

الجزء

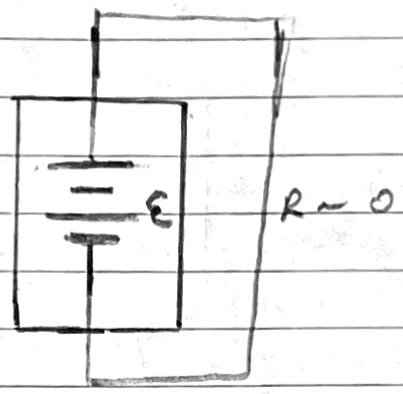
Experiment 2

Source internal Resistance, Loading problems and circuit impedance matching.

- * electromotive force (\mathcal{E}) القوة الدافعة الكهربائية: it is the open circuit voltage difference between its terminals, or it is the voltage difference between terminals of an open circuit.
- * An ideal voltage source connected to a short circuit ($R \sim 0$) should according to Ohm's law be able to provide an almost infinite current

ohm's law

$$I = \frac{\mathcal{E}}{R} \approx \infty \quad (R \sim 0)$$



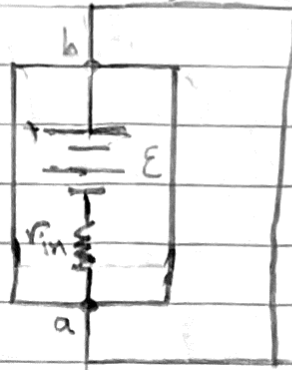
ideal battery or source

- * In real circuits - a voltage source connected to a short circuit can neither maintain its emf as a voltage difference across its terminals nor can it provide the circuit with unlimited current
- في الدارات الحقيقية ان توتر المصدر لا يثبت عند $R \sim 0$ ولا يستطيع ان يزود الدارة بتيار لا محدود
- Short circuit $(R \sim 0)$

لا يستطيع المحافظة على القوة الدافعة الكهربائية \mathcal{E} عند $R \sim 0$ ولا يستطيع ان يزود الدارة بتيار لا محدود

⇒ Therefore, each real voltage is assigned an internal resistance (r_{in})

$\frac{1}{2} \epsilon, r$



real battery or real source
 ↓
 has an internal resistance

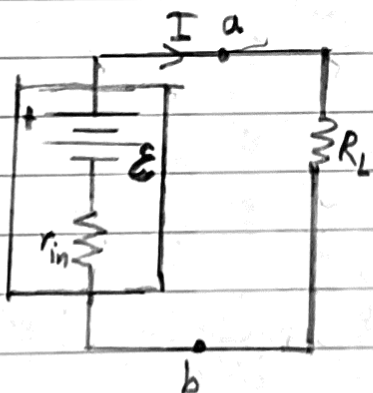
$V_{ab} \approx \epsilon$ for small r_{in}

⇒ Fig gives more realistic representation of a voltage source

- The voltage sources with small internal resistance can maintain most of their emf as a voltage difference between their terminals
- ⇒ So provide circuit with higher current values than would the ones with high internal resistance.

↳ Load: any component which consumes electrical power to produce useful work
 ⇒ and the resistance of such a component is called load resistance (R_L)

* Loading happens when r_{in} is comparable to R_L



The current passing through the simple series circuit is ⇒

$$I = \frac{\epsilon}{R_L + r_{in}}$$

(3)

The voltage difference between the source terminals is:

$$V_{ab} = V_{RL} = I R_L$$

$$\Rightarrow V_{RL} = \frac{\epsilon R_L}{(R_L + r_{in})}$$

* If $R_L \gg r_{in}$ then $R_L + r_{in} \approx R_L$ then

$$V_{RL} \approx \frac{\epsilon}{R_L} R_L$$

$\Rightarrow V_{RL} \approx \epsilon$ \Rightarrow the source delivers most of its emf as a voltage difference across its terminals.

If R_L is comparable:

* If R_L is comparable to r_{in} ($R_L \approx r_{in}$) then

$$V_{RL} \approx \frac{\epsilon}{(R_L + R_L)} R_L$$

$$V_{RL} \approx \frac{\epsilon}{2R_L} R_L$$

$\Rightarrow V_{RL} \approx \frac{\epsilon}{2}$ \Rightarrow in this case considerable amount of power is consumed inside the source and converted to (un)useful heat energy. \Rightarrow this case is said to be loaded.

* In practical circuits we want to avoid loading the source so we choose $R_L \geq 10 r_{in}$

Impedance Matching (Maximum Power Transfer)

* In real circuits, power consumed in the load produce useful work \Rightarrow therefore we seek to consume the maximum available power there

* The power consumed in the load resistor is

$$P = I^2 R_L$$

$$= \left(\frac{\epsilon}{R_L + r_{in}} \right)^2 R_L$$

$$\Rightarrow P = \frac{\epsilon^2 R_L}{(R_L + r_{in})^2}$$

\rightarrow represents the power consumed in the load as a function of the load resistance itself.

* The function $P(R_L)$ has a maximum value which can be obtained by setting $\frac{dP}{dR_L} = 0$

$$\Rightarrow R_L = r_{in} \Rightarrow \text{the condition for transferring maximum power to the load resistance}$$

\rightarrow This choice of load resistance is called impedance matching.

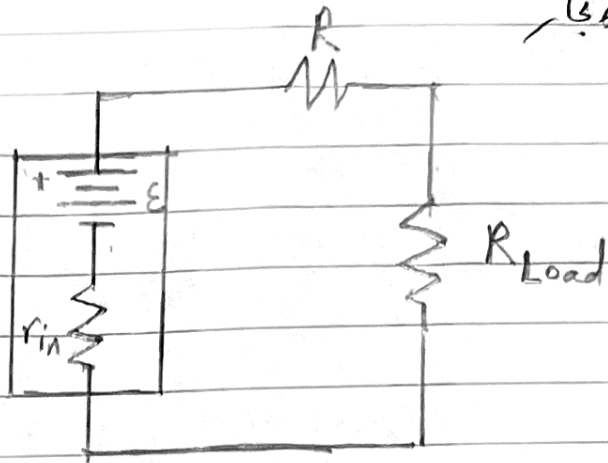
• To achieve this condition with avoiding loading problem additional resistance R is added

\Rightarrow this R helps in avoiding loading problem and fulfilling the condition of impedance matching for large load values.

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3.2.2

- The only disadvantage is that this additional resistance R consumes part of the power delivered to the circuit by the source.

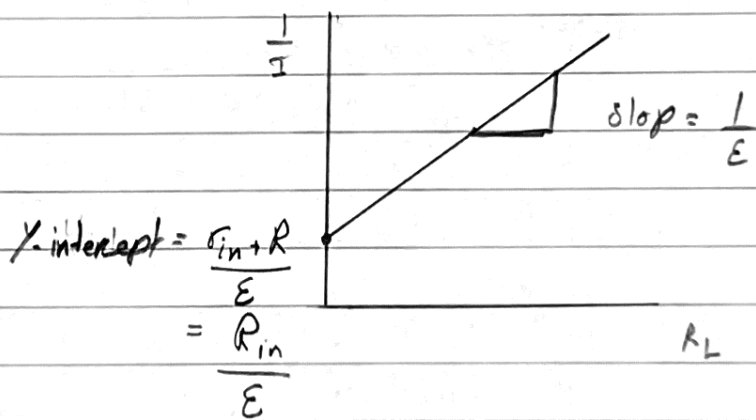


$$I = \frac{\epsilon}{r_{in} + R + R_L}$$

$$\frac{1}{I} = \frac{r_{in} + R + R_L}{\epsilon}$$

$$\frac{1}{I} = \frac{R_L}{\epsilon} + \frac{r_{in} + R}{\epsilon} \rightarrow r_{in} + R = R_{in}$$

plotting $\frac{1}{I}$ vs R_L on a linear graph



Find ϵ, R_{in} knowing $R = 1k\Omega \Rightarrow$ you can find r_{in}

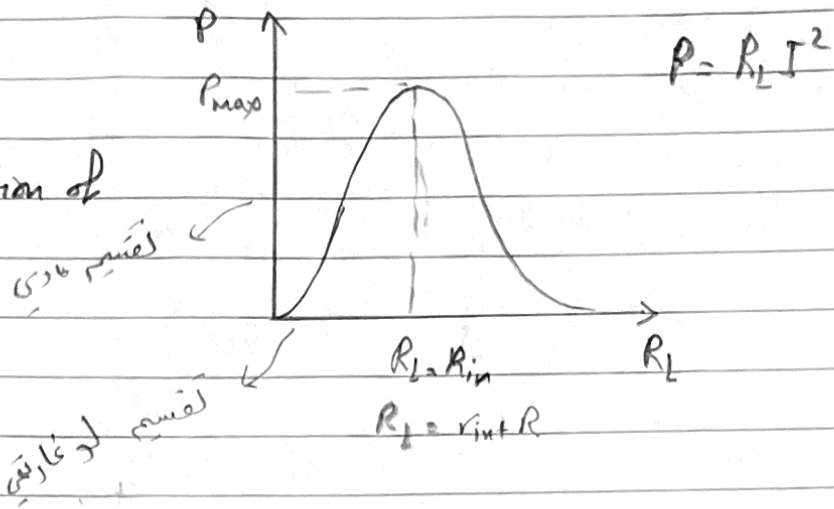
DM
 الارق ان تستعمل قيمته
 حيث تكون 983Ω

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13.2.1

Plotting P vs R_L on a semi-log graph paper

Find R_L that satisfies the condition of max power.

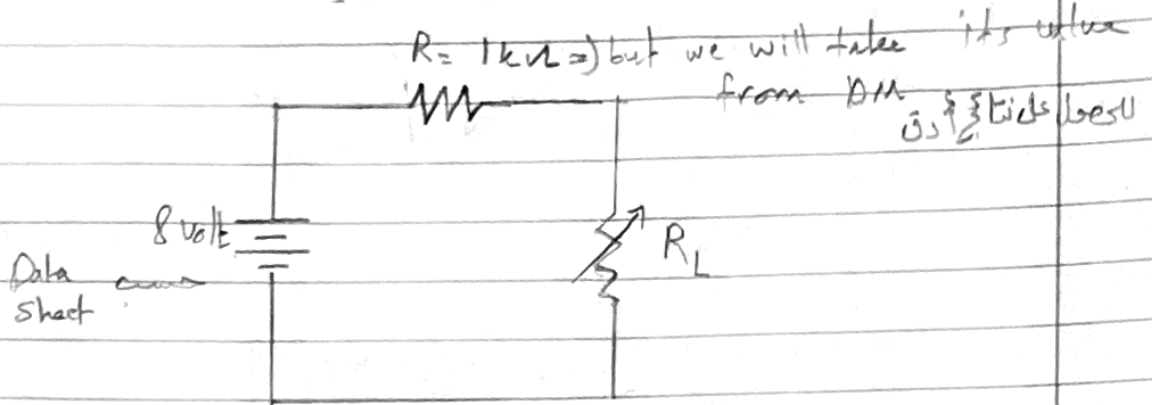


سأدعى

توصيل الدارة

a) Connect the circuit as in Fig

نقوم بوصل الدارة كما في الشكل



b) change R_L and record the value of current each time

غير قيم R_L تباعاً في data sheet و سجل قيمة التيار المراد ل R_L في كل مرة

c) Draw 1/I vs R_L on a linear graph to find the value of r_{in} and ε

y intercept = $\frac{R+r_{in}}{\epsilon}$ و R = 1kΩ ، ε : جهد المصدر

slope = $\frac{1}{\epsilon}$

من قراءة الجهد
عوضنا
983 في
1000

d) compute P for all values of I ⇒ (P = R_LI²)

e) plot P vs R_L on a semi-log paper

At P_{max} ⇒ R_L = R_{in} = r_{in} + R

⇒ You can find R_L that satisfies the condition of maximum power transfer.

r_{in} = R_L - R

للوصول على نتائج أدق
DM
P_{max} التي نحصلها