

Prove using **mathematical induction** or **disapprove** by **counterexample**, that the following two code segments will produce and print the same output for any integer value $n \geq 1$.

If you use mathematical induction, then you should **explain** each step and you should **highlight** $P(n)$, $P(k)$, $P(k+1)$, the inductive hypothesis, etc. Explaining each step is very important.

===== segment 1 =====

```
int i, n, s=0;
printf("enter any positive integer value\n");
scanf("%d", &n);
if(n >= 1){
    for(i=1; i <= n; ++i){
        s+= (i*(i+1)) / 2 ;
    }
    printf("The summation = %d \n", s);
}
```

===== segment 2 =====

```
int i, n, s=0;
printf("enter any positive integer value\n");
scanf("%d", &n);
if(n >= 1 ){
    s = ( n * (n+1) * (n+2)) / 6 ;
    printf("The summation = %d \n", s);
}
```

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Discrete Mathematics
 Quiz #3

Q.1 Segment 1 will print $\sum_{i=1}^n \frac{i(i+1)}{2}$, $n \geq 1$

Segment 2 will print $\frac{n(n+1)(n+2)}{6}$, $n \geq 1$

Show that n
 then: $\sum_{i=1}^n \frac{i(i+1)}{2} = \frac{n(n+1)(n+2)}{6} \leftarrow P(n)$
 $n \geq 1$

① Basis Step: Show that $P(1)$ is true.

$P(1)$ L.H.S $\sum_{i=1}^1 \frac{i(i+1)}{2} = 1$, R.H.S $\frac{1(1+1)(1+2)}{6} = 1$

so, L.H.S. = R.H.S = 1, thus $P(1)$ is true

② Inductive Step = show that for all integers $k \geq 1$
 (Particular but arbitrarily chosen) if $P(k)$ is true,
 then $P(k+1)$ is also true.

Suppose $\sum_{i=1}^k \frac{i(i+1)}{2} = \frac{k(k+1)(k+2)}{6}$ is true $\leftarrow P(k)$

$\sum_{i=1}^{k+1} \frac{i(i+1)}{2} = \frac{(k+1)(k+2)(k+3)}{6}$ \leftarrow inductive hypothesis $P(k+1)$

L.H.S $\rightarrow \sum_{i=1}^{k+1} \frac{i(i+1)}{2} = \underbrace{\sum_{i=1}^k \frac{i(i+1)}{2}}_{P(k)} + \frac{(k+1)(k+2)}{2}$

$= \frac{k(k+1)(k+2)}{6} + \frac{3(k+1)(k+2)}{6}$ by inductive hypothesis

$= \frac{(k+1)(k+2) [k+3]}{6} = \frac{(k+1)(k+2)(k+3)}{6} = \text{R.H.S.}$

so, L.H.S = R.H.S, then $P(k+1)$ is true when $P(k)$ is true
 Thus $P(n)$ is true for all integers $n \geq 1$