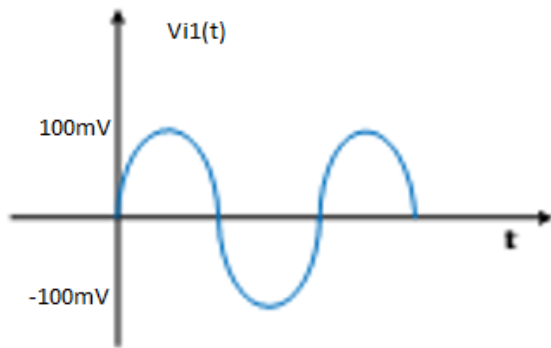
Simple Differential Amplifier

AC Small Signal Analysis:

now if $v_{i1} = v_{i2} = 100 \text{ mV peak}$

$$v_{o1} = 0$$

$$v_{o2} = 0$$



Differential Amplifiers

Simple Differential Amplifier

AC Small Signal Analysis:

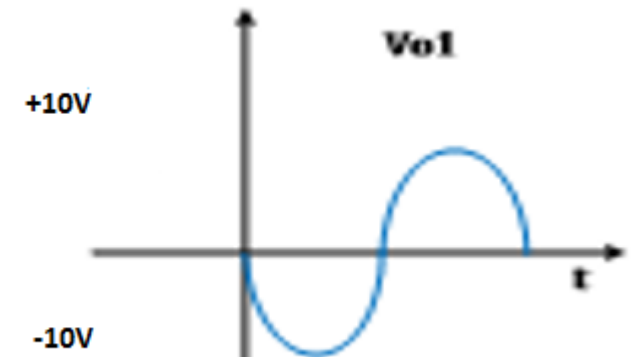
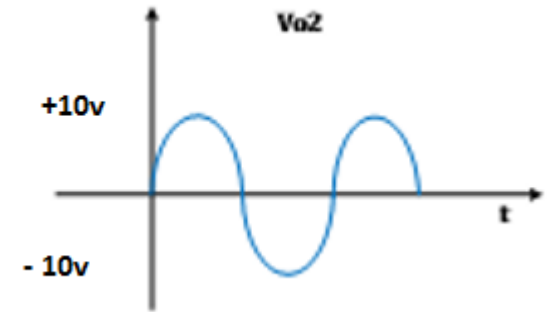
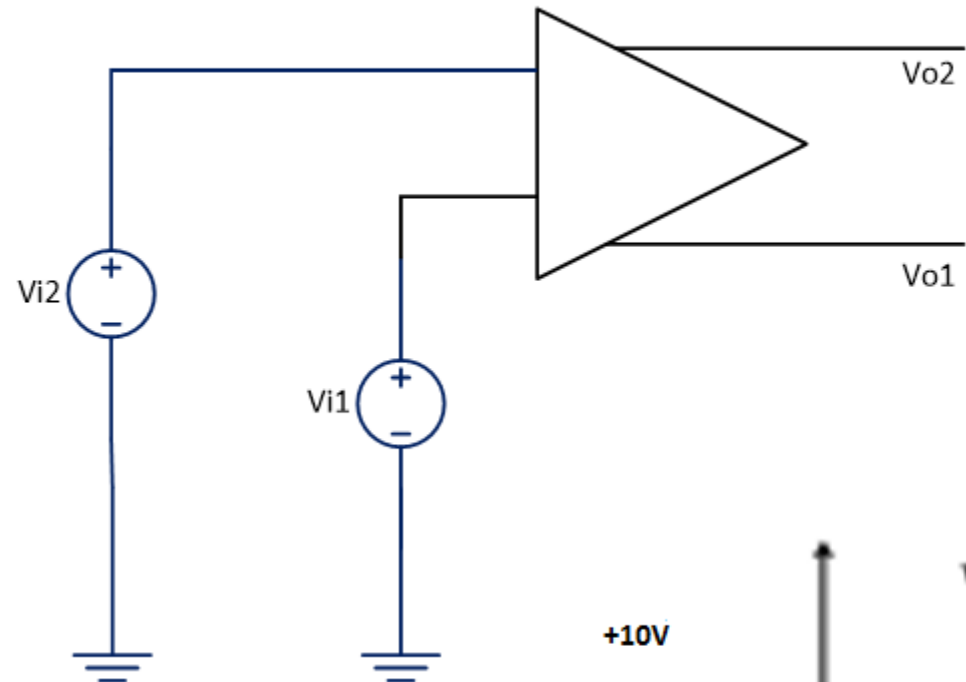
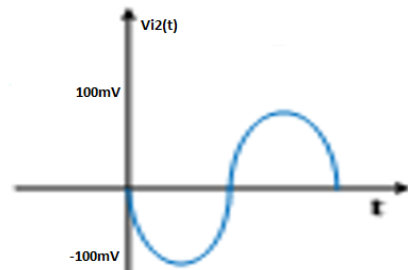
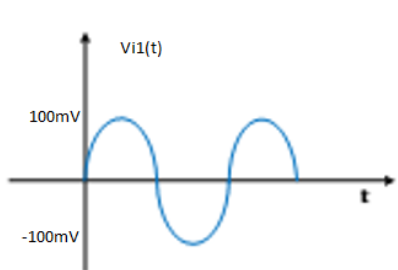
Using same steps for

$$v_{i1} = 100 \text{ mV peak}$$

$$v_{i2} = -100 \text{ mV peak}$$

$$v_{o2} = +10 \text{ V peak}$$

$$v_{o1} = -10 \text{ V peak}$$



Differential Amplifier Circuit:

Common Mode & Differential mode Signal

Since the differential amplifier is most often used to amplify the difference between two input signals.

$$\text{let } v_d = v_{i2} - v_{i1}$$

$v_d \equiv$ *Differential mode input signal*

$$\text{let } v_c = \frac{v_{i2} + v_{i1}}{2}$$

$v_c \equiv$ *Common mode input signal*

$$\therefore v_{i2} = v_c + \frac{v_d}{2}$$

$$v_{i1} = v_c - \frac{v_d}{2}$$

Differential Amplifiers

Differential Amplifier Circuit:

Common Mode & Differential mode Signal

Input voltage can be represented in terms of a common mode and differential mode input signals.

In the usual application of the differential amplifier, the differential mode input is desired and to be amplified, while the common mode input is to be rejected.

Differential Amplifier Circuit:

DC Analysis: $\rightarrow v_{i1} = v_{i2} = 0$

$$R_S I_{B1} + V_{BE1} + R_E I - 12 = 0$$

$$I = I_{E1} + I_{E2}$$

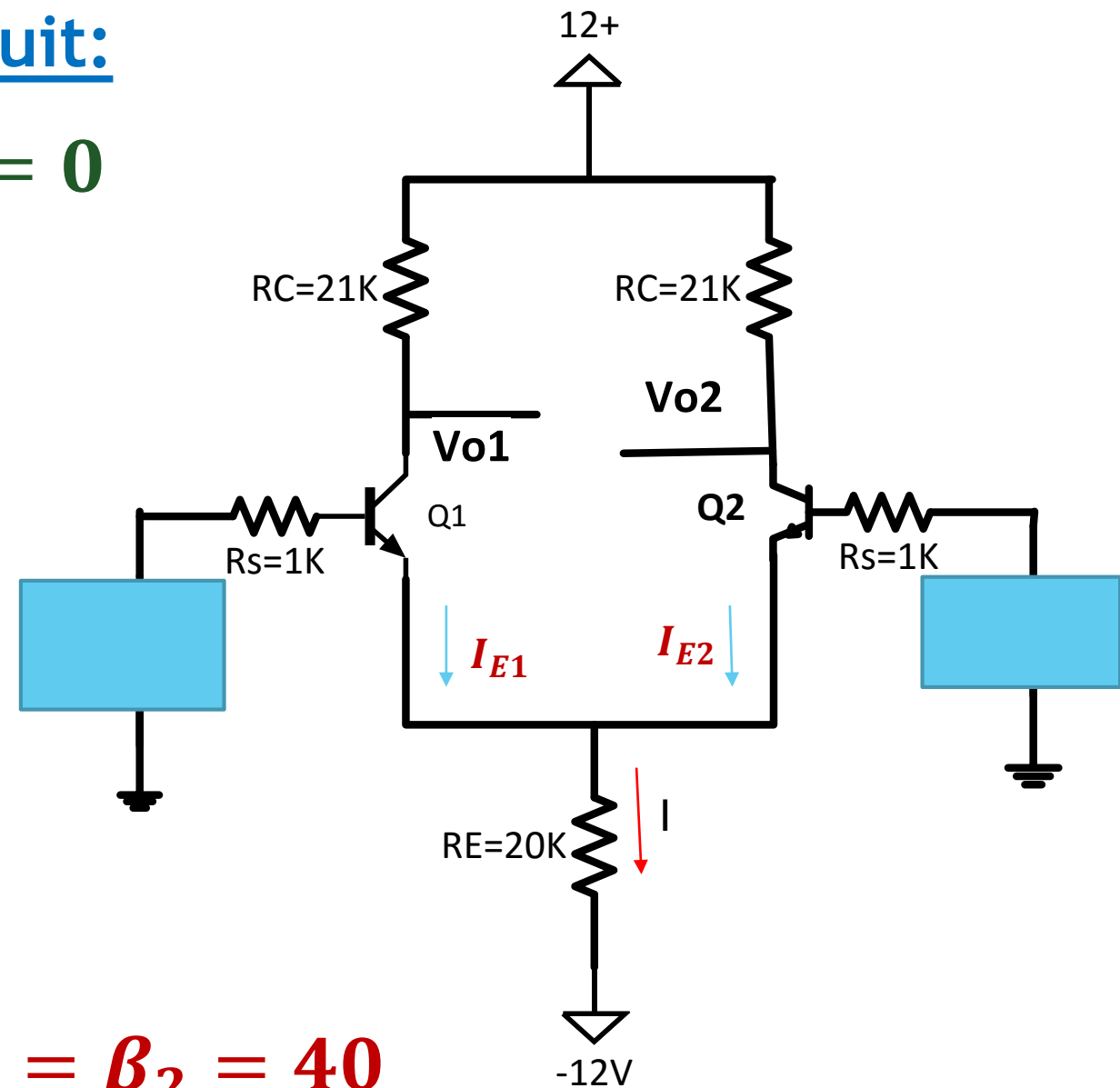
$$I_{E1} = I_{E2} \text{ [symmetry]}$$

$$I_{E1} = I_{E2} = \frac{12 - 0.7}{\frac{1k}{41} + (2)(20k)}$$

$$= 0.2825 \text{ mA}$$

$$\beta_1 = \beta_2 = 40$$

Q_1 and Q_2 identical



Differential Amplifiers

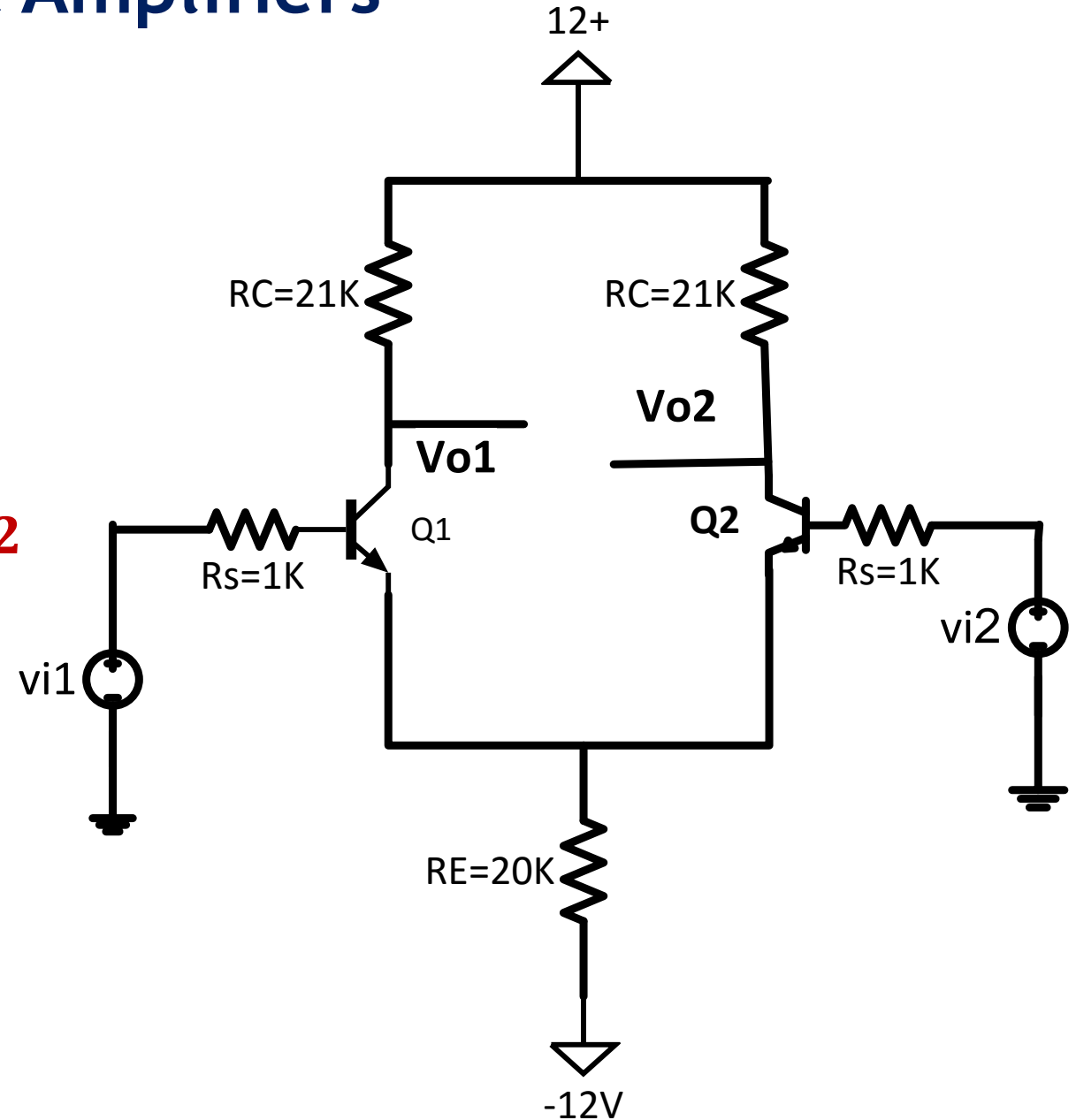
Differential Amplifier Circuit:

AC Analysis:

since $I_{E1} = I_{E2}$ and $\beta_1 = \beta_2$

$$h_{ie1} = h_{ie2} = h_{ie}$$

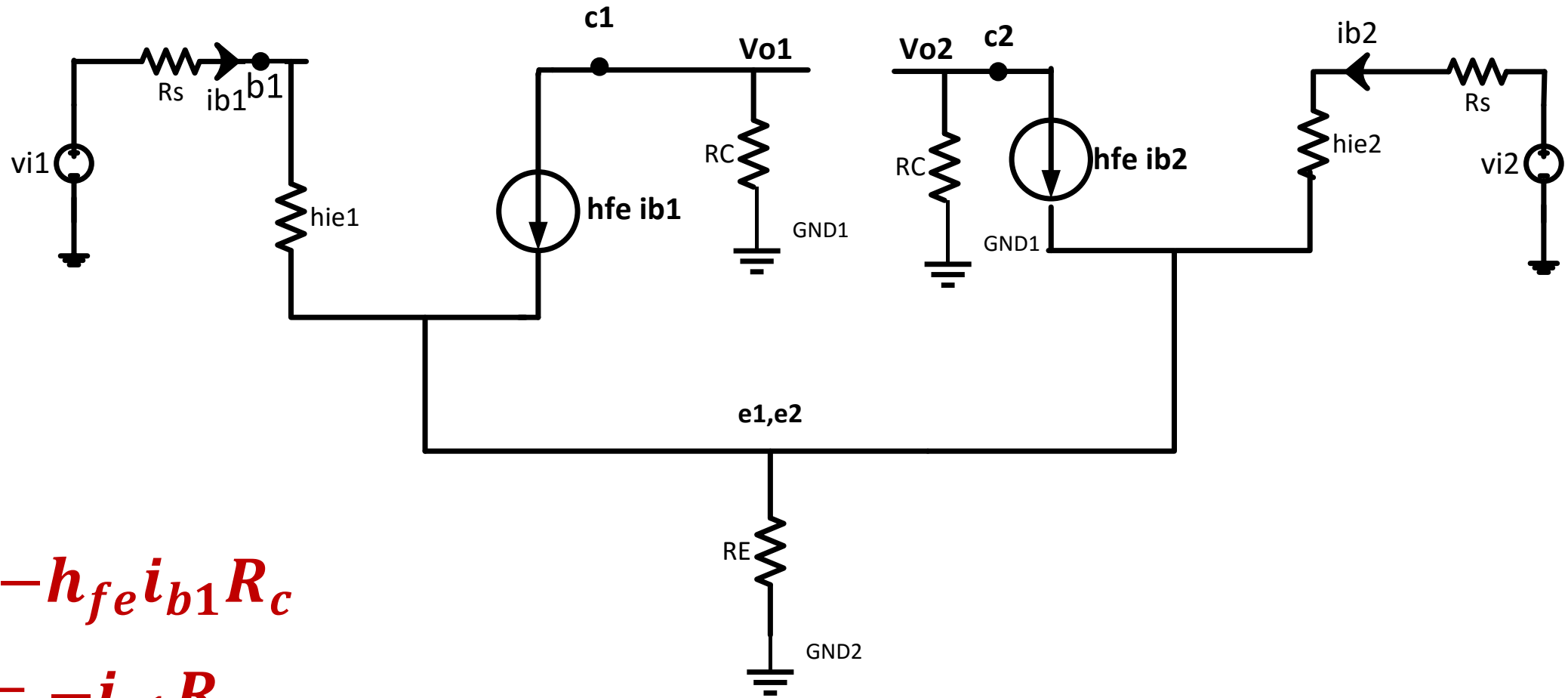
$$h_{ib1} = h_{ib2} = h_{ib}$$



Differential Amplifiers

Differential Amplifier Circuit:

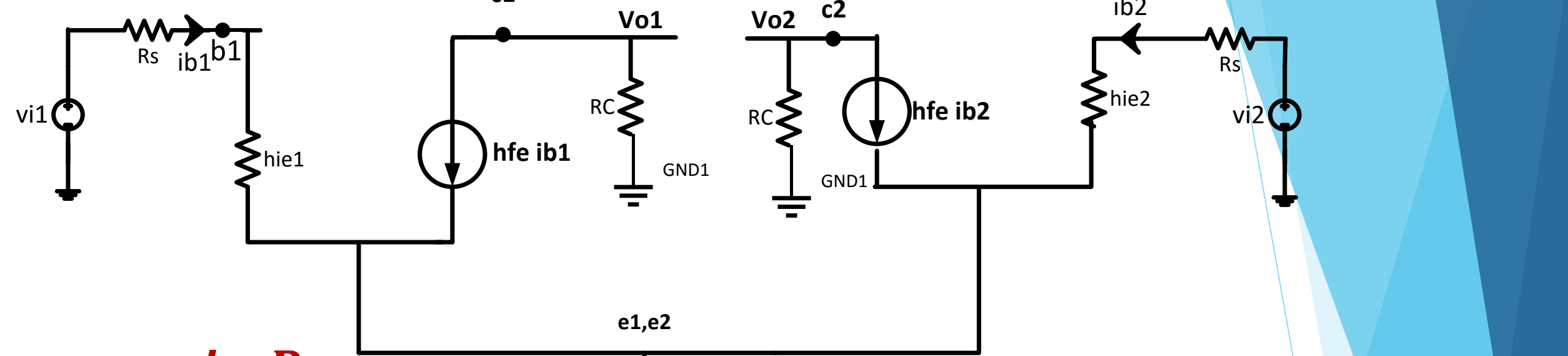
AC Analysis:



$$v_{o1} = -h_{fe}i_{b1}R_c$$

$$v_{o1} = -i_{c1}R_c$$

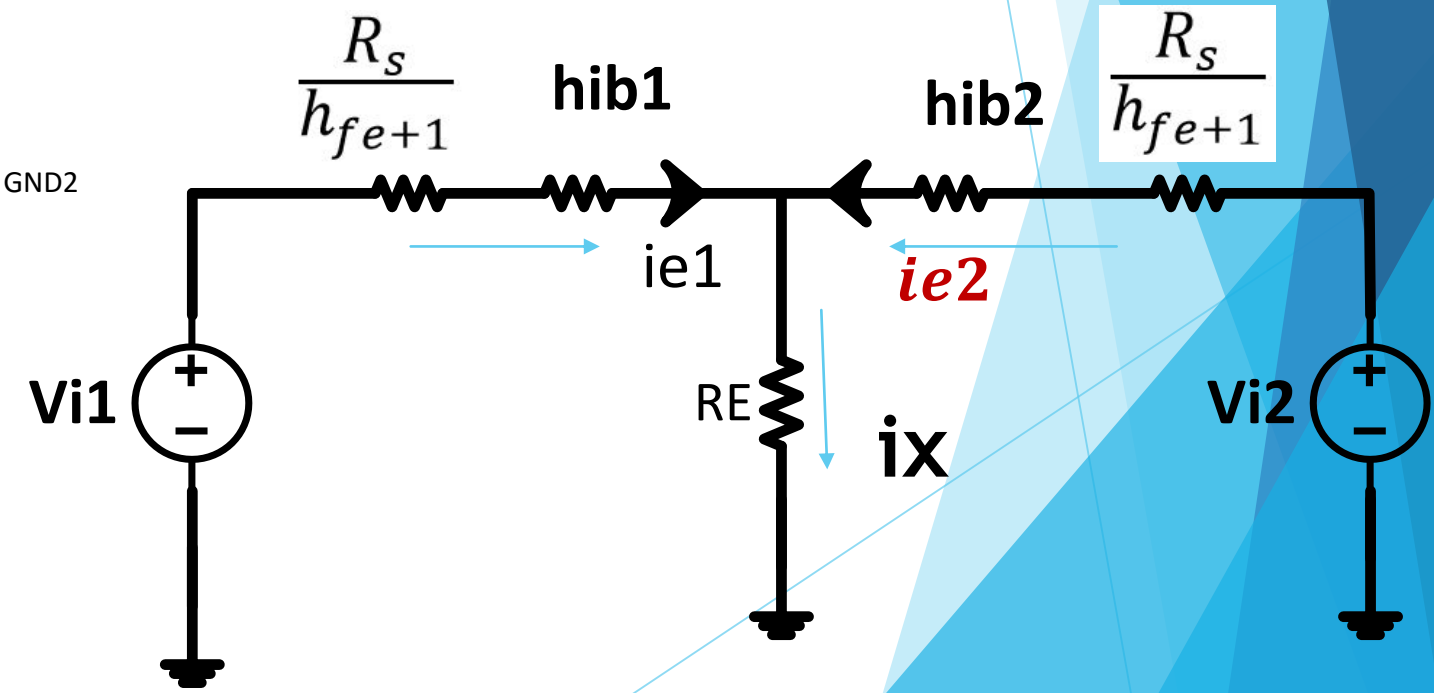
$$v_{o1} \approx -i_{e1}R_c$$



$v_{o1} \approx -i_{e1}R_c$

To find i_{e1}

Emitter equivalent circuit



Differential Amplifiers

Differential Amplifier Circuit:

Small Signal Analysis

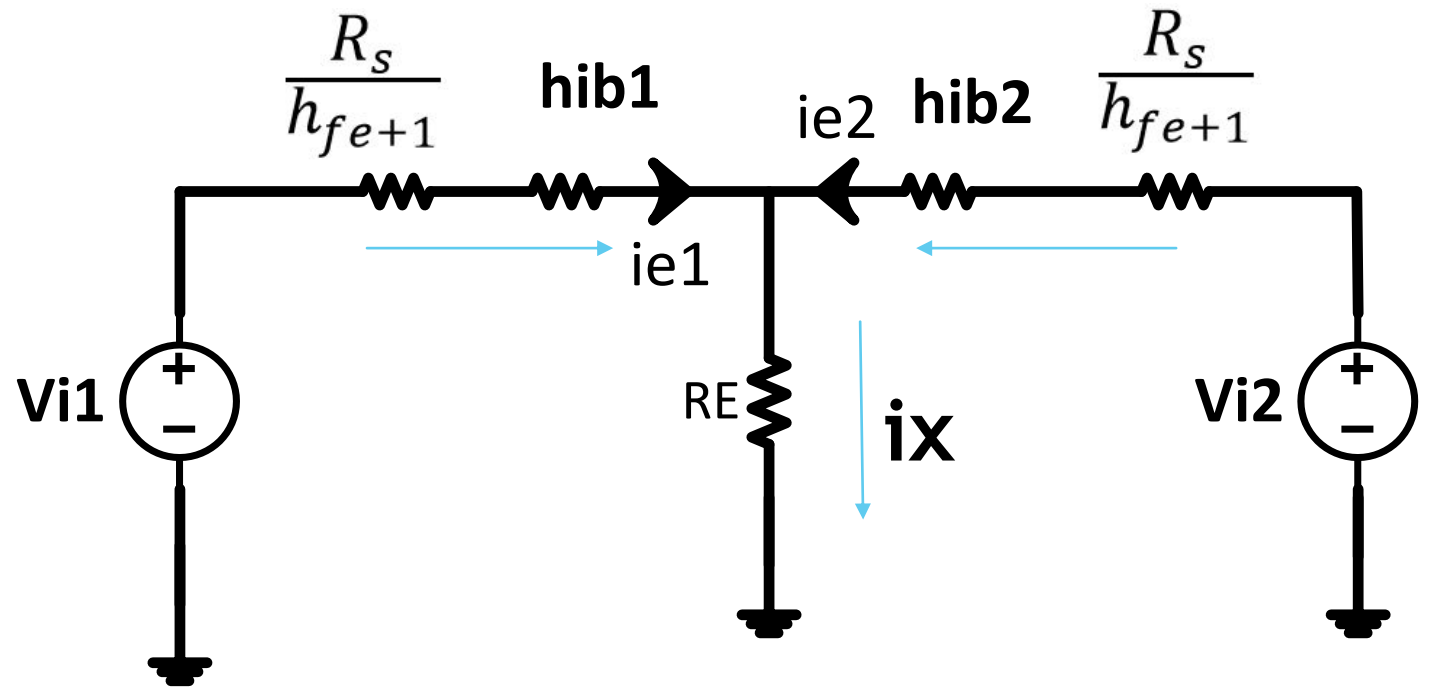
To find $ie1$ →

Using emitter equivalent ckt

$$v_{i1} = v_c - \frac{v_d}{2}$$

$$v_{i2} = v_c + \frac{v_d}{2}$$

$$v_{o1} \cong -ie1 \cdot Rc$$



Differential Amplifiers

$$v_{o1} \cong -ie1.Rc$$

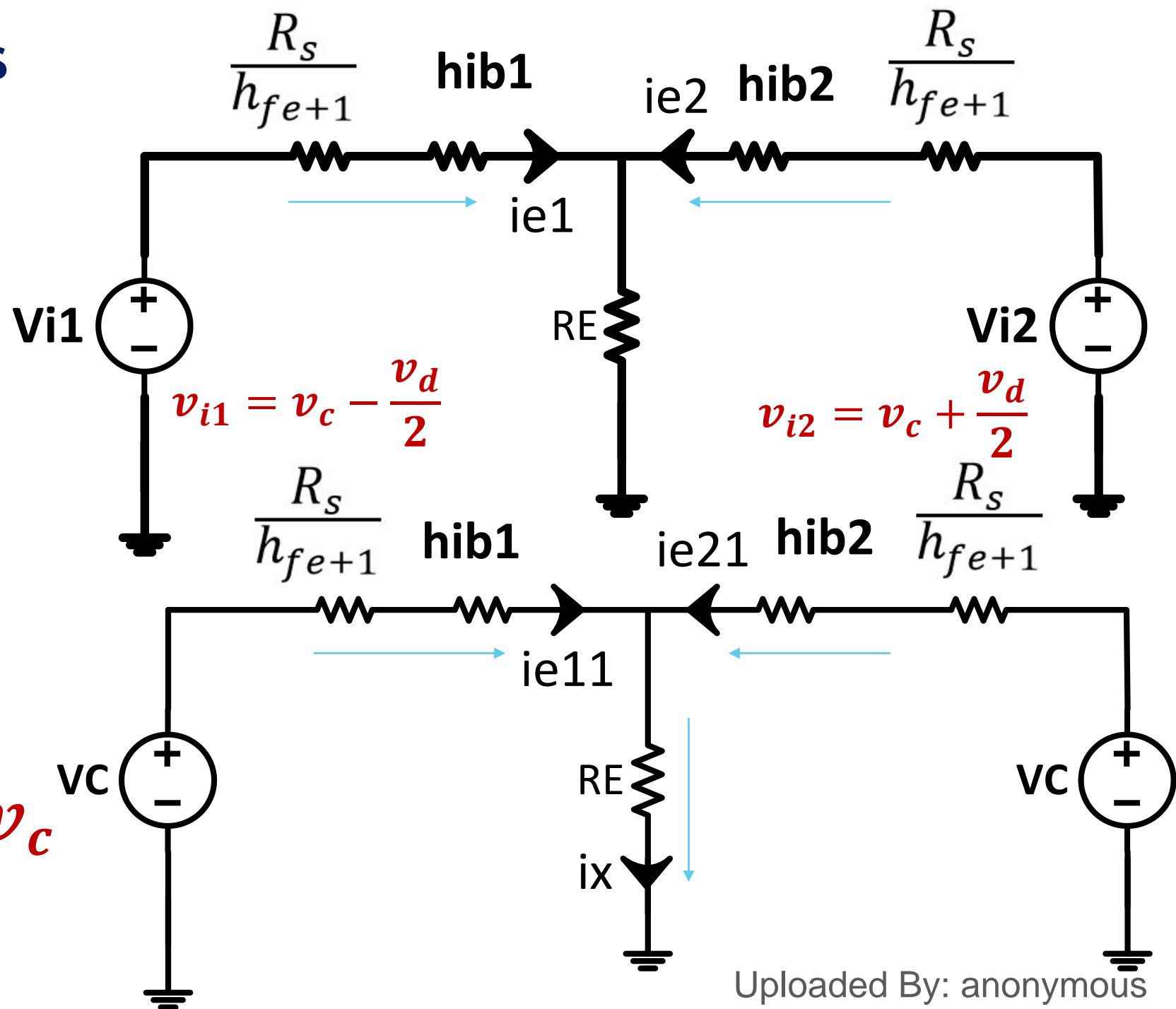
Using Superposition

$$ie1 = ie11 + ie12$$

To find $ie11$

let $v_d = 0$

$$v_{i1} = v_c ; v_{i2} = v_c$$



Differential Amplifiers

Small Signal Analysis

Using emitter equivalent ckt

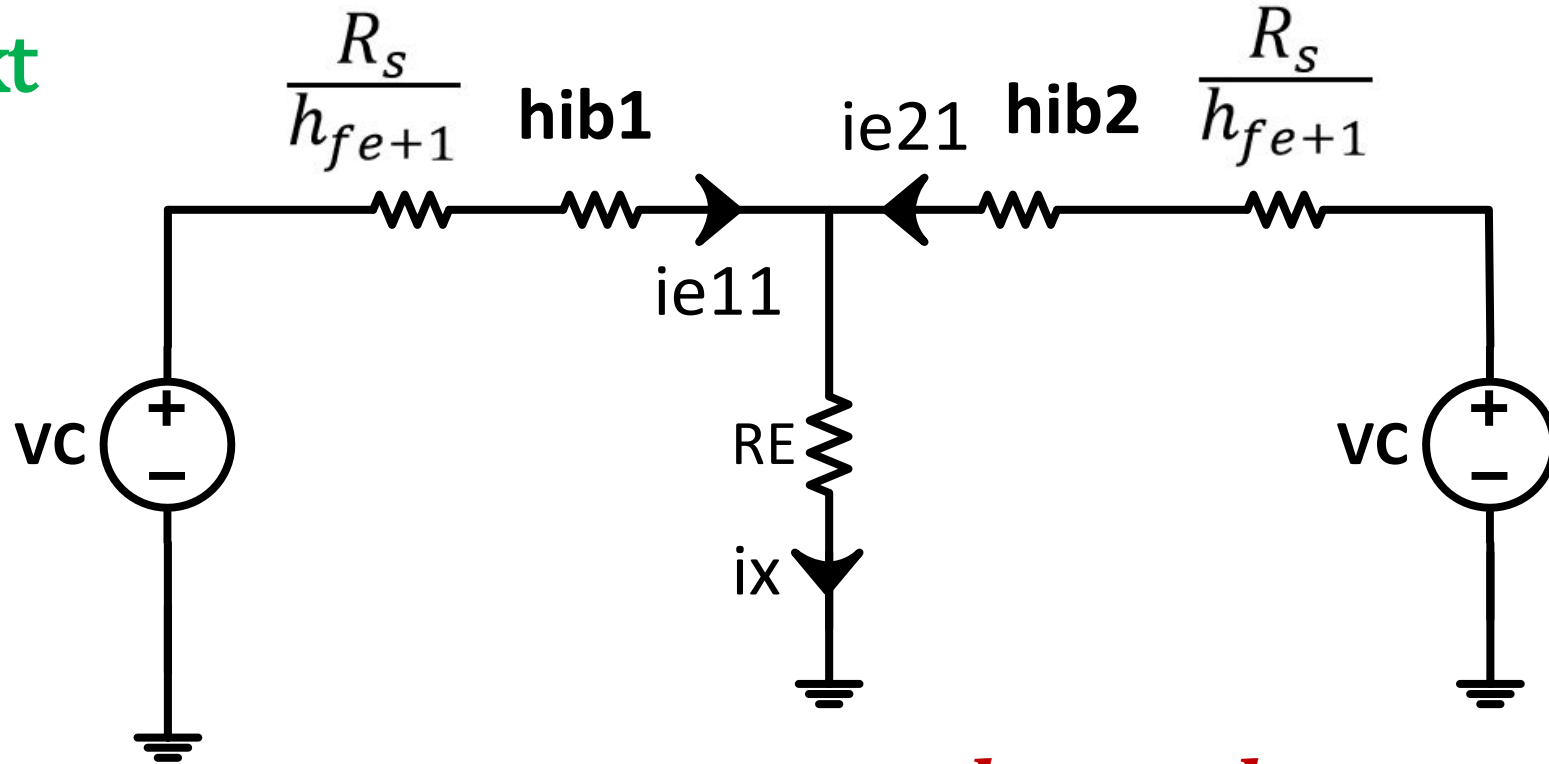
$$v_{i1} = v_c ; v_{i2} = v_c$$

By Symmetry

$$i_{e11} = i_{e21} ; i_x = 2i_{e11}$$

$$i_{e11} = \frac{v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$

$$i_{e21} = \frac{v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$



$$h_{ib1} = h_{ib2}$$

Differential Amplifiers

2) let $v_c = 0$

$$v_1 = -\frac{v_d}{2}; \quad v_2 = \frac{v_d}{2}$$

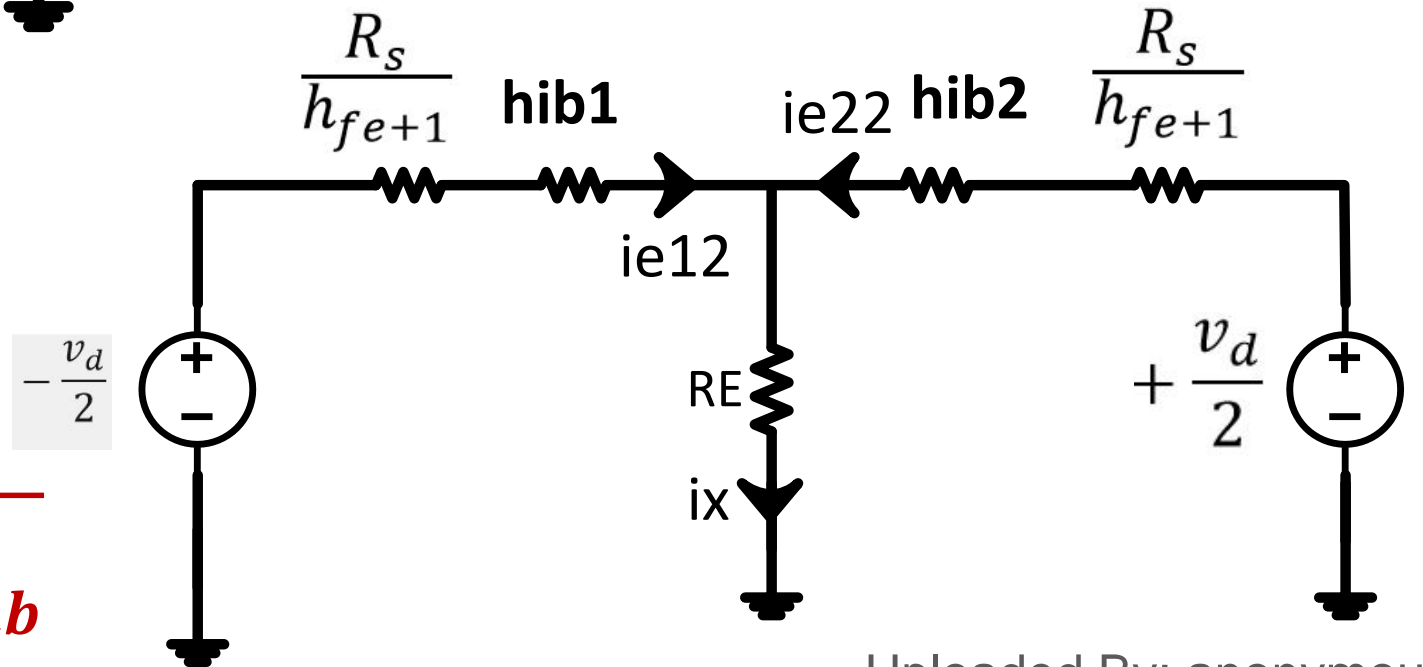
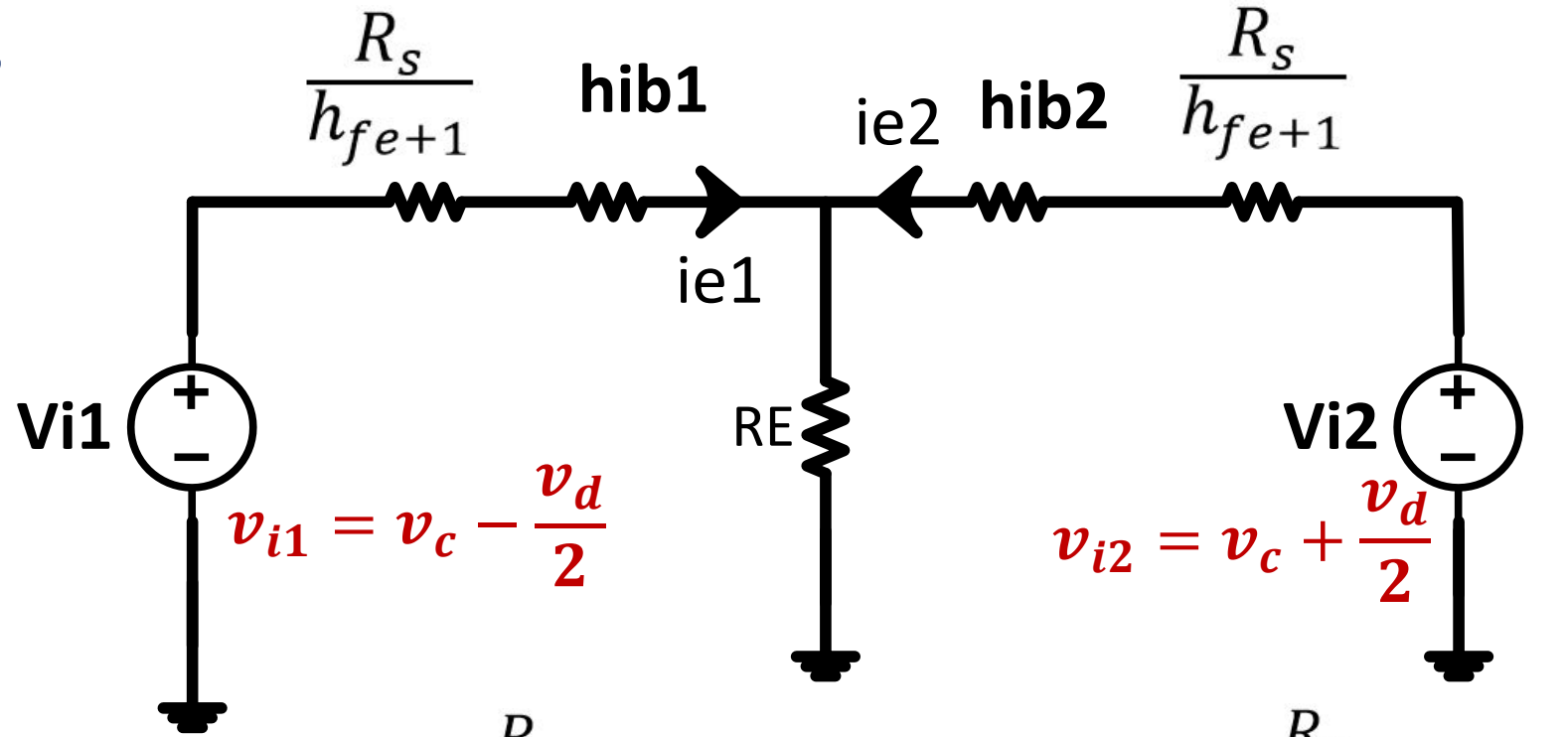
(Using symmetry)

$$i_{e12} = -i_{e22}$$

$$i_x = 0$$

$$i_{e12} = \frac{-v_d/2}{\frac{R_s}{h_{fe+1}} + h_{ib}}$$

$$i_{e22} = \frac{v_d/2}{\frac{R_s}{h_{fe+1}} + h_{ib}}$$



Differential Amplifiers

Differential Amplifier Circuit:

Using Superposition

$$i_{e1} = \frac{v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E} - \frac{v_d/2}{\frac{R_s}{h_{fe+1}} + h_{ib}}$$

$$i_{e2} = \frac{v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E} + \frac{v_d/2}{\frac{R_s}{h_{fe+1}} + h_{ib}}$$

$$v_{o1} = + \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)} - \frac{R_c v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$

$$v_{o2} = - \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)} - \frac{R_c v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$

$$v_{o1} - v_{o2} = \frac{R_c}{h_{ib} + \frac{R_s}{h_{fe+1}}} v_d$$

Differential Amplifiers

$$v_{o1} = + \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)} - \frac{R_c v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$

Ad \equiv ***Differential mode gain***

$$Ad = \frac{v_o}{v_d} \Big|_{v_c=0}$$

let $v_o = v_{o1}$

$$Ad = \frac{v_{o1}}{v_d} \Big|_{v_c=0}$$

$$Ad = \frac{R_c}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$

Differential Amplifiers

$$v_{o1} = + \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)} - \frac{R_c v_c}{h_{ib} + \frac{R_s}{h_{fe+1}} + 2R_E}$$

Ac \equiv Common mode gain

$$Ac = \frac{v_o}{v_c} \Big|_{v_d=0}$$

$$\text{let } v_o = v_{o1}$$

$$Ac = \frac{v_{o1}}{v_c} \Big|_{v_d=0}$$

$$Ac = \frac{-R_c}{2R_E + h_{ib} + \frac{R_s}{h_{fe+1}}}$$

Differential Amplifiers

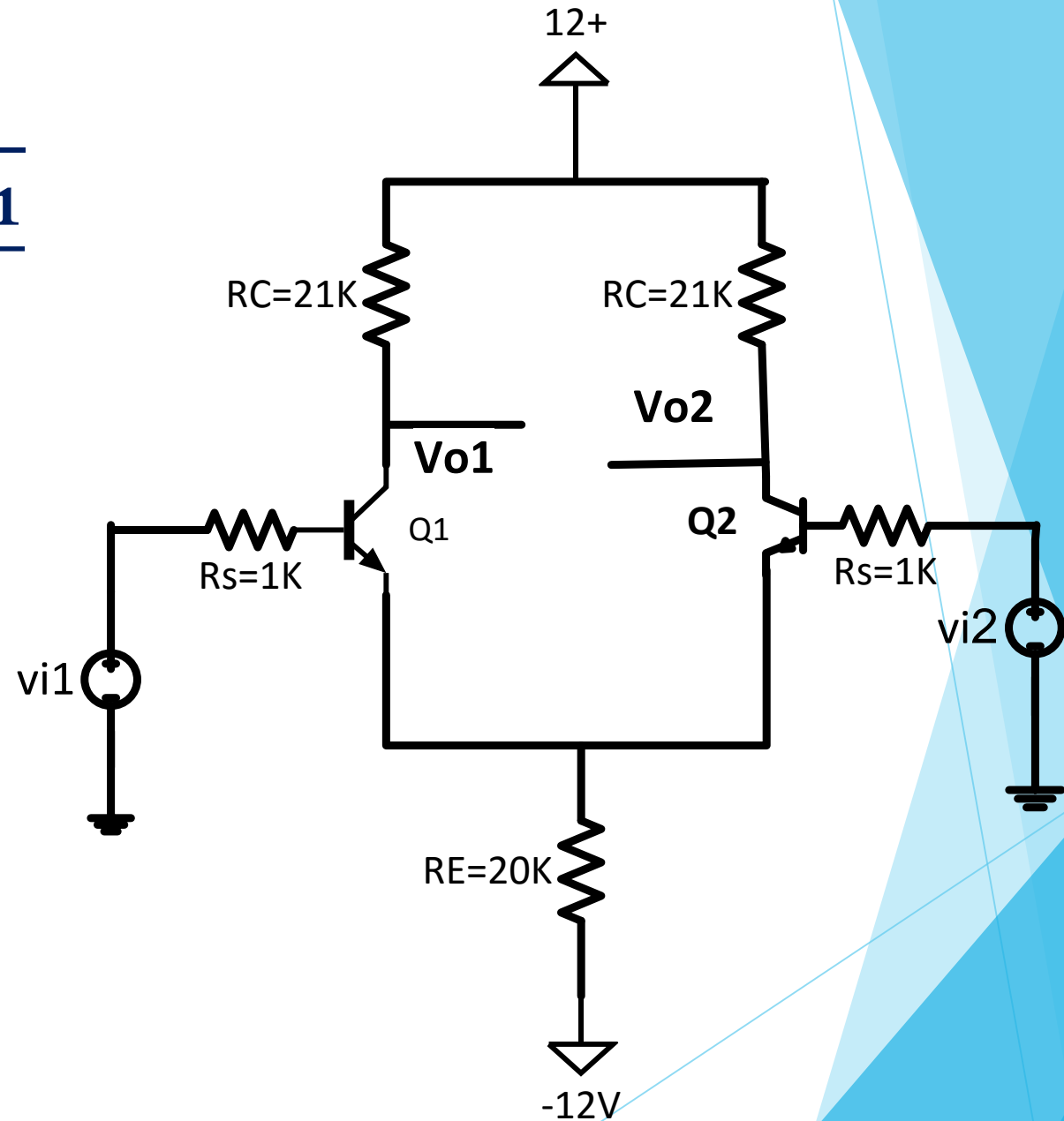
CMRR \equiv ***Common Mode Rejection Ratio***

$$CMRR = \left| \frac{A_d}{A_c} \right|$$

$$CMRR = \frac{2R_E + h_{ib} + \frac{R_s}{h_{fe+1}}}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$

To increase CMRR we need to increase R_E

$$CMRR = \frac{2R_E + h_{ib} + \frac{R_s}{h_{fe+1}}}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$



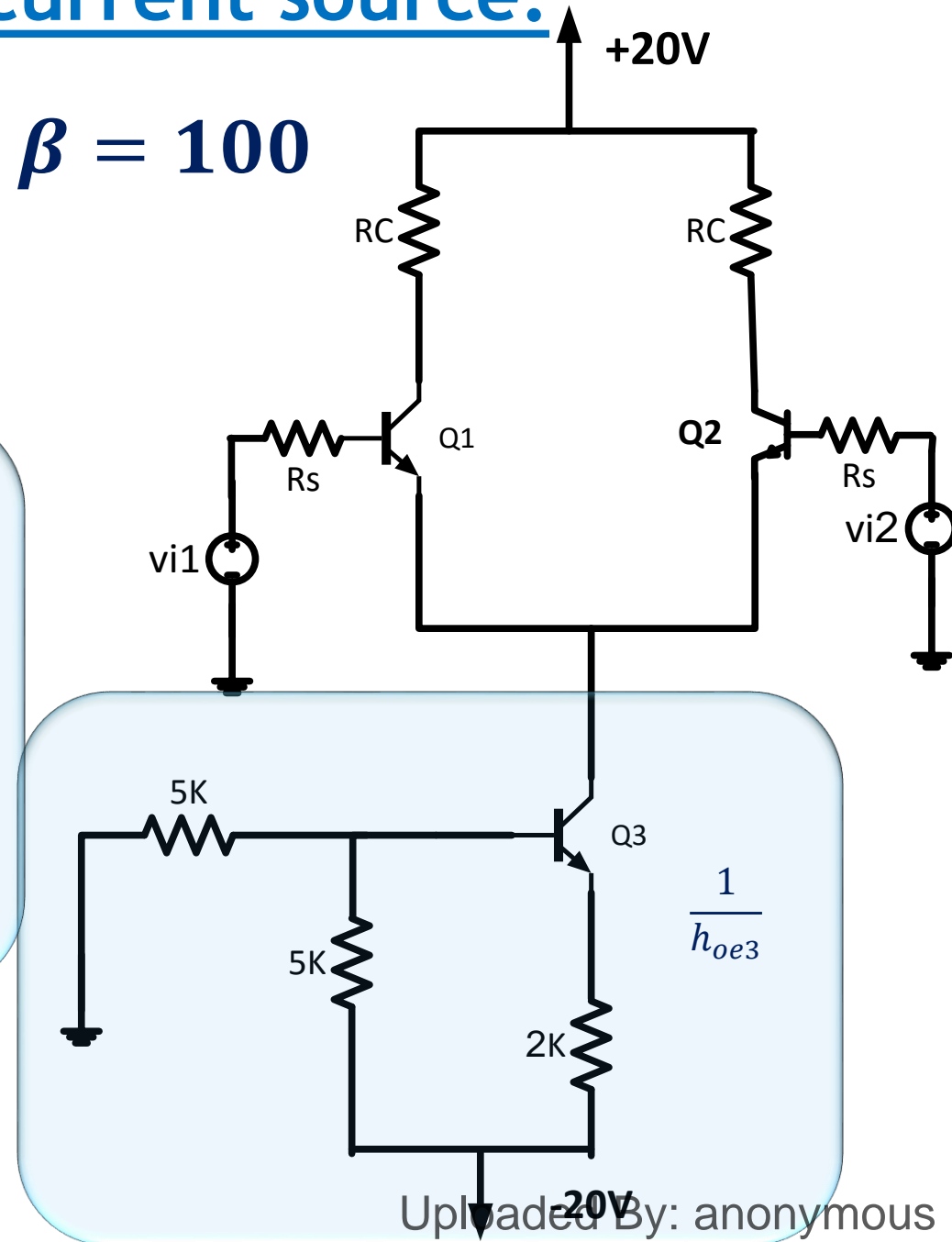
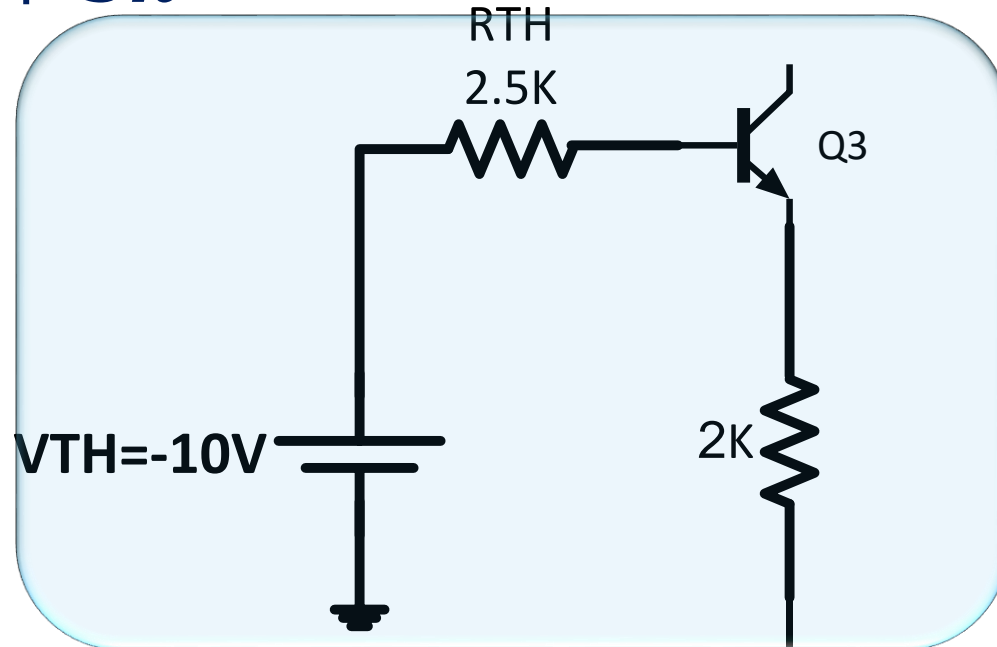
$$I_{E1} = I_{E2} = \frac{12 - 0.7}{\frac{R_s}{41} + 2R_E}$$

Differential Amplifier with constant current source:

$$R_{TH} = 5k \parallel 5k = 2.5k$$

$$V_{TH} = \frac{5k}{5k + 5k} (-20) = -10V$$

$$\beta = 100$$



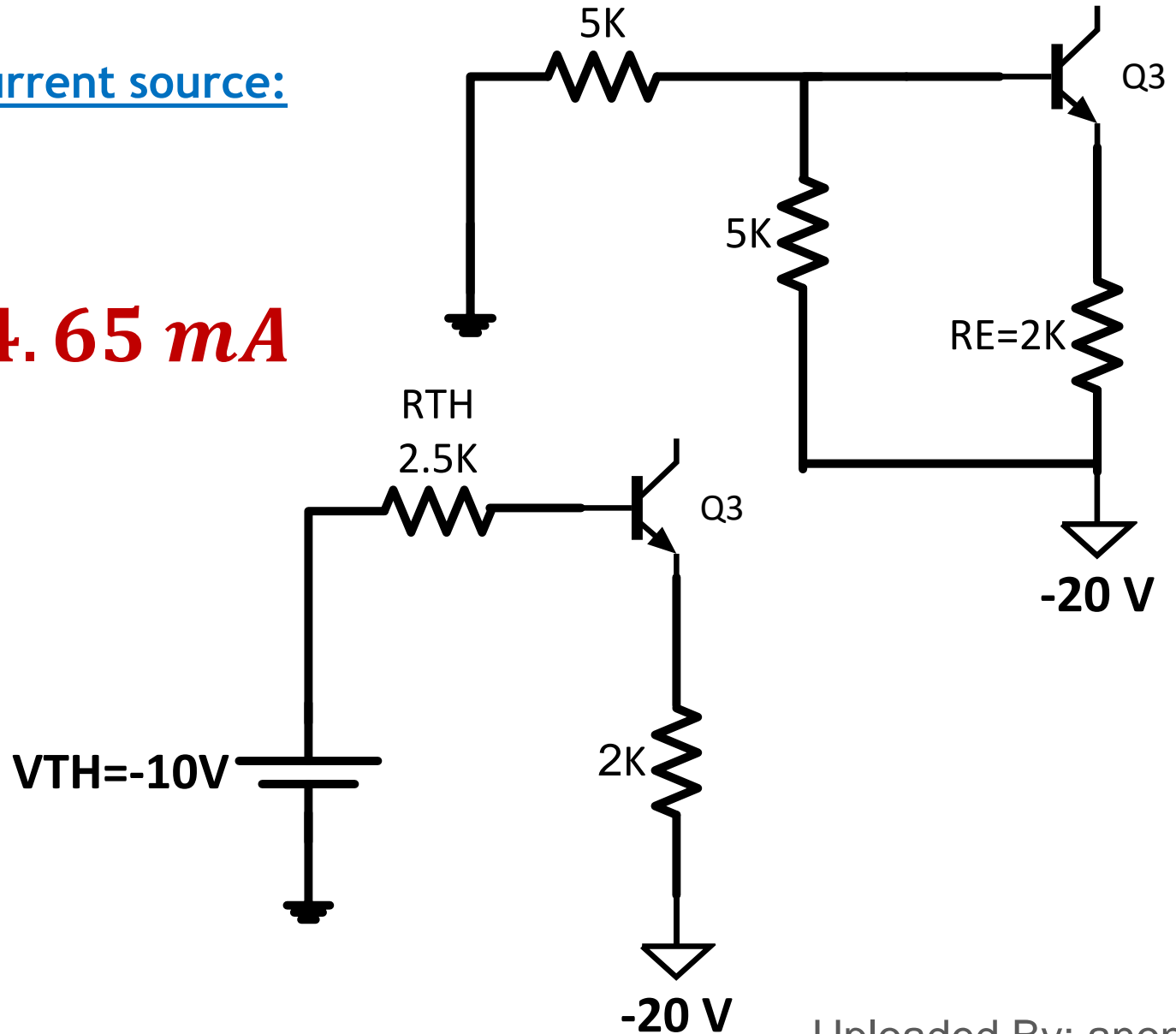
$$I_{E3} = \frac{10 - 0.7}{\frac{2.5k}{101} + 2k} = 4.65 \text{ mA}$$

Differential Amplifiers

Differential Amplifier with constant current source:

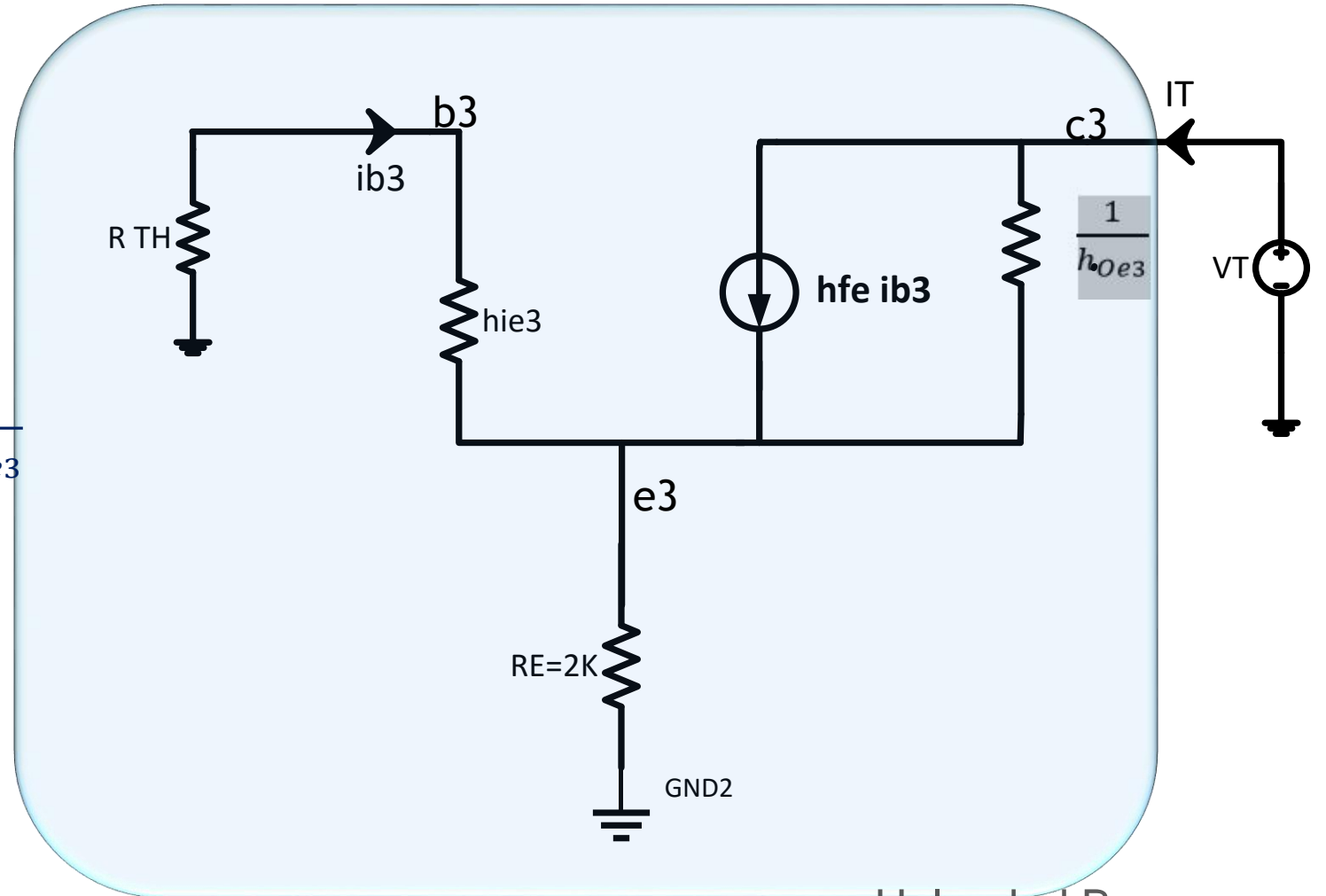
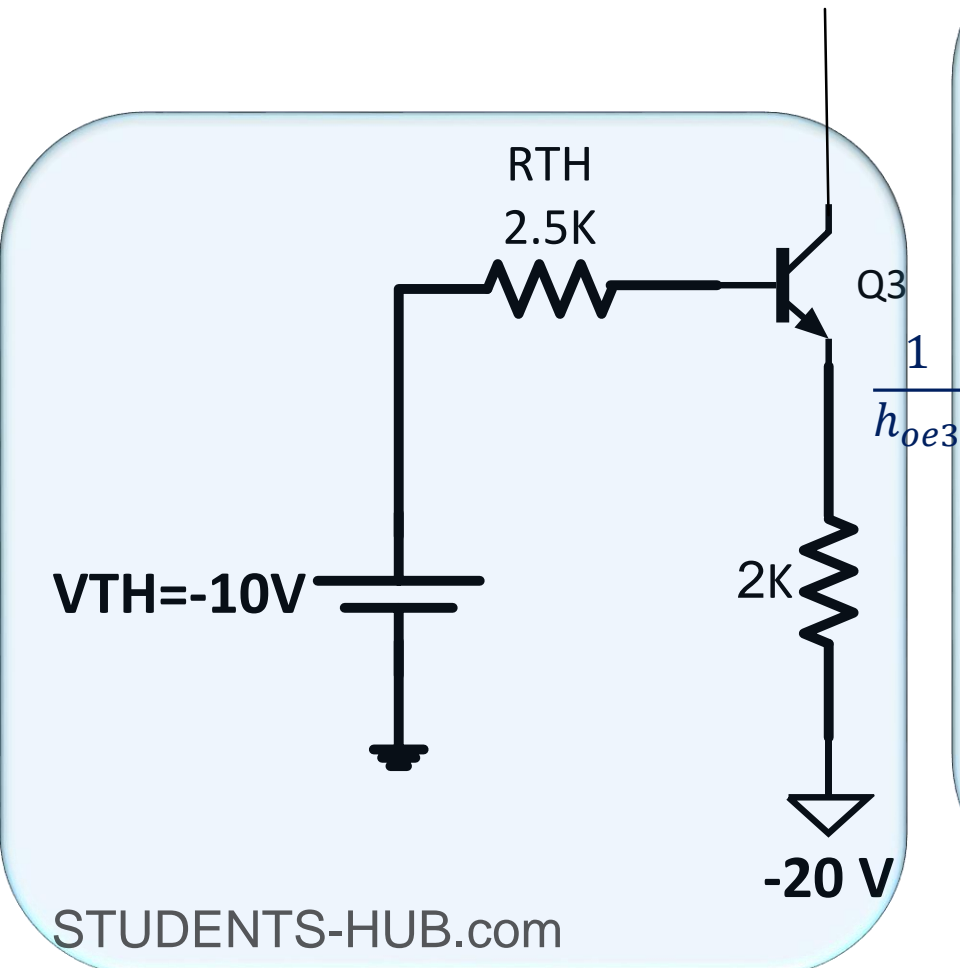
$$I_{E3} = \frac{10 - 0.7}{\frac{2.5k}{101} + 2k} = 4.65 \text{ mA}$$

$$h_{ie3} = \beta \frac{V_T}{I_{CQ3}} = 0.559 \text{ K}$$



Differential Amplifiers

Ac small signal equivalent circuit for the constant current source:

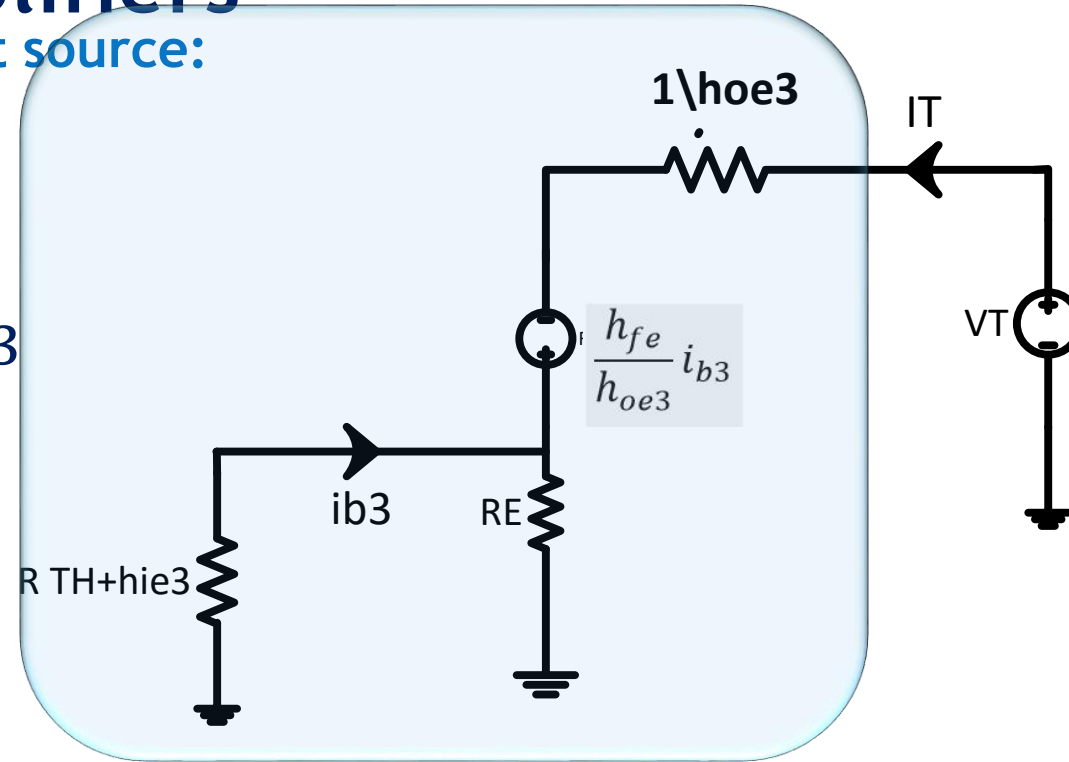


Differential Amplifiers

Ac small signal equivalent circuit for the constant current source:

$$V_T = \frac{1}{h_{oe3}} I_T - \frac{h_{fe}}{h_{oe3}} i_{b3} - (h_{ie3} + R_{TH}) i_{b3}$$

$$i_{b3} = - \frac{R_E}{R_E + h_{ie3} + R_{TH}} I_T$$

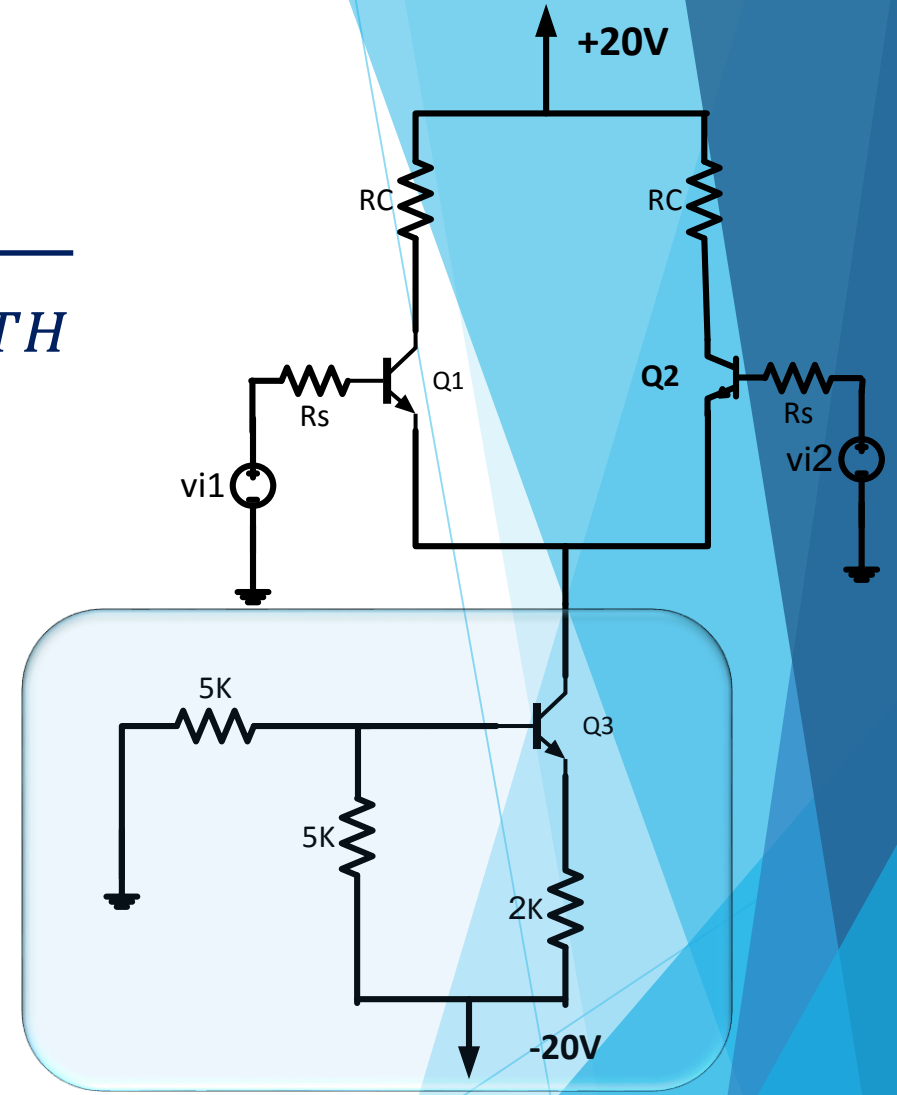


$$\begin{aligned} \therefore R_o &= \frac{V_T}{I_T} \\ &= \frac{1}{h_{oe3}} + \frac{h_{fe}}{h_{oe3}} \frac{R_E}{R_E + h_{ie3} + R_{TH}} + \frac{(h_{ie3} + R_{TH})}{R_E + h_{ie3} + R_{TH}} R_E \end{aligned}$$

$$R_o \approx \frac{1}{h_{oe3}} + \frac{h_{fe}}{h_{oe3}} \frac{R_E}{R_E + h_{ie3} + R_{TH}}$$

- ▶ let $\frac{1}{h_{oe}} = 80K$, $h_{ie} = 0.559k$
- ▶ $h_{fe} = 100$, $R_E = 2k$, $R_{TH} = 2.5k$
- ▶ $R_o = 3.25 M\Omega$

$$CMRR = \frac{2R_E + h_{ib} + \frac{R_s}{h_{fe+1}}}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$



Ro
 Uploaded By: anonymous

Differential Amplifiers

Bipolar transistor current sources:

Q1 and Q2 are in the active region

1. Current mirror : Simple

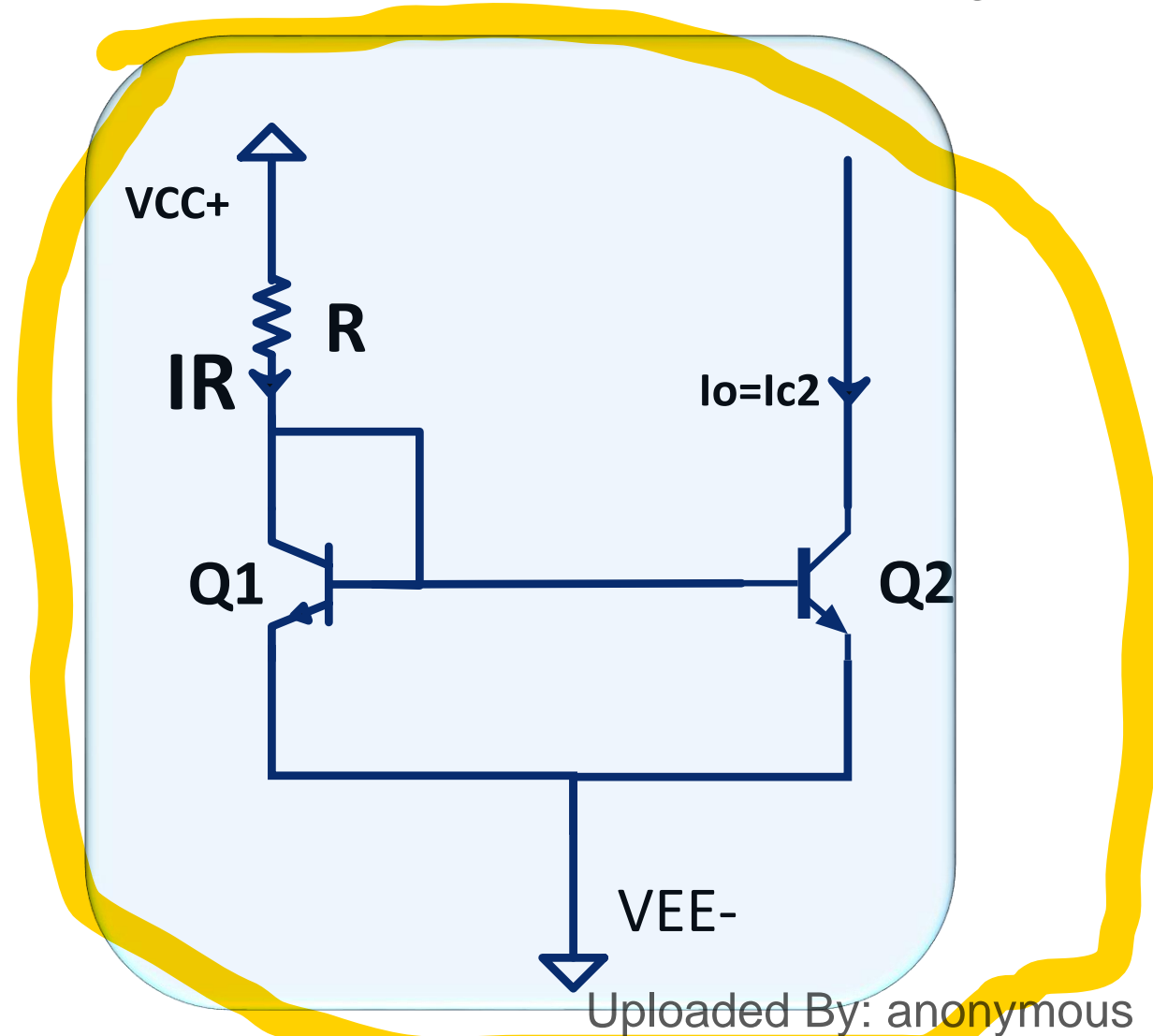
$$I_C = I_S e^{\frac{V_{BE}}{V_T}}$$

If Q_1 is matched to Q_2

$$\beta_1 = \beta_2 ; I_{S1} = I_{S2} ; V_{T1} = V_{T2}$$

And since $V_{BE1} = V_{BE2}$

$$\therefore I_{C1} = I_{C2} = I_o$$

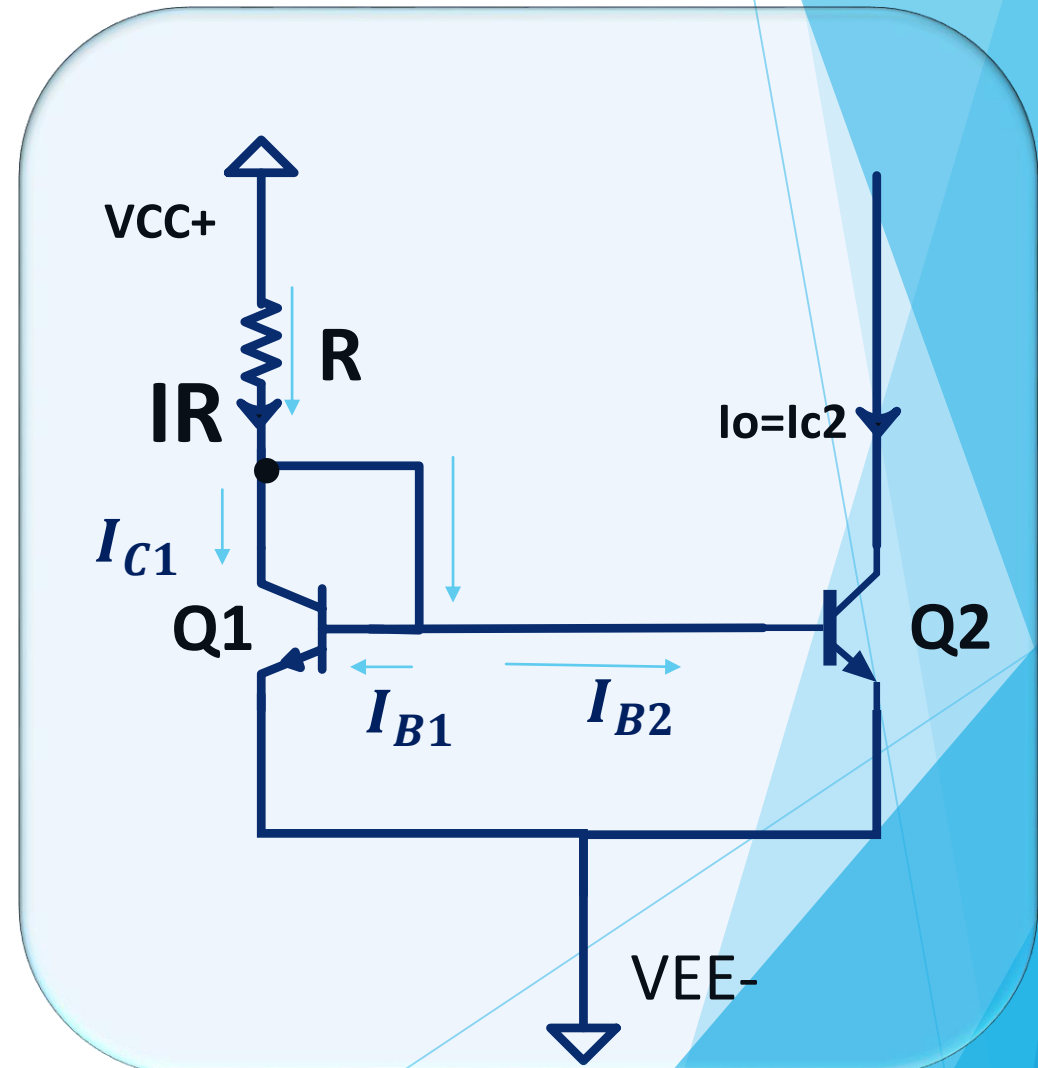


To find I_o in terms of I_R

▶ **KCL** $I_R = I_{C1} + I_{B1} + I_{B2}$

▶ $I_{C1} = I_{C2}$; $I_{B1} = I_{B2}$

▶ $\therefore I_o = I_{C2} = \frac{I_R}{1 + \frac{2}{\beta}}$



Differential Amplifiers

Bipolar transistor current sources:

1. Current mirror : Simple

1) if $\beta = \infty$

$$I_o = I_R$$

2) if $\beta = 100$

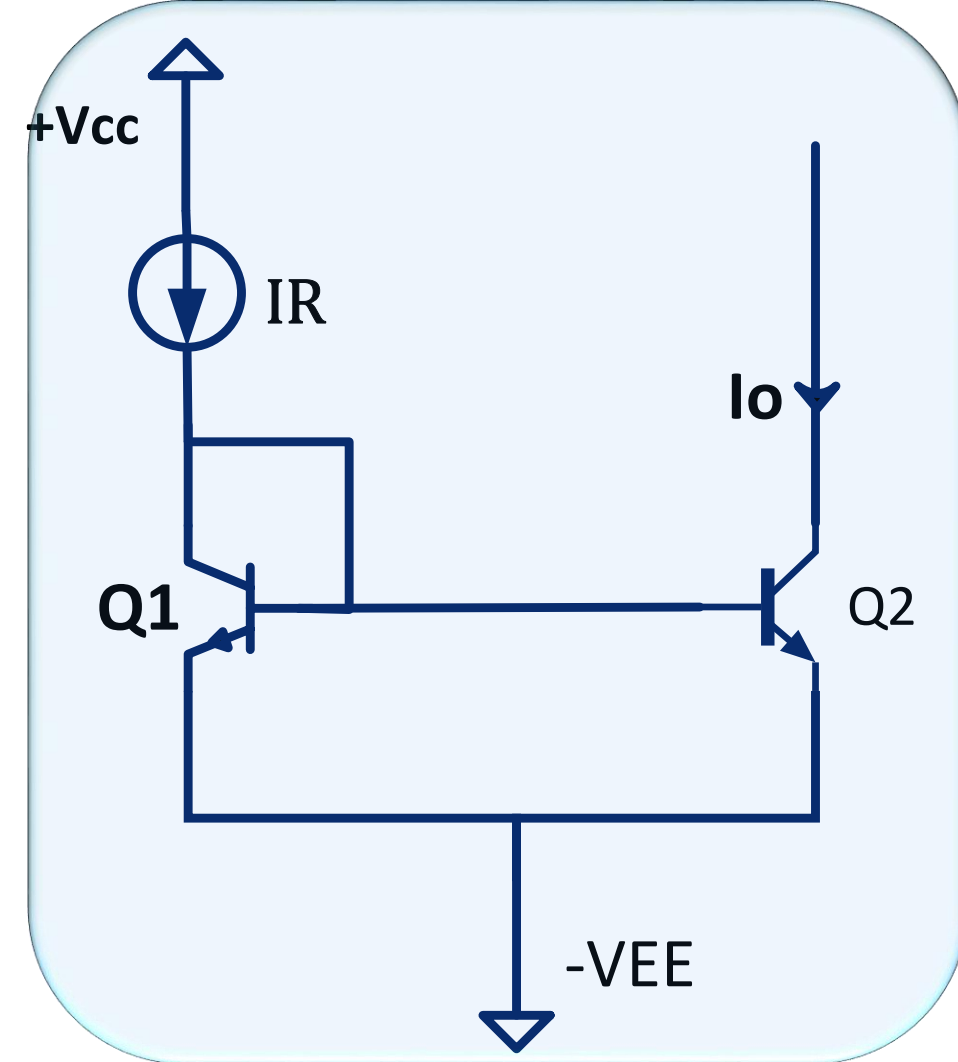
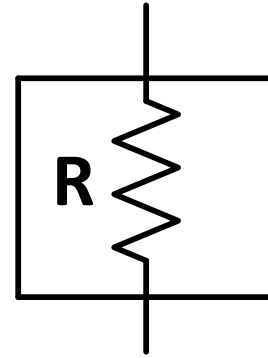
$$I_o = I_R \quad ; \quad 2\% \text{ error}$$

To find I_R

$$\text{KVL: } V_{CC} = R I_R + V_{BE1} - V_{EE}$$

$$I_R = \frac{V_{CC} + V_{EE} - V_{BE}}{R}$$

STUDENTS-HUB.com



$$I_o = I_{C2} = \frac{I_R}{1 + \frac{2}{\beta}}$$

Uploaded By: anonymous

Bipolar transistor current sources:

$$I_C = I_S e^{\frac{V_{BE}}{V_T}}$$

1. Current mirror : Simple

If the area of the EB junction of Q2 is m times that of Q1

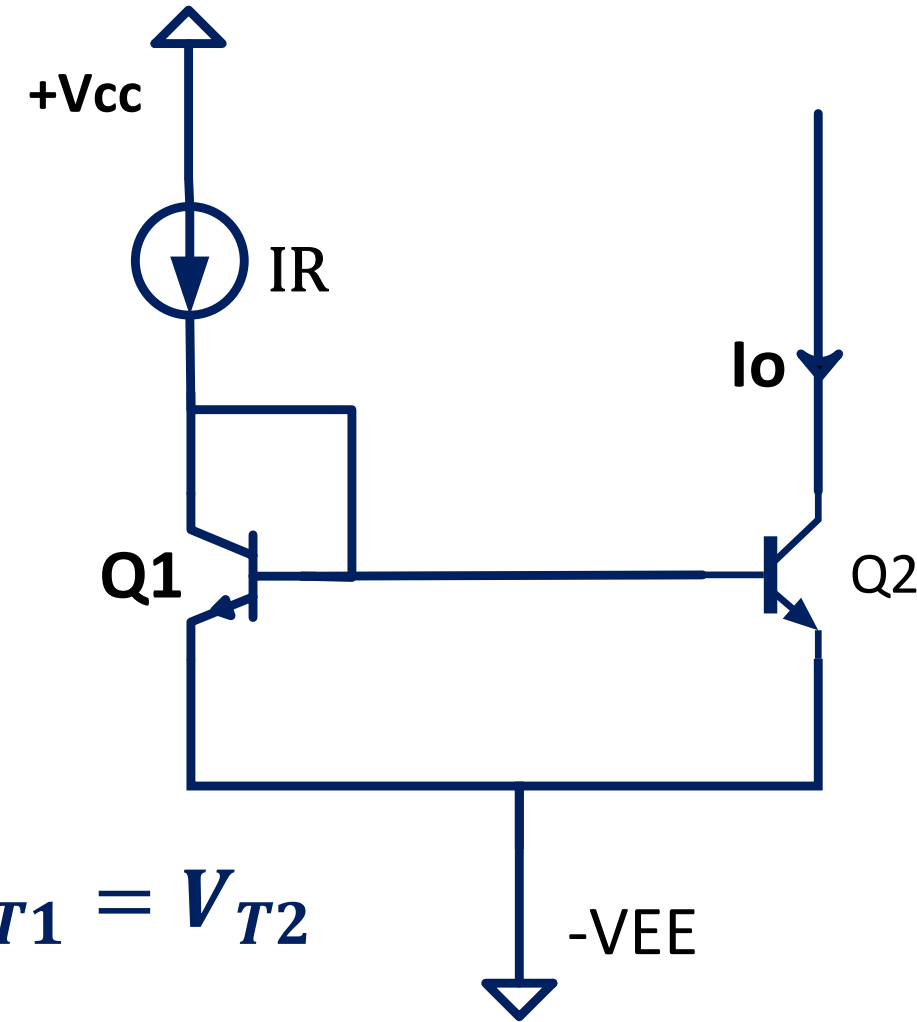
$$\therefore I_{S2} = m I_{S1}$$

And since $V_{BE1} = V_{BE2}$ and $\beta_1 = \beta_2$; $V_{T1} = V_{T2}$

$$\therefore I_{C2} = m I_{C1}$$

KCL: $I_R = I_{C1} + I_{B1} + I_{B2}$

$$I_R = \frac{I_{C2}}{m} + \frac{I_{C2}}{\beta m} + I_{B2}$$



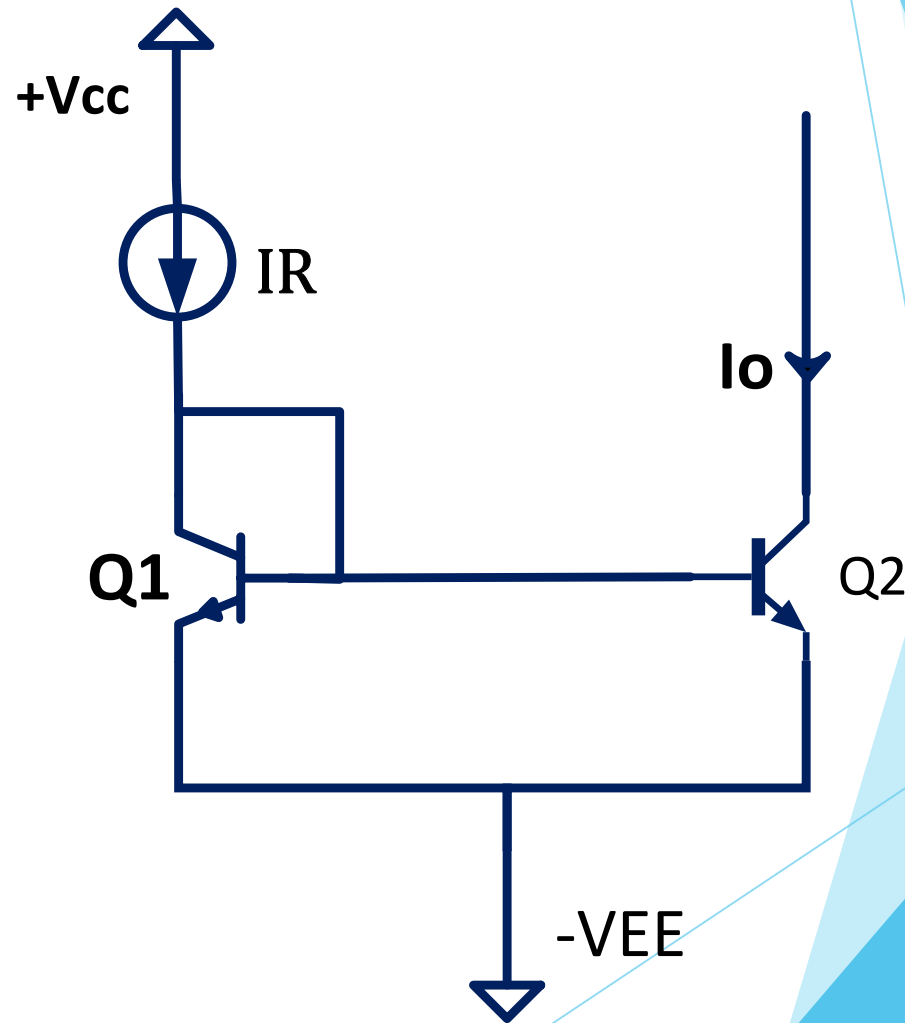
$$I_R = \frac{I_{C2}}{m} + \frac{I_{C2}}{\beta m} + I_{B2}$$

$$I_{C2} = m I_{C1}$$

$$\therefore I_{C2} = I_o = I_R \frac{m}{1 + \frac{m+1}{\beta}}$$

if $\beta = \infty$

$$I_o = I_{C2} = m I_R$$

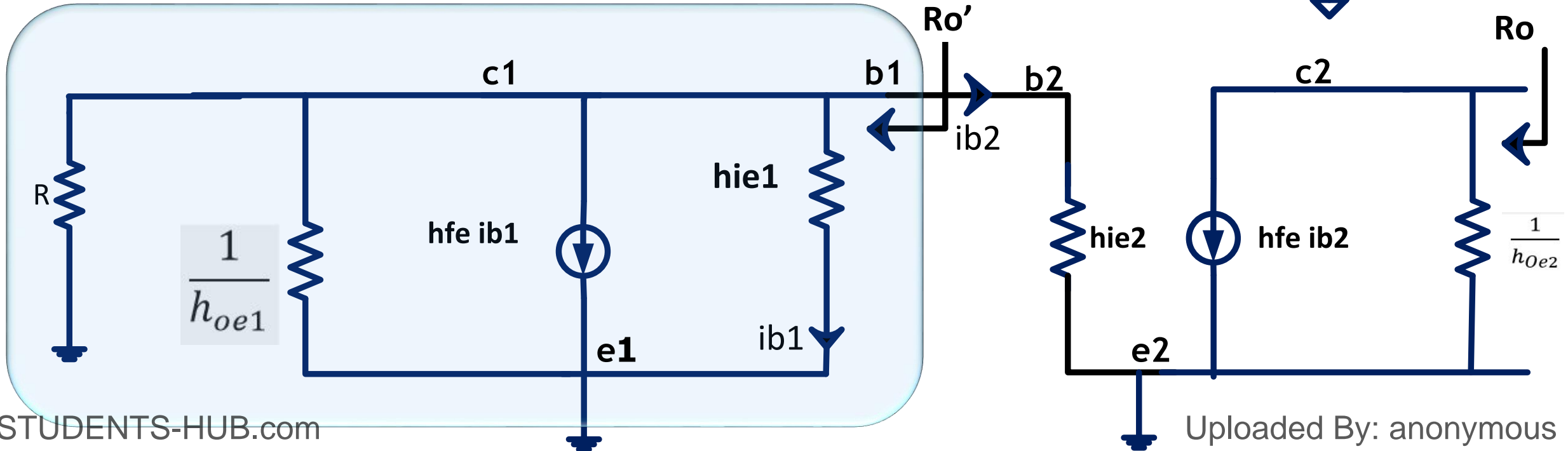
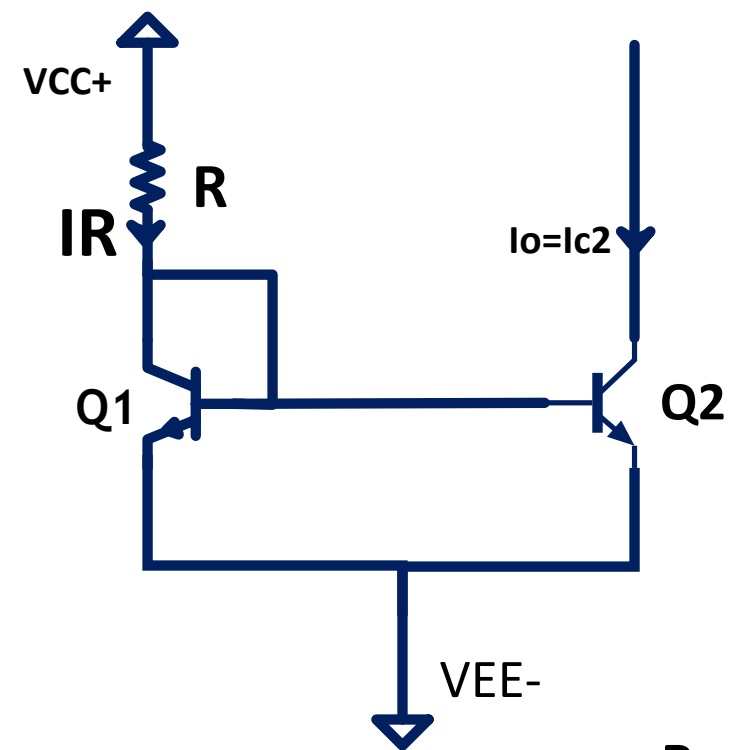


Bipolar transistor current sources:

Output - Impedance:

To find $R_o = \frac{V_T}{I_T}$

Ac small signal equivalent circuit

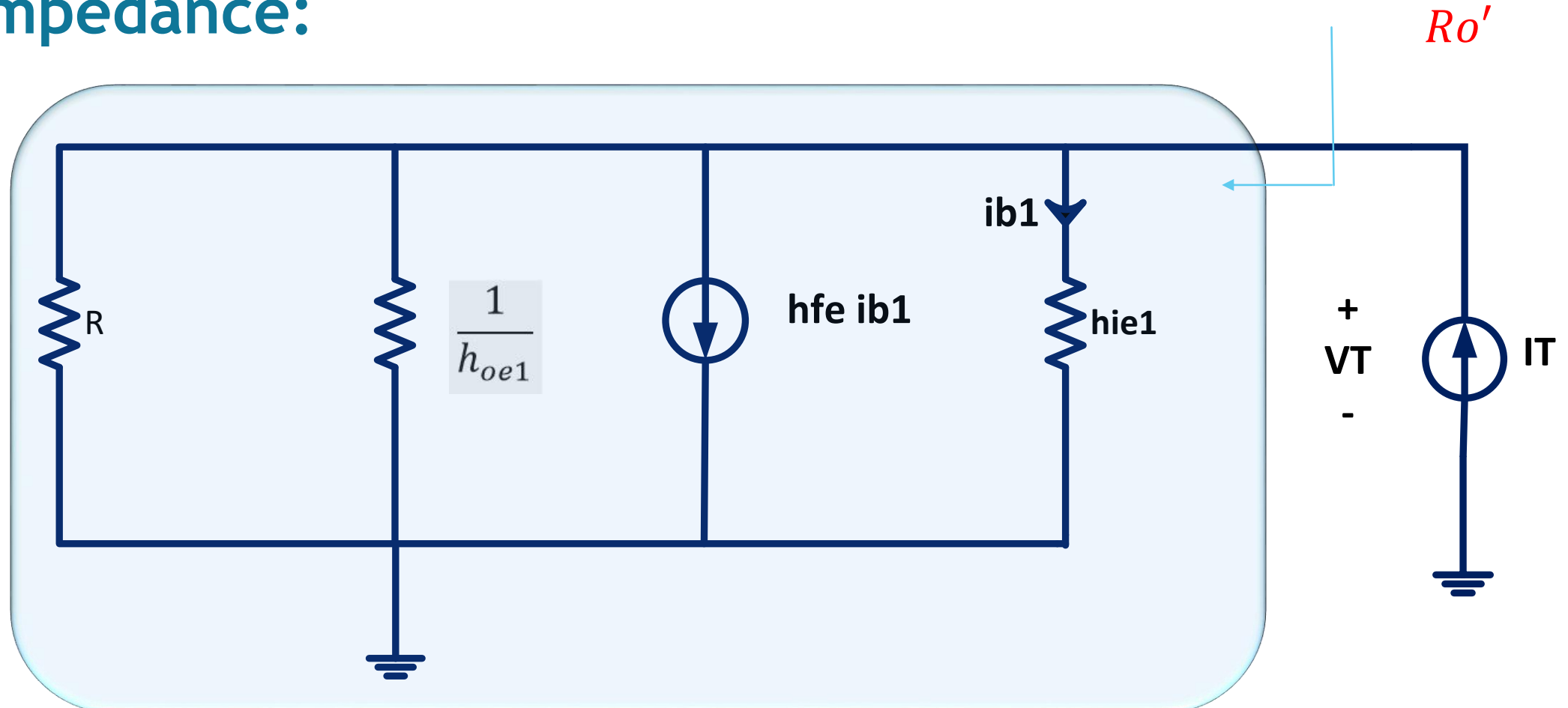


Differential Amplifiers

Bipolar transistor current sources:

Output - Impedance:

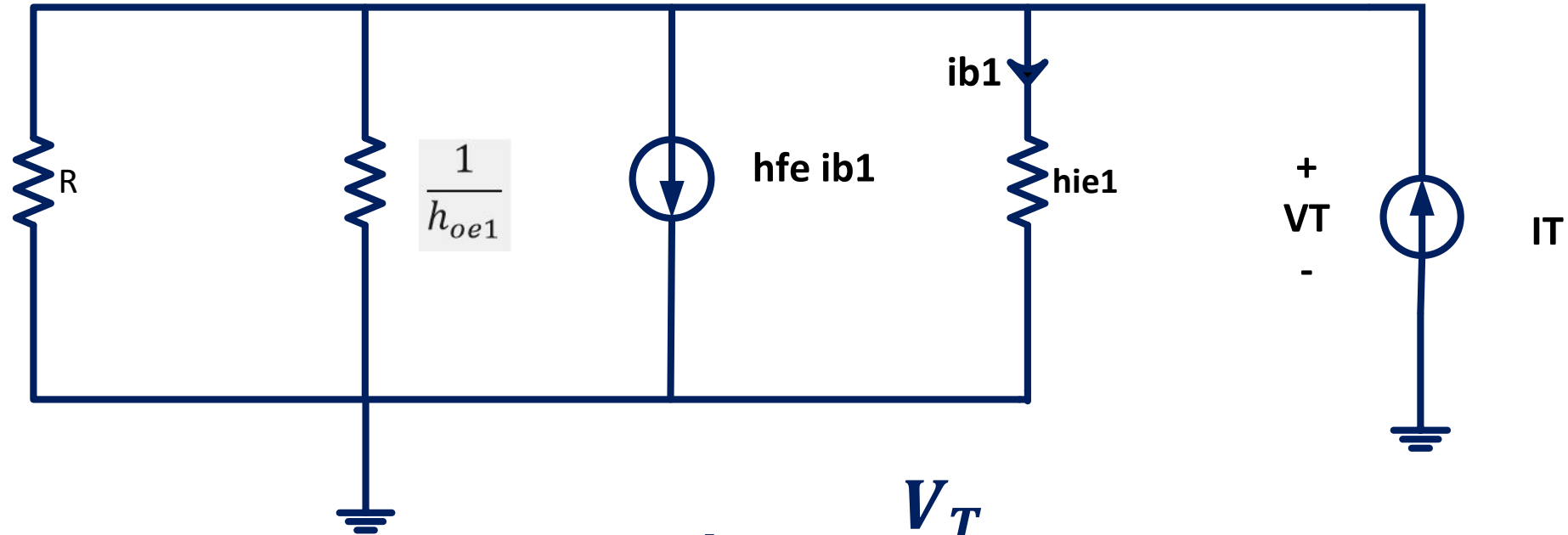
To find $R_{o'}$



Bipolar transistor current sources:

To find $R_{o'} = \frac{V_T}{I_T}$

Output - Impedance:



$$I_T = \frac{V_T}{R \parallel \frac{1}{h_{oe1}} \parallel h_{ie1}} + h_{fe} i_{b1}$$

$$i_{b1} = \frac{V_T}{h_{ie1}}$$

$$g_{m1} = \frac{h_{fe1}}{h_{ie1}}$$

$$I_T = \frac{h_{fe}}{h_{ie1}} V_T + \frac{V_T}{R \parallel h_{ie1} \parallel \frac{1}{h_{oe1}}}$$

$$R_{o'} = R \parallel h_{ie1} \parallel \frac{1}{h_{oe1}} \parallel \frac{1}{g_{m1}}$$

Differential Amplifiers

Bipolar transistor current sources:

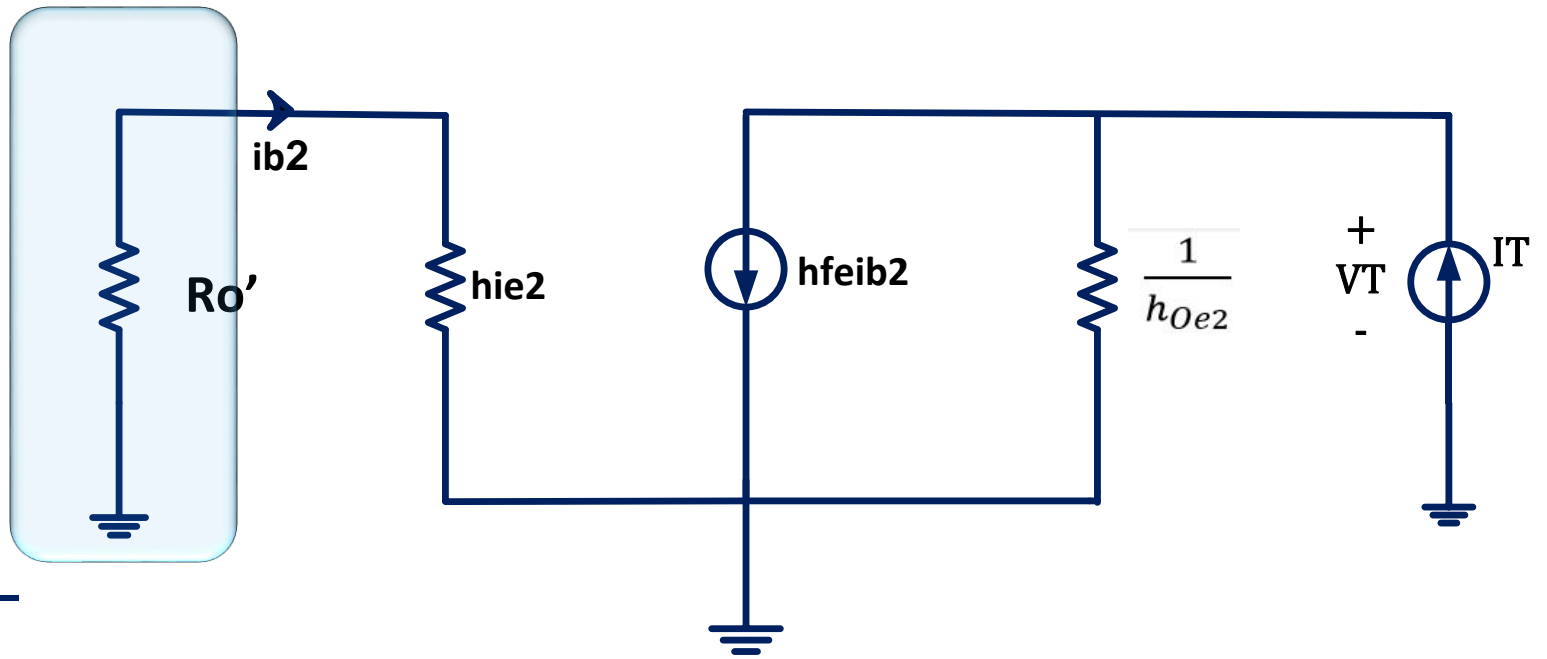
Output - Impedance:

To find $R_o = \frac{V_T}{I_T}$

$$I_T = h_{fe} i_{b2} + \frac{V_T}{\frac{1}{h_{oe2}}}$$

$$i_{b2} = 0$$

$$\therefore \frac{V_T}{I_T} = \frac{1}{h_{oe2}}$$



Bipolar transistor current sources:

2. Bipolar mirror with base-current compensation:



Q_1, Q_2 are matched

$$\beta_1 = \beta_2 ; I_{S1} = I_{S2} ; V_{T1} = V_{T2}$$

And since $V_{BE1} = V_{BE2}$

$$\therefore I_{C1} = I_{C2} = I_o$$

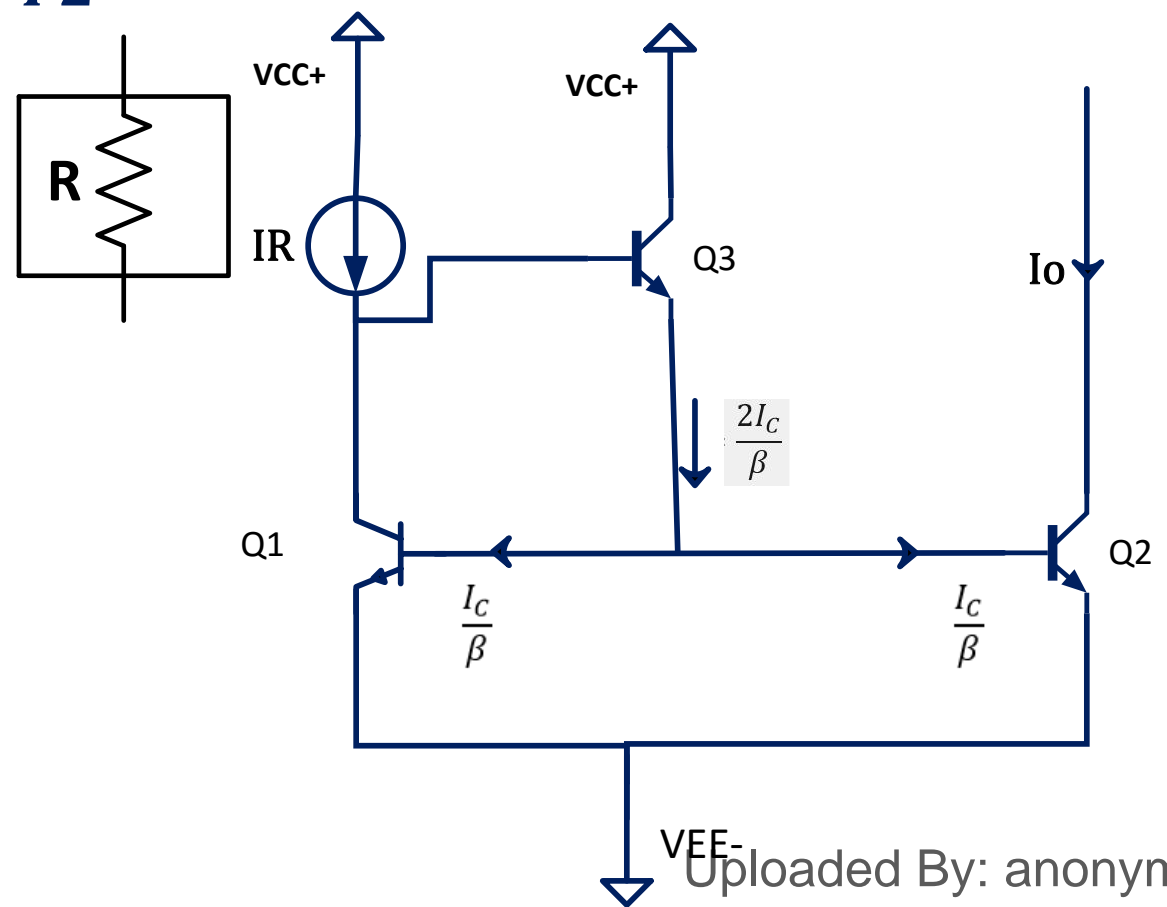
$$I_{B1} = I_{B2}$$

$$\therefore I_R = I_{C1} + I_{B3}$$

$$I_{B3} = \frac{I_{E3}}{\beta + 1}$$

$$I_{E3} = \frac{2I_C}{\beta}$$

Reduce the β dependence

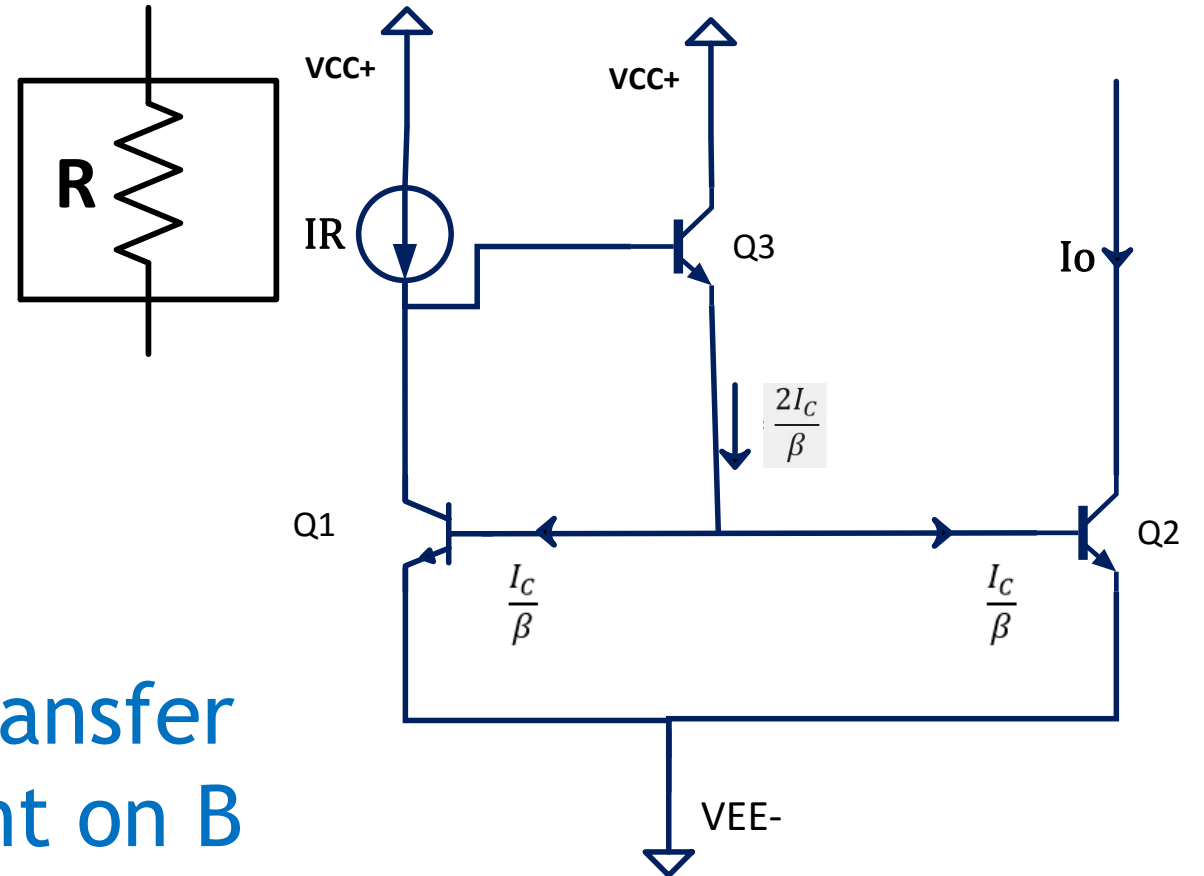


Bipolar transistor current sources:

2. Bipolar mirror with base-current compensation:

$$\therefore I_R = I_C + \frac{2I_C}{\beta(\beta + 1)}$$

$$\therefore I_O = I_R \cdot \frac{1}{1 + \frac{2}{\beta^2 + \beta}}$$



Current source with a current transfer ratio that is much less dependent on β than that of the simple current mirror.

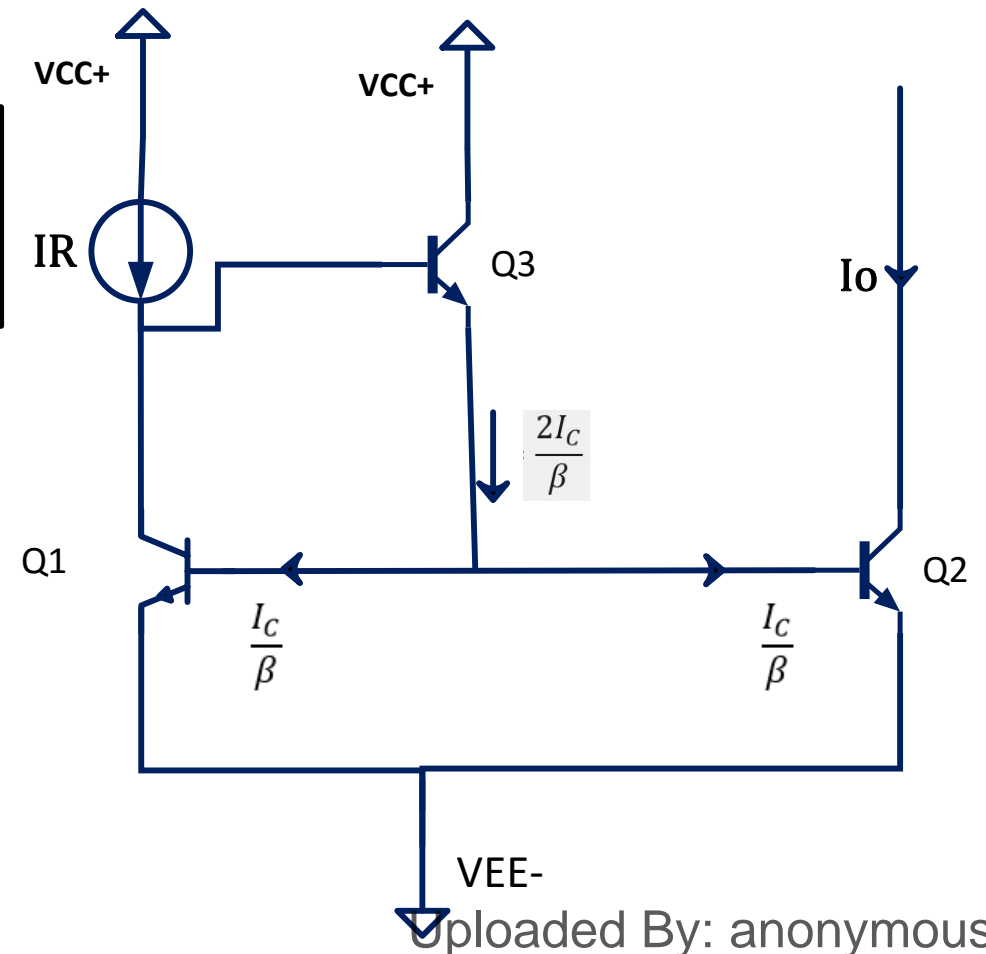
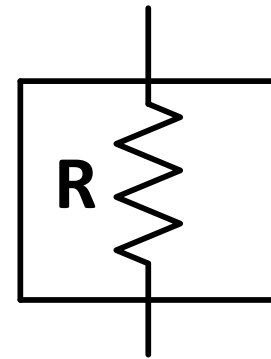
Bipolar transistor current sources:

2. Bipolar mirror with base-current compensation:

Show that :

$$R_o = \frac{1}{h_{oe2}}$$

$$I_R = \frac{V_{CC} + V_{EE} - V_{BE3} - V_{BE1}}{R}$$



Bipolar transistor current sources:

3. The Wilson Current:

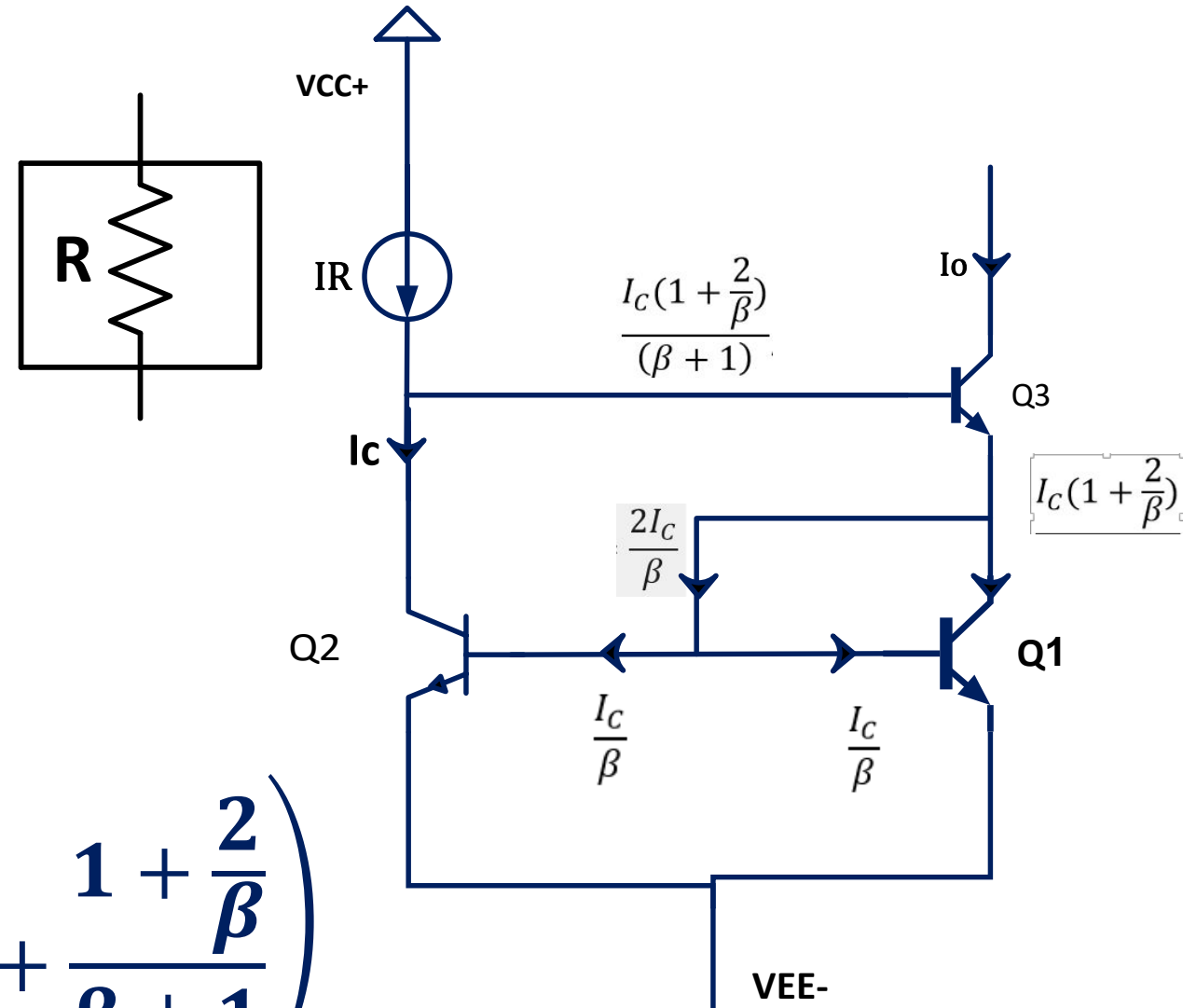
1) Reduce the B dependence

2) Increase $R_o = \frac{h_{fe}}{2} \frac{1}{h_{oe3}}$

Q_1, Q_2 are matched

$$I_{C1} = I_{C2} = I_C$$

$$I_R = I_C + \frac{I_C \left(1 + \frac{2}{\beta}\right)}{\beta + 1} = I_C \left(1 + \frac{1 + \frac{2}{\beta}}{\beta + 1}\right)$$



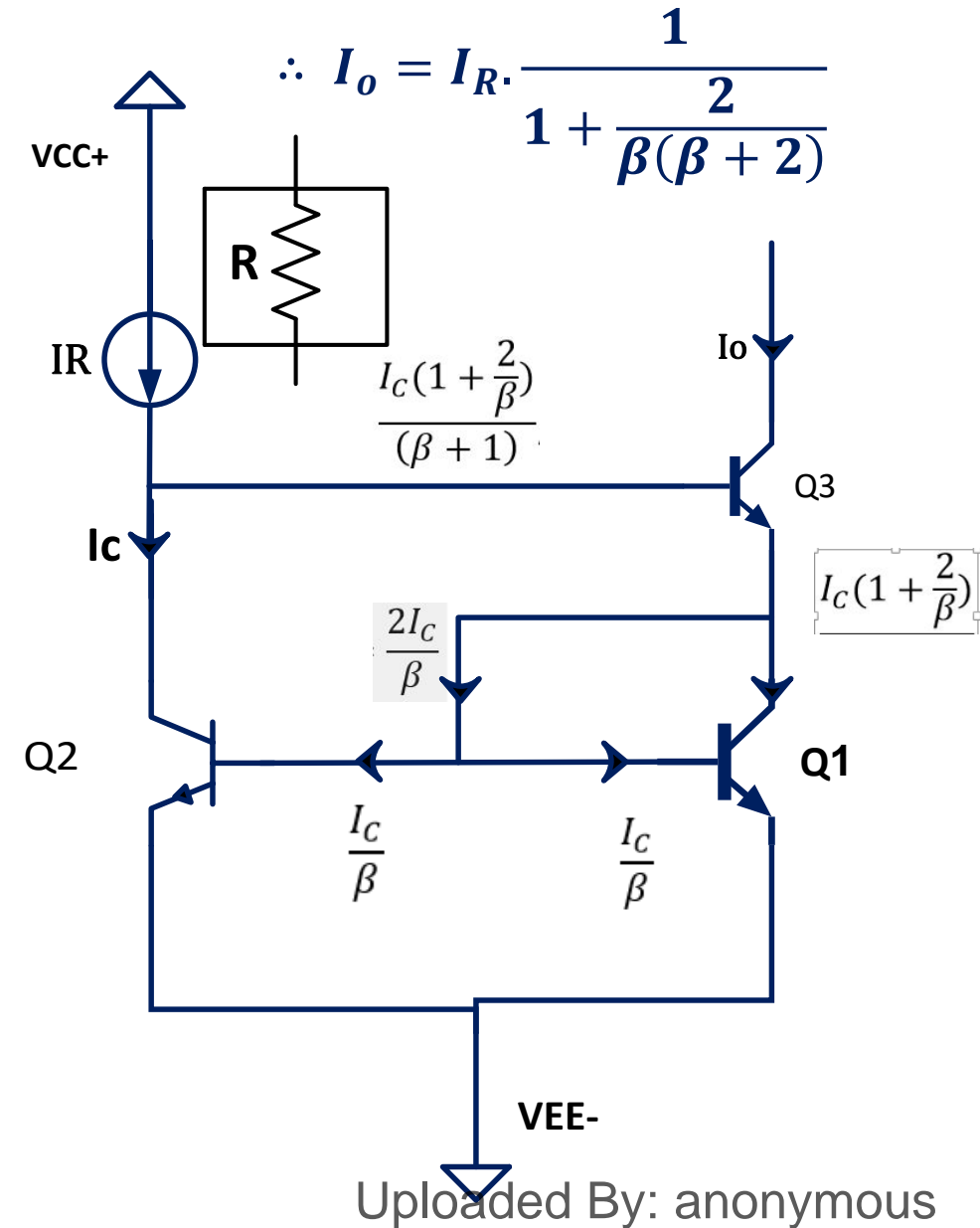
Bipolar transistor current sources:

3. The Wilson Current:

$$I_o = I_{C3} = \frac{\beta}{\beta + 1} I_{E3} = \frac{\beta \left(1 + \frac{2}{\beta}\right)}{\beta + 1} I_C$$

$$\frac{I_o}{I_R} = \frac{I_C \left(1 + \frac{2}{\beta}\right) \left(\frac{\beta}{\beta + 1}\right)}{I_C \left(1 + \frac{1 + \frac{2}{\beta}}{\beta + 1}\right)}$$

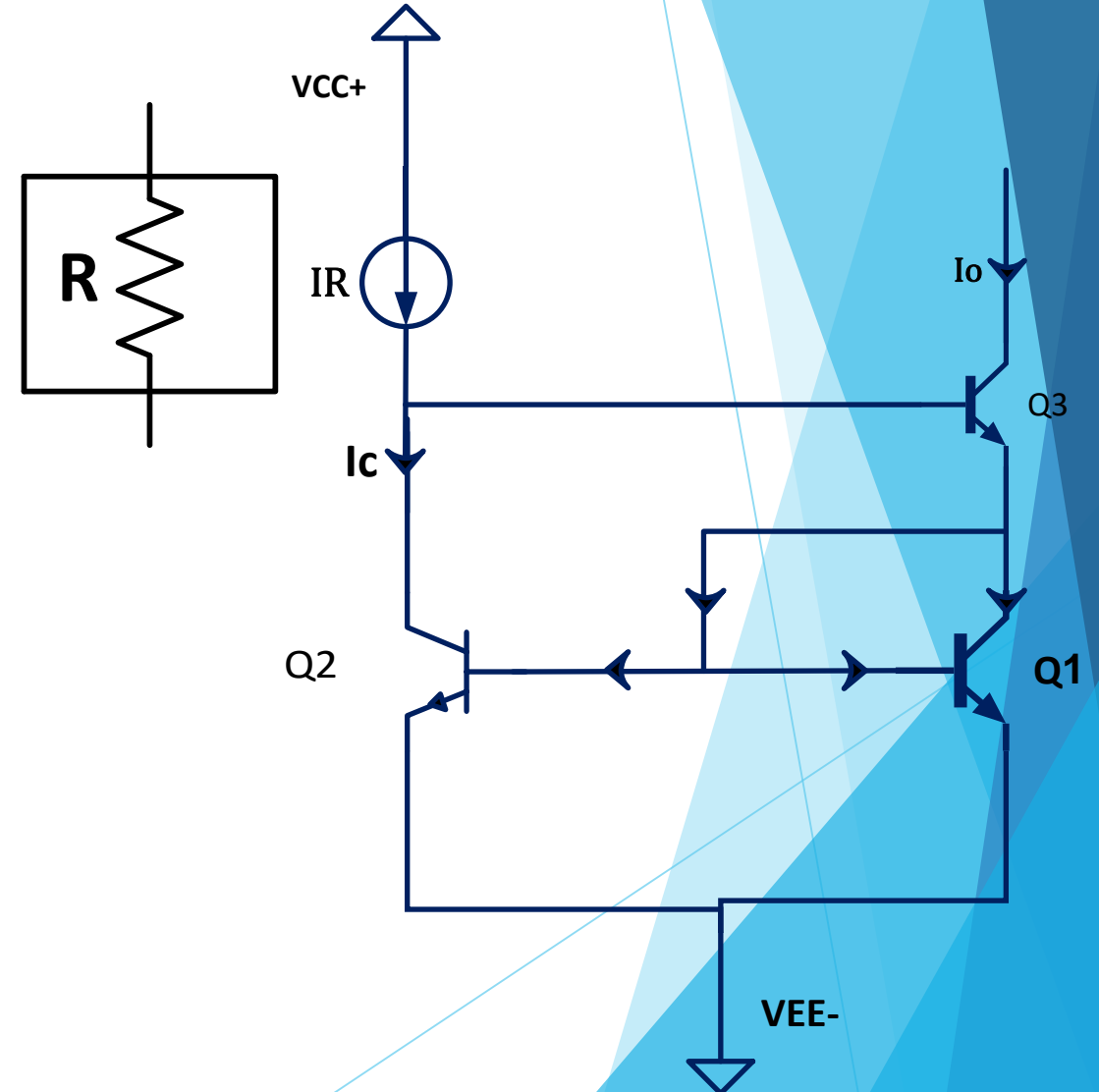
$$I_o = I_R \frac{1}{1 + \frac{2}{\beta(\beta + 2)}}$$



Differential Amplifiers

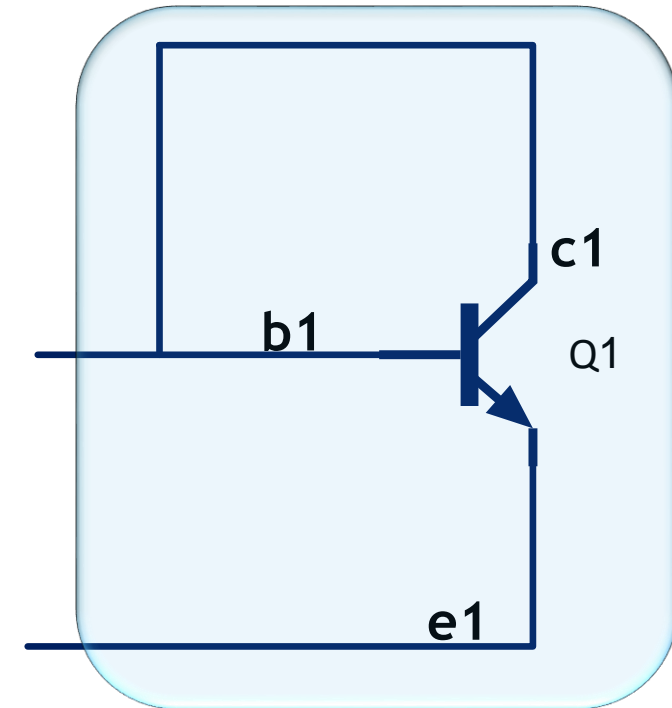
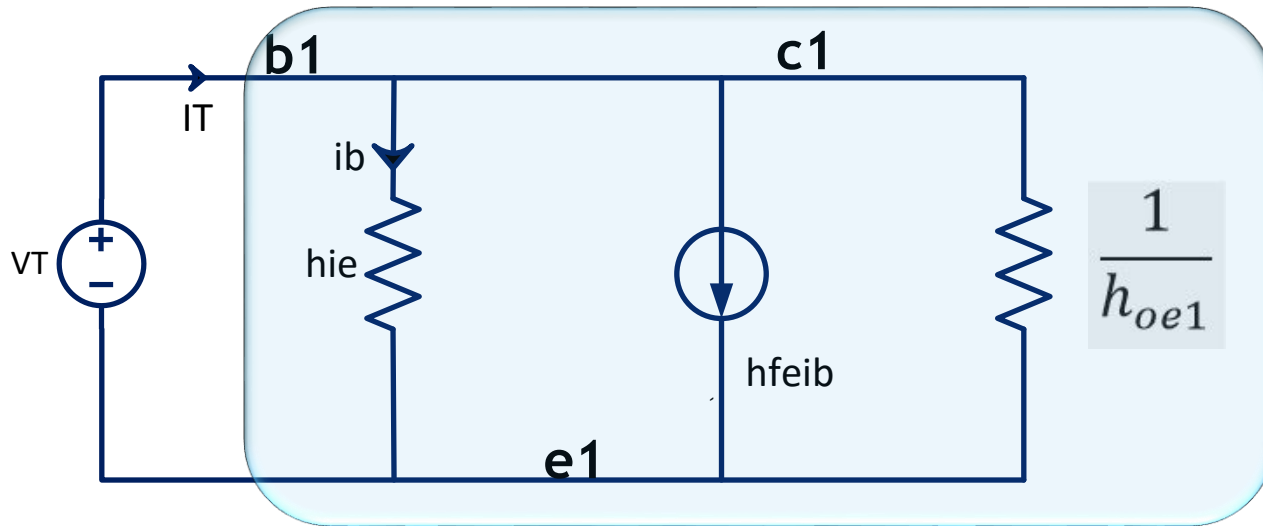
The Wilson current mirror

To prove that $R_o \approx \frac{h_{fe}}{2} \frac{1}{h_{oe}}$



Bipolar transistor current sources:

The Equivalent circuit for a diode connected transistor



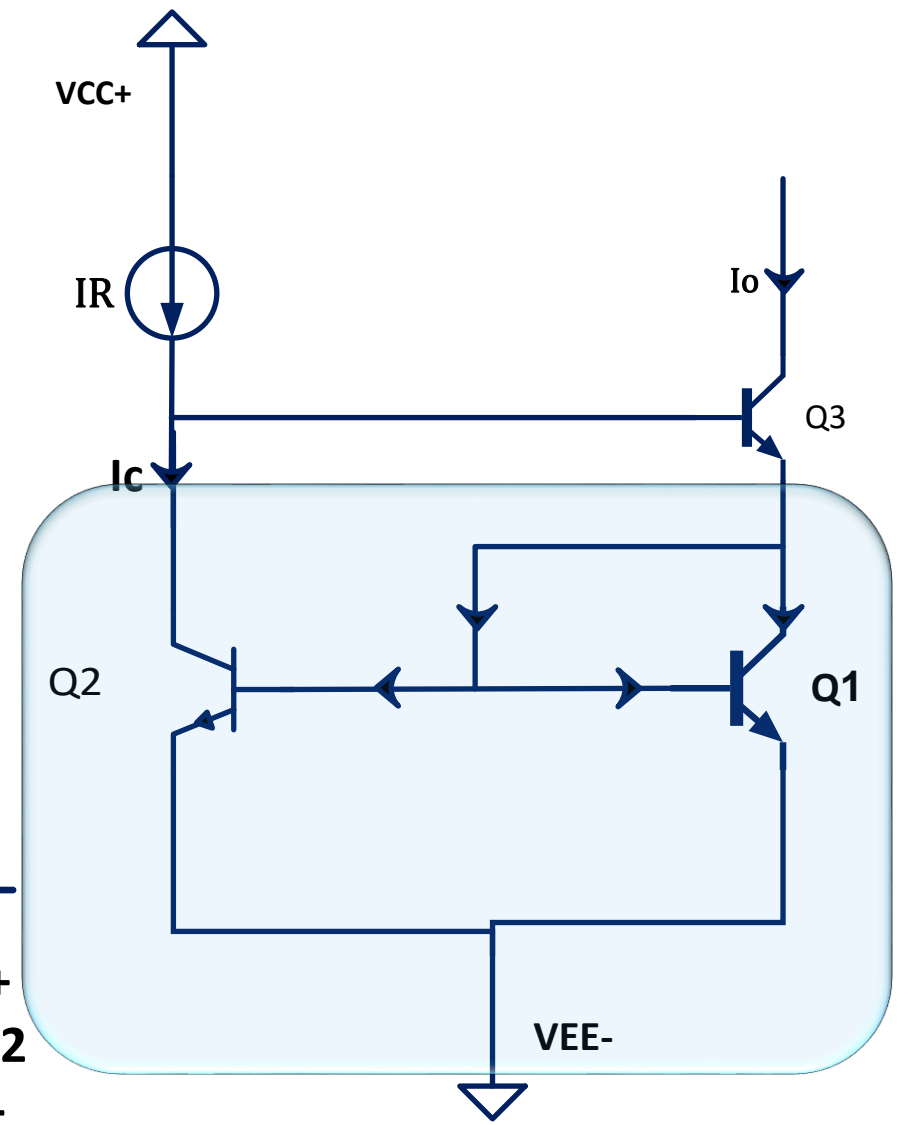
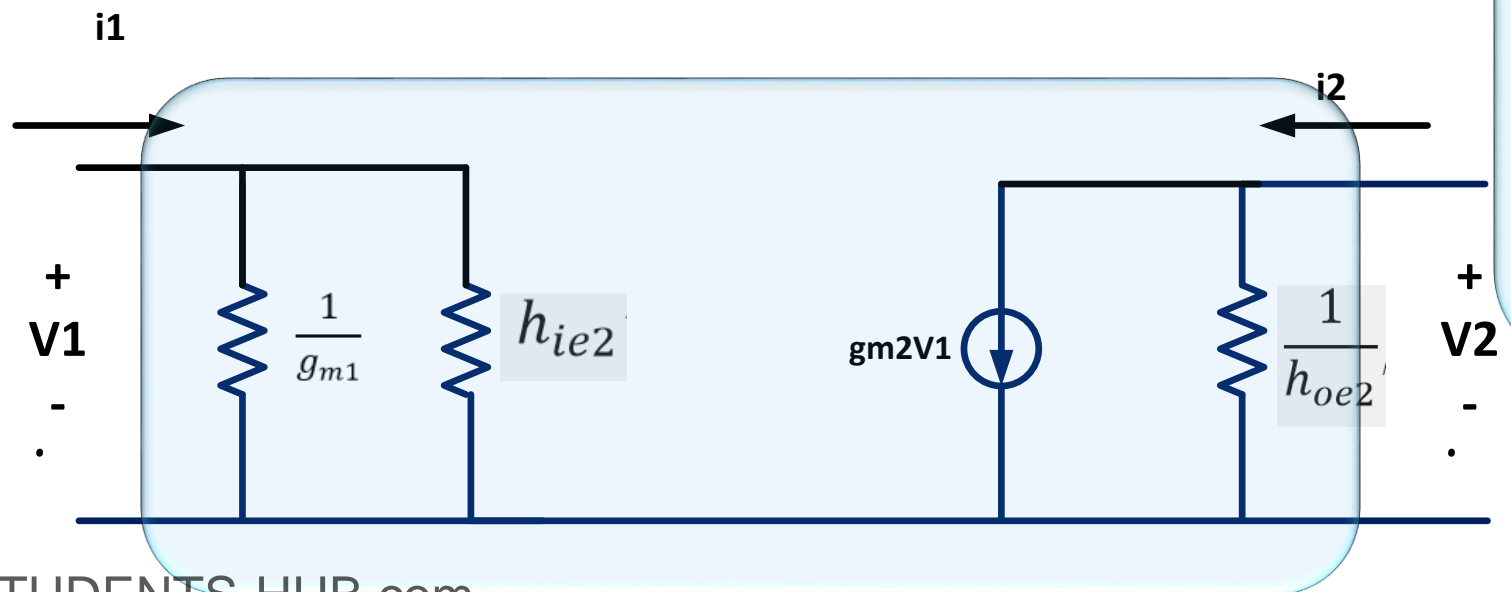
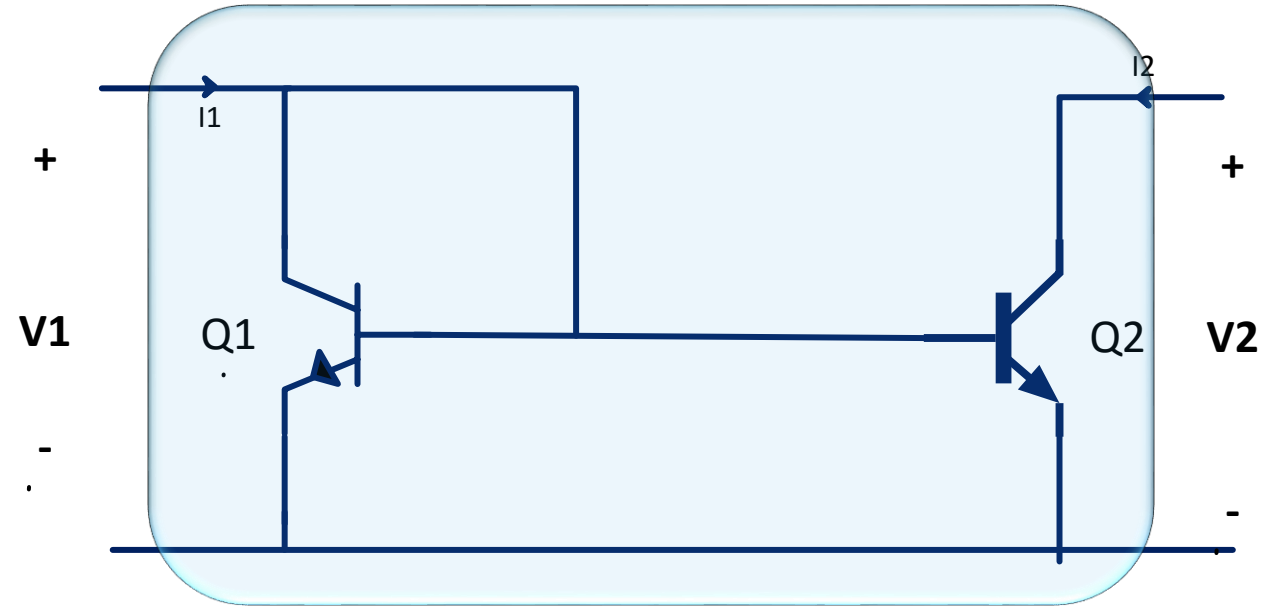
$$I_T = h_{fe1} i_{b1} + \frac{V_T}{h_{ie1} \parallel \frac{1}{h_{oe1}}}$$

$$i_{b1} = \frac{V_T}{h_{ie1}}$$

$$\therefore \frac{V_T}{I_T} = \frac{1}{g_{m1}} \parallel h_{ie1} \parallel \frac{1}{h_{oe1}}$$

$$R_{TH} \approx \frac{1}{g_{m1}} \approx h_{ib1}$$

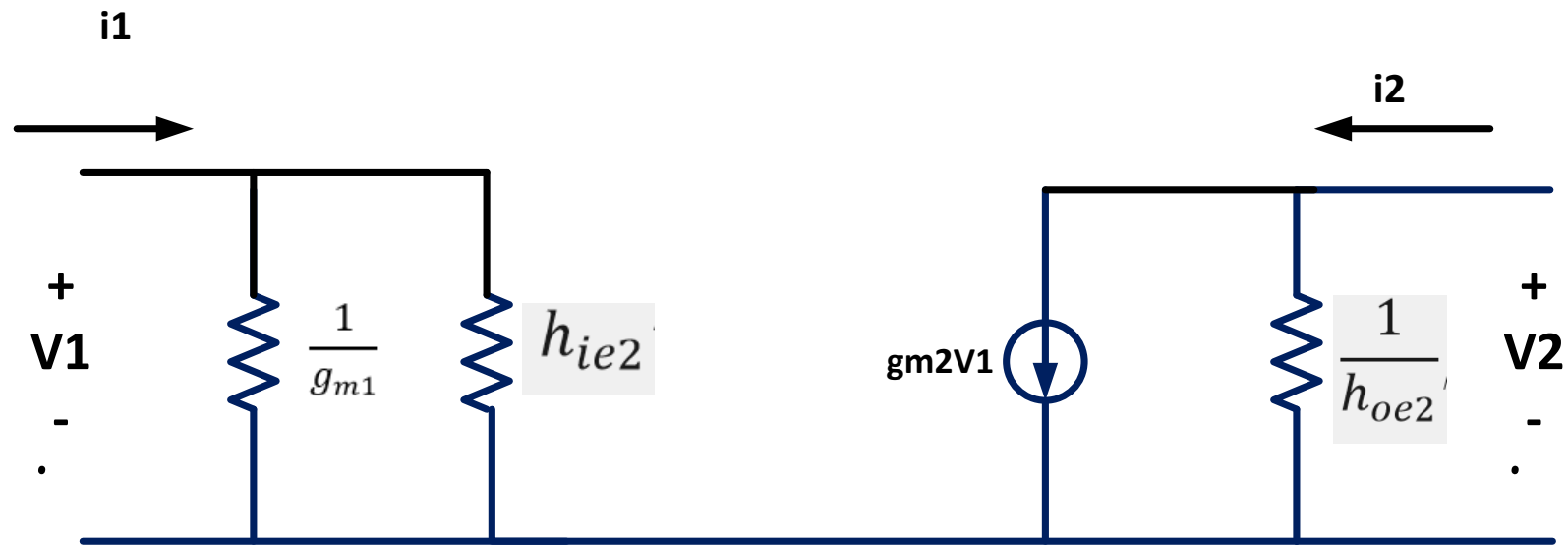
Two Port Model for the current mirror



Two Port Model for the current mirror

$$V_1 = h_{11} i_1 + h_{12} V_2$$

$$i_2 = h_{21} i_1 + h_{22} V_2$$



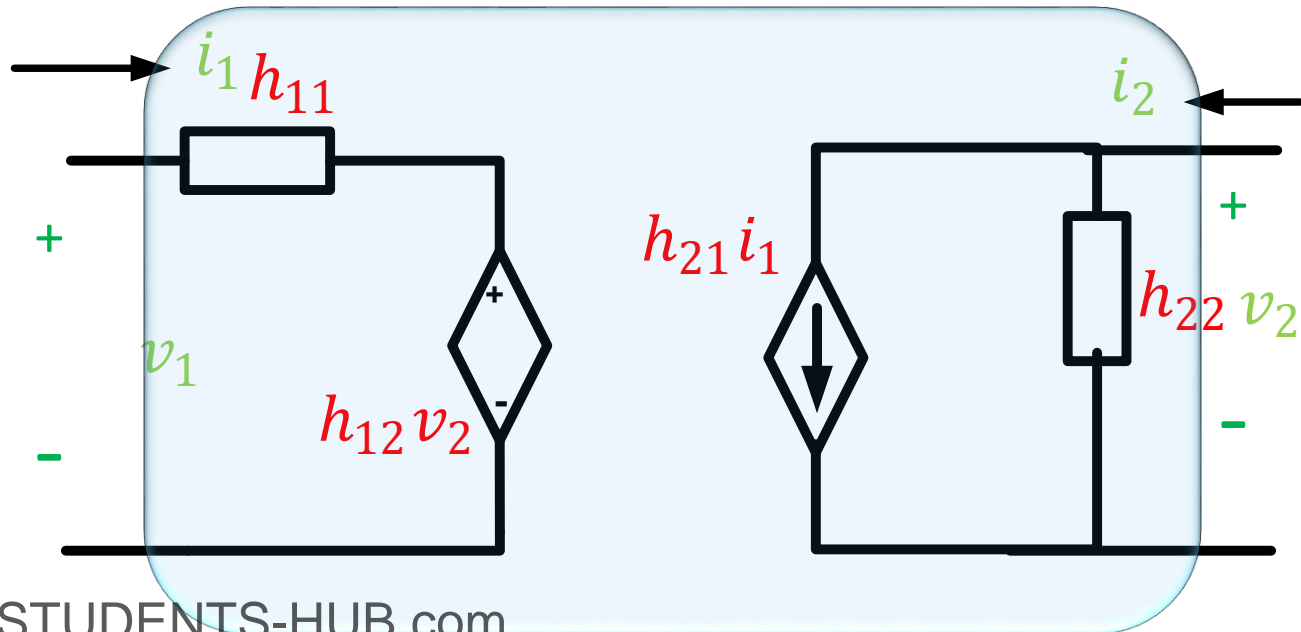
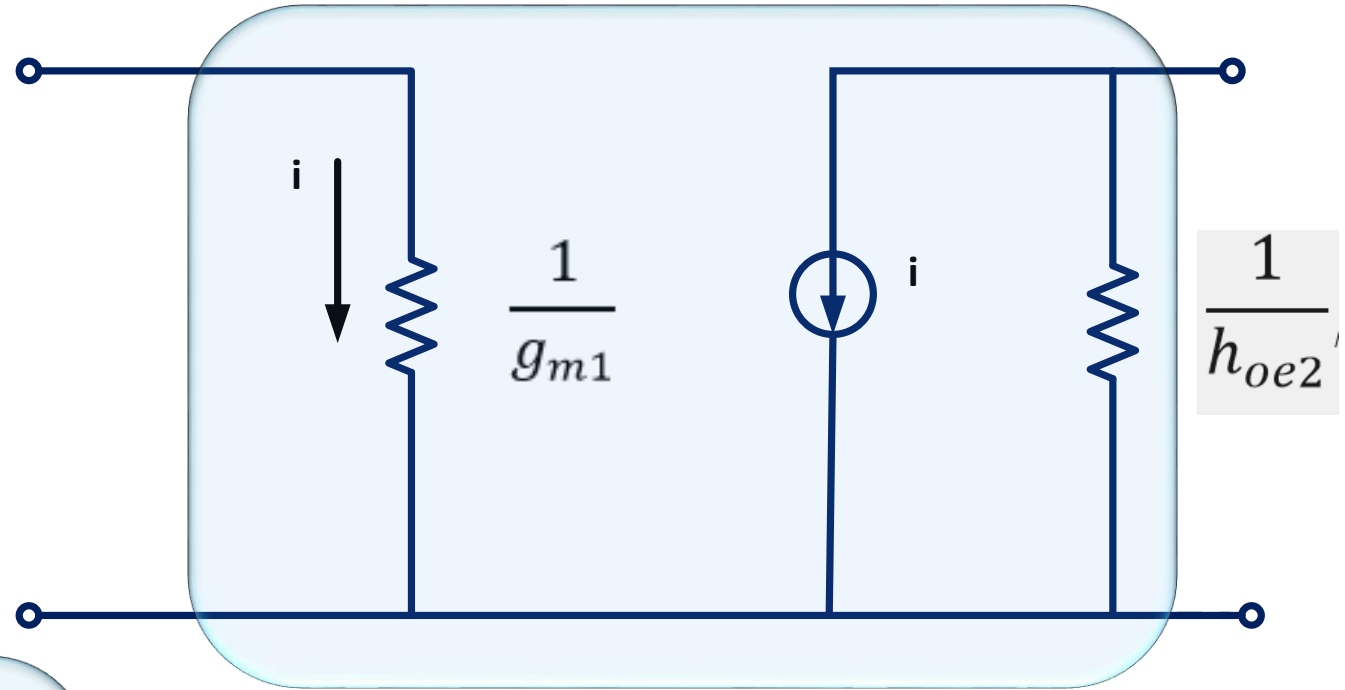
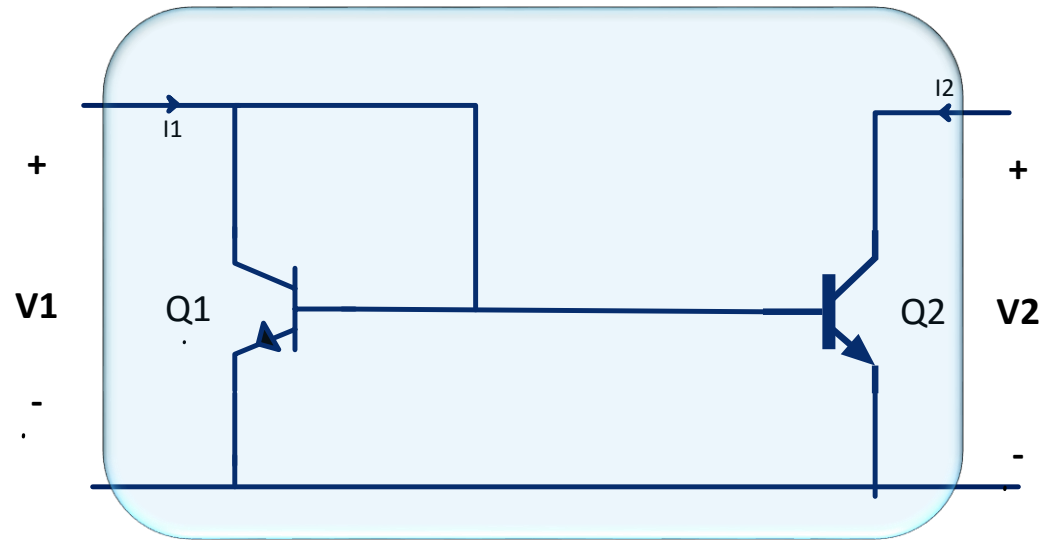
$$h_{11} = \frac{v_1}{i_1} \Big|_{v_2=0} = \frac{1}{g_{m1}} \parallel h_{ie2} \approx \frac{1}{g_{m1}}$$

$$h_{12} = \frac{v_1}{v_2} \Big|_{i_1=0} = 0$$

$$h_{22} = \frac{i_2}{v_2} \Big|_{i_1=0} = h_{oe2}$$

$$h_{21} = \frac{i_2}{i_1} \Big|_{v_2=0} = \frac{g_{m2} h_{ie2}}{1 + g_{m1} h_{ie1}} \approx \frac{g_{m2}}{g_{m1}} = 1$$

Two Port Model for the current mirror



$$h_{11} = \frac{1}{g_{m1}}$$

$$h_{12} = 0$$

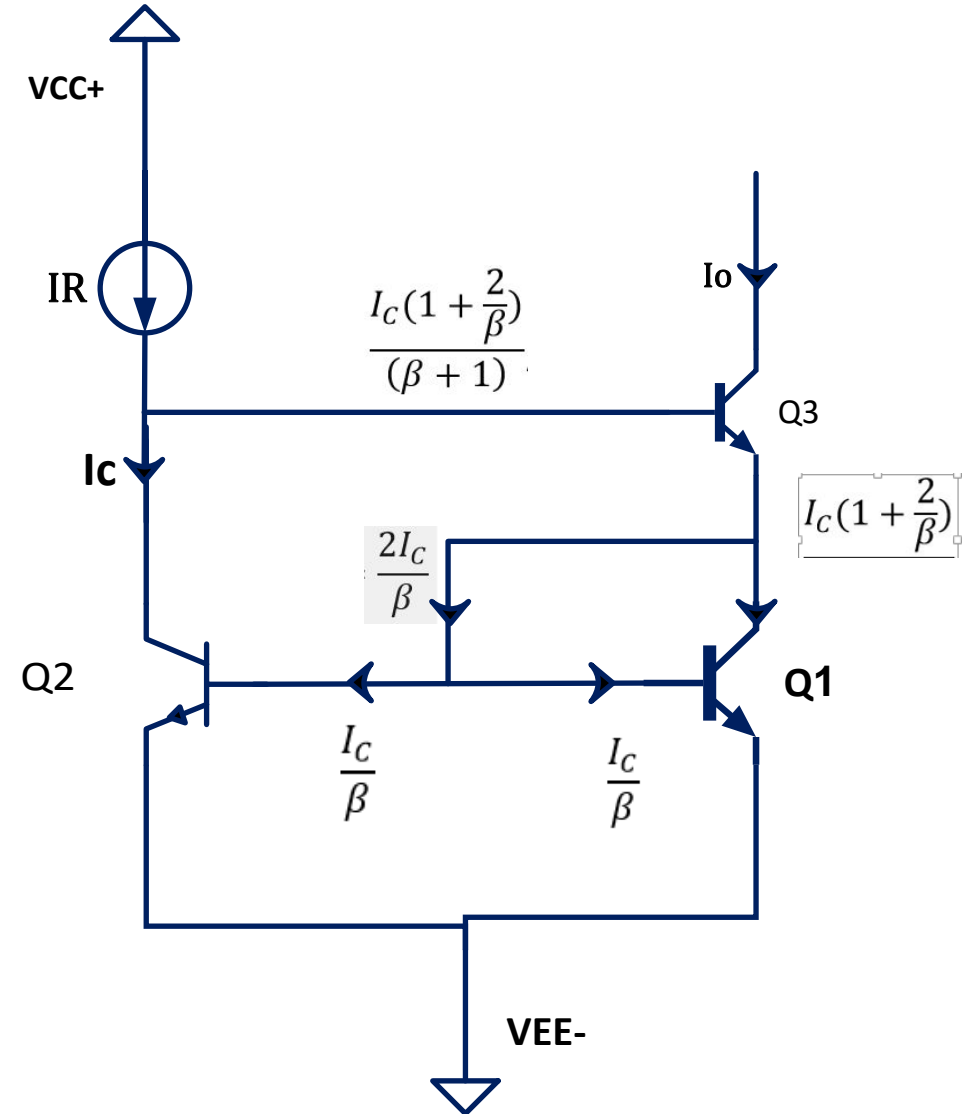
$$h_{21} = 1$$

$$h_{22} = h_{oe2}$$

Differential Amplifiers

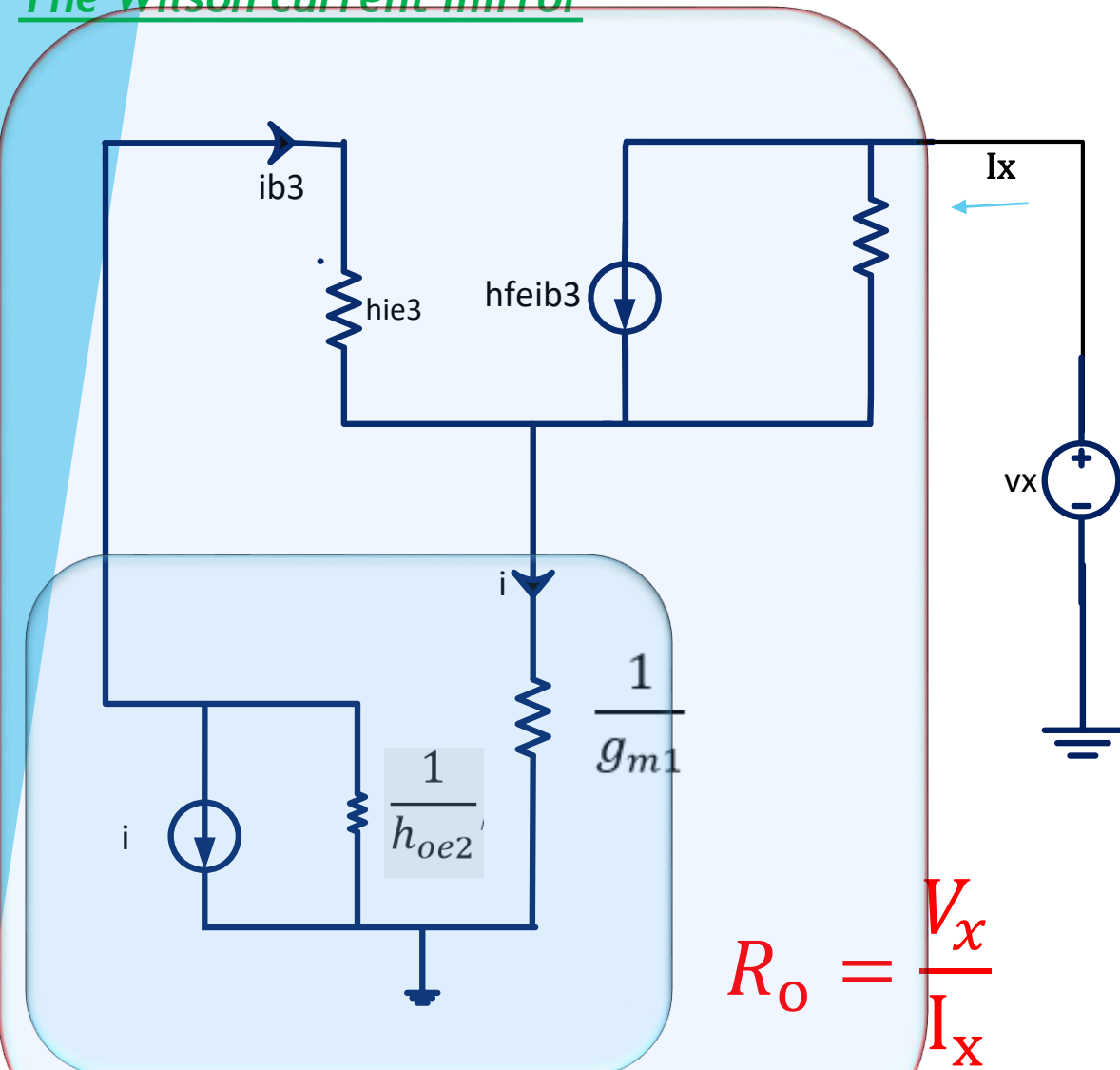
The Wilson Current:

To proof $R_o \cong \frac{h_{fe}}{2} \cdot \frac{1}{h_{oe3}}$

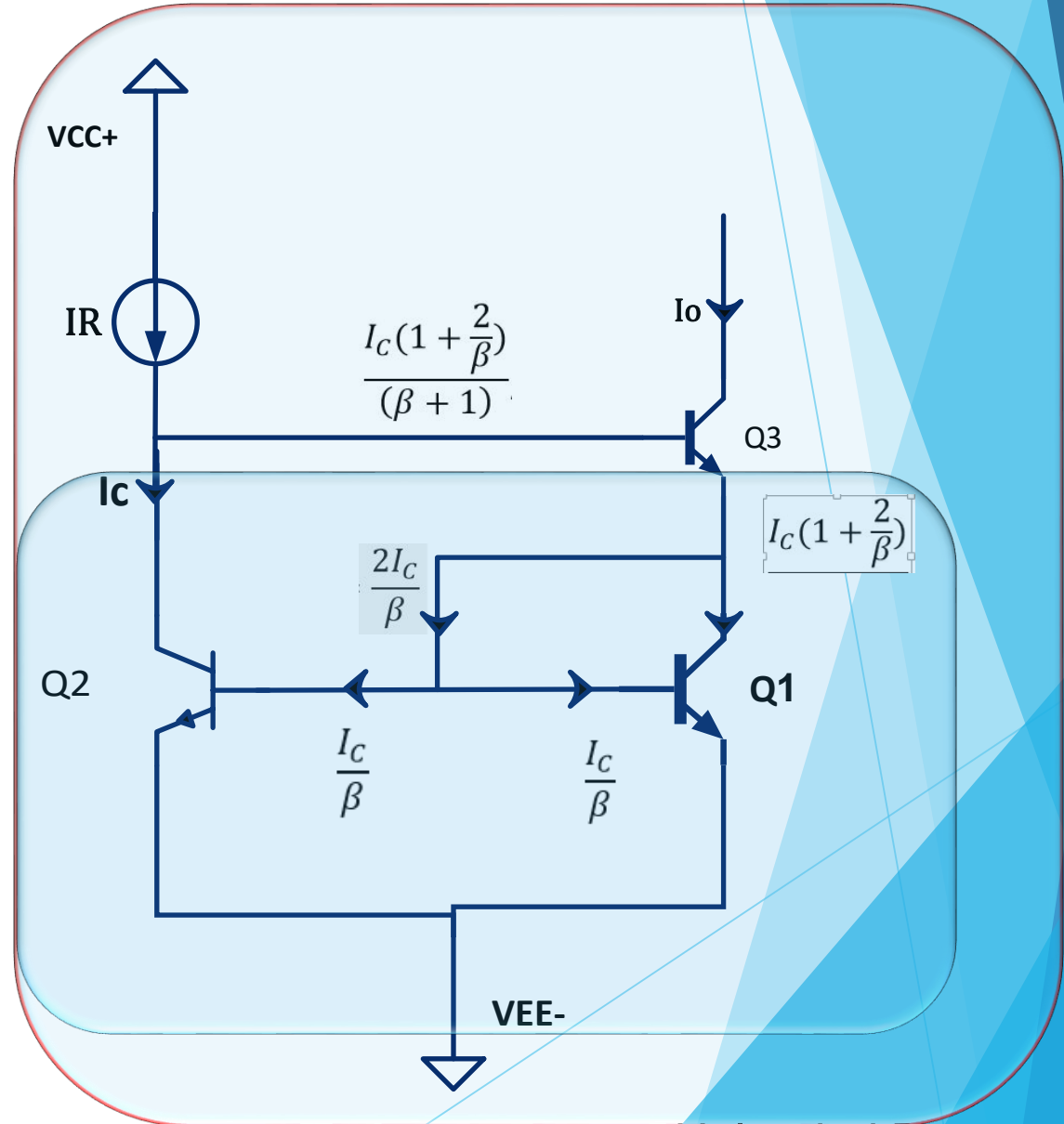


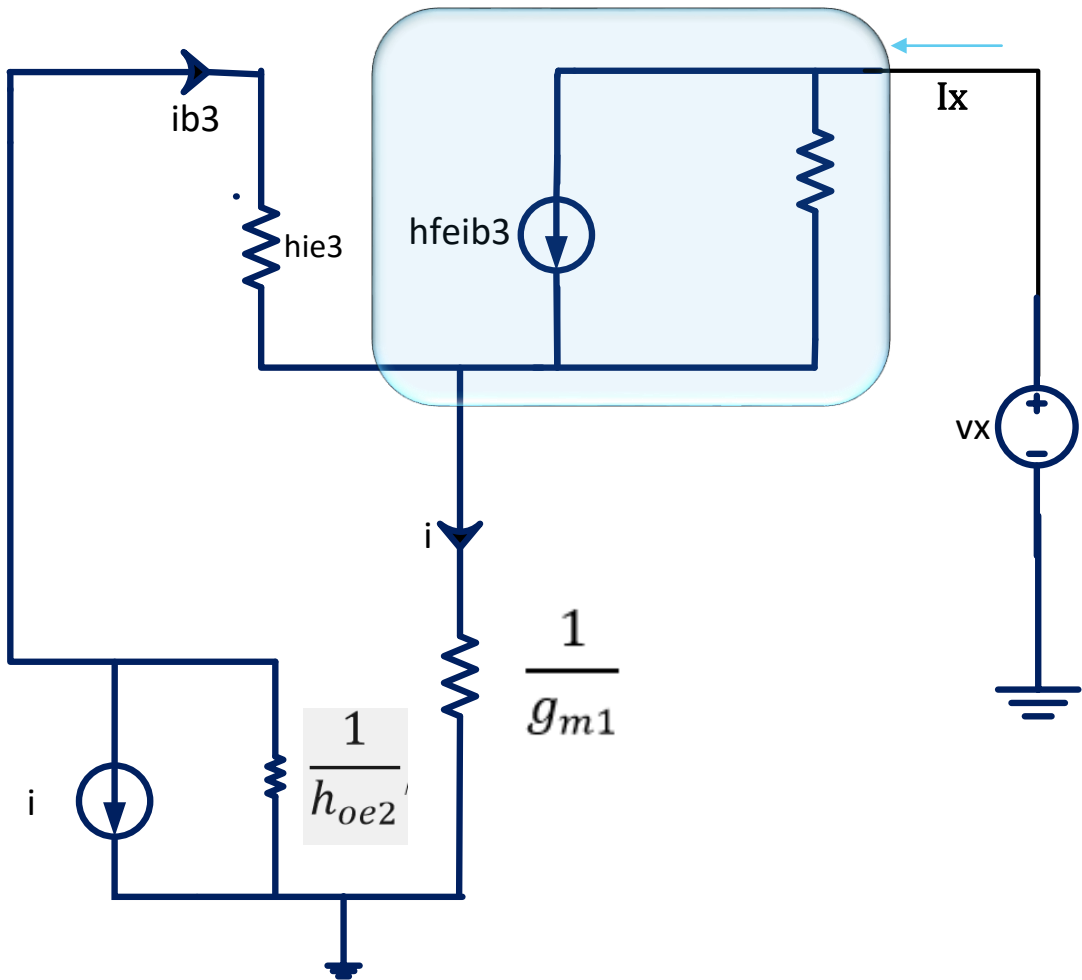
Differential Amplifiers

The Wilson current mirror

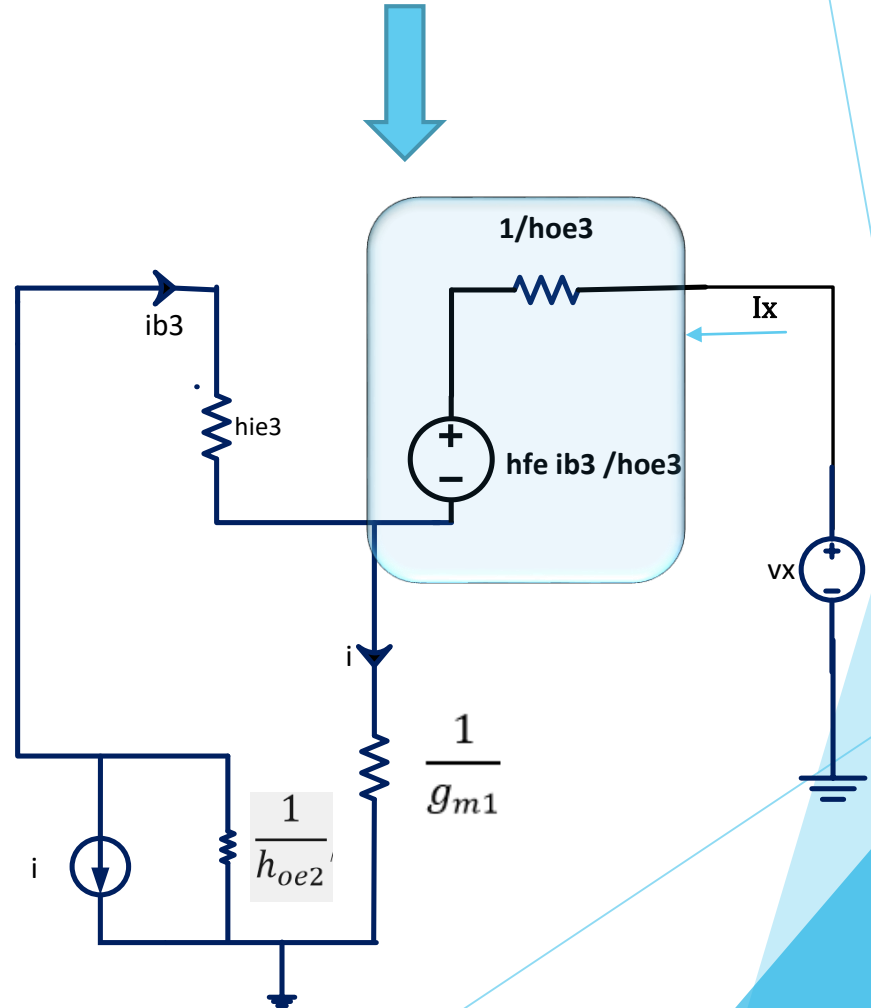


$$R_o = \frac{V_x}{I_x}$$





Source transformation



The Wilson current mirror

$$V_X + \frac{h_{fe}}{h_{oe3}} ib_3 = \left(\frac{1}{h_{oe3}} + \frac{1}{g_{m1}} \right) I_X + \frac{1}{g_{m1}} ib_3$$

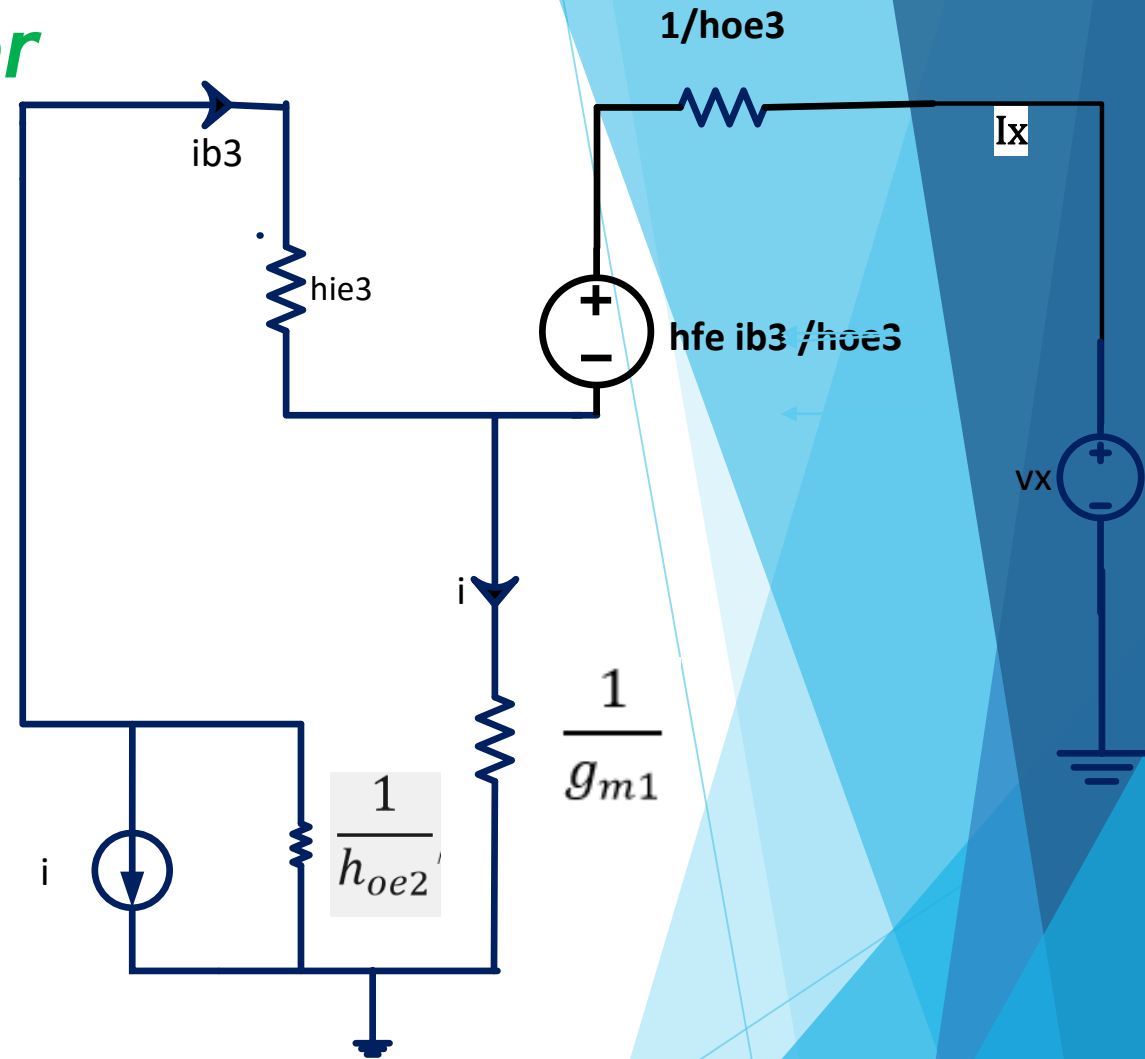
$$V_X = \left(\frac{1}{h_{oe3}} + \frac{1}{g_{m1}} \right) I_X + \left(\frac{1}{g_{m1}} - \frac{h_{fe}}{h_{oe3}} \right) ib_3$$

since $\frac{1}{h_{oe3}} \gg \frac{1}{g_{m1}}$ and $\frac{h_{fe}}{h_{oe3}} \gg \frac{1}{g_{m1}}$

$$V_X = \frac{1}{h_{oe3}} I_X - \frac{h_{fe}}{h_{oe3}} ib_3 \rightarrow (1)$$

$$-\frac{i}{h_{oe2}} = \frac{1}{g_{m1}} I_X + \left(h_{ie3} + \frac{1}{g_{m1}} + \frac{1}{h_{oe2}} \right) ib_3 \rightarrow (2)$$

$$i = ib_3 + I_X \rightarrow (3)$$

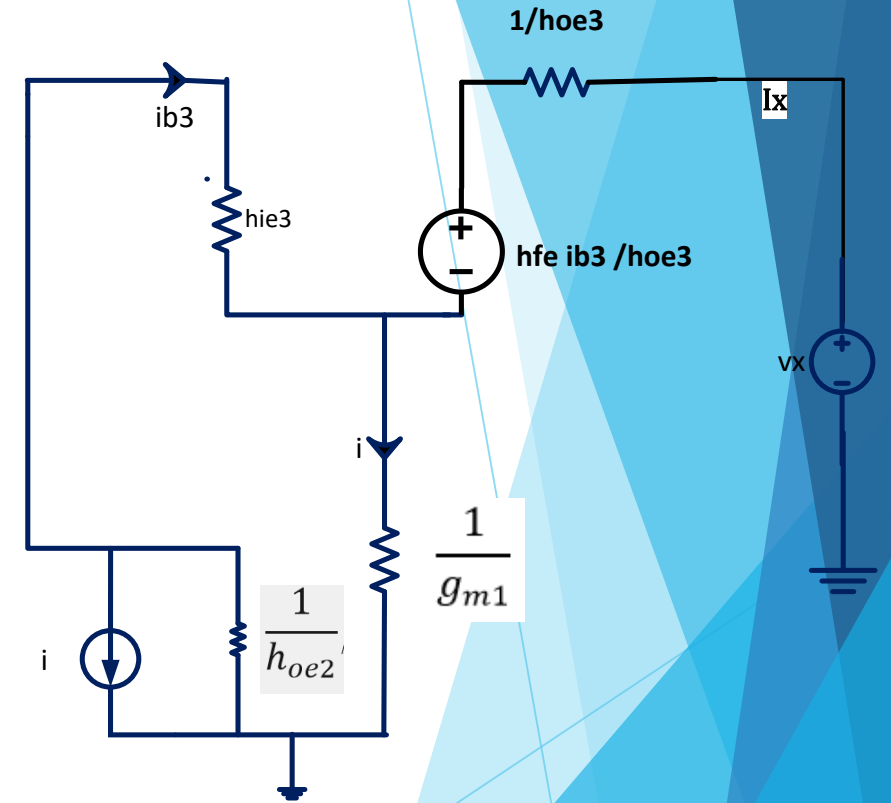


sub (3) into (2) ▶

$$0 = \left(\frac{1}{h_{oe2}} + \frac{1}{g_{m1}} \right) I_X + \left(\frac{1}{g_{m1}} + h_{ie3} + \frac{2}{h_{oe2}} \right) ib_3 \quad \blacktriangleright$$

since $\frac{1}{h_{oe2}} \gg \frac{1}{g_{m1}}$ and $\frac{2}{h_{oe2}} \gg \frac{1}{g_{m1}} + h_{ie3}$ ▶

$$0 = \frac{1}{h_{oe2}} I_X + \frac{2}{h_{oe2}} ib_3 \rightarrow (4) \quad \blacktriangleright$$



The Wilson current mirror

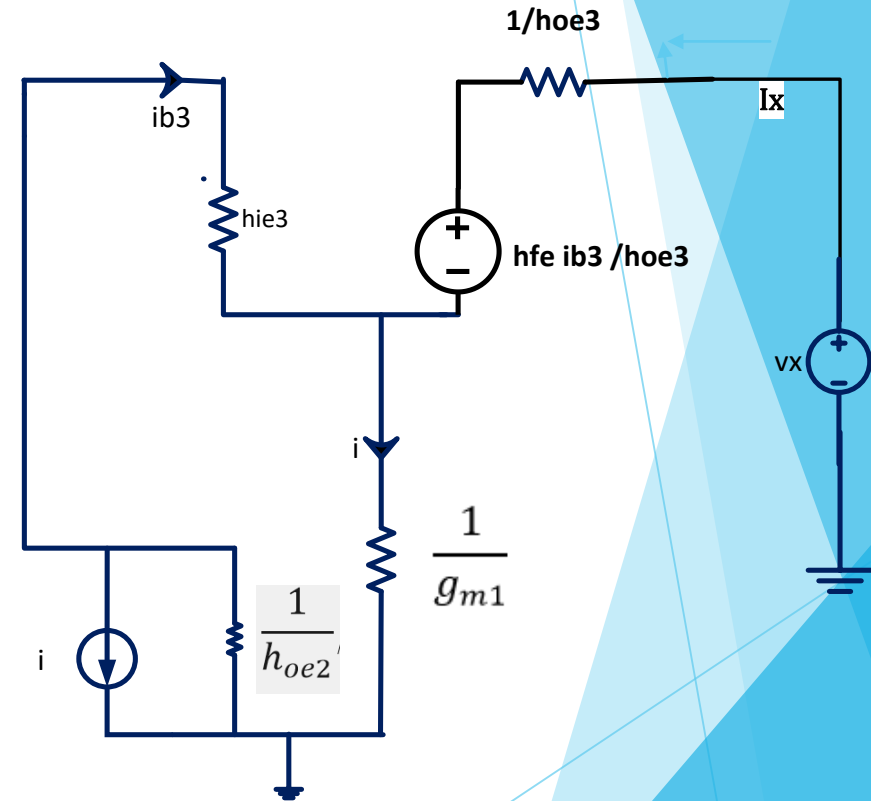
$$V_X = \frac{1}{h_{oe3}} I_X - \frac{h_{fe}}{h_{oe3}} ib_3 \rightarrow (1)$$

using (4) we get $ib_3 = -\frac{I_X}{2}$

$$\therefore V_X = \frac{1}{h_{oe3}} I_X + \frac{h_{fe}}{2} \frac{1}{h_{oe3}} I_X$$

$$\therefore \frac{V_X}{I_X} = \left(\frac{h_{fe}}{2} + 1 \right) \frac{1}{h_{oe3}}$$

$$\therefore R_o = \frac{V_X}{I_X} \approx \frac{h_{fe}}{2} \frac{1}{h_{oe3}}$$



4. Widlar Current Source:

- To Produce Very small I_o
- To increase R_o

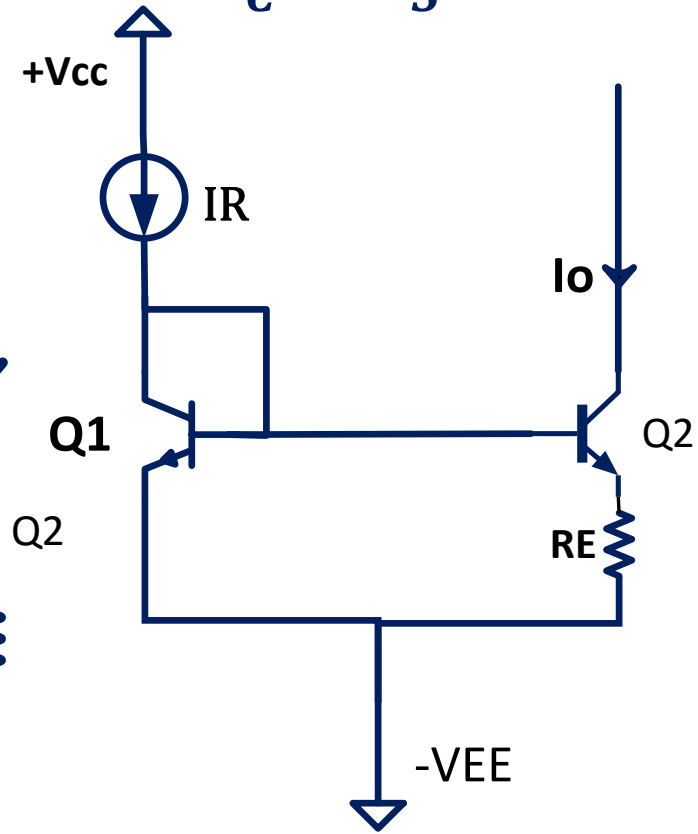
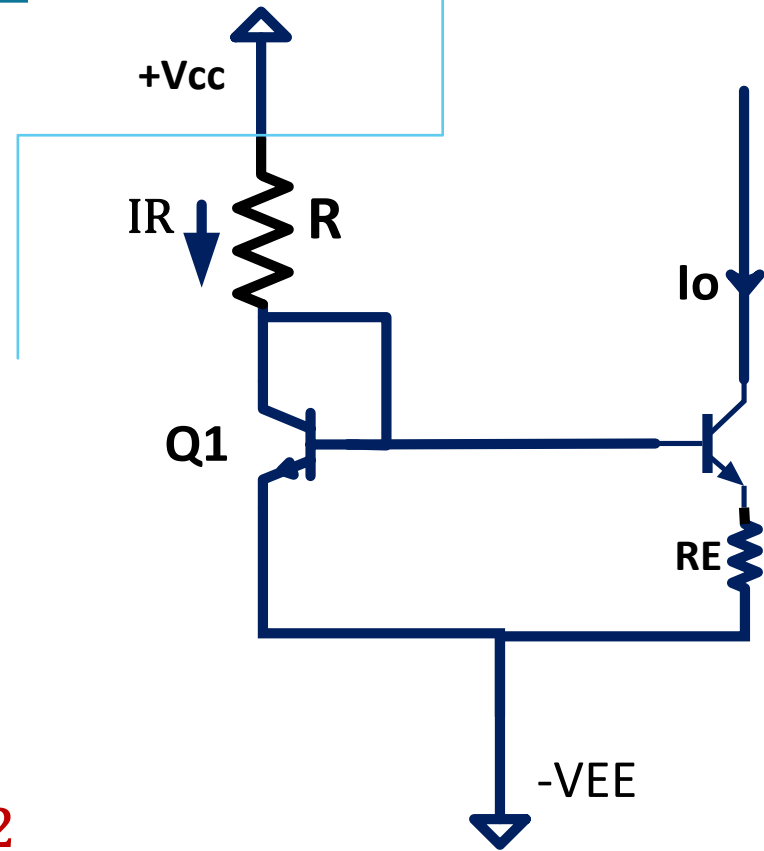
$$KVL : V_{BE1} = V_{BE2} + R_E I_{E2}$$

$$V_T \ln \frac{I_{C1}}{I_{S1}} = V_T \ln \frac{I_{C2}}{I_{S2}} + R_E I_{E2}$$

$$V_T \ln \frac{I_{C1}}{I_{S1}} - V_T \ln \frac{I_{C2}}{I_{S2}} = R_E I_{E2}$$

if Q_1 and Q_2 are matched

$$I_{C1} > I_{C2} = I_o \quad I_C = I_S e^{\frac{V_{BE}}{V_T}}$$



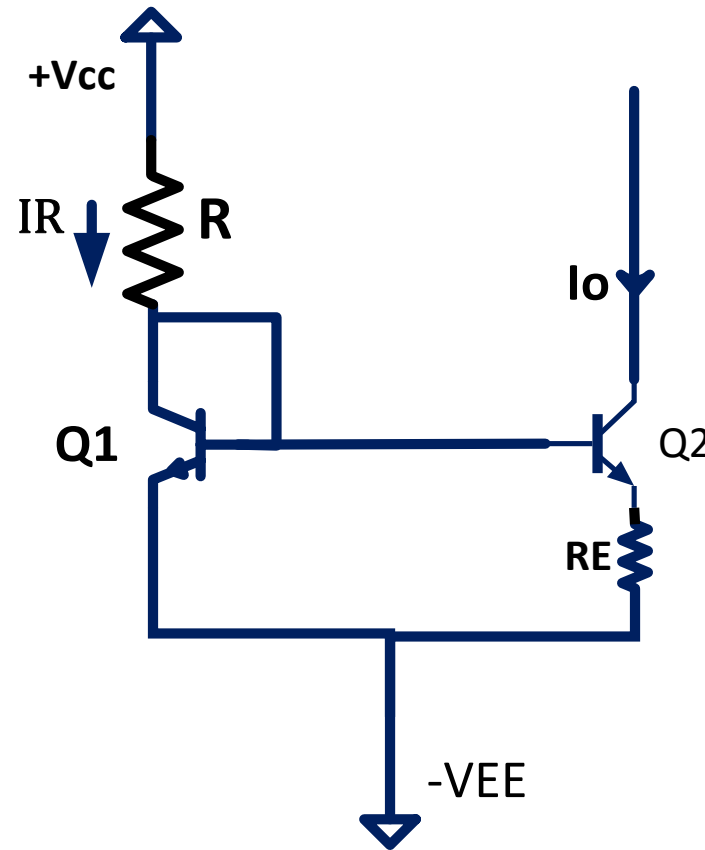
$$V_T \ln \frac{I_{C1}}{I_{C2}} = R_E I_{E2}$$

$$V_T \ln \frac{I_{C1}}{I_{C2}} = R_E I_{E2}$$

if $\beta = \infty$

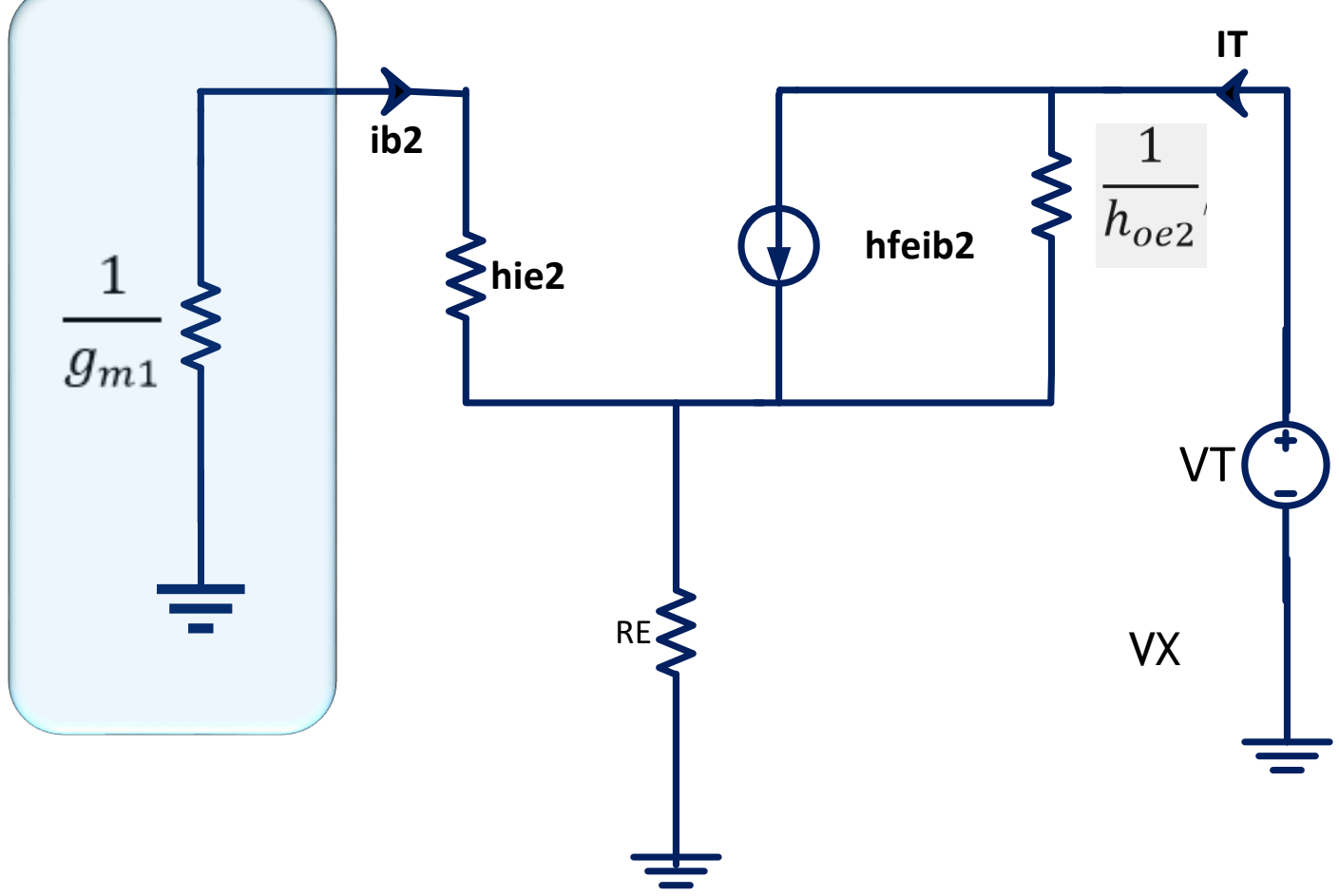
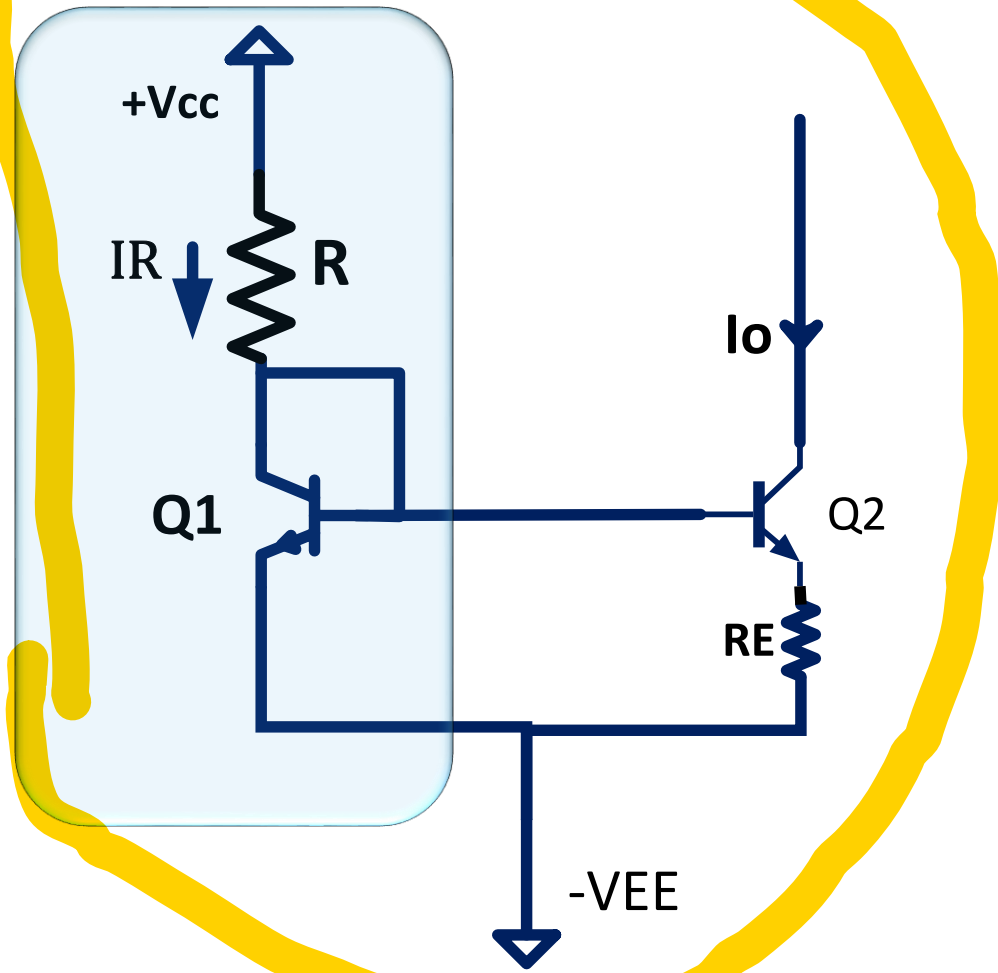
$$V_T \ln \frac{I_R}{I_0} = R_E I_0$$

$$I_R = \frac{V_{CC} + V_{EE} - V_{BE1}}{R}$$



4. Widlar Current Source:

- To Find R_o :



$$R_o \approx \frac{1}{h_{oe2}} + \frac{h_{fe}}{h_{oe2}} \frac{R_E}{R_E + h_{ie2} + \frac{1}{g_{m1}}}$$

Design a simple current mirror to generate $I_o = 10\mu\text{A}$
given that $V_{BE} = 0.7\text{ V}$ @ 1mA

Assume $\beta = \infty$, $V_{CC} = 10\text{V}$ and $V_{EE} = 0\text{V}$

We need to find the value of V_{BE} @ $10\mu\text{A}$

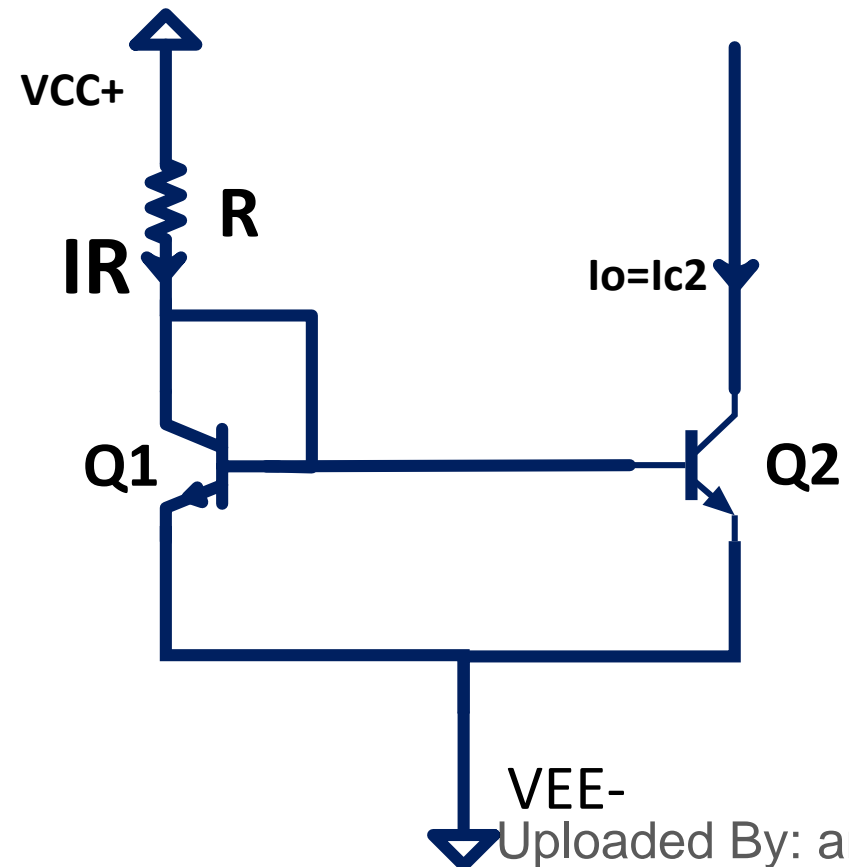
$$V_{BE} = V_T \ln \frac{I_C}{I_S}$$

$$V_{BE2} - V_{BE1} = V_T \ln \frac{I_{C2}}{I_{C1}}$$

$$V_{BE2} = V_{BE1} + V_T \ln \frac{I_{C2}}{I_{C1}}$$

$$= 0.7 + V_T \ln \frac{10\mu\text{A}}{1\text{mA}}$$

$$= 0.58\text{ V}$$



Differential Amplifiers

Design a simple current mirror to generate $I_o = 10\mu A$
given that $V_{BE} = 0.7 V @ 1mA$

Assume $\beta = \infty$, $V_{CC} = 10V$ and $V_{EE} = 0V$

$$V_{BE} = 0.7 V @ I_C = 1mA$$

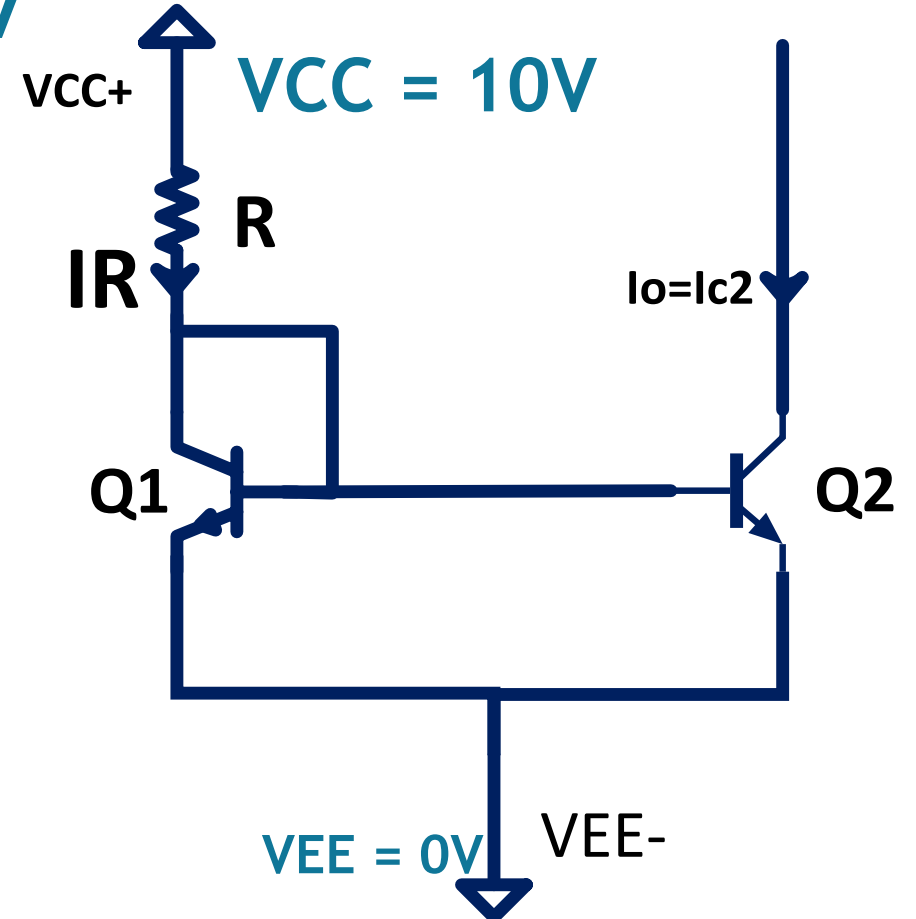
$$V_{BE} = 0.58 V @ I_C = 10\mu A$$

$$KVL : V_{CC} = R I_R + V_{BE}$$

$$\text{since } \beta = \infty$$

$$I_R = I_o = 10\mu A$$

$$R = 942K$$



Too Large , Not Practical

Design a Wedlar current source to generate $I_o = 10\mu A$

given that $V_{BE} = 0.7 V$ @ $I_c = 1mA$

Assume $\beta = \infty$, $V_{CC} = 10V$ and $V_{EE} = 0V$

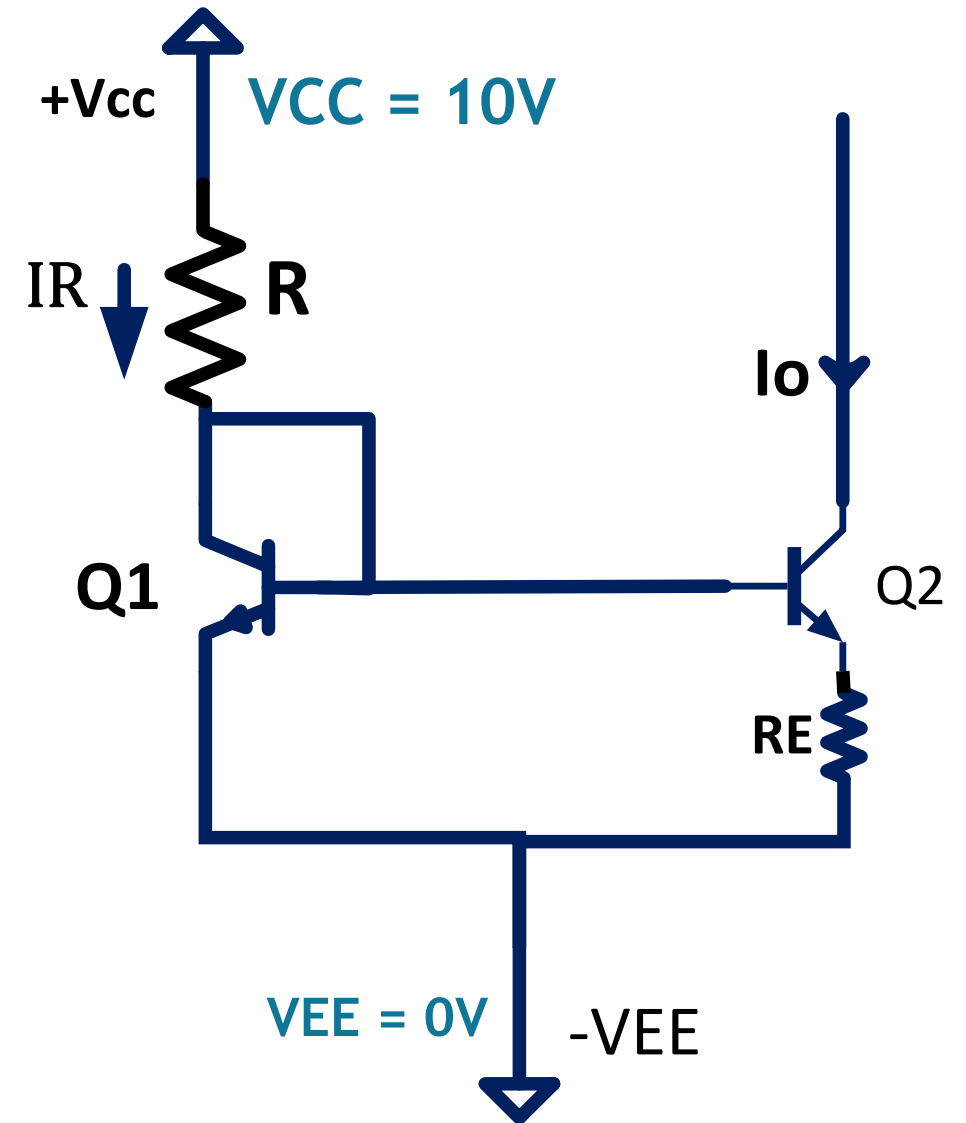
Assume that $I_R = 1mA$

$$\therefore V_{BE1} = 0.7 V$$

$$R = \frac{V_{CC} - V_{BE1}}{I_R} = 9.3k$$

$$I_o R_E = V_T \ln \frac{I_R}{I_o}$$

$$\therefore R_E = 11.5k$$

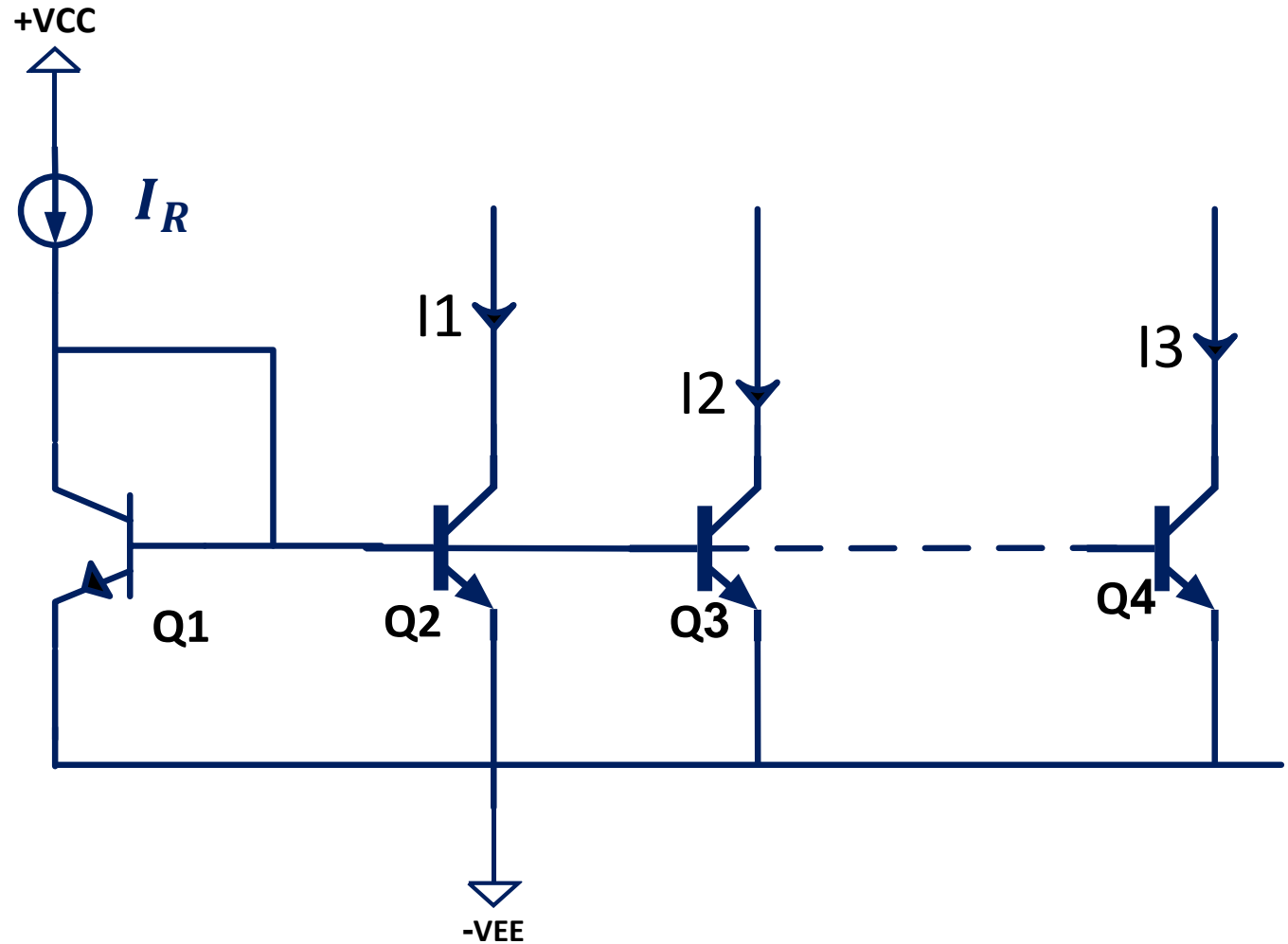


smaller resistor ; smaller chip area

Multitransistor Current Mirror

If β is finite and all the transistors are matched:

$$I_1 = I_2 = I_3 = \frac{I_R}{1 + \frac{(N + 1)}{\beta}}$$



Generalized Current Mirror

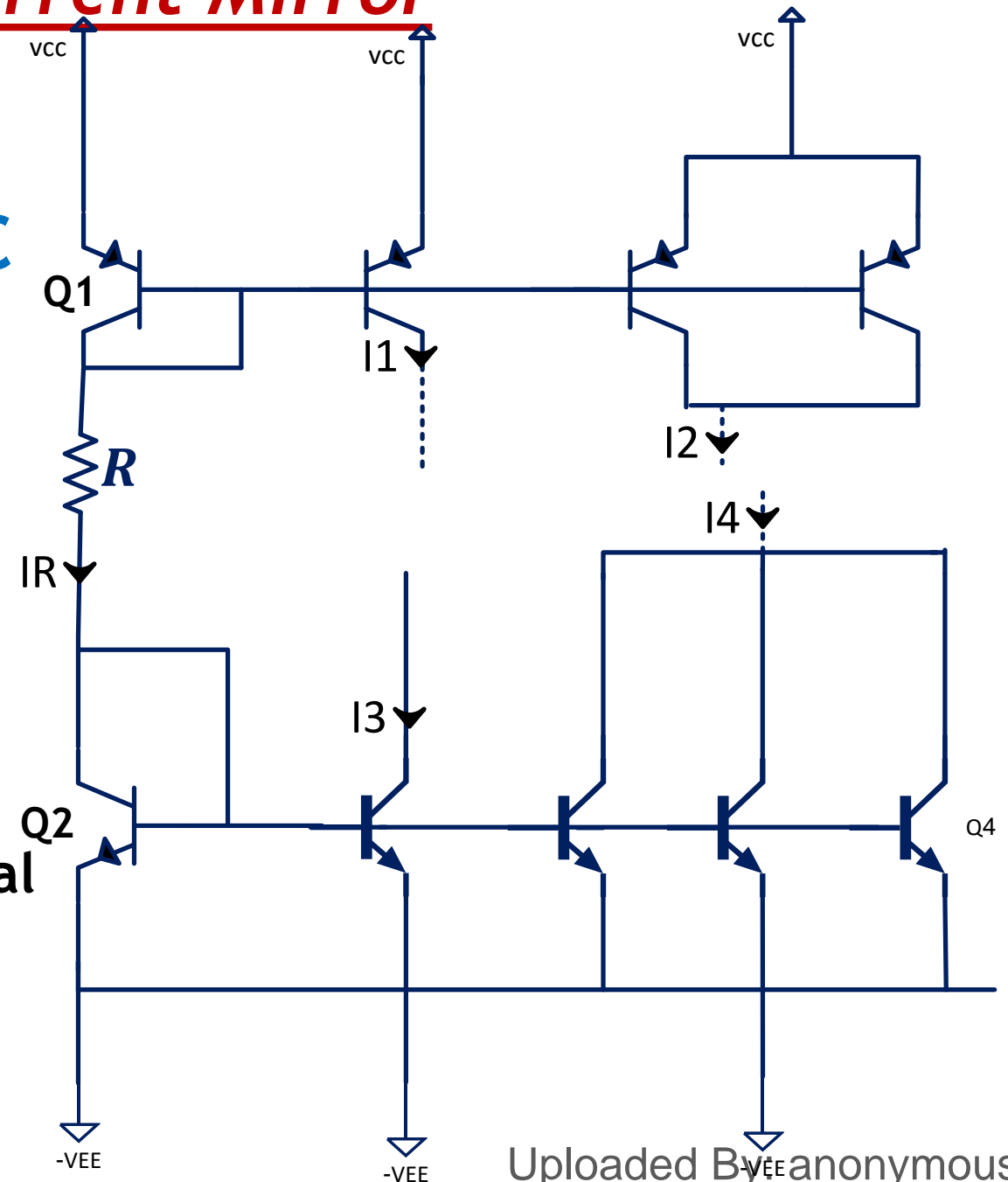
To Generate bias currents for different amplifier stages in an IC

$$I_R = \frac{V_{CC} + V_{EE} - V_{EB1} - V_{BE2}}{R}$$

if $\beta \rightarrow \infty$

Since $|V_{BE}|$ For all the transistors are equal

$$I_1 = I_R ; I_2 = 2I_R ; I_4 = 3I_R$$



Mosfet Current Sources:

The Basic mosfet Current Source

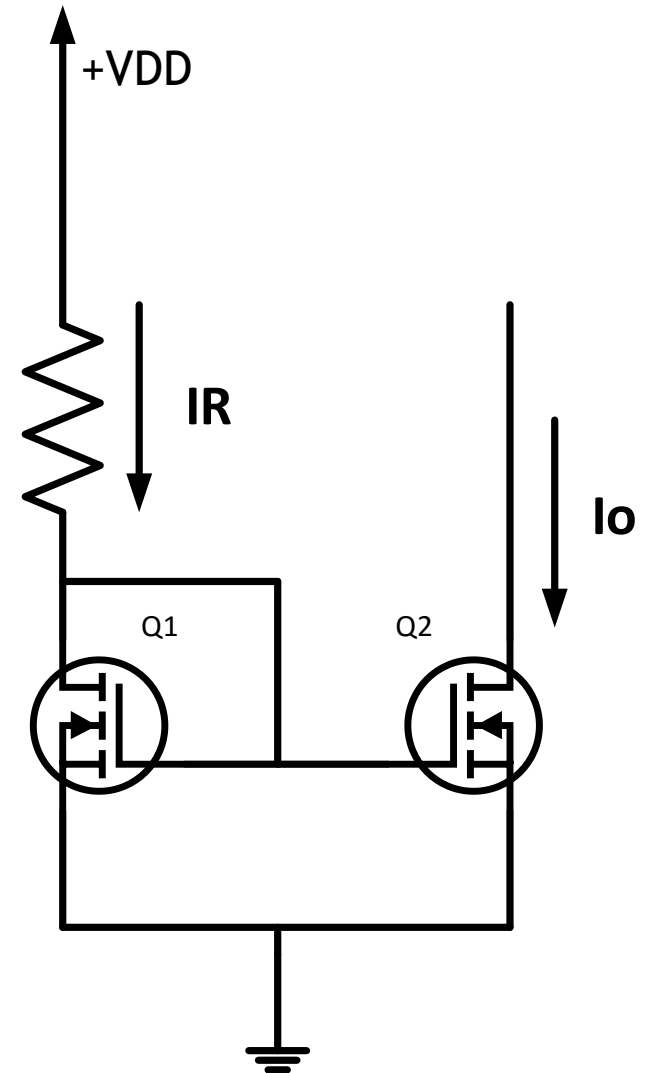
Since $V_{G1} = V_{D1}$ and $V_{GS} = V_{DS}$
 $|V_{DS}| > |V_{GS} - V_T|$

$\therefore Q1$ is operated in the pinch off region

$$I_{DS1} = \frac{1}{2} \bar{K}_{n1} \left(\frac{W}{L}\right)_1 (V_{GS1} - V_T)^2$$

$$I_o = I_{DS2} = \frac{1}{2} \bar{K}_{n2} \left(\frac{W}{L}\right)_2 (V_{GS2} - V_T)^2$$

$$I_R = I_{DS1} + I_{G1} + I_{G2} = I_{DS1}$$

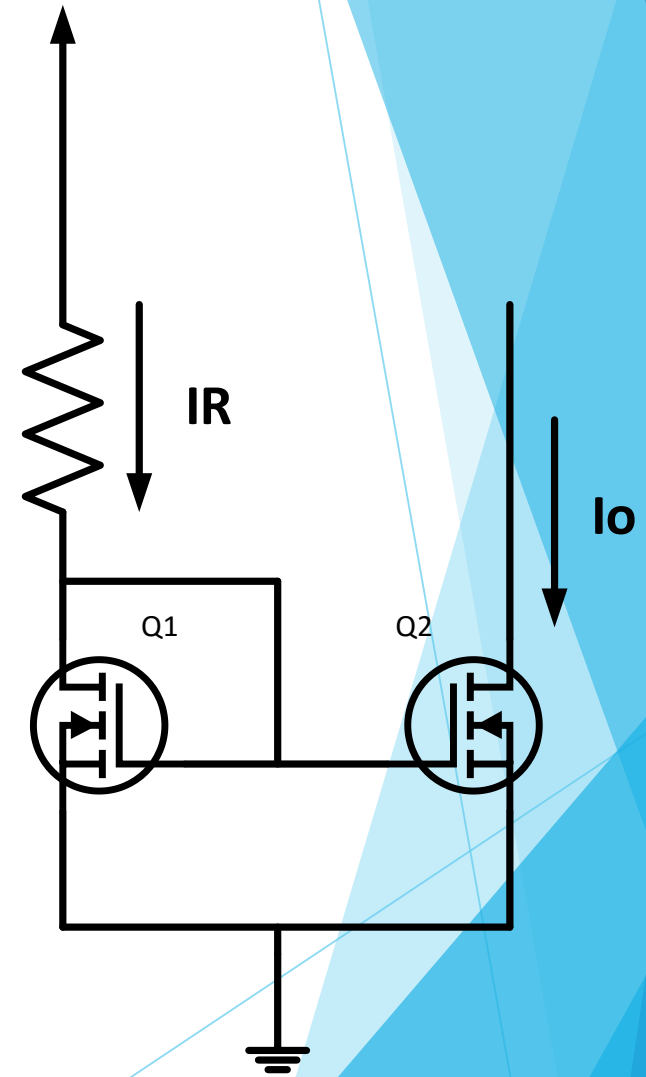


$$I_R = I_{DS1} = \frac{1}{2} \bar{K}_{n1} \left(\frac{W}{L} \right)_1 (V_{GS1} - V_T)^2$$

$$I_o = I_{DS2} = \frac{1}{2} \bar{K}_{n2} \left(\frac{W}{L} \right)_2 (V_{GS2} - V_T)^2$$

*Since $V_{GS1} = V_{GS2}$
and $V_{T1} = V_{T1}$, and $\bar{K}_{n1} = \bar{K}_{n2}$*

$$\therefore \frac{I_o}{I_R} = \frac{\left(\frac{W}{L} \right)_2}{\left(\frac{W}{L} \right)_1} \equiv \text{current gain}$$



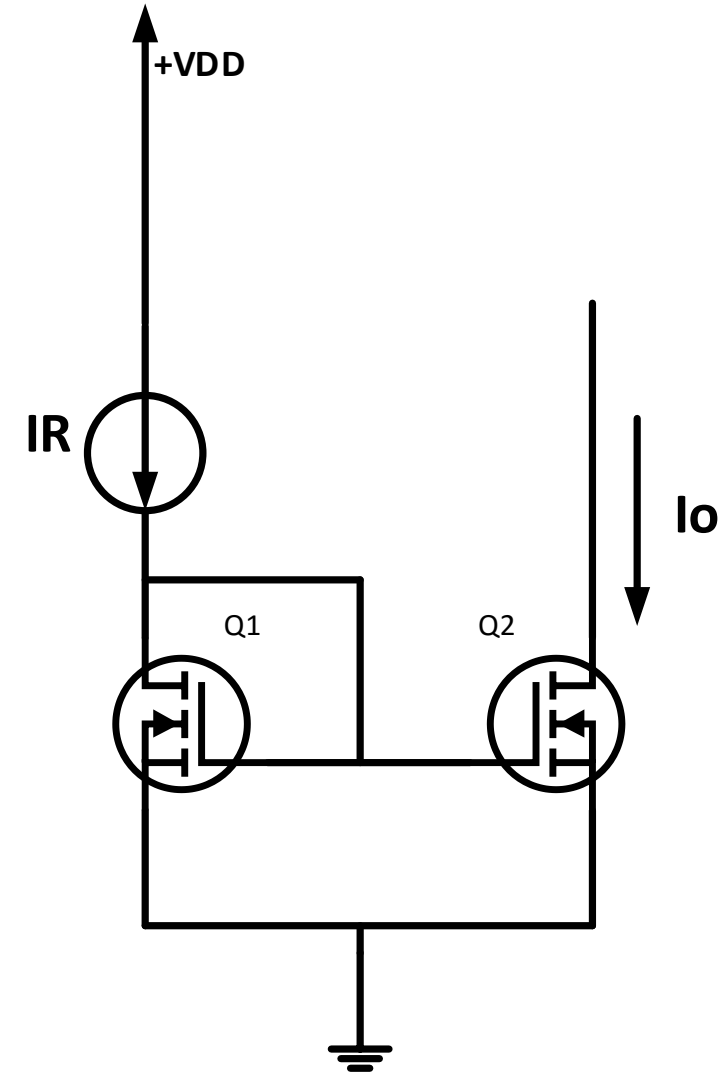
Mosfet Current Sources:

The Basic mosfet Current Source

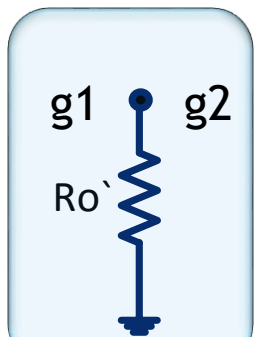
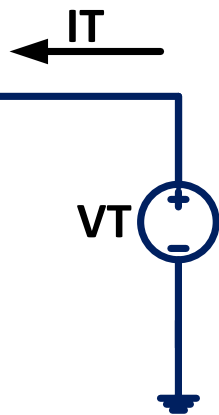
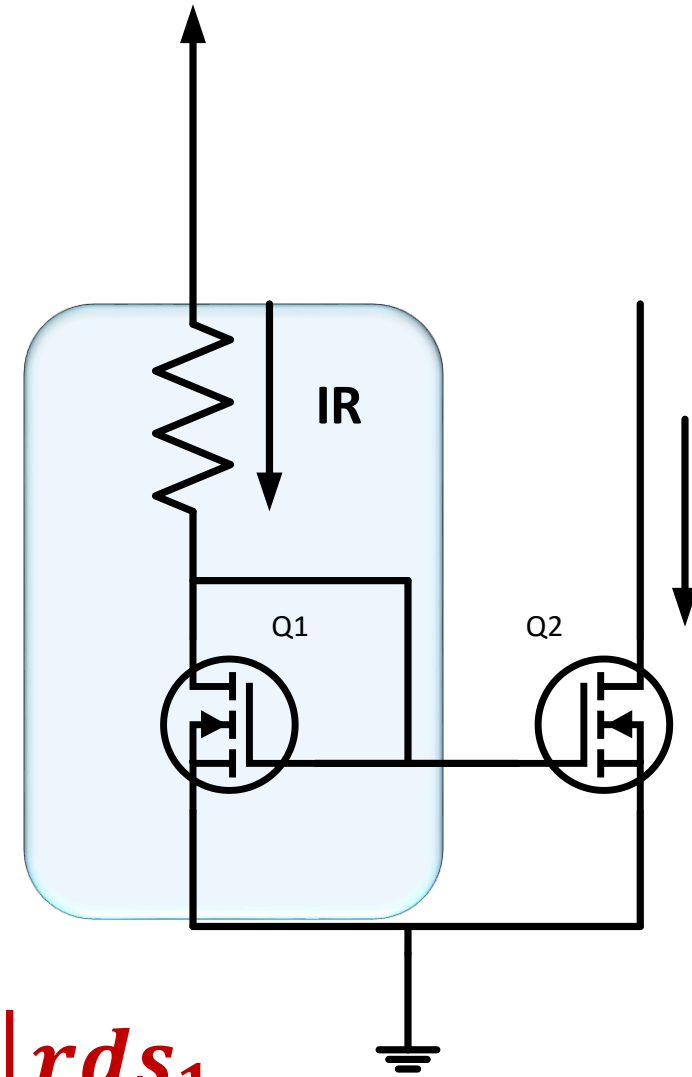
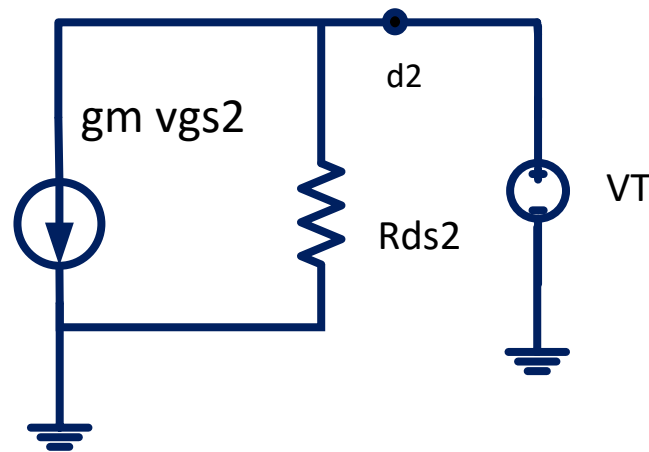
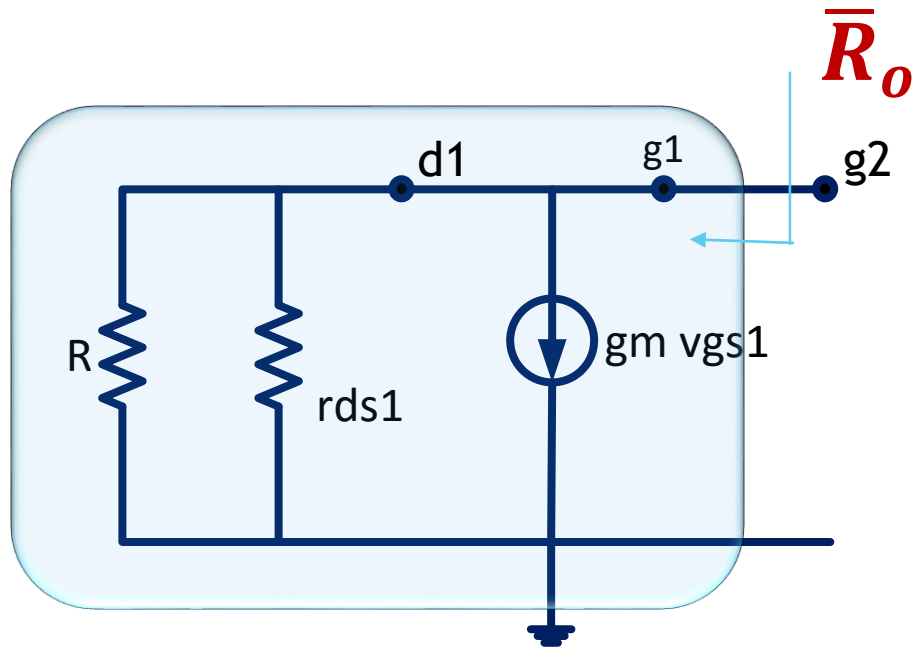
If we have matched Transistors

$$\frac{I_o}{I_R} = 1$$

$I_o = I_R$ current mirror



Mosfet Current Sources:



$$\bar{R}_o = \frac{1}{g_{m1}} \parallel R \parallel r_{ds1}$$

$$R_o = \frac{V_T}{I_T} = r_{ds2}$$

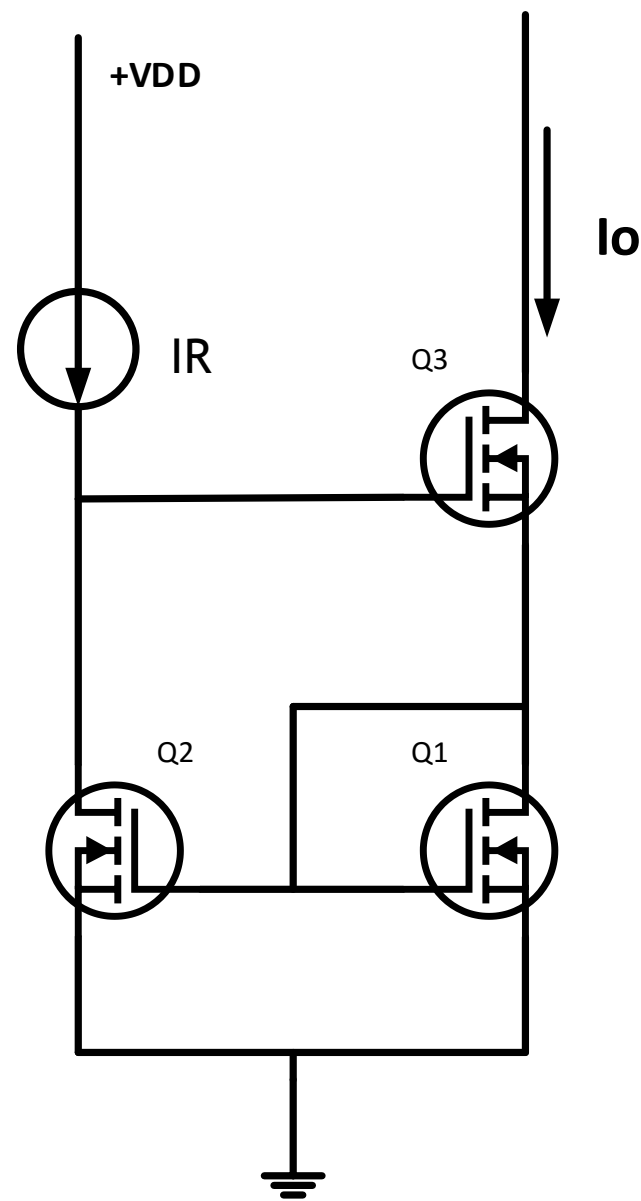
Mosfet Current Sources:

The Wilson mosfet current mirror

Q_1, Q_2 are matched

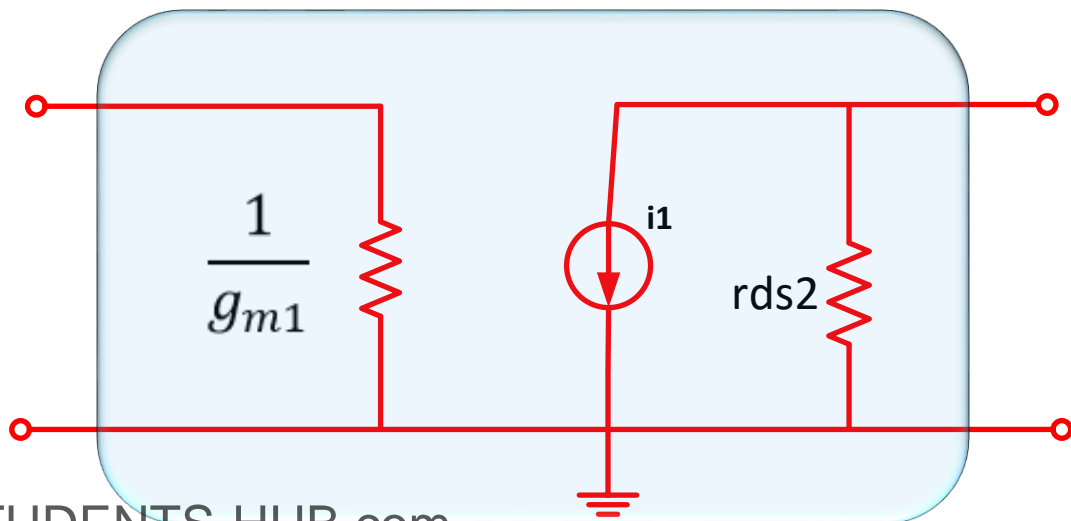
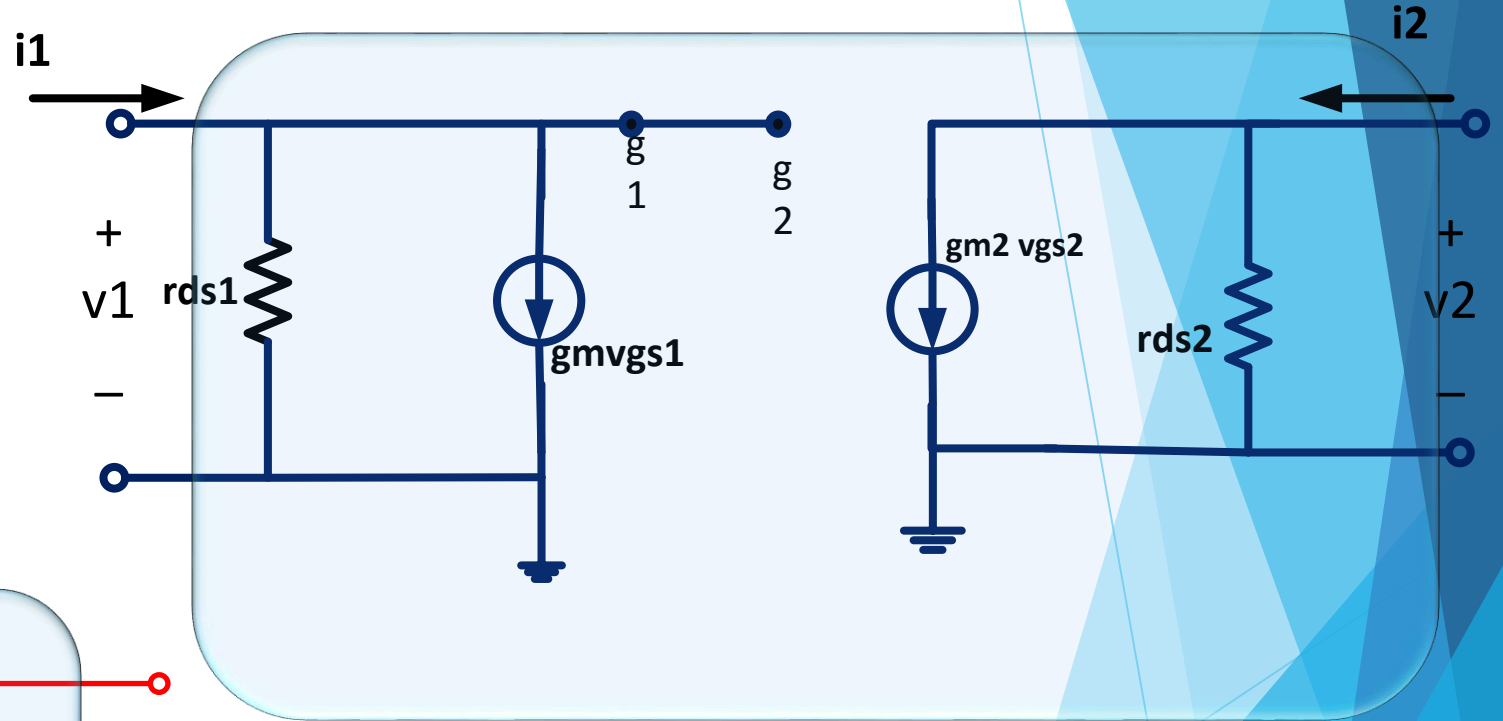
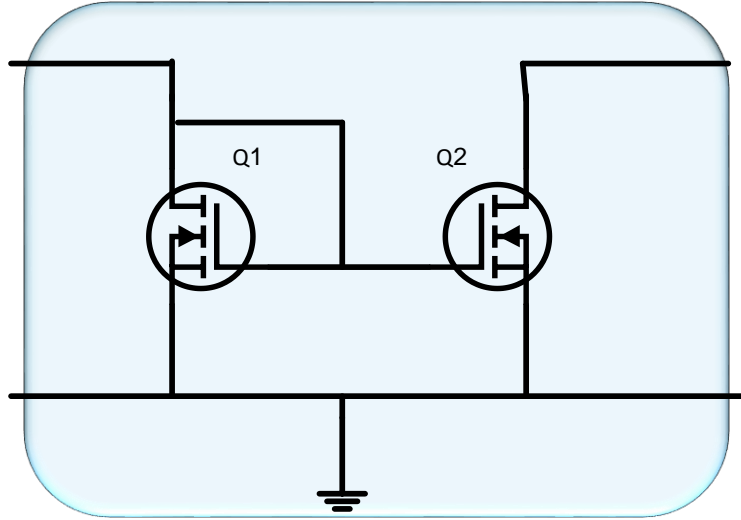
$$\therefore I_o = I_R$$

$$R_o \cong gm_3 r_{ds3} r_{ds2}$$



Mosfet Current Sources:

Two Port Model for Mosfet Current Mirror



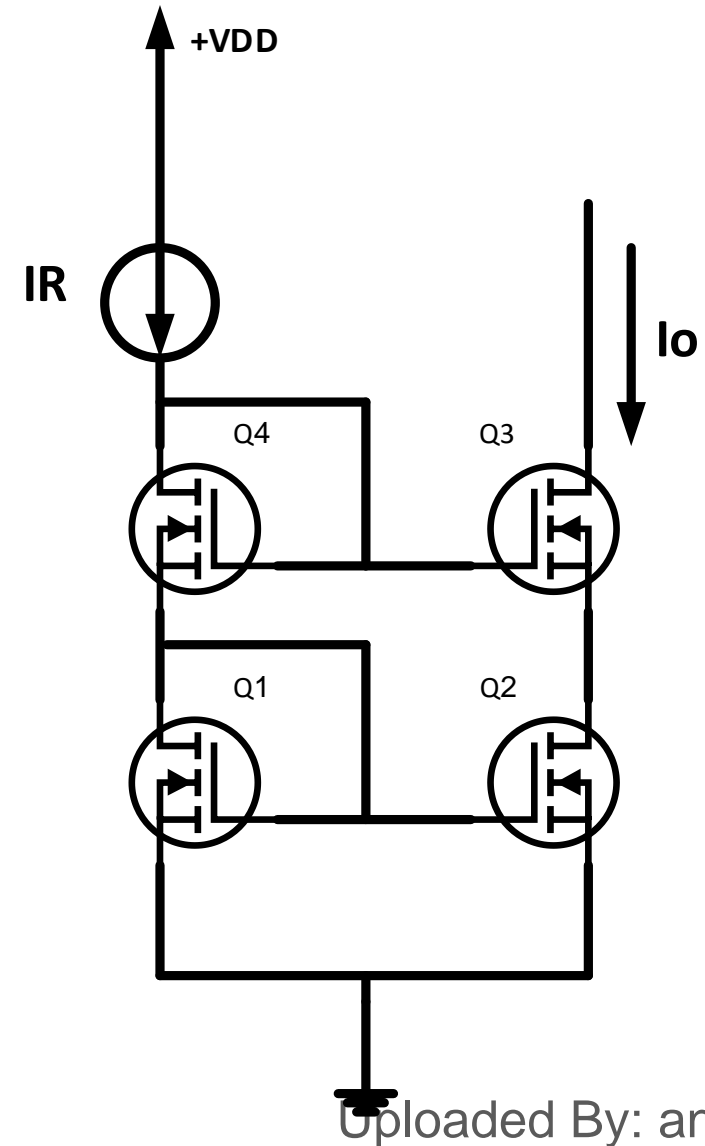
Mosfet Current Sources:

Cascode mosfet current mirror

$$I_{DS1} = \frac{1}{2} \bar{K}_n (V_{GS1} - V_T)^2 \left(\frac{W}{L}\right)_1 = I_R$$

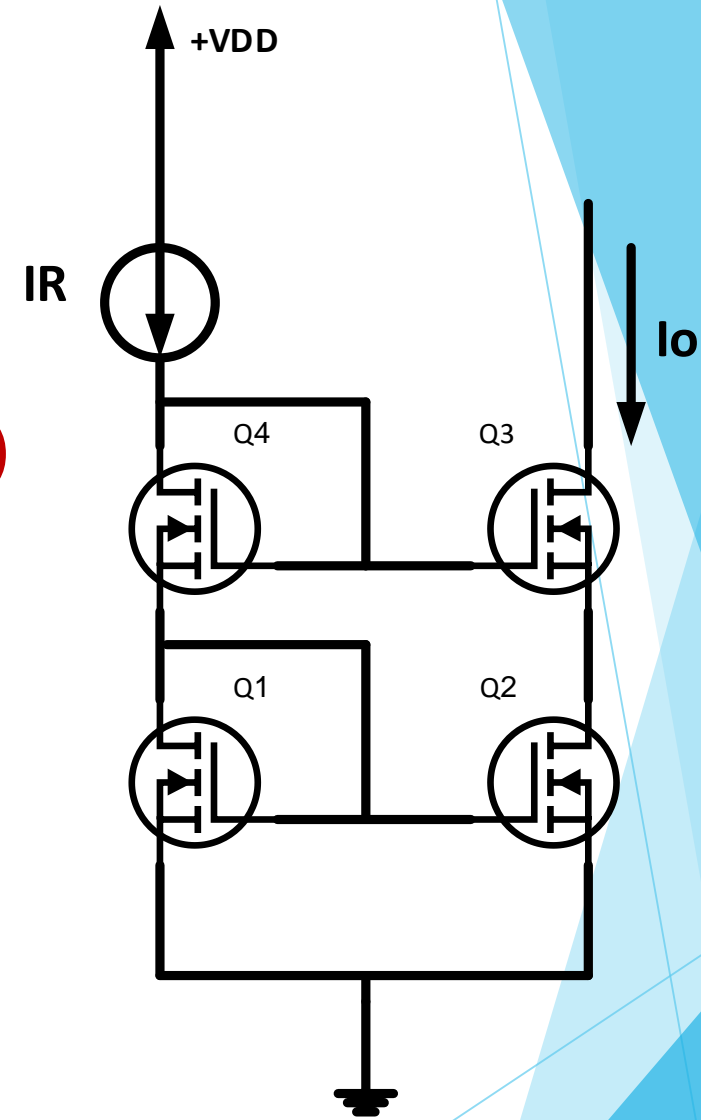
$$I_{DS2} = \frac{1}{2} \bar{K}_n (V_{GS2} - V_T)^2 \left(\frac{W}{L}\right)_2 = I_o$$

$$\frac{I_o}{I_R} = \frac{\left(\frac{W}{L}\right)_2}{\left(\frac{W}{L}\right)_1}$$



▶ $R_o = rds_3 + rds_2(1 + gm rds_3)$

$R_o \approx rds_2 rds_3 gm$



Circuits With Active Load

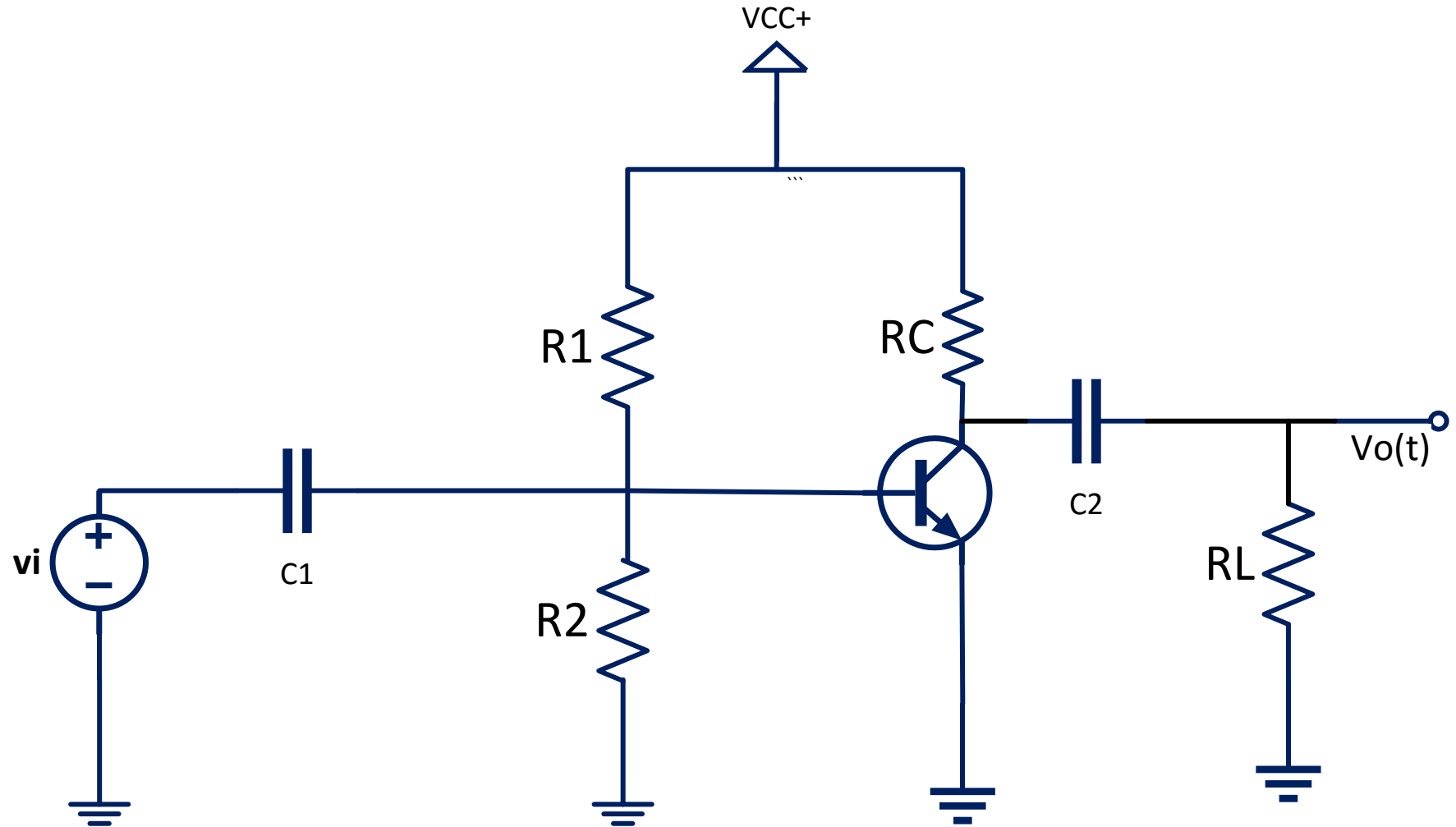
Find $A_v = \frac{V_o}{V_i}$

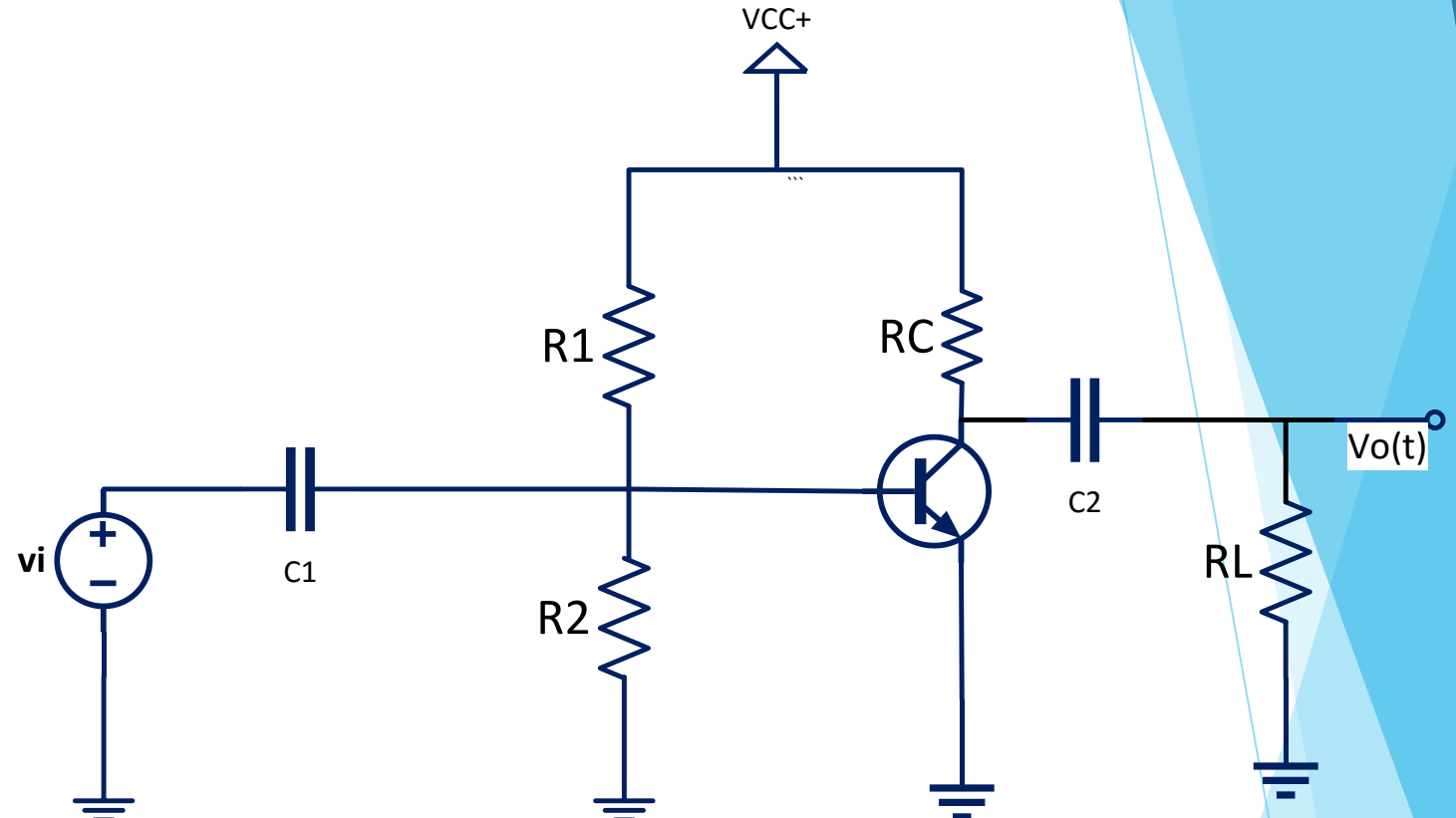
Let $R_C = 5k$,

$I_{CQ} = 1mA$,

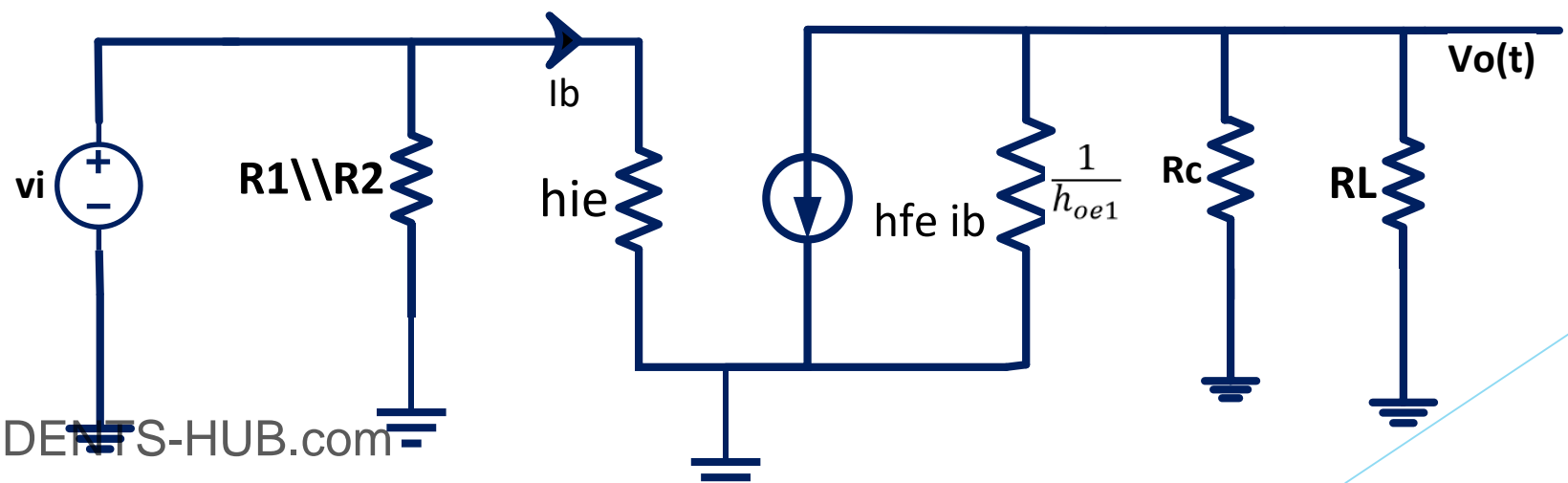
and $\frac{1}{h_{oe}} = 120k$

$R_L = 10k$

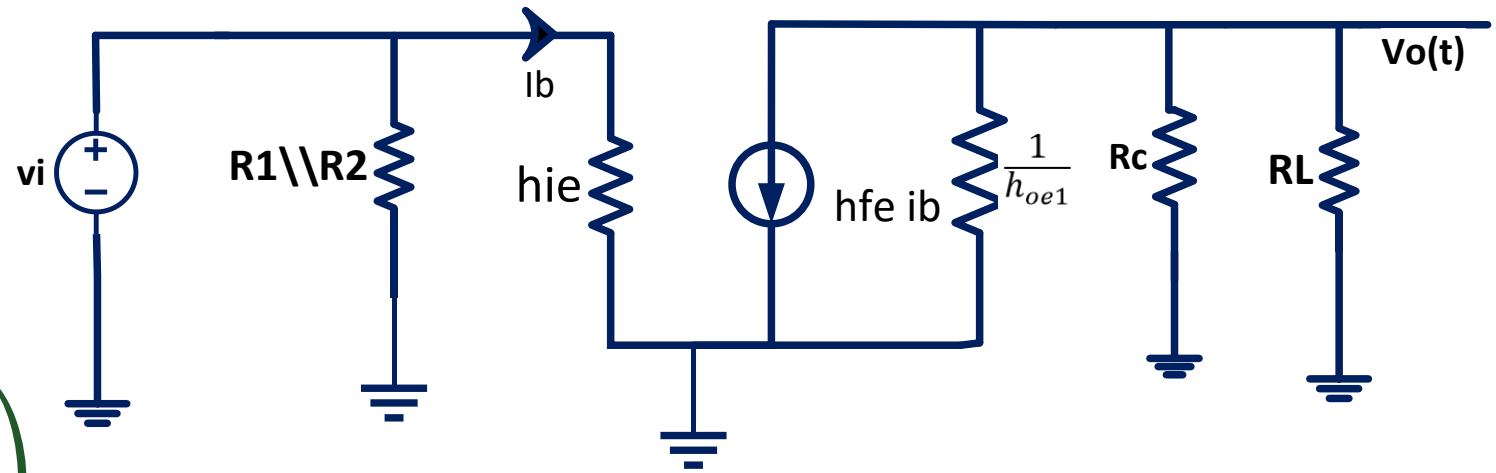




Ac Small signal equivalent Circuit



Circuits With Active Load



$$V_o = -h_{fe} i_b \left(R_C \parallel R_L \parallel \frac{1}{h_{oe}} \right)$$

$$i_b = \frac{v_i}{h_{ie}}$$

*To increase $|A_v|$, $R_C \uparrow$, $V_{CE} \downarrow$
 → Transistor enters saturation*

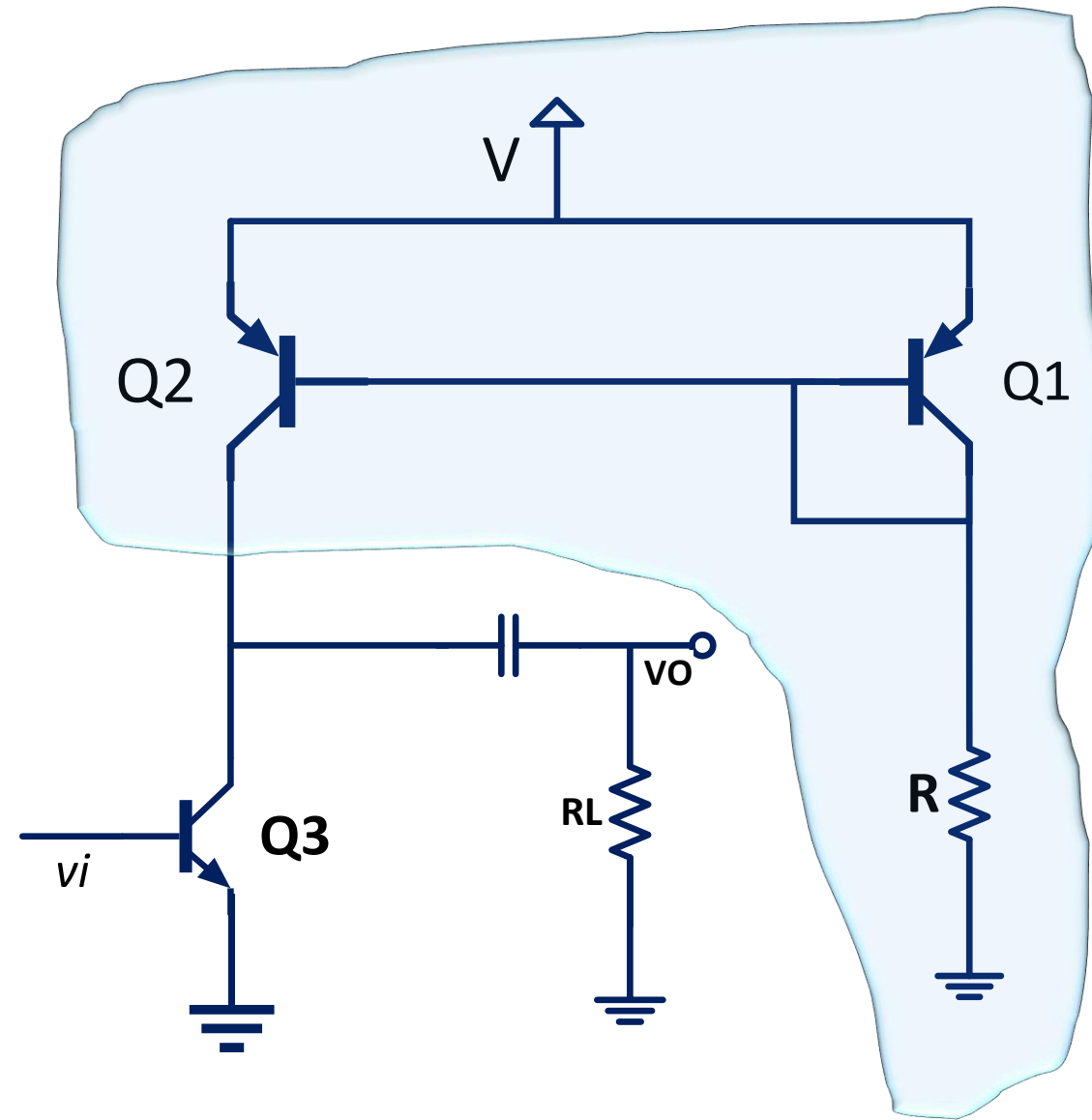
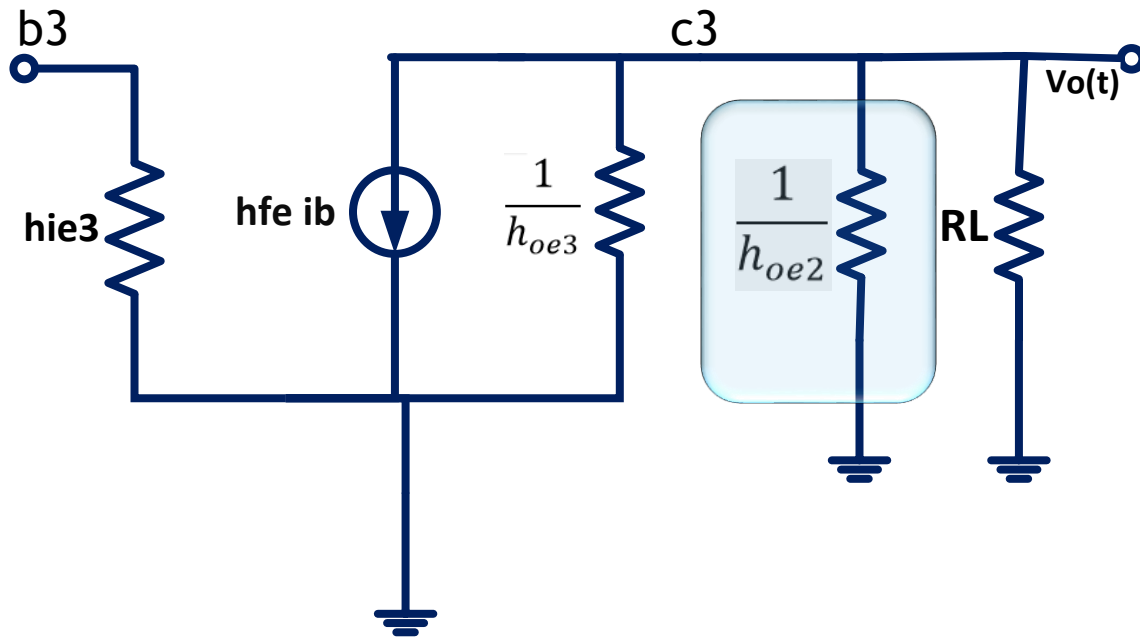
$$\therefore A_v = -\frac{h_{fe}}{h_{ie}} \left(R_C \parallel R_L \parallel \frac{1}{h_{oe}} \right)$$

$$A_v = -gm \left(R_C \parallel R_L \parallel \frac{1}{h_{oe}} \right) = -125$$

$$V_{CE} = V_{CC} - R_C I_{CQ}$$

Amplifier With an Active Load

Ac Small signal equivalent Circuit



Amplifier With an Active Load

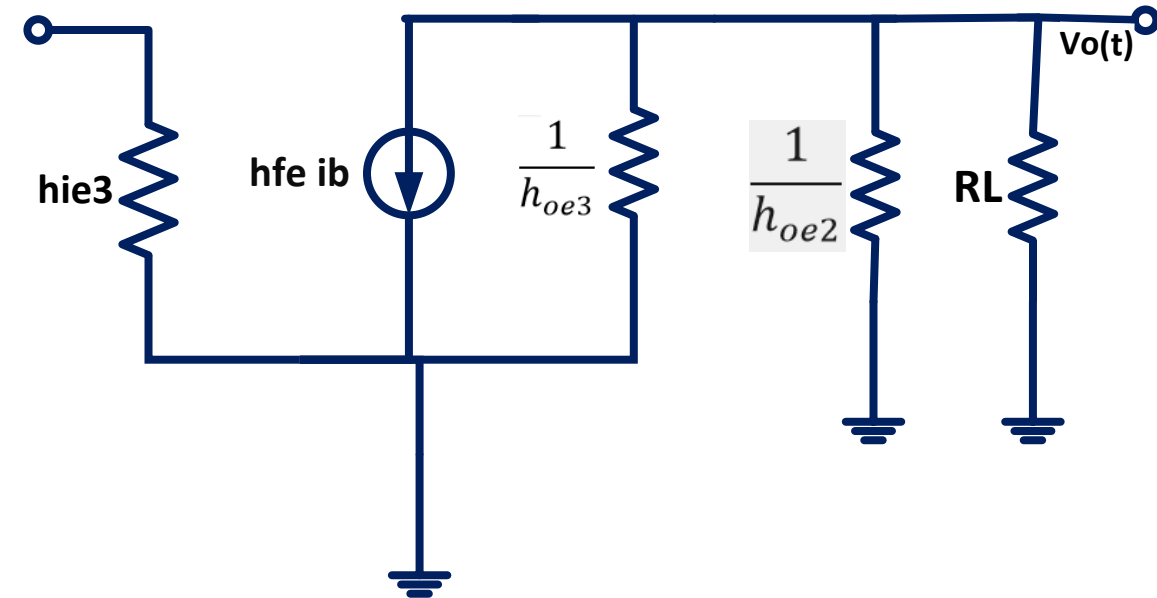
$$A_v = -g_m \left(\frac{1}{h_{oe3}} \parallel \frac{1}{h_{oe3}} \parallel R_L \right)$$

$$\text{let } \frac{1}{h_{oe3}} = 120k$$

$$\frac{1}{h_{oe2}} = 80k$$

$$, I_{CQ} = 1mA$$

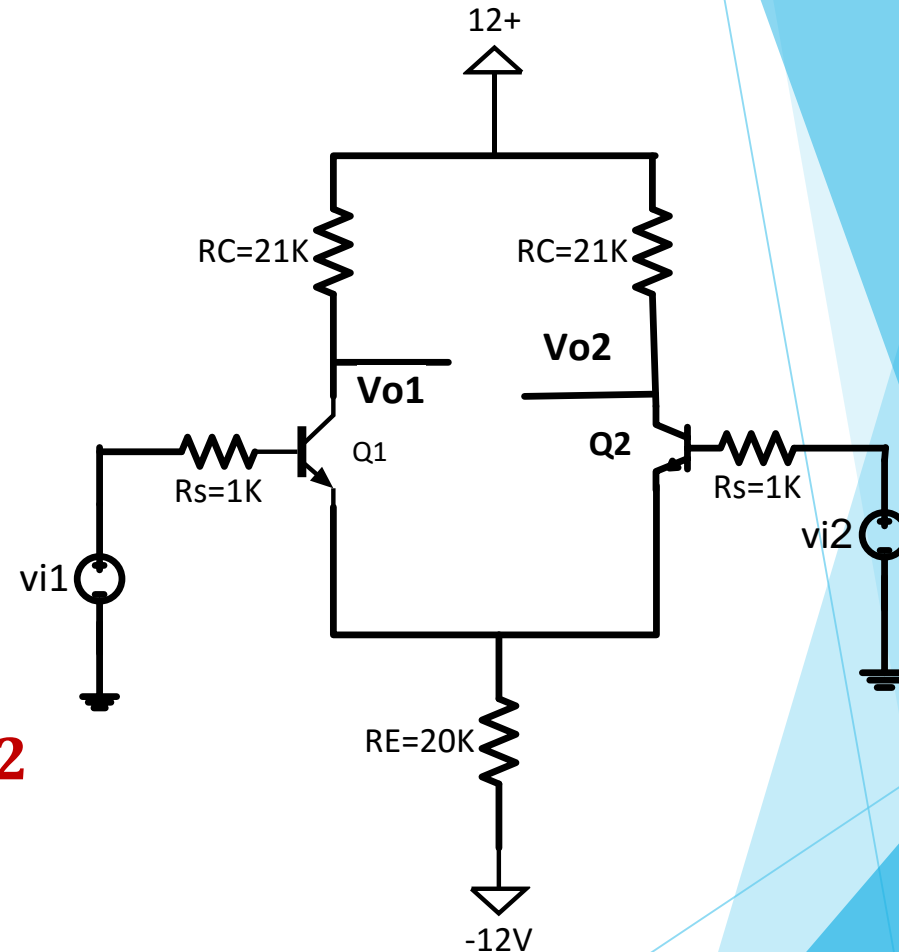
$$\therefore g_m = \frac{h_{fe3}}{h_{ie3}} = \frac{I_{CQ}}{V_T} = 38.46 \Omega$$



$$V_o = \begin{cases} -1846 v_i ; R_L = \infty \\ -1247 v_i ; R_L = 100k \\ -318 v_i ; R_L = 10k \end{cases}$$

Differential Amplifiers

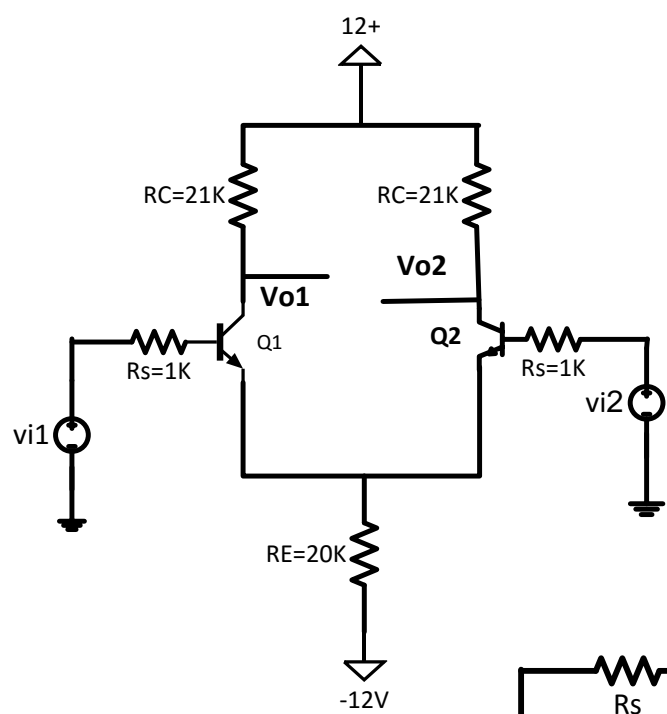
AC Analysis: Input Impedance



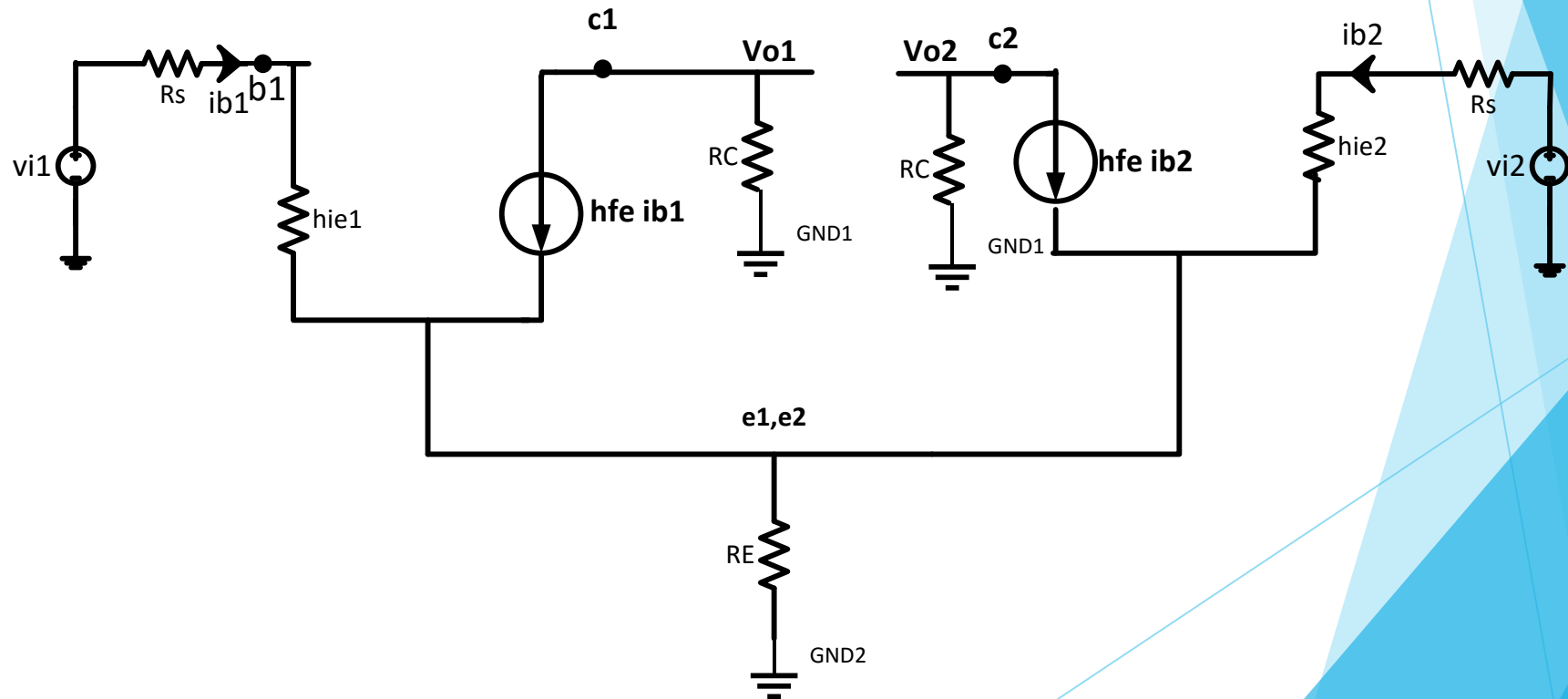
since $I_{E1} = I_{E2}$ and $\beta_1 = \beta_2$

$$h_{ie1} = h_{ie2} = h_{ie}$$

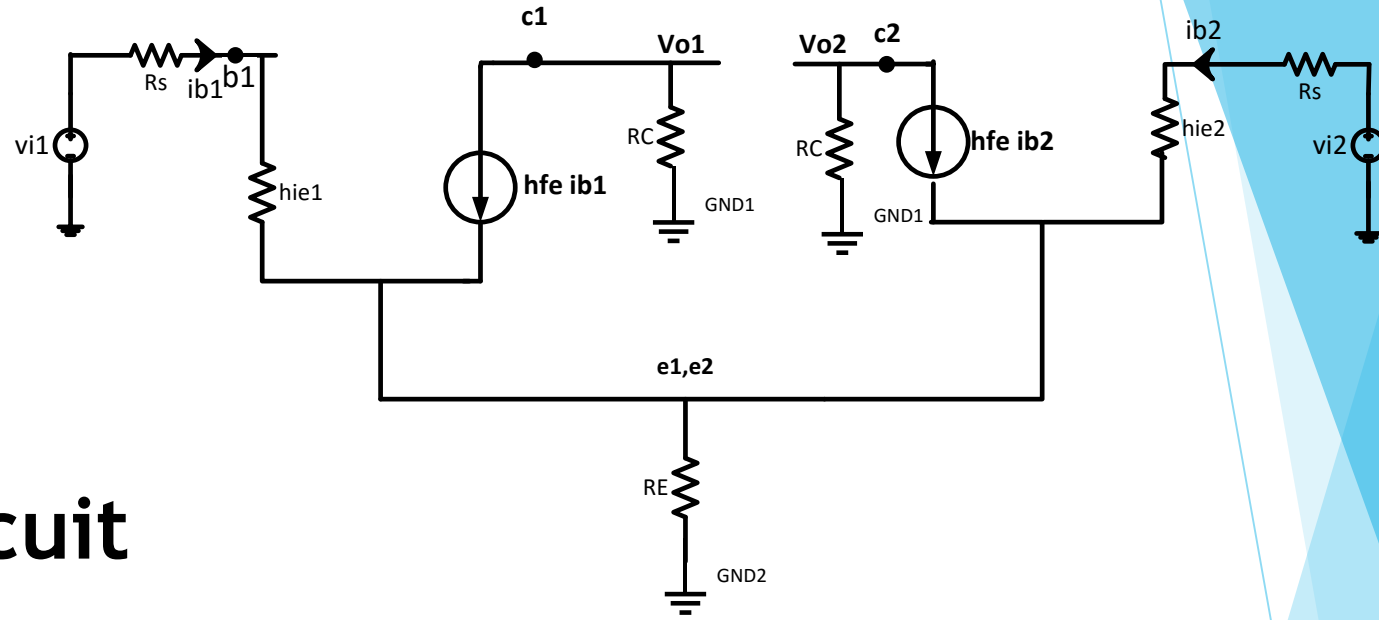
$$h_{ib1} = h_{ib2} = h_{ib}$$



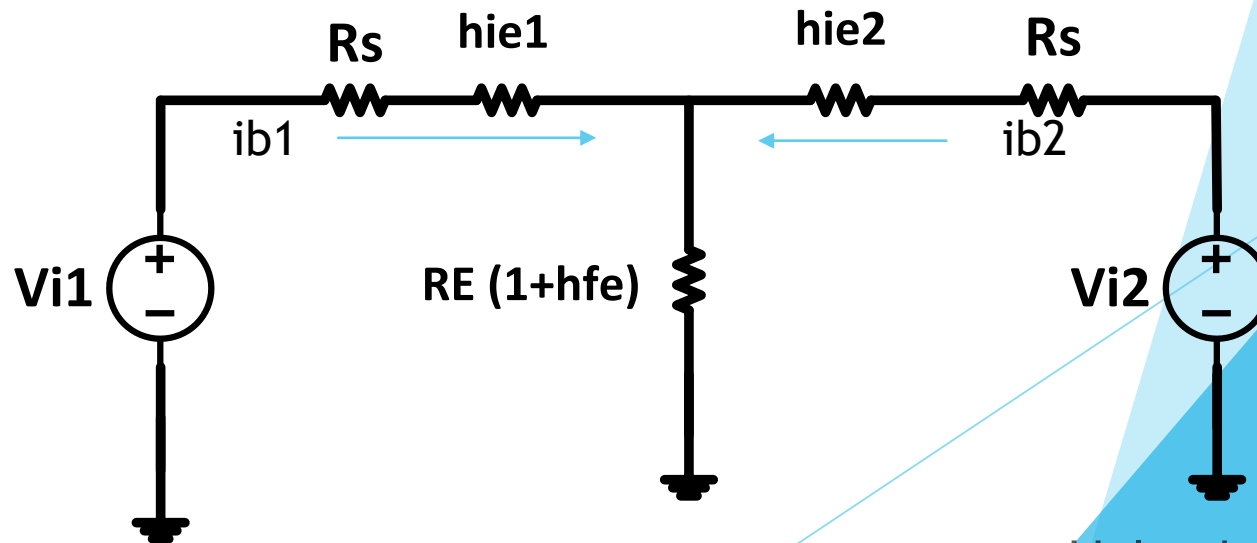
Ac small signal equivalent circuit



To find the input impedance



Base equivalent circuit



Input Impedance:

Base equivalent circuit

Differential mode input impedance $\equiv Z_{id}$

$$Z_{id} = \left. \frac{v_d}{i_b} \right|_{v_c=0}$$

Common mode input impedance $\equiv Z_{ic}$

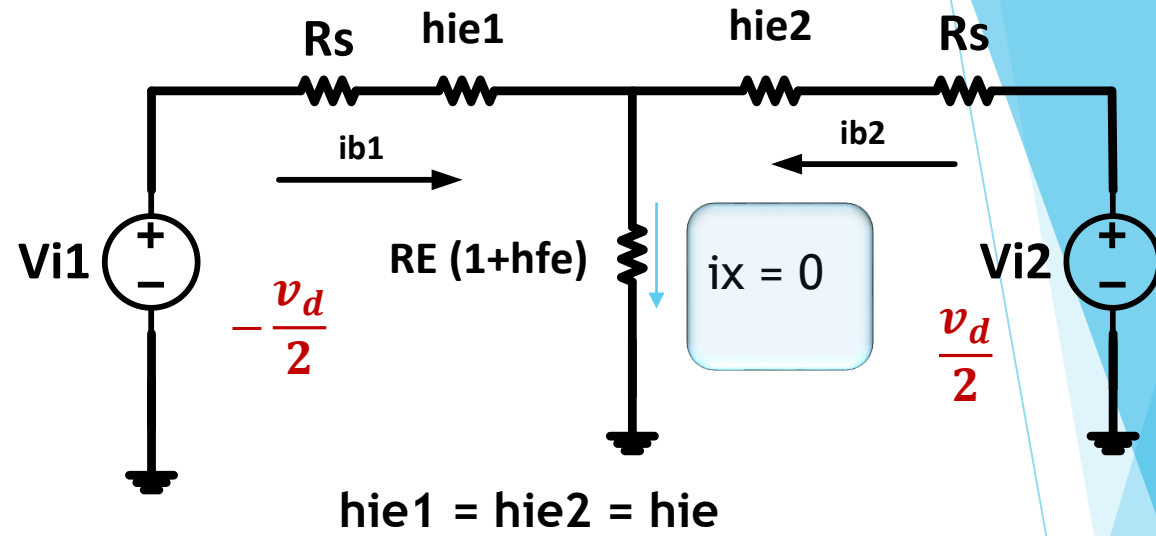
$$Z_{ic} = \left. \frac{v_c}{i_b} \right|_{v_d=0}$$

Input impedance

$$Z_{id} = \left. \frac{v_d}{i_b} \right|_{v_c=0}$$

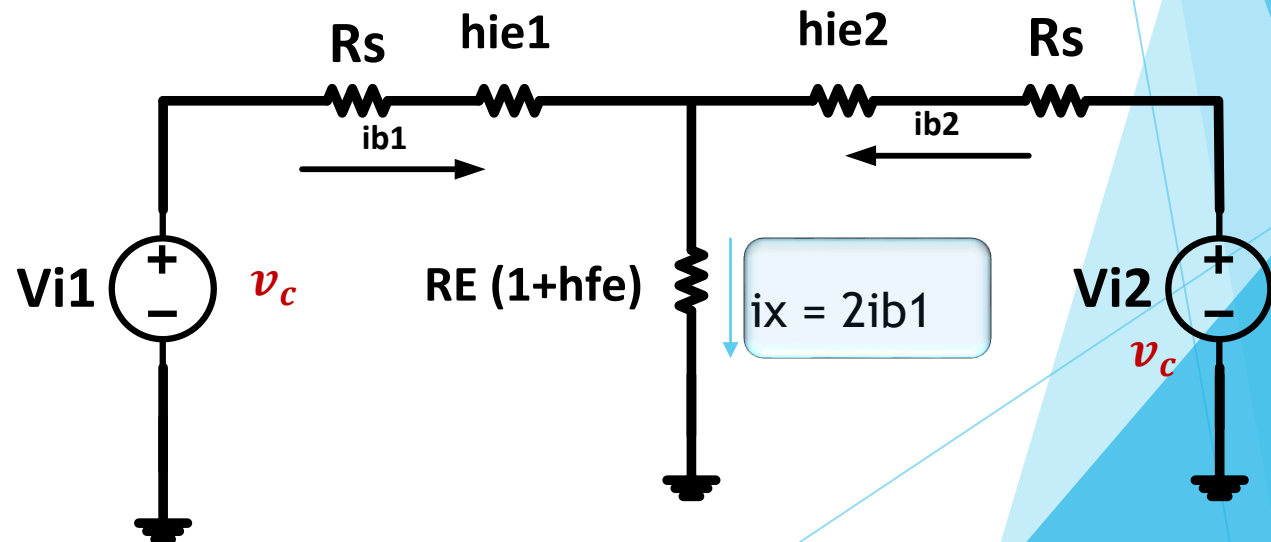
$$v_{i1} = -\frac{v_d}{2}; v_{i2} = \frac{v_d}{2}$$

$$Z_{id} = 2(R_S + h_{ie})$$



$$Z_{ic} = \left. \frac{v_c}{i_b} \right|_{v_d=0}$$

$$v_{i1} = v_c; v_{i2} = v_c$$



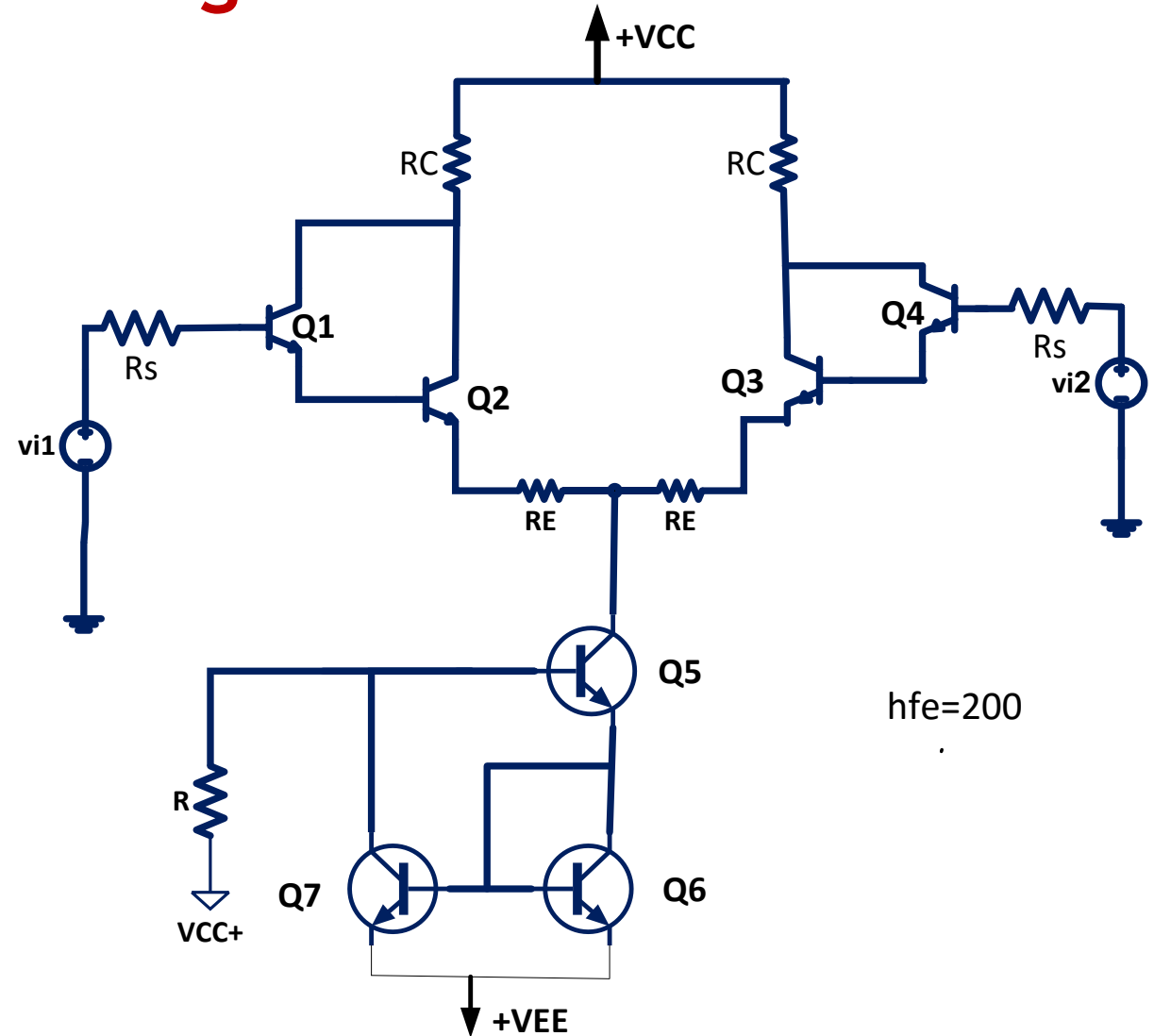
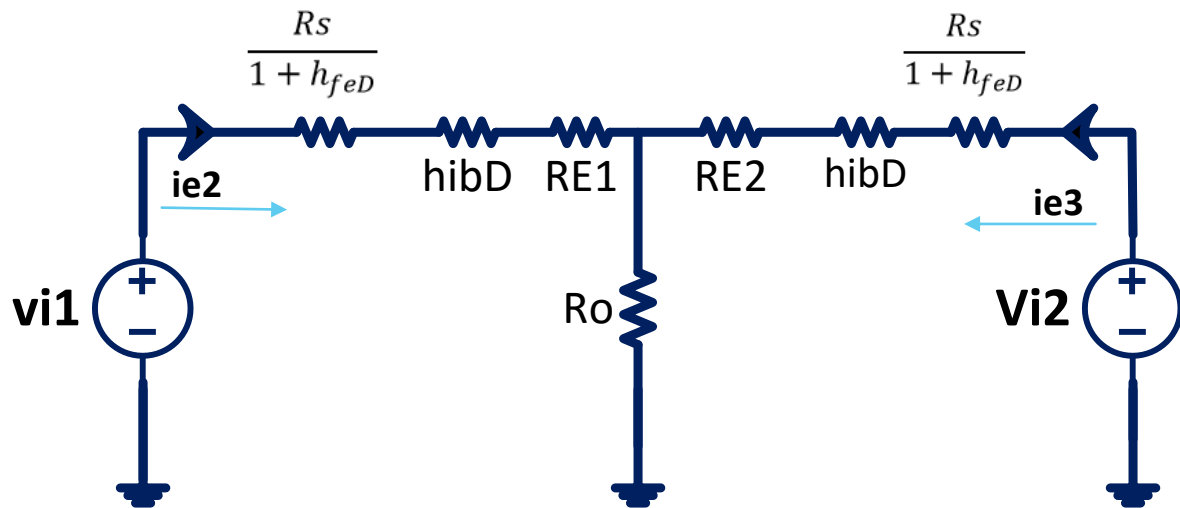
$$Z_{ic} = R_S + h_{ie} + 2(1 + h_{fe})RE$$

Differential Amplifiers Using Darlington and FET

Differential Amplifiers Using Darlington

To find A_c & A_d :

Emitter equivalent circuit

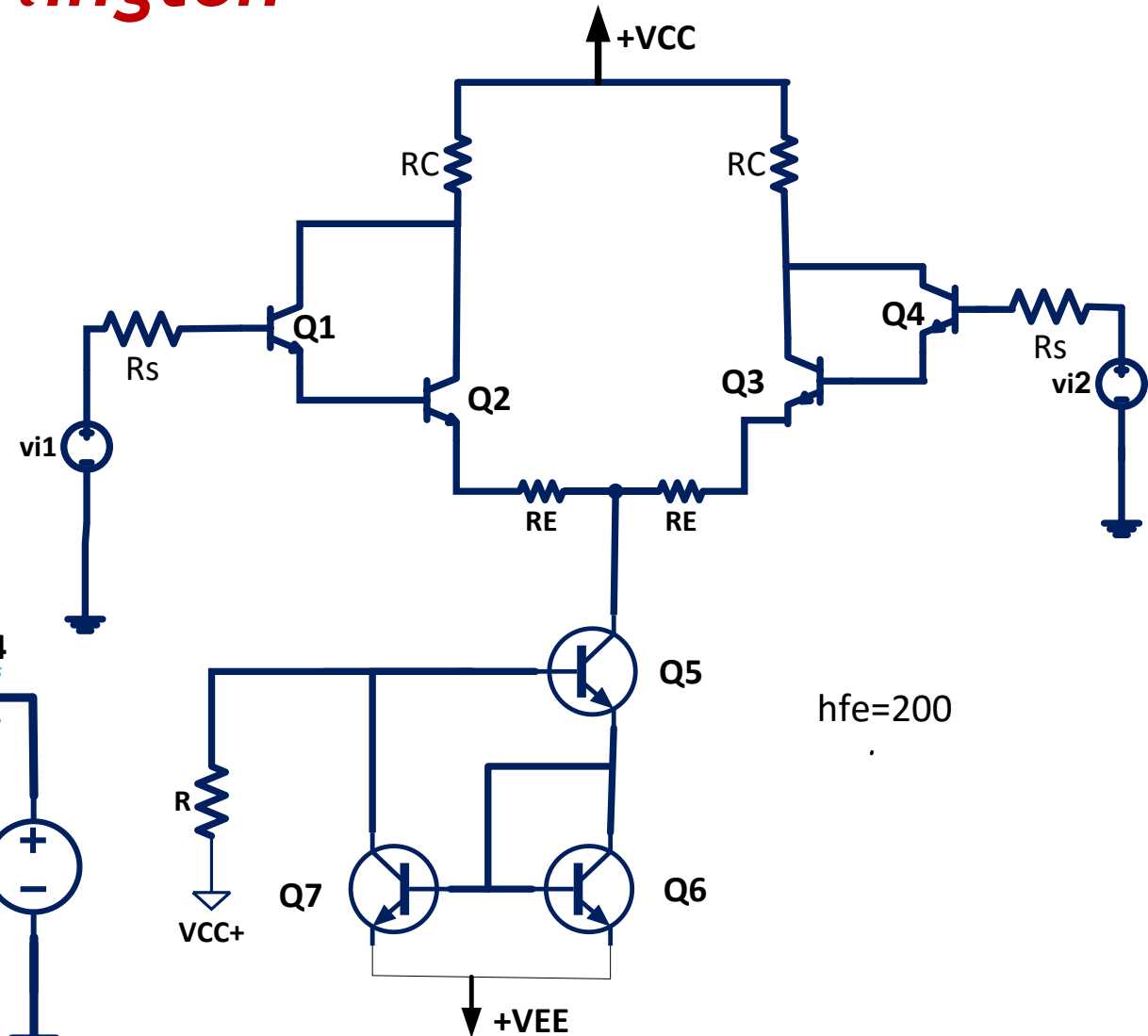
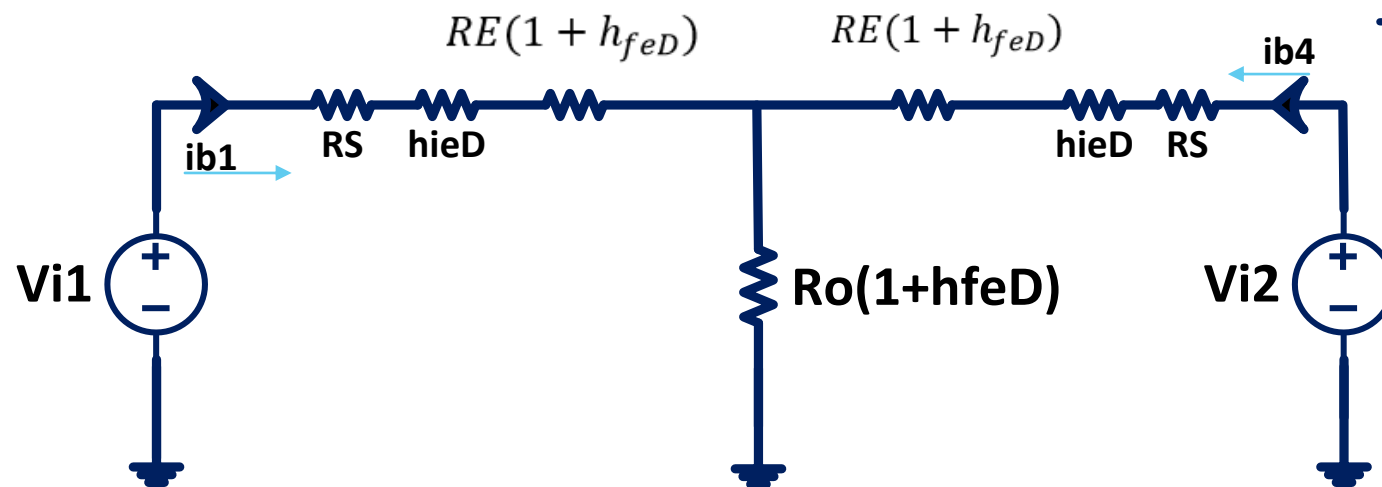


Differential Amplifiers Using Darlington and FET

Differential Amplifiers Using Darlington

To find Z_{id} :

Base equivalent circuit

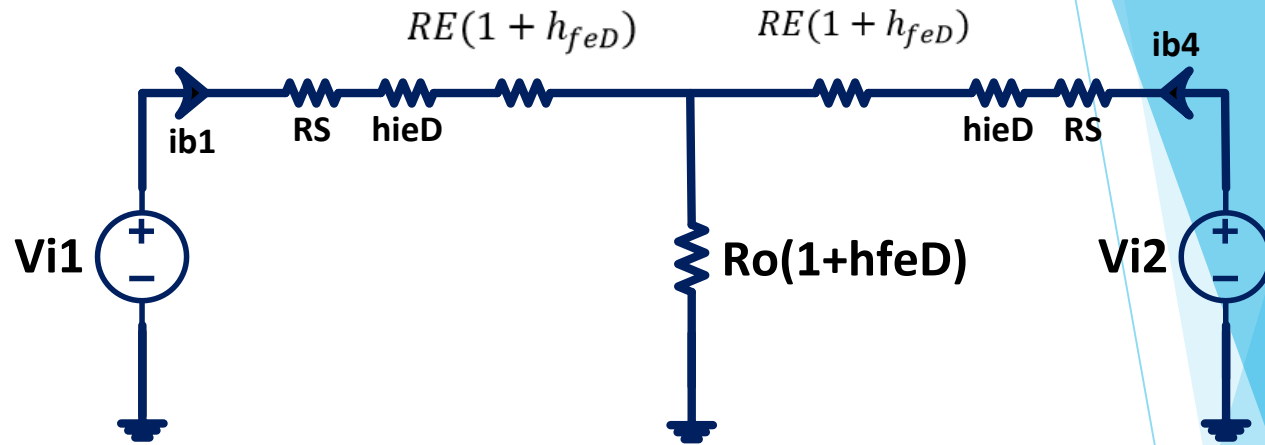


Input Impedance:

Base equivalent circuit

$$Z_{id} = \left. \frac{v_d}{i_{b1}} \right|_{v_c=0}$$

$$v_{i1} = -\frac{v_d}{2}; v_{i2} = \frac{v_d}{2}$$



$$Z_{id} = 2 \left(R_S + h_{ieD} + R_E(1 + h_{feD}) \right)$$

$$Z_{ic} = \left. \frac{v_c}{i_b} \right|_{v_d=0}$$

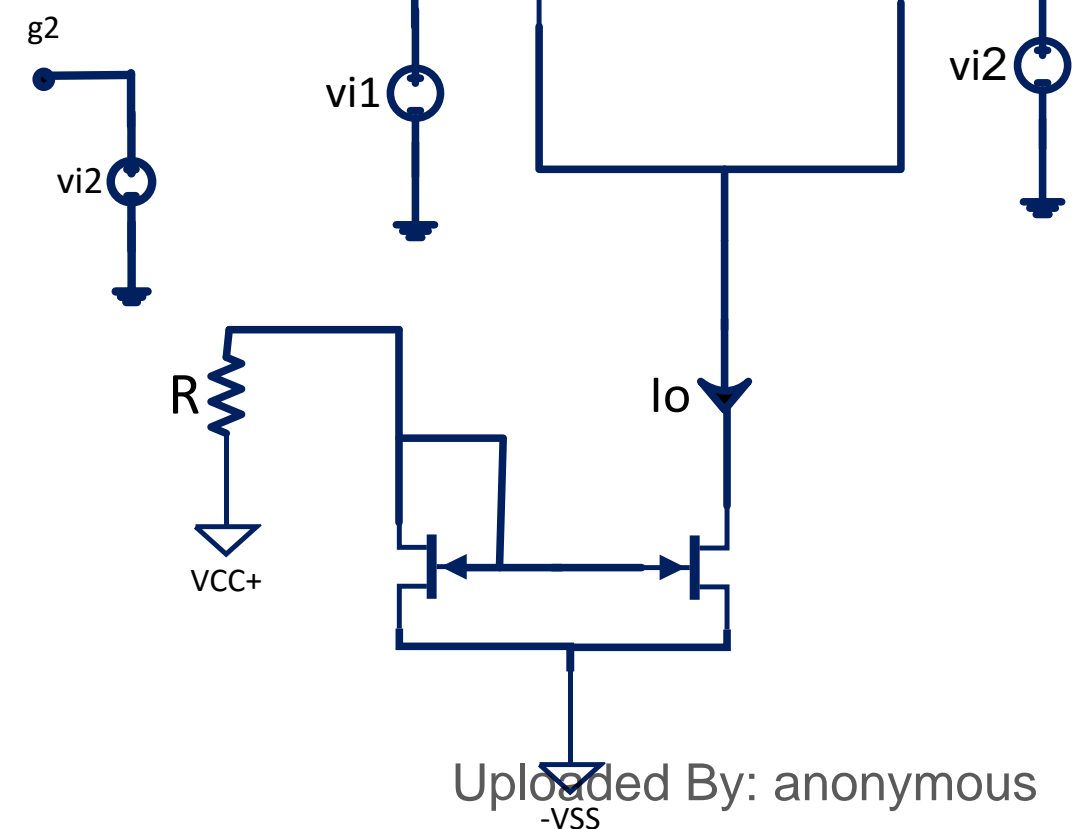
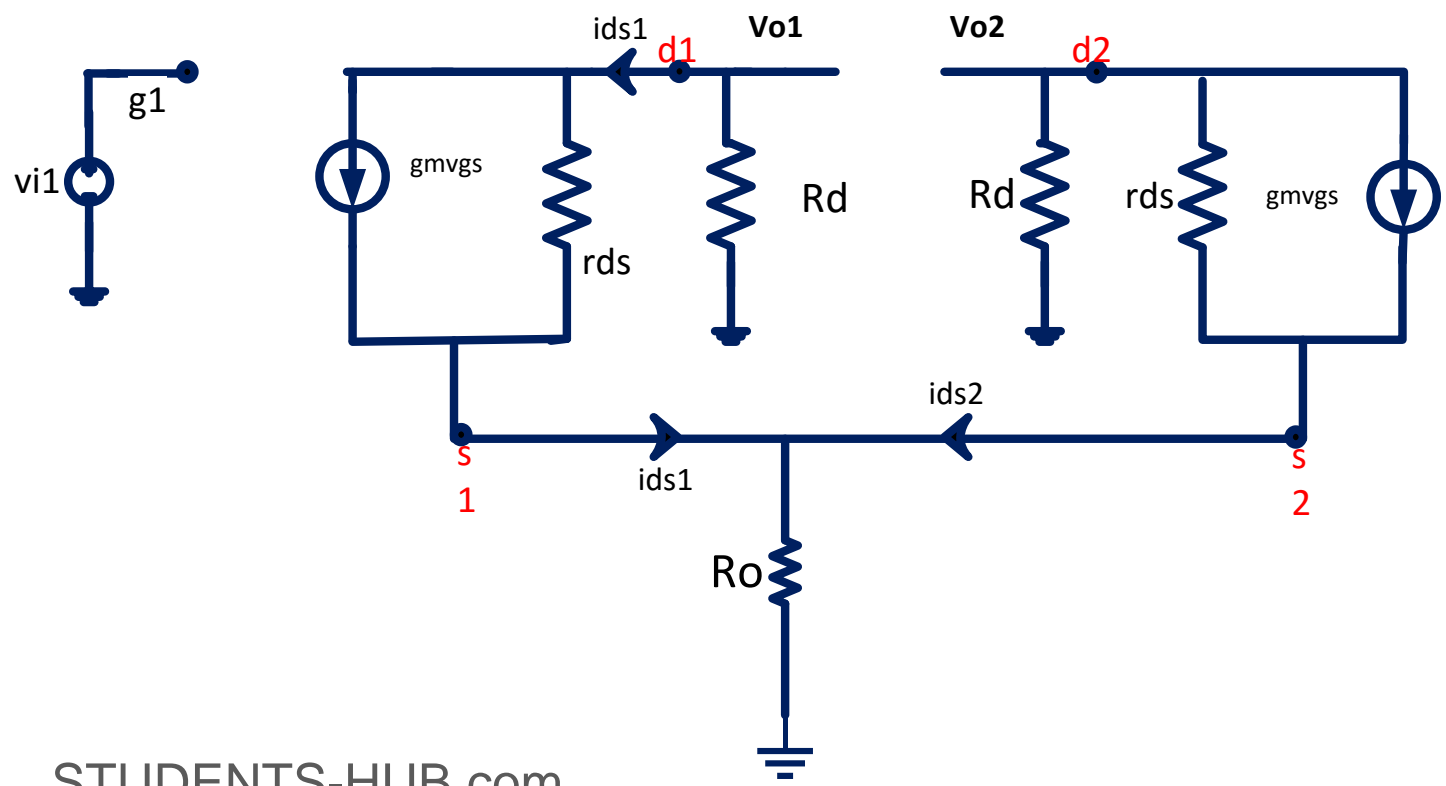
$$v_{i1} = v_c; v_{i2} = v_c$$

$$Z_{ic} = R_S + h_{ieD} + R_E(1 + h_{feD}) + 2R_o(1 + h_{feD})$$

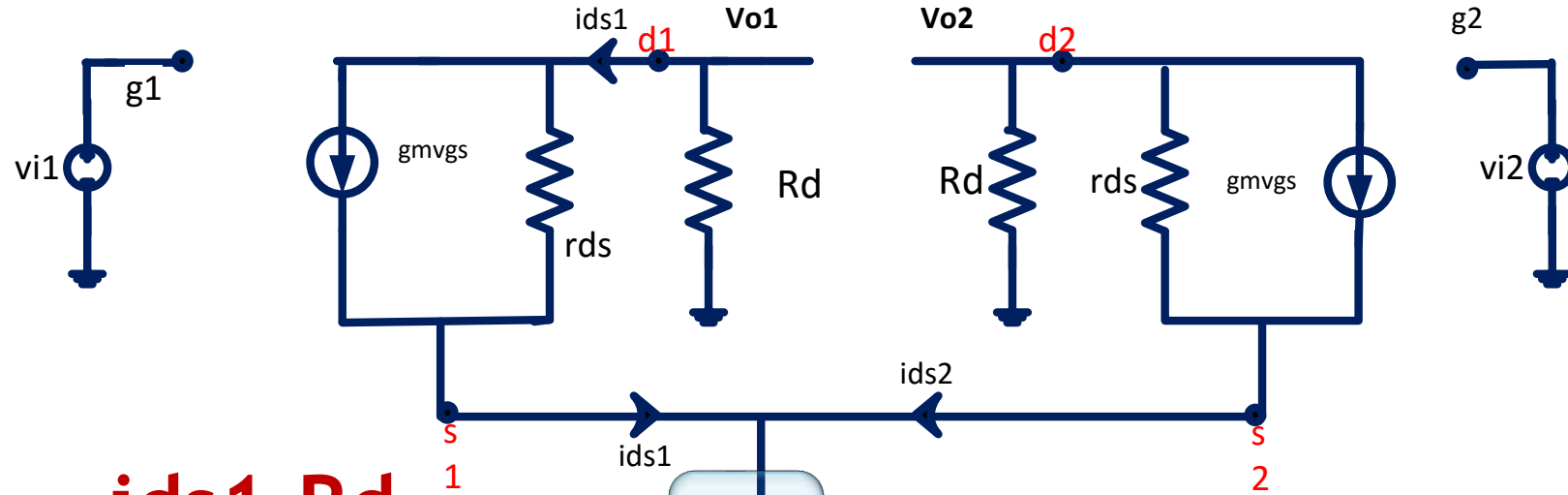
Differential Amplifiers Using Darlington and FET

Differential Amplifiers Using FET

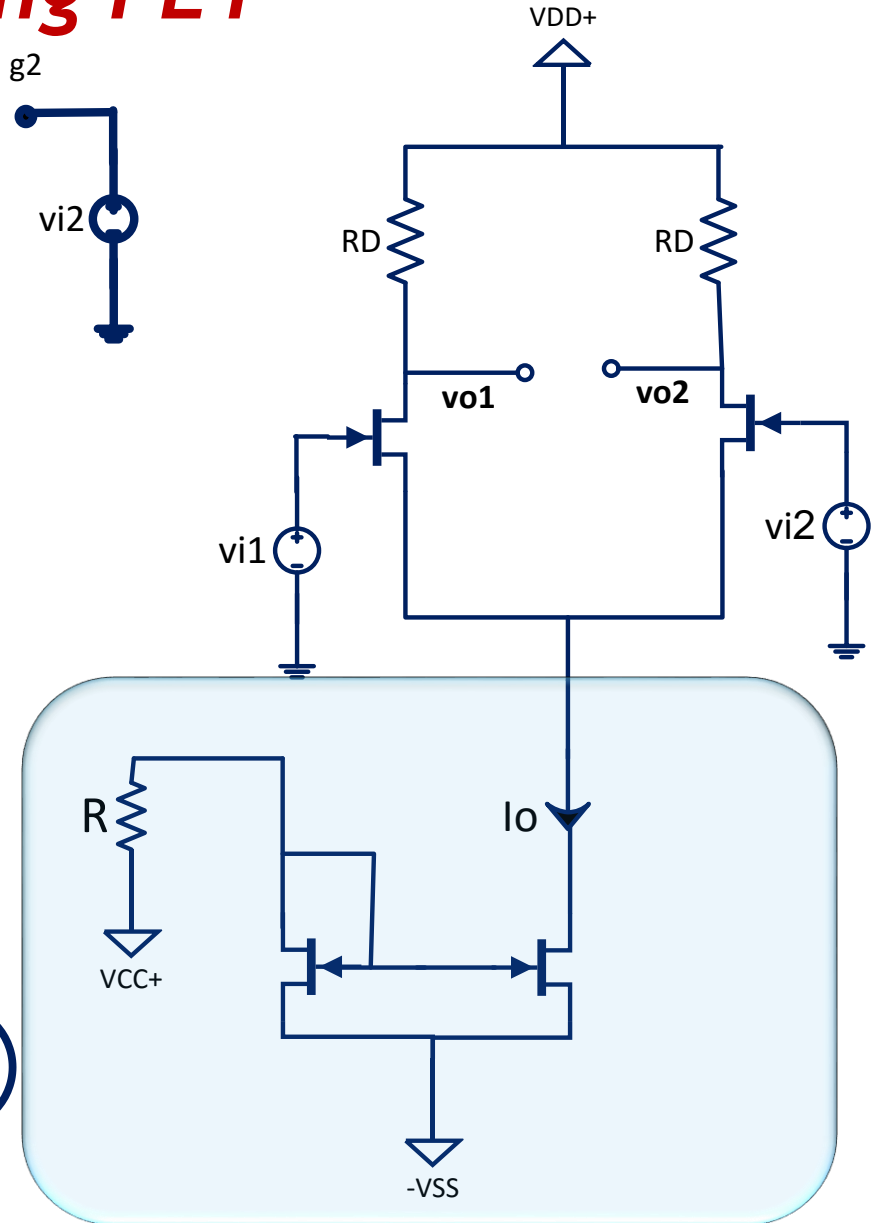
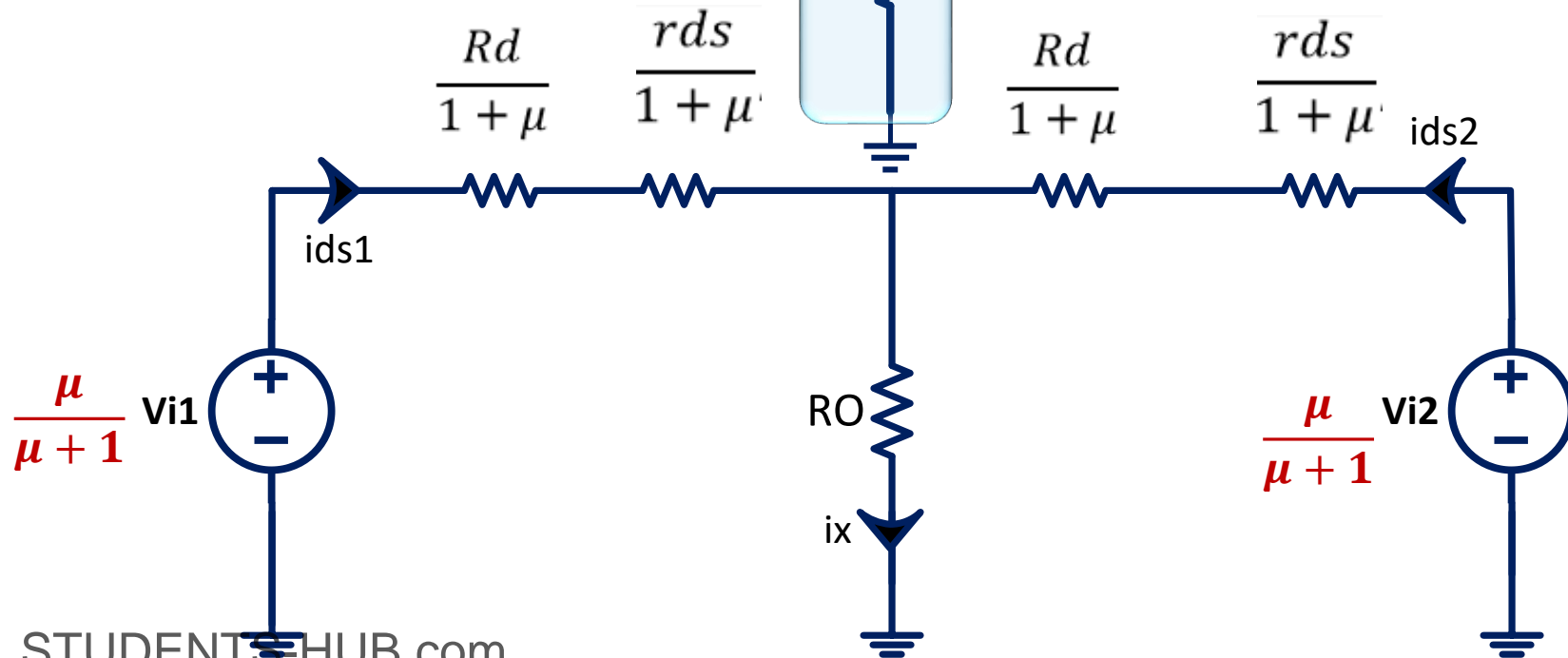
Ac Small signal equivalent Circuit:



Differential Amplifiers Using FET



$V_{o1} = -i_{ds1} \cdot R_d$

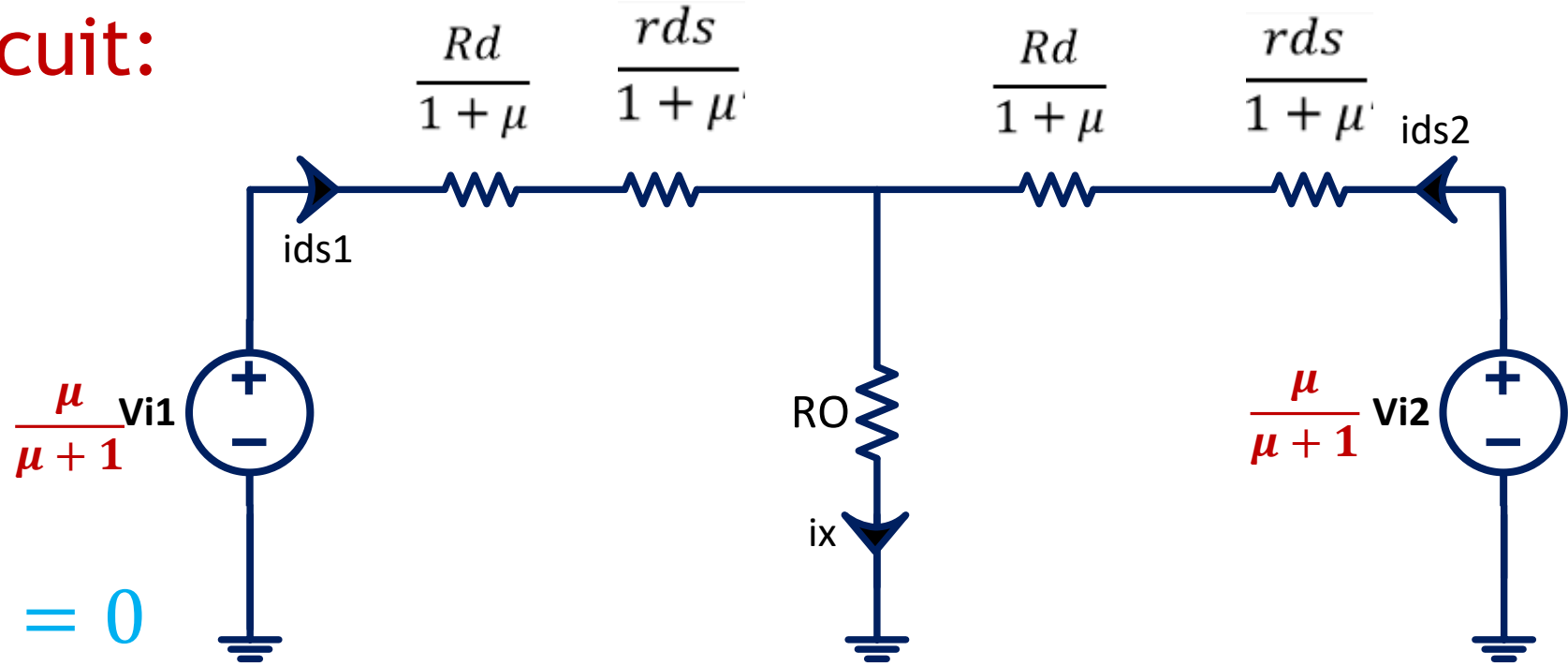


Differential Amplifiers Using FET

Source equivalent Circuit:

$$v_{i1} = v_c - \frac{v_d}{2}$$

$$v_{i2} = v_c + \frac{v_d}{2}$$



1) To find A_d ; set $v_c = 0$

$$v_{i1} = -\frac{v_d}{2}$$

$$v_{i2} = \frac{v_d}{2}$$

$$i_{ds1} = -i_{ds2}$$

$$i_{ds1} = \frac{\frac{\mu}{\mu+1} \left(-\frac{v_d}{2} \right)}{\frac{R_d + r_{ds}}{\mu+1}}$$

$$v_{o1} = \frac{R_d \frac{\mu}{\mu+1} v_d}{2 \left(\frac{R_d + r_{ds}}{\mu+1} \right)}$$

$i_x = 0$ symmetry

$$v_{o1} = \frac{R_d \frac{\mu}{\mu + 1} v_d}{2 \left(\frac{R_d + r_{ds}}{\mu + 1} \right)}$$

$$A_d = \left. \frac{v_{o1}}{v_d} \right|_{v_c=0}$$

$$A_d = \frac{R_d \frac{\mu}{\mu + 1}}{2 \left(\frac{R_d + r_{ds}}{\mu + 1} \right)}$$

Differential Amplifiers Using FET

Ac Small signal equivalent Circuit:

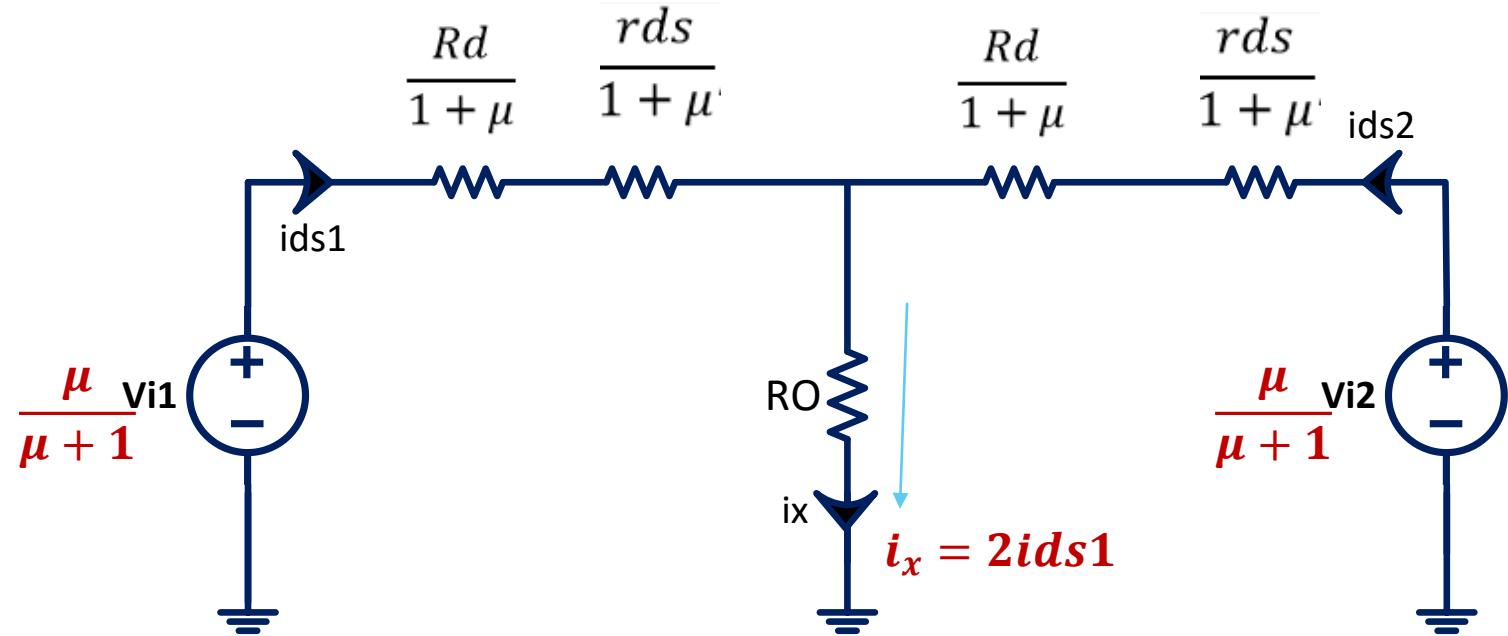
2) To find $A_c = \frac{v_{o1}}{v_c} \Big|_{v_d=0}$

$$v_{i1} = v_c$$

$$v_{i2} = v_c$$

$$i_{ds1} = i_{ds2}$$

$$i_x = 2i_{ds1}$$

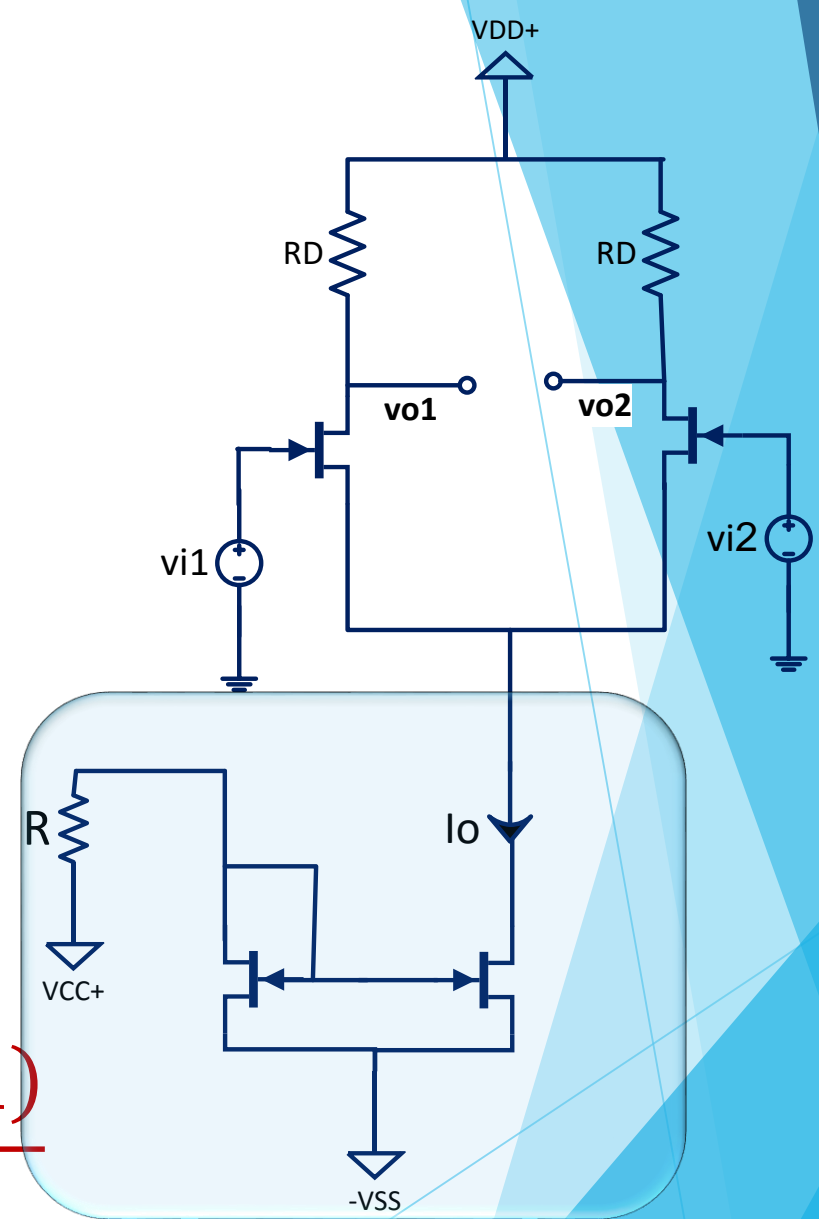


$$i_{ds1} = \frac{v_c \frac{\mu}{\mu + 1}}{\left(\frac{R_d + r_{ds}}{\mu + 1} \right) + 2R_o}$$

$$v_{o1} = \frac{-R_d \frac{\mu}{\mu + 1}}{\left(\frac{R_d + r_{ds}}{\mu + 1}\right) + 2R_o} v_c$$

$$\therefore A_c = \frac{R_d \frac{\mu}{\mu + 1}}{\left(\frac{R_d + r_{ds}}{\mu + 1}\right) + 2R_o}$$

$$CMRR = \left| \frac{A_d}{A_c} \right| = \frac{r_{ds} + R_d + 2R_o(\mu + 1)}{2(R_d + r_{ds})}$$



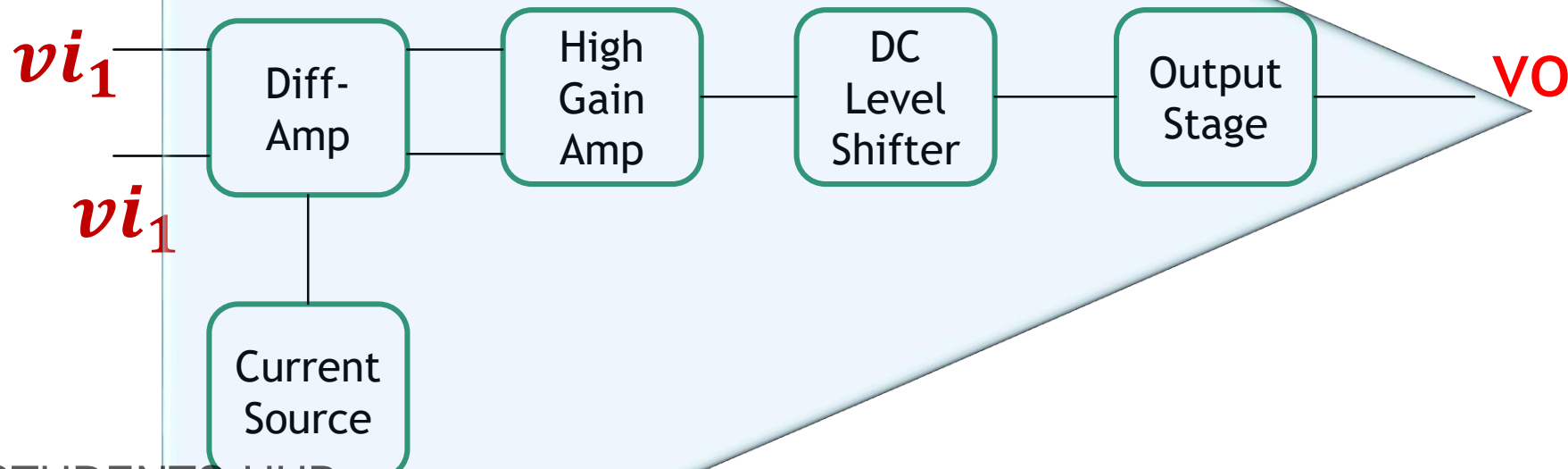
The Operational Amplifier

Very high voltage gain ; 200,000

Very High input impedance ; 10M ohm

Very small output impedance ; 75ohm

Designed to do mathematical operations such as addition , subtraction



The Operational Amplifier

DC Level Shifter

To make $v_o = 0$, when
 $v_{i1} = v_{i2} = 0$

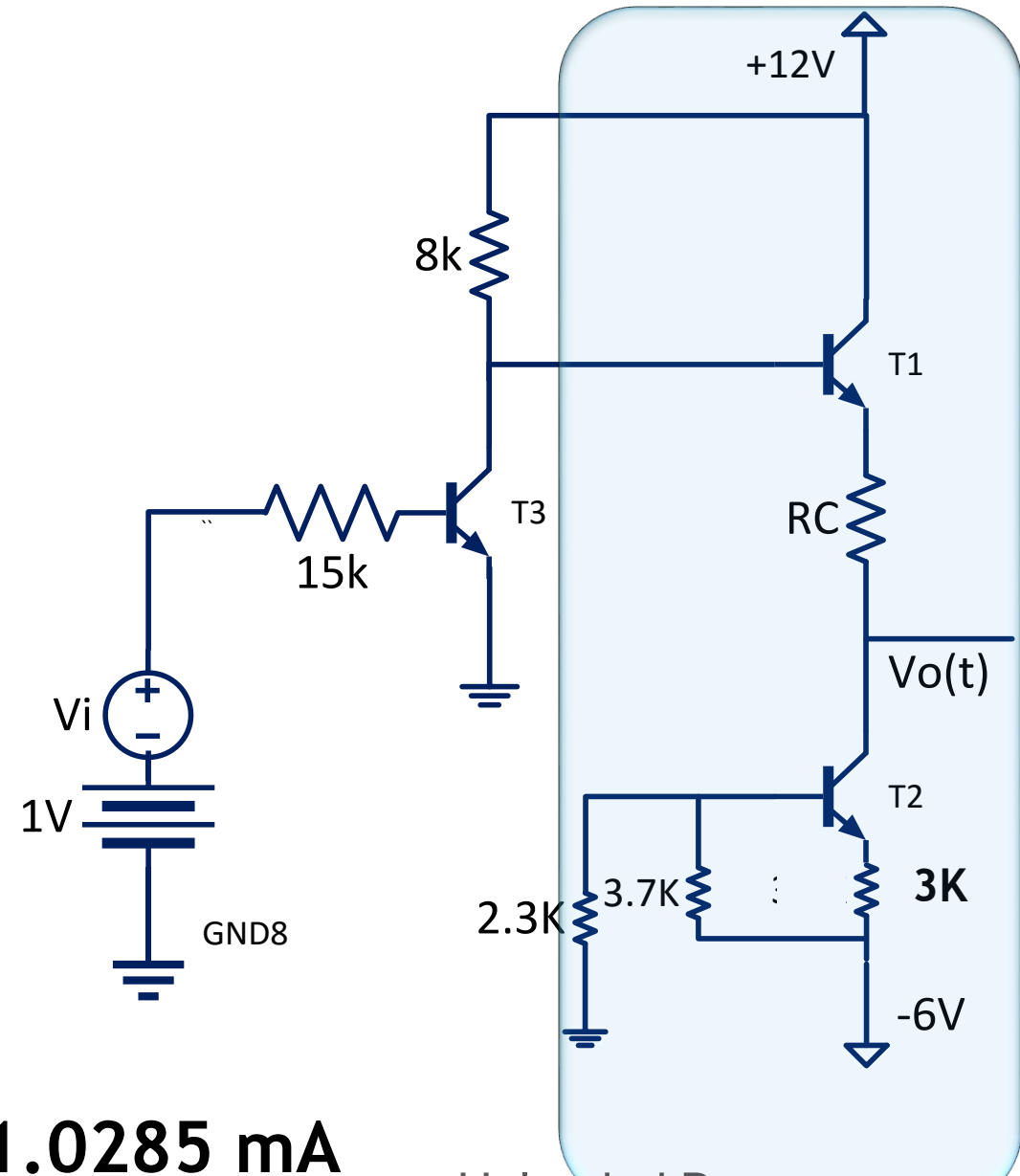
$$R_C = \text{?????}$$

$$R_{TH} = 2.3k || 3.7k = 1.418k$$

$$V_{TH} = \frac{2.3k}{2.3k + 3.7k} (-6) = -2.2V$$

$$I_{E2} = \frac{V_{TH} - 0.7 + 6}{3k + \frac{R_{TH}}{\beta + 1}}$$

$$I_{E2} = 1.0285 \text{ mA}$$

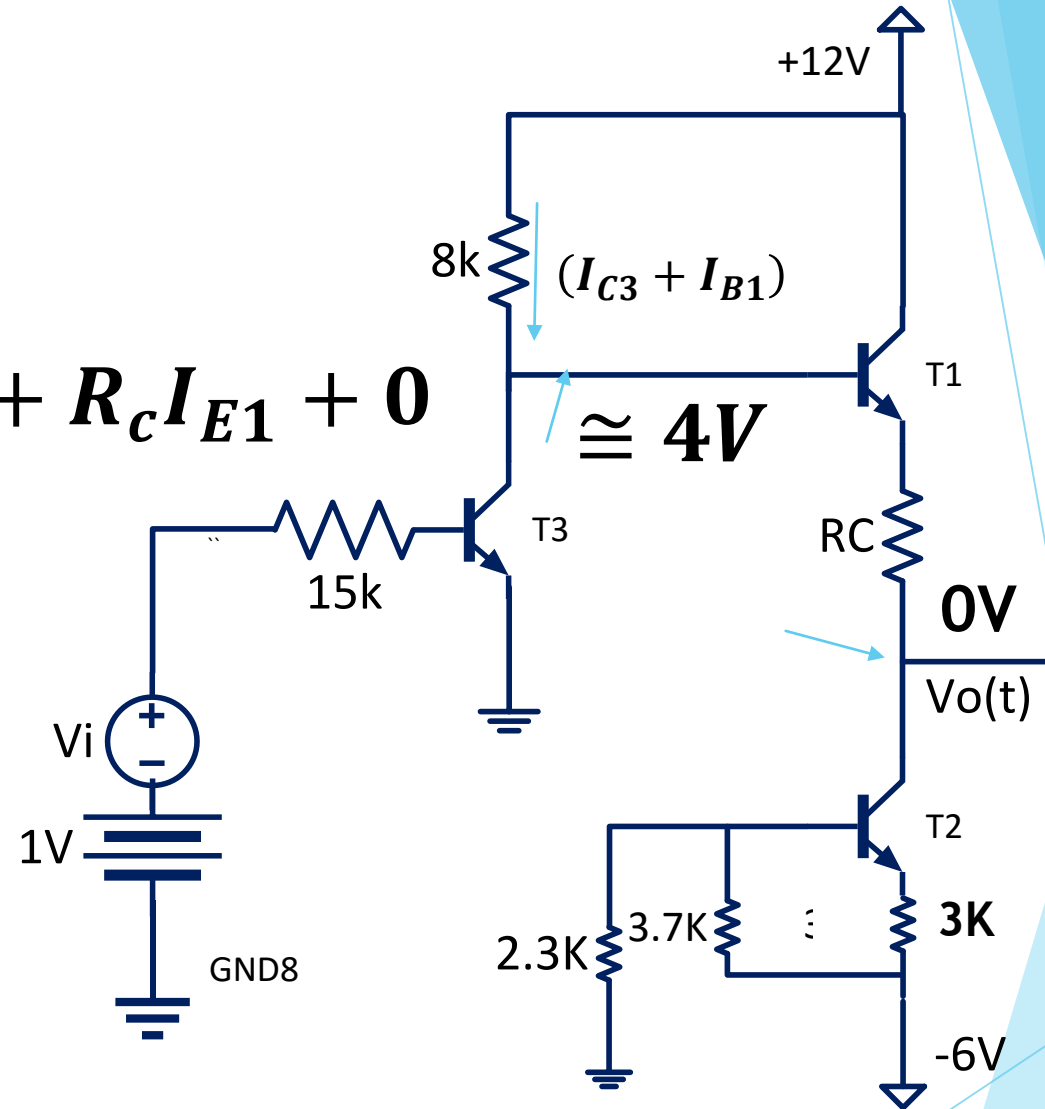


$$I_{B3} = \frac{1-0.7}{15k} = 0.02\text{mA} \blacktriangleright$$

$$I_{C3} = 1\text{mA}$$

$$12 = 8k(I_{C3} + I_{B1}) + 0.7 + R_c I_{E1} + 0$$

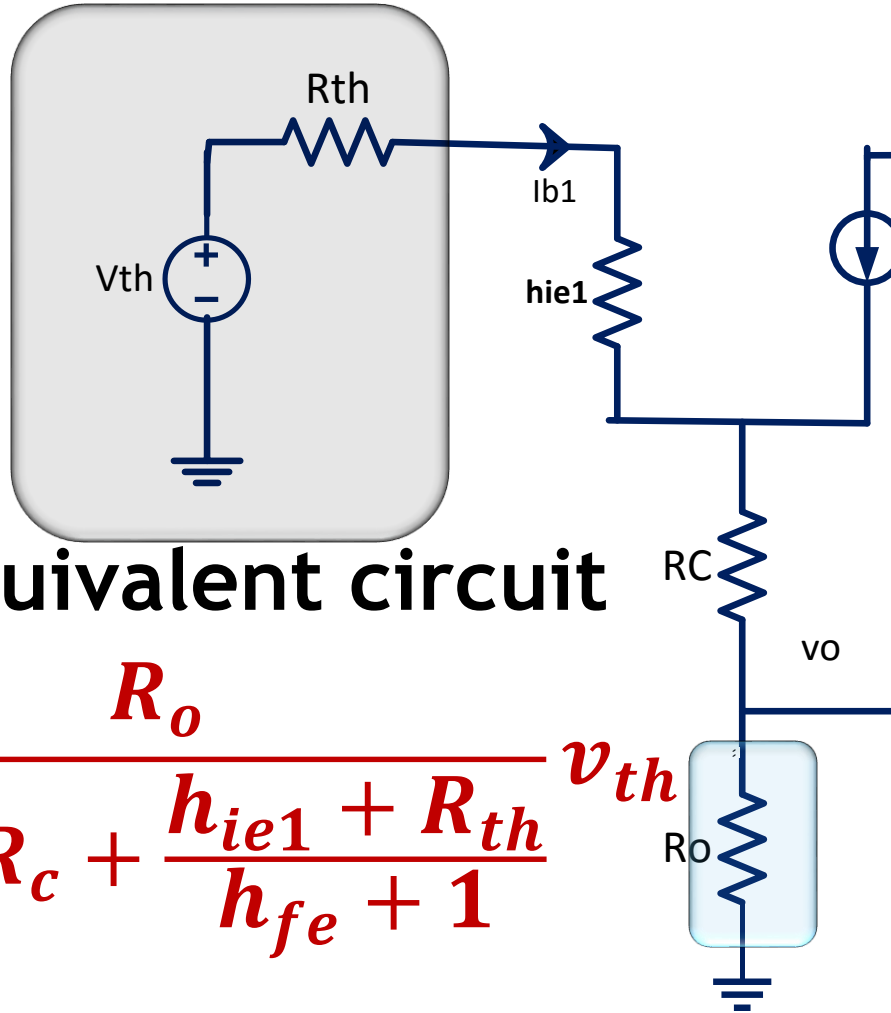
$$\therefore R_c \cong 3.3k$$



THE FUNCTION OF THE CAPACITOR

The Operational Amplifier

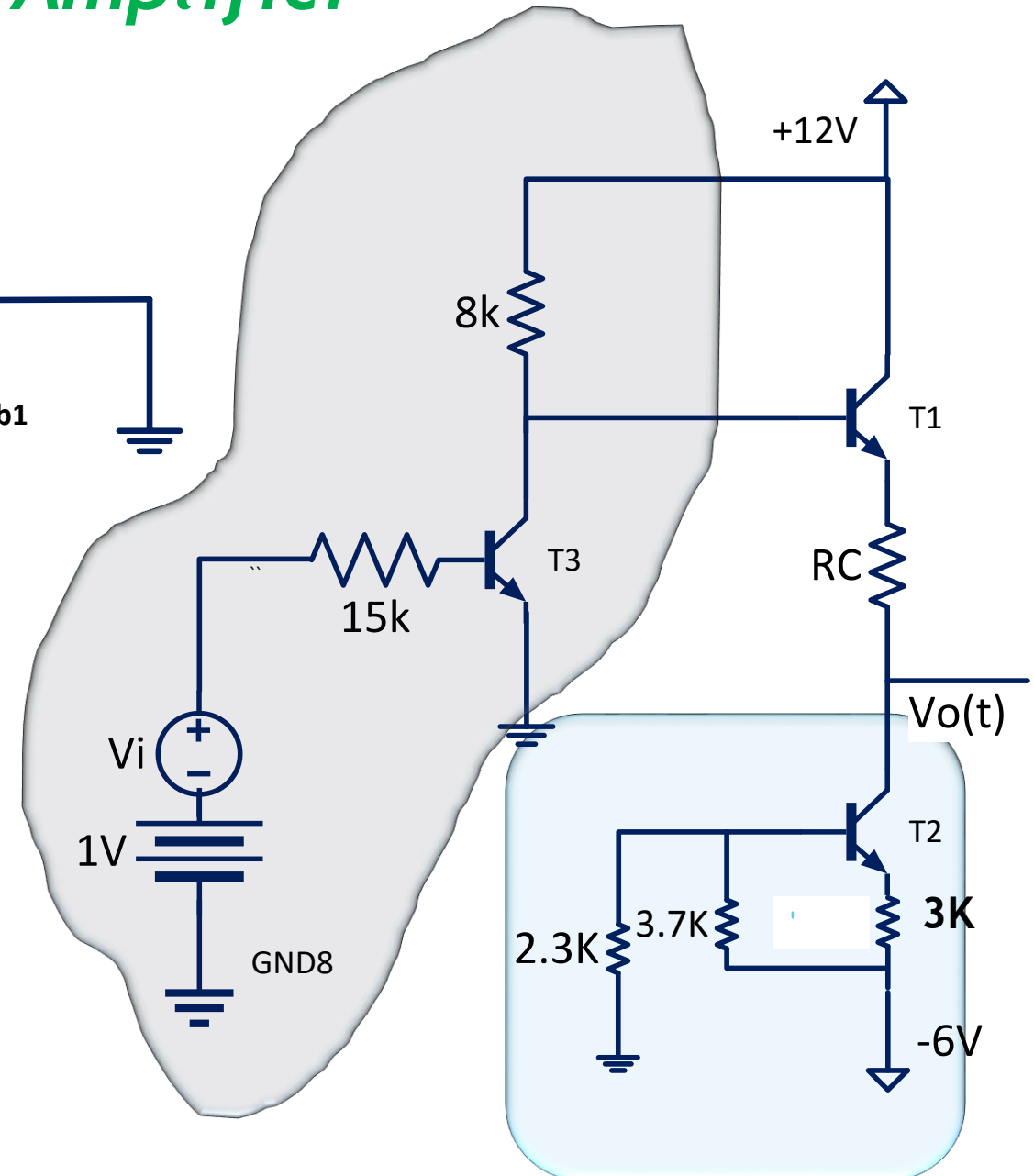
Ac Small signal equivalent Circuit:



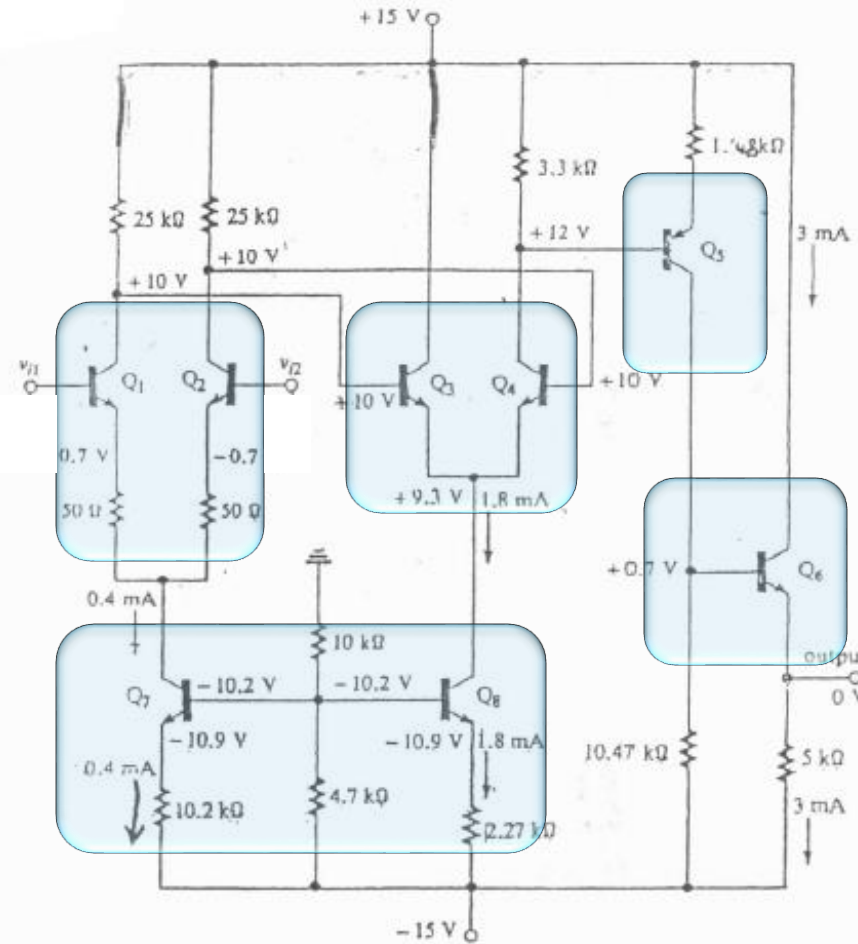
Emitter equivalent circuit

$$v_o = \frac{R_o}{R_o + R_c + \frac{h_{ie1} + R_{th}}{h_{fe} + 1}} v_{th}$$

$$v_o \approx v_{th}$$



Complete Operational Amplifier



Q5 pnp DC Level Shifter

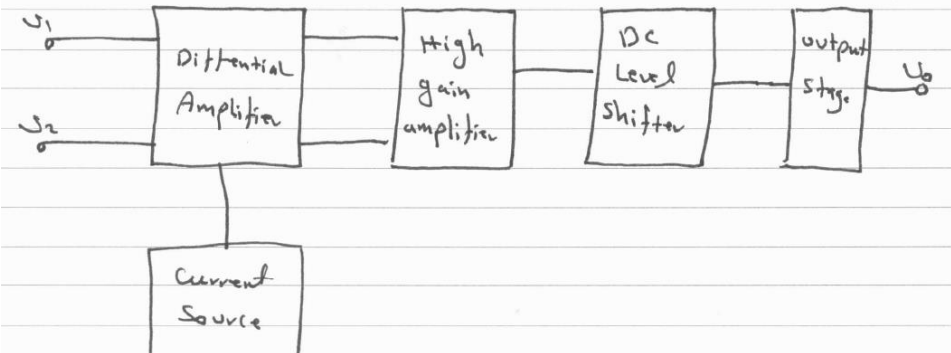
ALL $\beta = 100$

Q6 Output Stage CC

Q1 and Q2 Differential Amplifier

Q3 and Q4 High Gain Amplifier

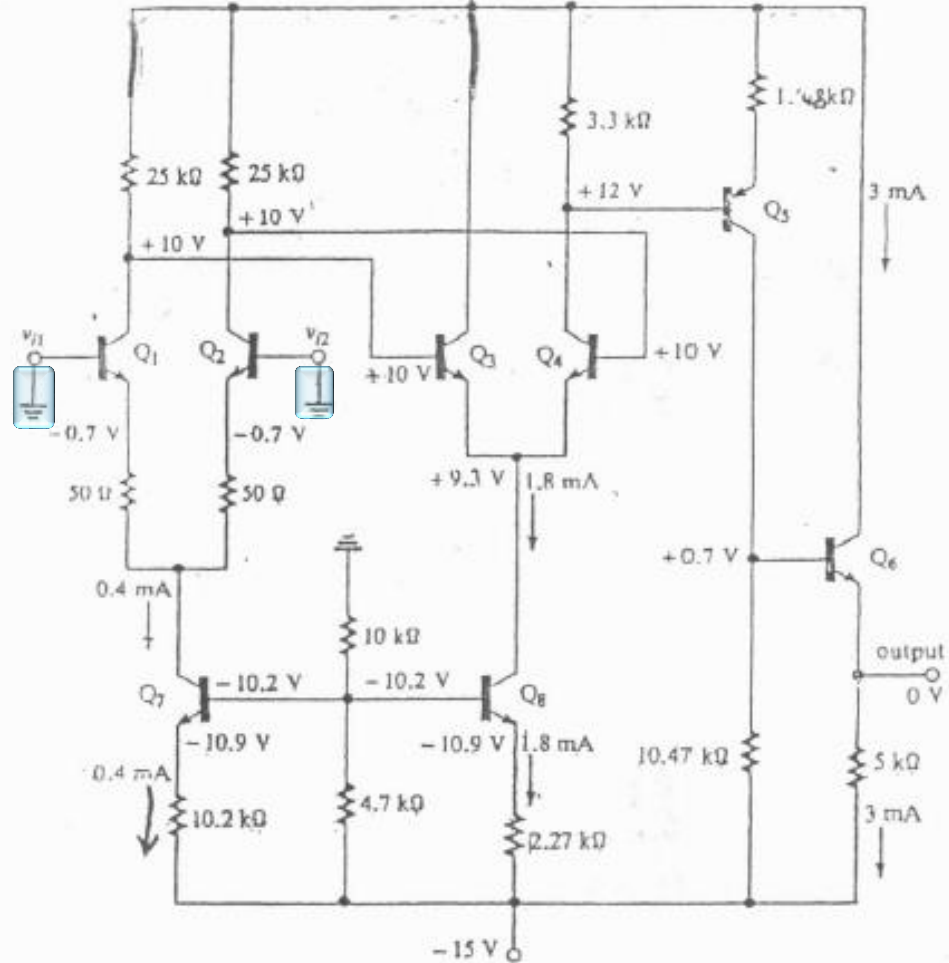
Q7 and Q8 Current Source



Complete Operational Amplifier :

DC Analysis :

$$V_{i2} = V_{i1} = 0$$



All $\beta = 100$

ALL $\beta = 100$

$$V_{B7} = V_{B8} = (10\text{K}) \cdot (-15\text{V}) / (10\text{K} + 4.7\text{K}) = -10.2\text{ V}$$

$$V_{E7} = V_{E8} = -10.2\text{V} - 0.7\text{V} = -10.9\text{V}$$

$$I_{E7} = (+15 - 10.9) / R_{E7} = 0.4\text{mA}$$

$$I_{E8} = (+15 - 10.9) / R_{E8} = 1.8\text{mA}$$

$$I_{CQ1} = I_{CQ2} = 0.5 I_{E7} = 0.2 \text{ mA}$$

$$I_{CQ3} = I_{CQ4} = 0.5 I_{E8} = 0.9 \text{ mA}$$

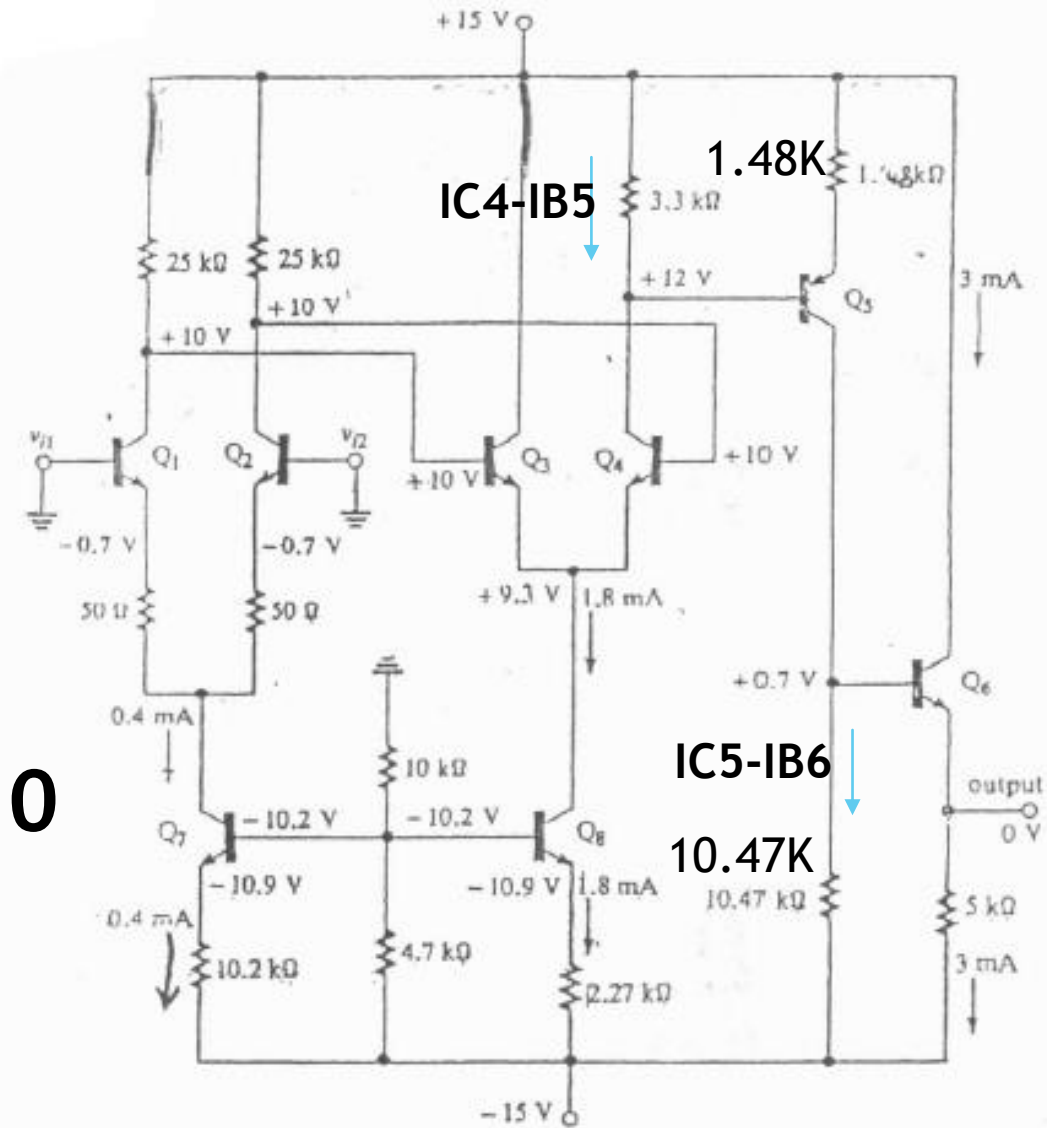
$$0 = 3.3 \text{ K} (I_{C4} - I_{B5}) + V_{BE5} - 1.48 \text{ K} I_{E5}$$

$$I_{E5} = 1.53 \text{ mA}$$

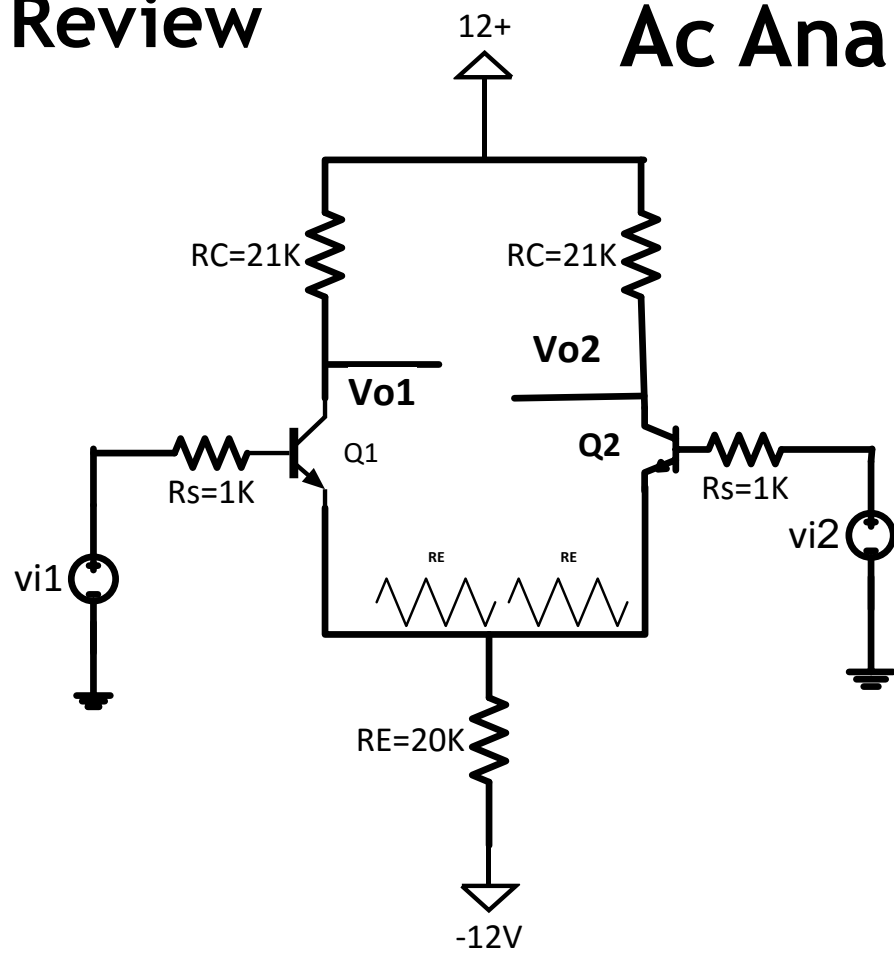
$$V_{BE6} + 5 \text{ K} I_{E6} - 10.47 \text{ K} (I_{C5} - I_{B6}) = 0$$

$$I_{E6} = 3 \text{ mA}$$

$$\text{Or } I_{E6} = \frac{0 - (-15)}{5 \text{ K}} = 3 \text{ mA}$$



Review



Ac Analysis : Differential Mode Analysis

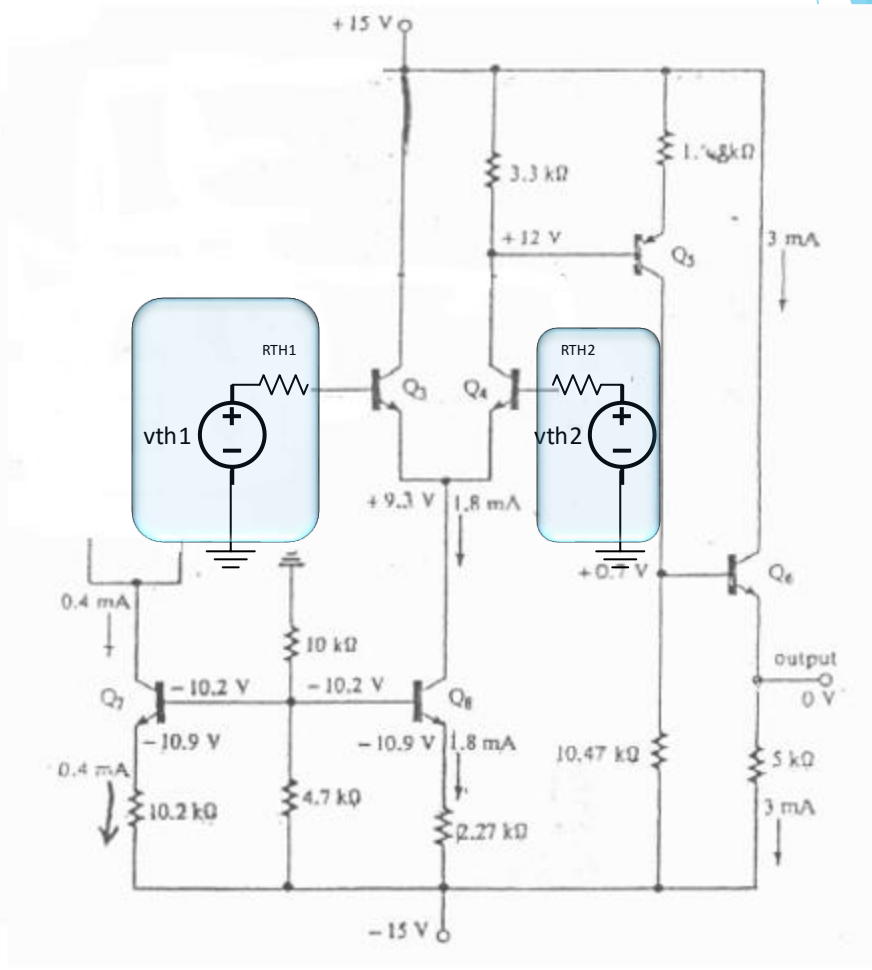
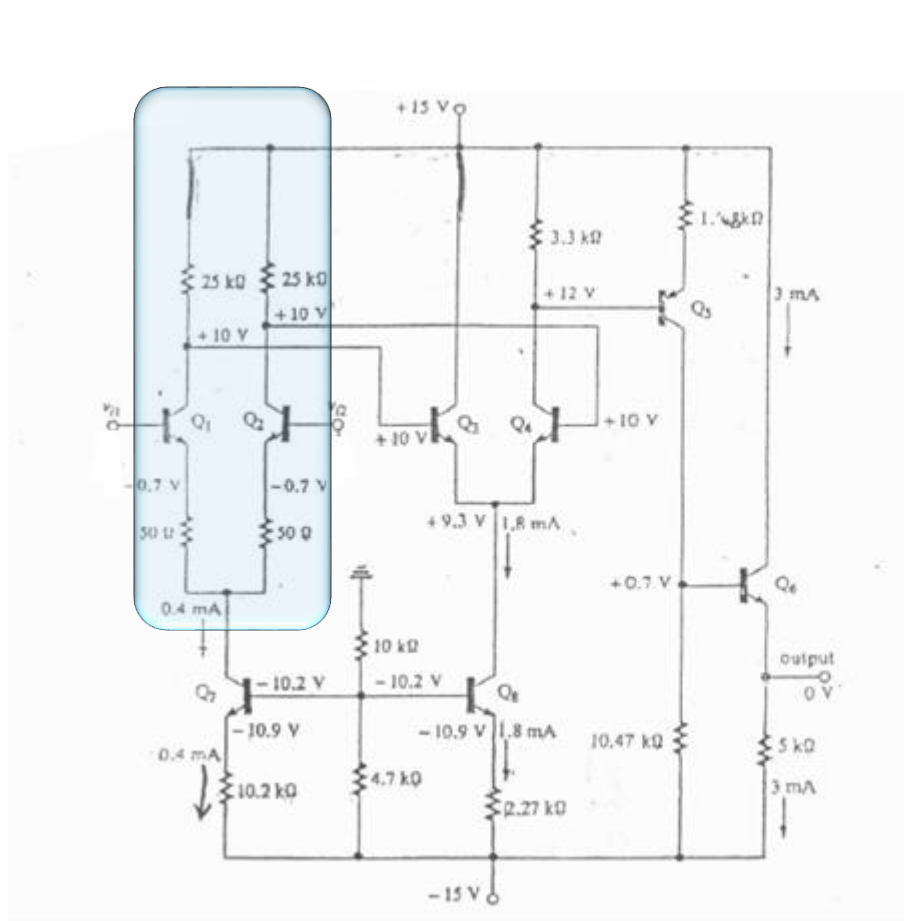
If we have $RE1 = RE2$

$$v_{o1} = \frac{R_c v_d}{2 \left(h_{ib} + RE1 + \frac{R_s}{h_{fe+1}} \right)}$$

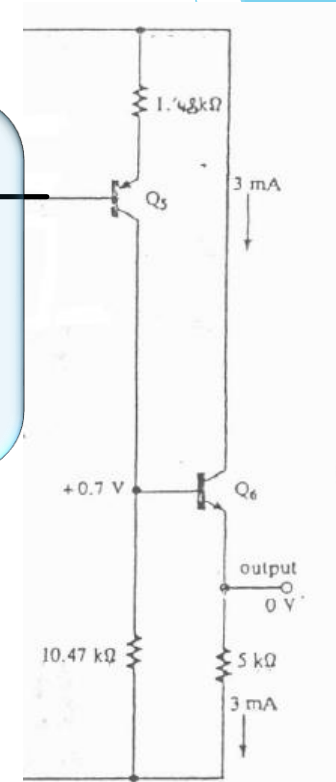
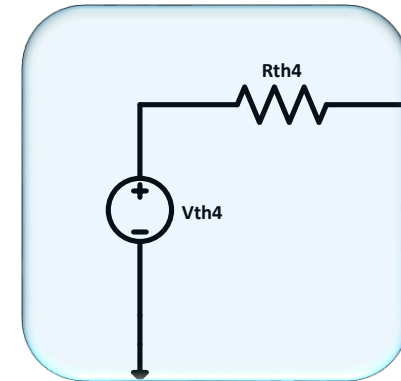
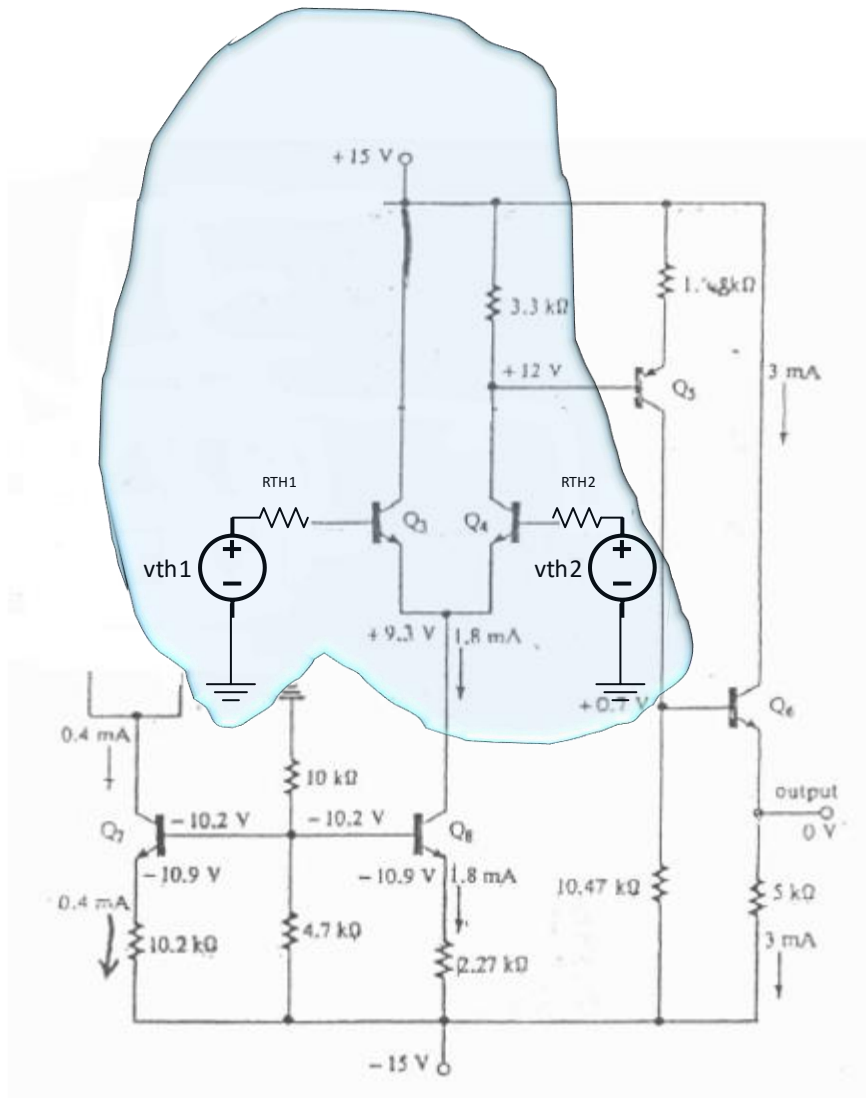
$$v_{o2} = - \frac{R_c v_d}{2 \left(h_{ib} + RE1 + \frac{R_s}{h_{fe+1}} \right)}$$

$$v_{o1} = \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$

$$v_{o2} = - \frac{R_c v_d}{2 \left(h_{ib} + \frac{R_s}{h_{fe+1}} \right)}$$



All $\beta = 100$



All $\beta = 100$

111

Ac Small signal Analys

- hie1 = 13kΩ
- hie2 = 13kΩ
- hie3 = 2.89KΩ
- hie4 = 2.89KΩ
- hie5 = 1.7KΩ
- hie6 = 0.87KΩ

$$V_{th1} = \frac{\left(+\frac{vd1}{2}\right)R_{c1}}{R_{e1} + h_{ib1} + R_{s1}/(h_{fe} + 1)}$$

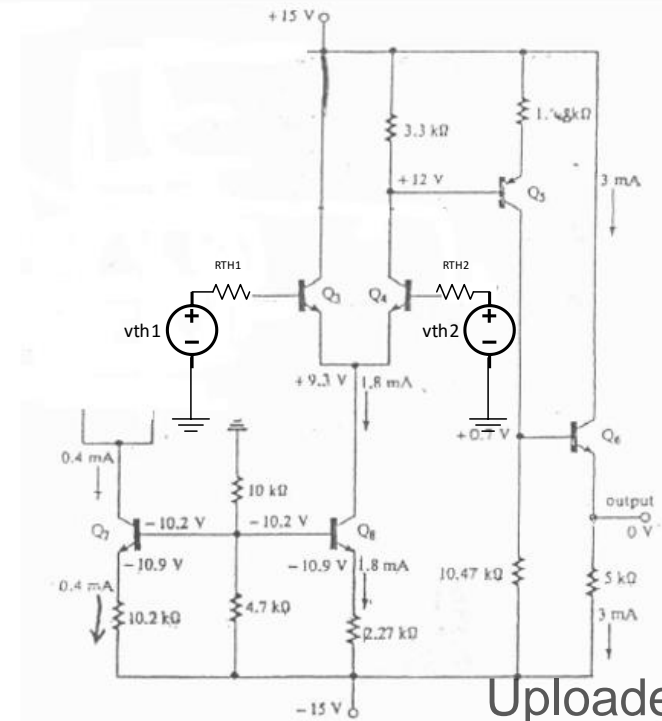
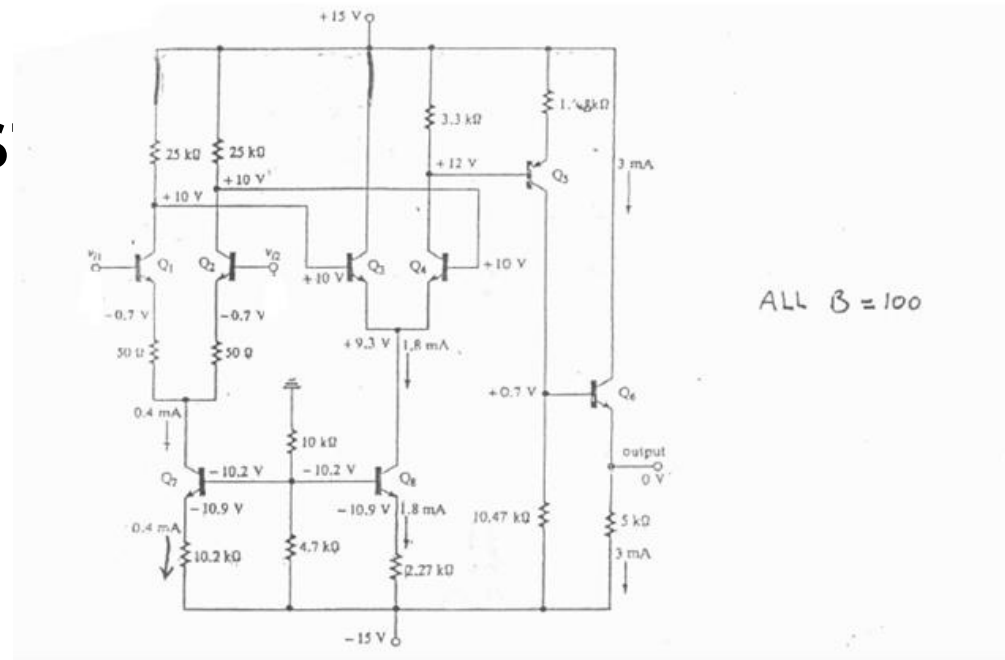
$$R_{s1} = 0 \quad v_{d1} = V_{i2} - V_{i1}$$

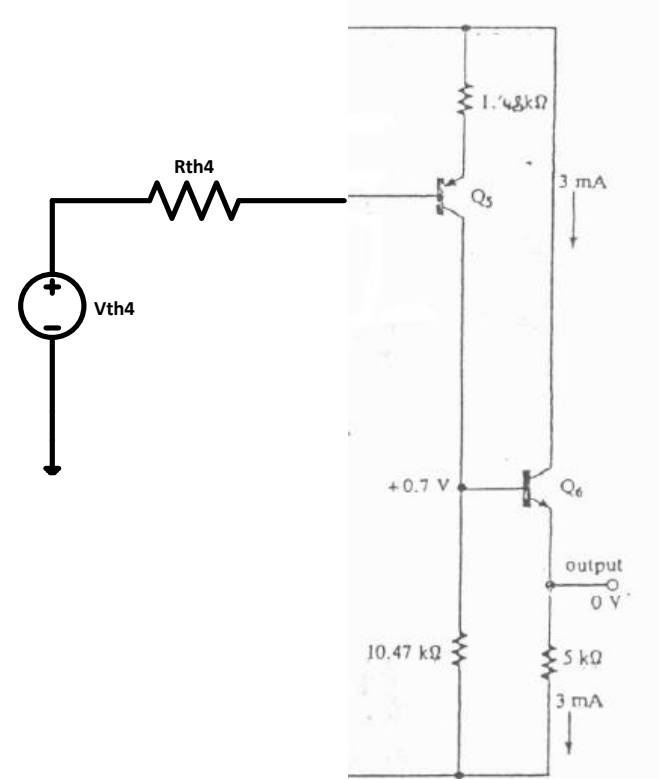
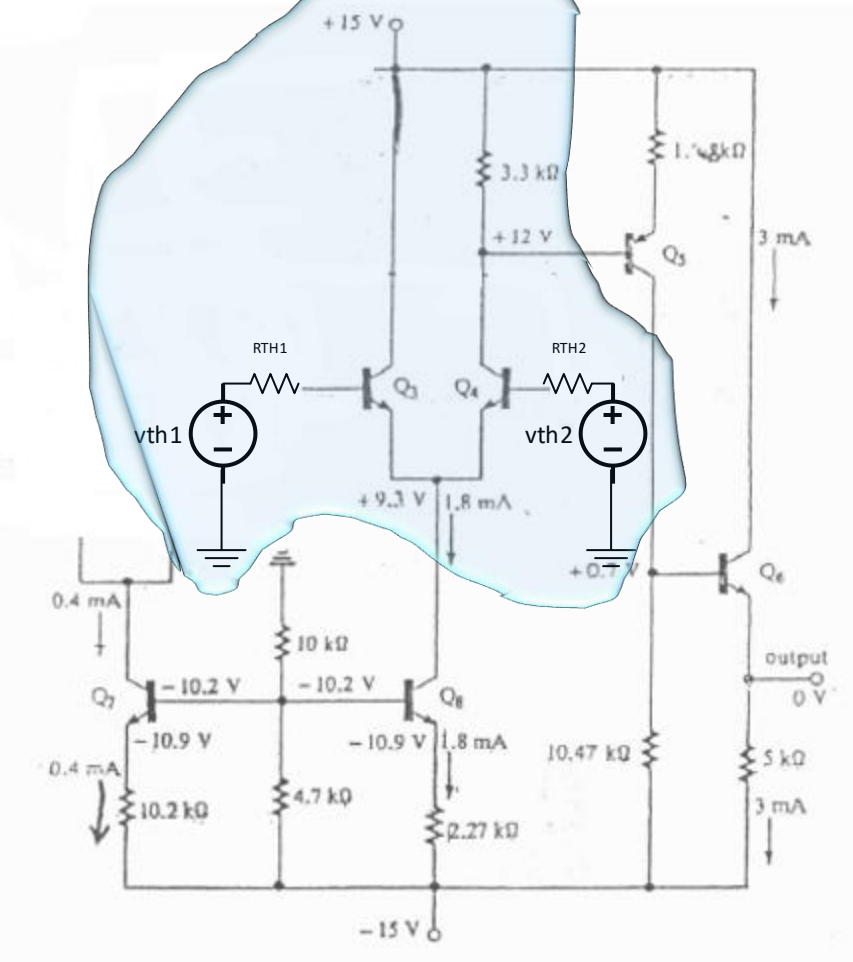
$$V_{th1} = 69.4 V_{d1} \quad R_{th1} = R_{c1} = 25K$$

$$V_{th2} = -V_{th1} = \frac{-\left(+\frac{vd1}{2}\right)R_{c1}}{R_{e1} + h_{ib1} + R_{s1}/(h_{fe} + 1)}$$

$$V_{th2} = -69.4 V_{d1}$$

$$R_{th2} = 25K$$





$$V_{th4} = \frac{-\left(+\frac{v_{d4}}{2}\right)RC_4}{R_{e4} + h_{ib4} + R_{s4}/(h_{fe} + 1)} = 829 V_{d4}$$

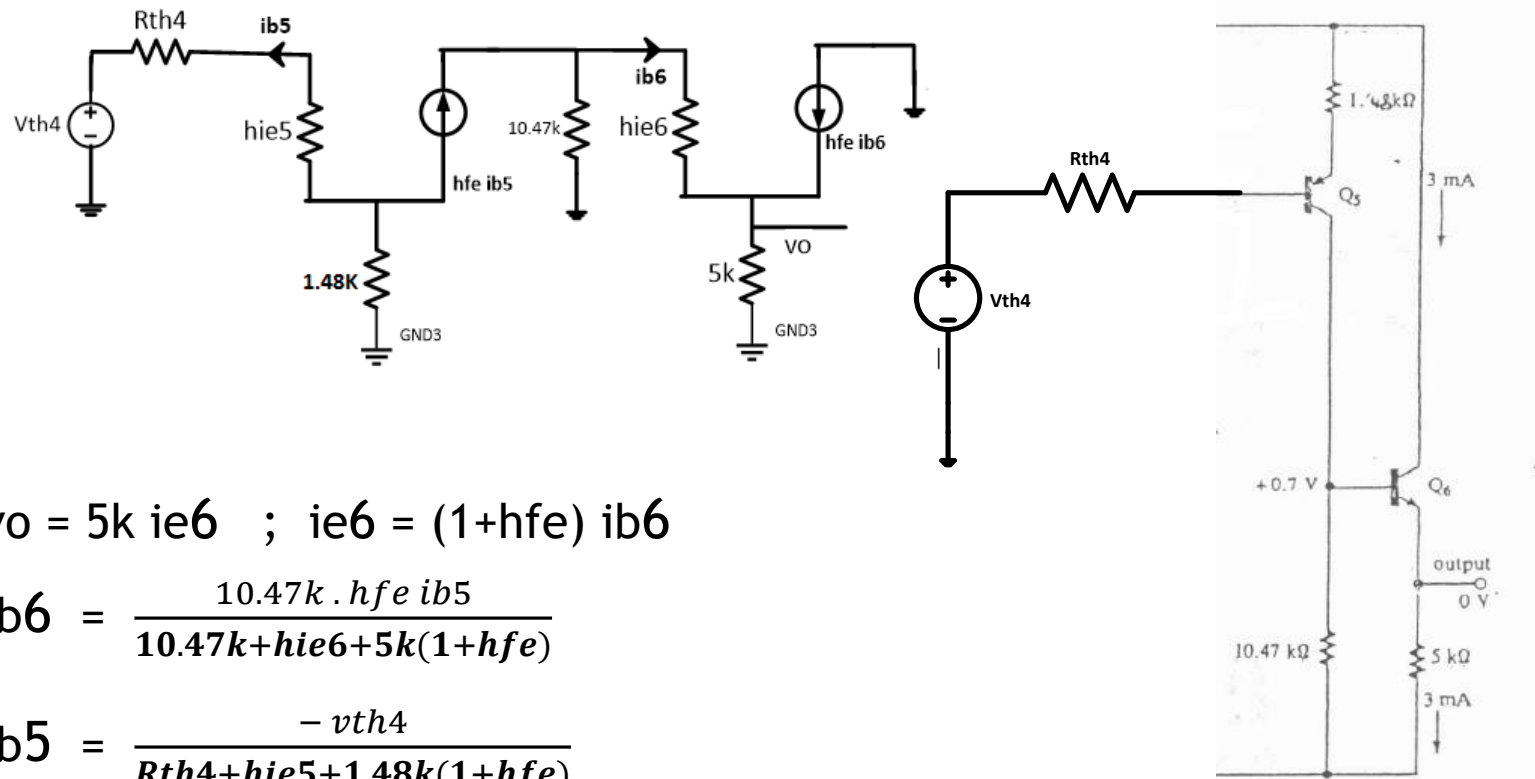
$$R_{e4} = 0$$

$$R_{s4} = 25K$$

$$V_{d4} = (V_{th2} - V_{th1})$$

$$R_{th4} = 3.3k$$

Ac Small Signal Equivalent Circuit Of the DC Level Shifter and the Output Stages :

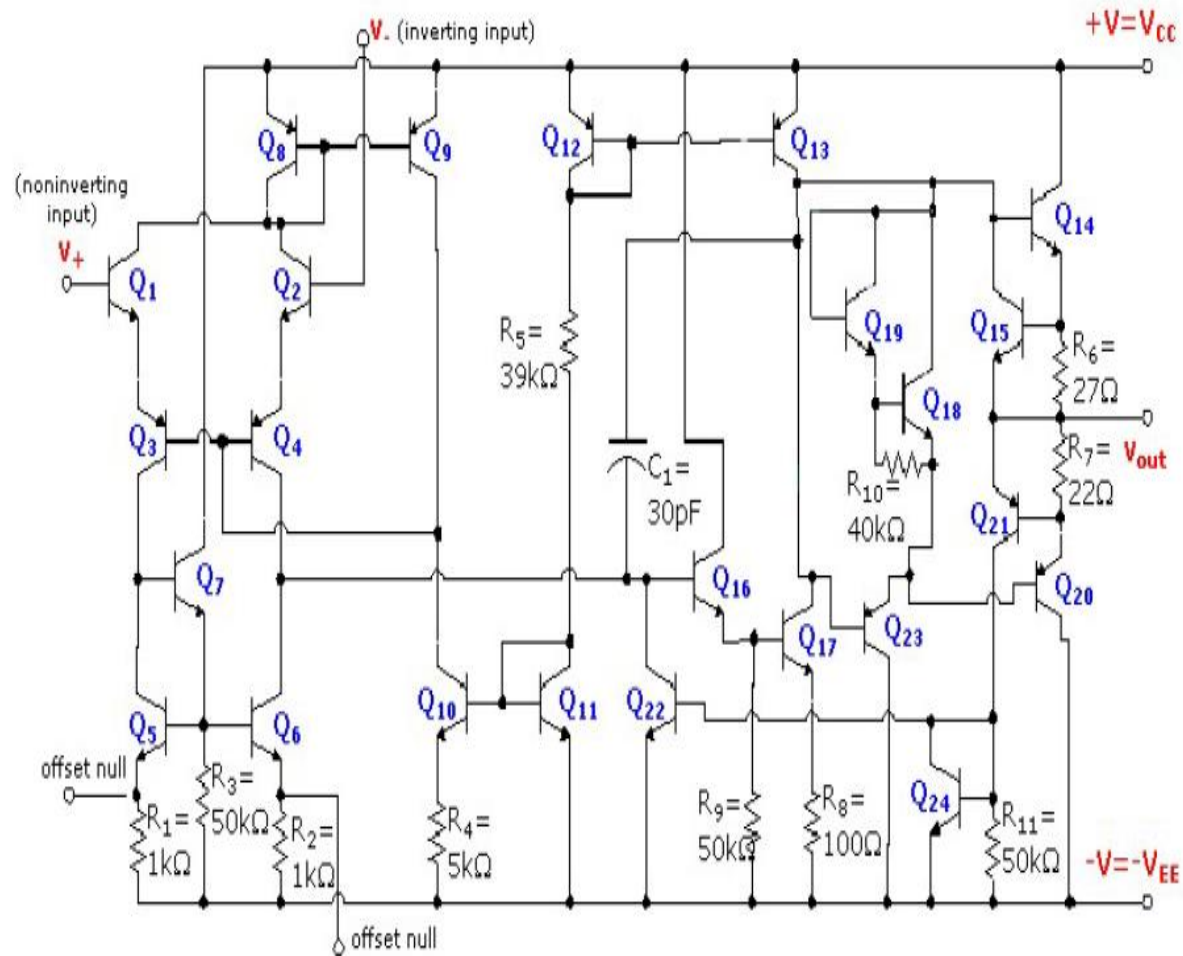


$$v_o = 5k i_{e6} \quad ; \quad i_{e6} = (1+h_{fe}) i_{b6}$$

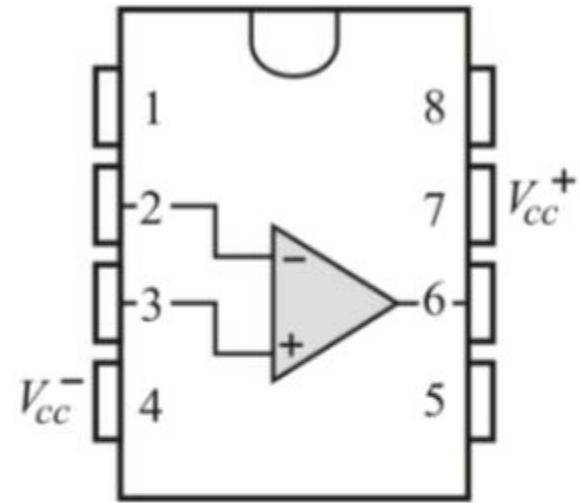
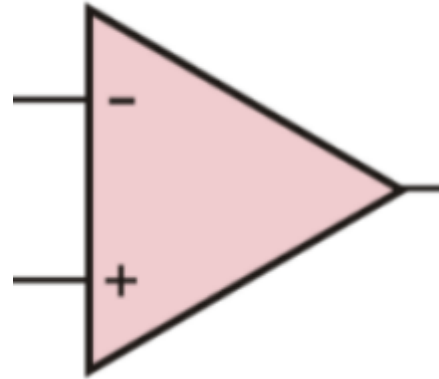
$$i_{b6} = \frac{10.47k \cdot h_{fe} i_{b5}}{10.47k + h_{ie6} + 5k(1+h_{fe})}$$

$$i_{b5} = \frac{-v_{th4}}{R_{th4} + h_{ie5} + 1.48k(1+h_{fe})}$$

$$V_o = - 5540 v_{d1} = + 5540 (v_{i1} - v_{i2})$$



Operational Amplifier



741 Op-Amp Pin out