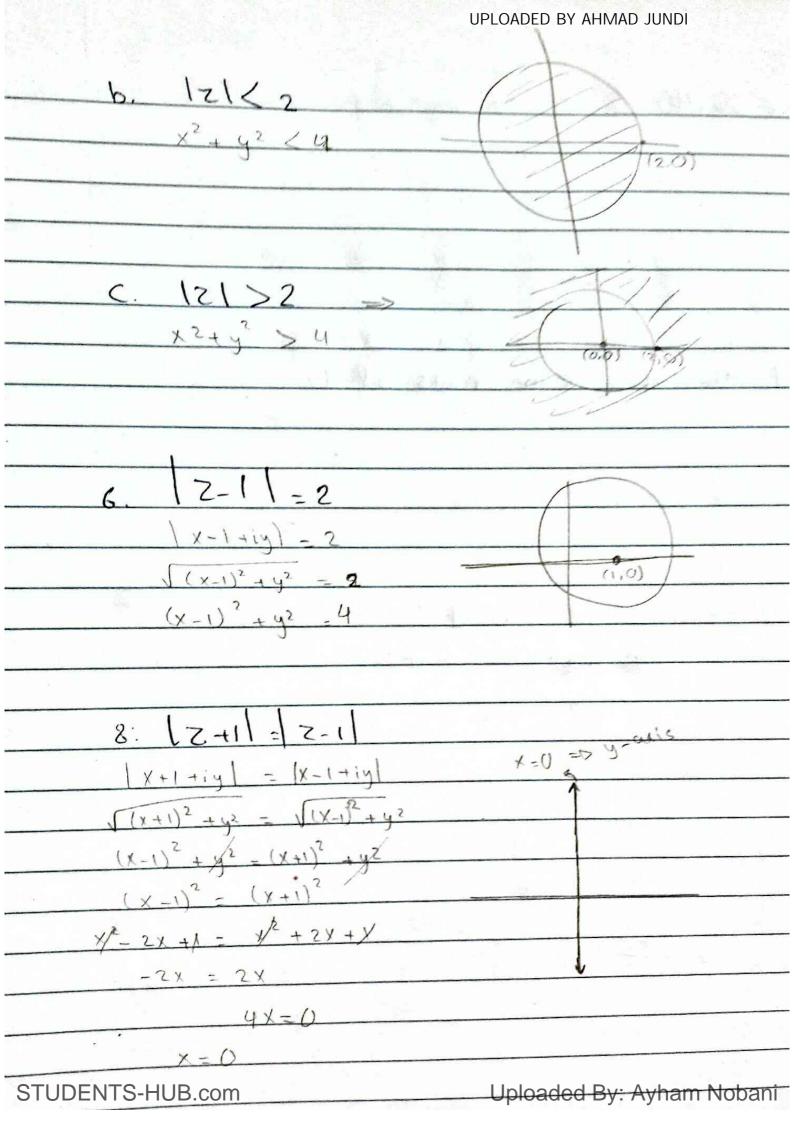
UPLOADED BY AHMAD JUNDI	
AY Chalan	
A.J. Complex number	
$(3+4i)^2 - 2(x-iy) = x + iy$	
9. + 24 11 - 16 26. 21	
9. + 24u - 16 - 2x + 2iy = x + iy +2x - 2iy + 2x - 2iy	
-7 + 24i = 3x - 2y	
3 X=-7-1 + X=-4	
$\frac{3 \times = -7}{-4y} \Rightarrow \frac{4 - 4}{-24}$	
1. ·	*
$\frac{b(1+i)^2+(1-1+i)^2}{b(1+i)^2+(1-1+i)^2}$	
$\frac{b(1+i)^2+(1-1+i)^2}{(1-i)^2+(1-1+i)^2}$	***
1 (1 +i) 1 1 +i) 2 1 (x +iy) = 1	
$\frac{\left(1+i\right)\left(1+i\right)^{2}}{\left(1-i\right)\left(1+i\right)^{2}} + \frac{1\left(x-iy\right)}{\left(x+iy\right)\left(x-iy\right)} = \frac{1}{2}, 1+i$	
112	
$\left(\frac{1}{1+1}, \frac{2}{1+1}\right)^{2} + \frac{x-iy}{x^{2}+y^{2}} = 1+i$	-
/11/2	
$\frac{(0)}{\sqrt{2}} + \frac{x - iq}{\sqrt{2}} = \frac{q}{\sqrt{2}} + i$	
7+49	
$\frac{1}{1} + \frac{1}{12} = \frac{1}{12} + \frac{1}{12}$	
x2+y2, x2+y2;	
$\frac{1}{x} + \frac{1}{x} = 1$ () $\frac{x}{x} = 2(x^2 + y^2)$	-0
X TY's	
$- \frac{2}{3} \frac{y}{y} = - $	2
$\frac{1}{x^2+y^2}$	
$\bigcirc - + D \times = -2! = D \times = -24$	
$((-2)^2, (2)2 (442 + 42)$	
$\frac{-29}{2} = \frac{2}{2} \left(\frac{(-29)}{4} + \frac{4}{3} \right) = \frac{3}{2} \left(\frac{(-29)}{4} + \frac{4}{3} + \frac{3}{3} \right) = \frac{3}{2} \left(\frac{(-29)}{4} + \frac{4}{3} + \frac{3}{3} + 3$	
$-y = 5y^2 - D - 2y^2 + y = U \Rightarrow y + 2y + 1$	_1
9=0,9=	5
(X=-12X-7==6)	d
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UPLOADED BY AHMAD JUNDI (C) (3-2i) (x+ig) = 2(x-2ig) +2i-1 $\frac{3x + 3ix}{-2x} - 2ix + 2y = 2x - 4iy + 2i - 1$ 2ix + 2y - - 7ig + 2i - 1 - 2x + 2y + Tiy = 2 -1 1 7/y - 2/x - 2/ - 0 7y - 2x - 2 - 0 $x + 2y = -1 - 0 \times + 2y - -1 - 0$ $\frac{7}{4}$ $\frac{2}{4}$ = 2 $\frac{7}{4}$ $\frac{7}{4}$ X + 2x0 = -1 = X = -1a. (71-2 (=2 $\sqrt{x^2 + y^2} = 2 \Rightarrow 4 = x^2 + y^2$ Uploaded By: Ayham Nobani STUDENTS-HUB.com

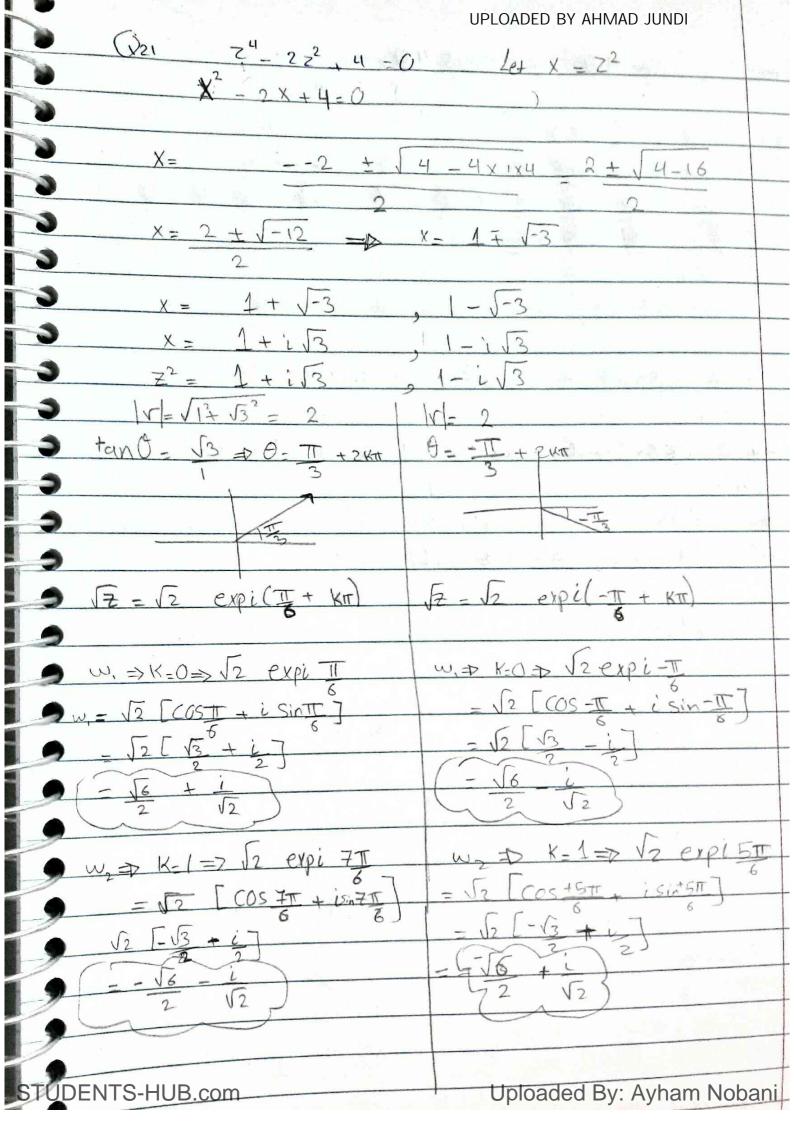


Q16: Sin 40, COS 40.
Cos 40 + i sin 40 = (6050 + i sin 0)4 Demoviers
(coso + 21 cososino + sino) (coso 9+ 21 coso sino + sino)
= cos40 + (21 sin 0 cos30) cos20 sin20 + 21 sin 0 cos20 + 400020 sin30 - 2100 0 sin30
= (Fsin 20 COs 2) 2 i COs (9 sin 30 + sin 0)
= COS 4 4 i sin 0 cos 30 - 6 cos 30 sin 30 - 4 i COSOS in 30 + Sin 9
-COS'0+sin'0-6cos 20 sin'0 + 4 isin 0 cos 30 - 4 i cos 0 sin 30
= cos 40 + sin 40 - 6605 20 sin 20 + i (4 sin 0 cos 30 - 4005 9 sin 30)
COS40 = COS 0 + Sin 0 - 6005 8 Sin 0
- sin 40 = 4 (sina cos6 - cos0 sin30)

17. find the three Cube roots of	7 1
	1
3/1	- Ja Sc. 111
7-1 = rei0	1. 1. 1 x 1
Y = 1 - 1	1
D=0+2πK, k=0,01,=	t 2, ·
	· · · · · · · · · · · · · · · · · · ·
Z=1 e (0+211K)	
$Z = 1 e^{i(\theta + 2\pi k)}$ $Z = 1 e^{i(\theta + 2\pi k)}$ $Z = 1 e^{i(\theta + 2\pi k)}$	11-81-11-51 1
$\sqrt[3]{z} = 1e^{i\frac{2\pi k}{3}}$	
$K=0$, $W_{1}=1e^{\frac{12\pi 0}{3}}=1e^{\frac{1}{3}}=1$	
$K = 1$, $W_0 = 1e^{\frac{i2\pi x_1}{3}} = 1e^{\frac{2\pi}{3}} = 1$	[COS 2T + LSin 2T]
$\frac{1}{2} - \frac{1}{2} + \frac{1}{3}i$	
$K-2$, $W_3 = 1e^{\frac{12\pi \times 2}{3}} - 1e^{\frac{19\pi}{3}} = 1$	ces 4 1 - i Sin 4#
$\frac{1}{2}$	13 6
	0.52

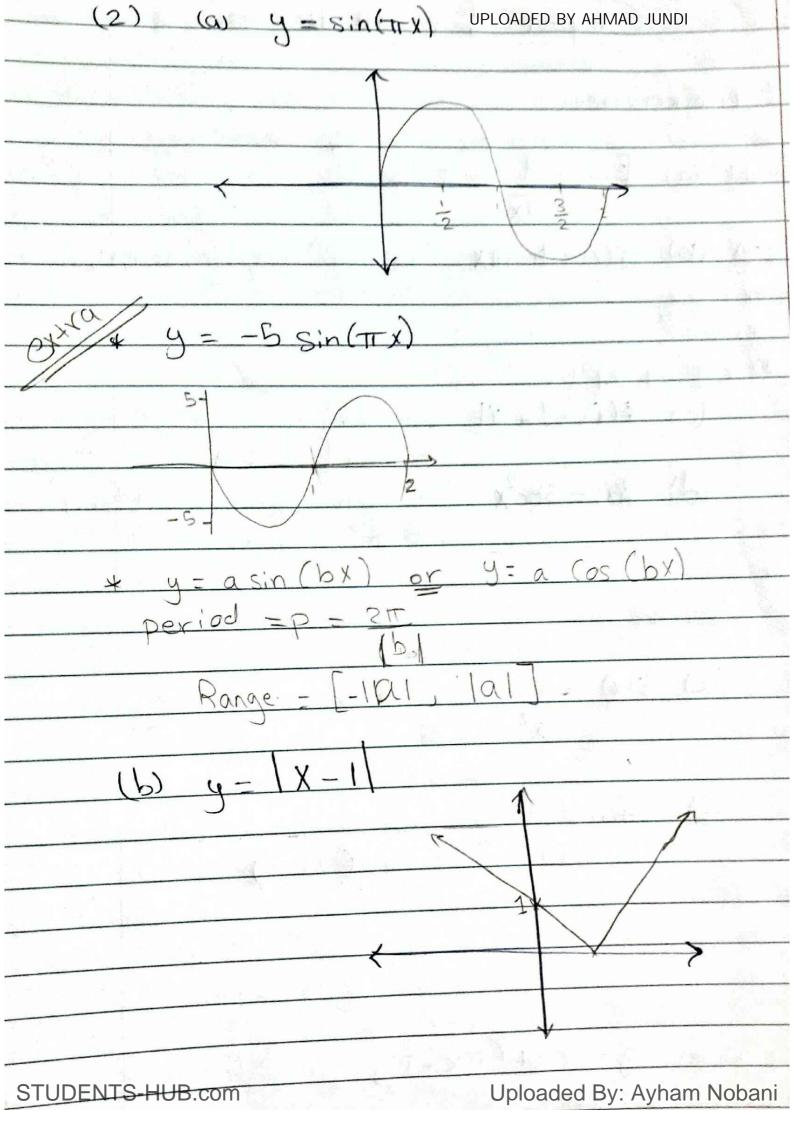
16. Find the two square voots = 1. $ \frac{2}{\sqrt{-1}} $ $ \frac{1}{\sqrt{-1}} $ $ \frac{1}{$	
$ \frac{7}{4} = -1 - \sqrt{e^{i\theta}} $ $ \frac{7}{4} = -1 = 1 $ $ \frac{7}{4} = \sqrt{e} $ $ \frac{7}{4} = -\sqrt{e} $ $ \frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = -2\pi K, K = 0, \pm 1 $ $\frac{7}{4} = $	18. Find the two square roots of:
$V = -1 = 1$ $0 = 180 + 2\pi K, K = 0, \pm 1$ $V = -1 = 1$ $0 = 2\pi + 2\pi K, K = 0, \pm 1$	25-1
$ \frac{1}{2} = \frac{1}{4} = \frac{1}{4} $ $ \frac{1}{4} \frac{1}{4} = \frac{1}{4} $ $\frac{1}{4} = \frac{1}{4} $ 1	7 1 - vei0
$ \frac{1}{2} = \frac{1}{4} = \frac{1}{4} $ $ \frac{1}{4} \frac{1}{4} = \frac{1}{4} $ $\frac{1}{4} = \frac{1}{4} $ 1	V = 1 - 11 = 1
$V = -1 = 1$ $0 = 2\pi + 2\pi \times (K = 0, +1)$ $2 = 1e^{i(2\pi + 2\pi \times 1)} \times (2\pi + 2\pi \times 1) \times (2\pi \times 1) \times (2\pi$	0 = 180 + 2TK, K= 0, +1
$V = -1 = 1$ $0 = 2\pi + 2\pi \times (K = 0, +1)$ $= 1e^{i(2\pi + 2\pi \times 1)} \times (2\pi + 2\pi \times 1) \times (2\pi \times 1) \times (2$	7-4-10
$\frac{3e^{2} + 1e^{i(2\pi + 2\pi k)/2}}{e^{2} + 1e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$ $\frac{2^{2} - 1^{2} e^{i(2\pi + 2\pi k)/2}}{e^{i(2\pi + 2\pi k)/2}}$	v= \-1\= 1
U 0) = 1e = 1 (Cos TT + US: NTT) = +4	9=2++2+K, K=0,+1
Wed, we let - 1 Eros 2TT + i Sin2TTJ= t	$V \cap V = 1e = 1 Cos + Usin $
	K=1, w2-1e=1 [cos 2TT + isin2TT]=+

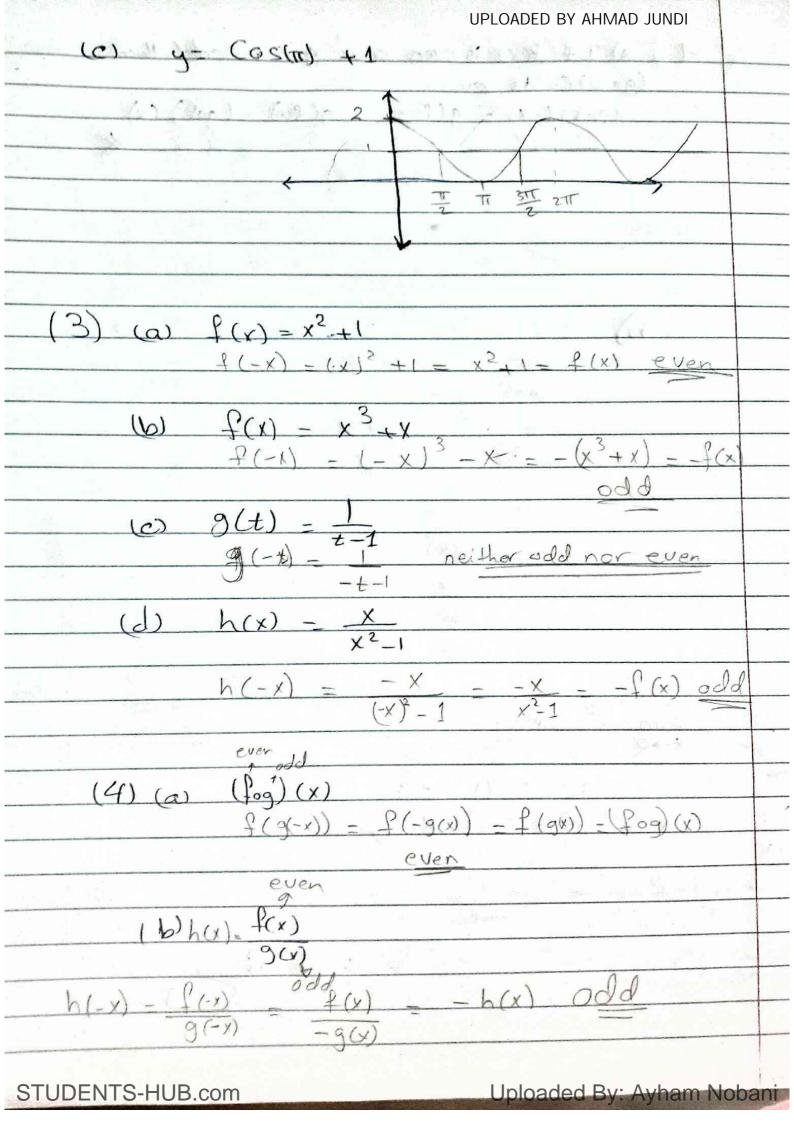
Q20 Find the Sixth roots of 64.
$Z = 64 \Rightarrow \qquad \begin{array}{c} X + iy \Rightarrow 64 + i0 \\ 121 = 64 & \qquad +an\theta = 0 \\ 64 & \qquad 64 \end{array}$
$V = 64$ $9 = 0$ $400 = 0$ $9 = 0$ $0 \Rightarrow 0 + 2\pi K$ $9 = 0$
5/2=164 expi(0+211K)
$\frac{6\sqrt{2} = 2 \exp(i\pi x)}{4 + 10}$ $\frac{3}{4 + 10} \Rightarrow 2 \exp(i\pi x)$ $2 \left[\cos 0 + i\sin 0\right] = 2\left[1 + 0\right] = 2$
$W_{2} \Rightarrow k=1 \Rightarrow 2expiT_{2} \Rightarrow 2\left[\cos T_{2} + i\sin T_{3}\right] = 2\left[\frac{1}{2} + i\sqrt{3}\right] = 1 + i\sqrt{3}$ $W_{3} \Rightarrow k=2 \Rightarrow 2expiT_{2} \Rightarrow 2\left[\cos 2T_{2} + i\sin 2T_{3}\right] - 2\left[-\frac{1}{2} + i\sqrt{3}\right] = -1 + i\sqrt{3}$
$W_{5} \Rightarrow K=3 \Rightarrow 200p \ i \pi \Rightarrow 2 \left[COSTI + i Sin \pi \right] - 2 \left[-1 + i O \right] = -2$ $W_{5} \Rightarrow K=4 \Rightarrow 200p \ i \pi \Rightarrow 2 \left[COS \ 4\pi + i Sin \ 4\pi \right] = 2 \left[-\frac{1}{2} + i \sqrt{3} \right] = -1 - i \sqrt{3}$
We => K=5 => 2exp 1 T/5 +> 2[cos 15TI + i sin 5TI] = 2[1 - iv3] - 1 - iv3



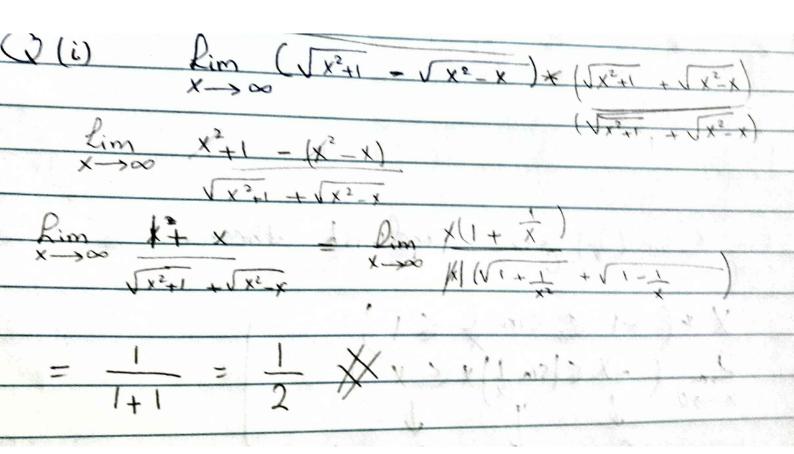
(24) $x^{4}+1-0 = x^{4}-1$
$9 = \pi + 2K\pi$ $(3,0)$
$\frac{y}{x} = em \left(\frac{\pi}{2} + 2 \frac{\pi}{4} \right) $ (-1,0)
$V = \exp\left(\left(\frac{1}{4} + 5 K \mu\right)\right)$
$X = \exp i \left(T + 2K\pi \right) - \exp i \left(T + K\pi \right)$
$W_1 \Rightarrow K-0 \Rightarrow \exp i \frac{\pi}{4} \Rightarrow \left[\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right] = \frac{1}{\sqrt{2}} + i \frac{1}{\sqrt{2}}$
$W_2 \Rightarrow K-1 \Rightarrow expi \left(\frac{TT+TT}{4} \right) \rightarrow \left[\cos 3TT + i \sin 3TT \right] = -\frac{1}{\sqrt{2}} + i \frac{1}{\sqrt{2}}$
311
W3 => K=2 => exp i (5T) => [cos 5TT + i sin 5TT] = -1 - i]
W3 = R=2 = OP ((511) = CO 4 4 V2 V2
(-) [7- : C: 747] !
Wy = K-3 => exp i (7TT) => [cos 7TT + i Sin 7TT] - 1 - i]

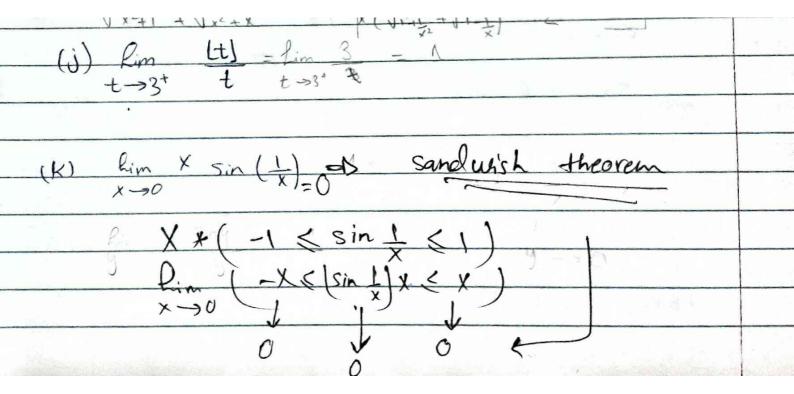
		UPLOADED BY AHMAD JUNDI	
S Tree land			
S	Charler	1 (Function)	
•			
1.4	Exercises:	P 100	
•			1
(1)	(a) $f(x) = 1$	$D = (0, \infty)$	
3	νx	R = (0,00)	
(12)	(b) f(x) = tan	$\prod X \qquad D = \mathbb{R} \setminus X - 1 + n, n = A$,+1,
* +an TTY =	Sintex	R= IR	
COSITX	\$ 0	<u> </u>	1
# XT =	$\frac{1}{8} = D \times \frac{1}{2} + D$		
3	(c) f(x) -1+	IXI D = IR	-
3		$R = (1, \infty)$, ,
•	(d) $f(x) = Sec^2$		4,)
* secx =	COSX	R=[Loo)	
COSI +	0		
	THAT		
9	(6) $\xi(x) = 1$	D = R \ O	
2	χ^2		
2		() = (0)	4
	(f) f(x) = 1	7-1-1	
	(3) 4(x) = 1		
1-x2>			
(- x)	3 V 2		
1	V \1-		
12)	X 21-		
-	Valor 0 = CC	4 (TX+T) D=R/1/x=1+	nyn-C
		3	119
$\Rightarrow CO + (\pi x + \frac{1}{2})$	$\frac{\pi}{3} = \frac{\cos(\pi x + \pi)}{\sin(\pi x + \pi)}$		
3)			
TY + TY = 3			
TY =	. 5		
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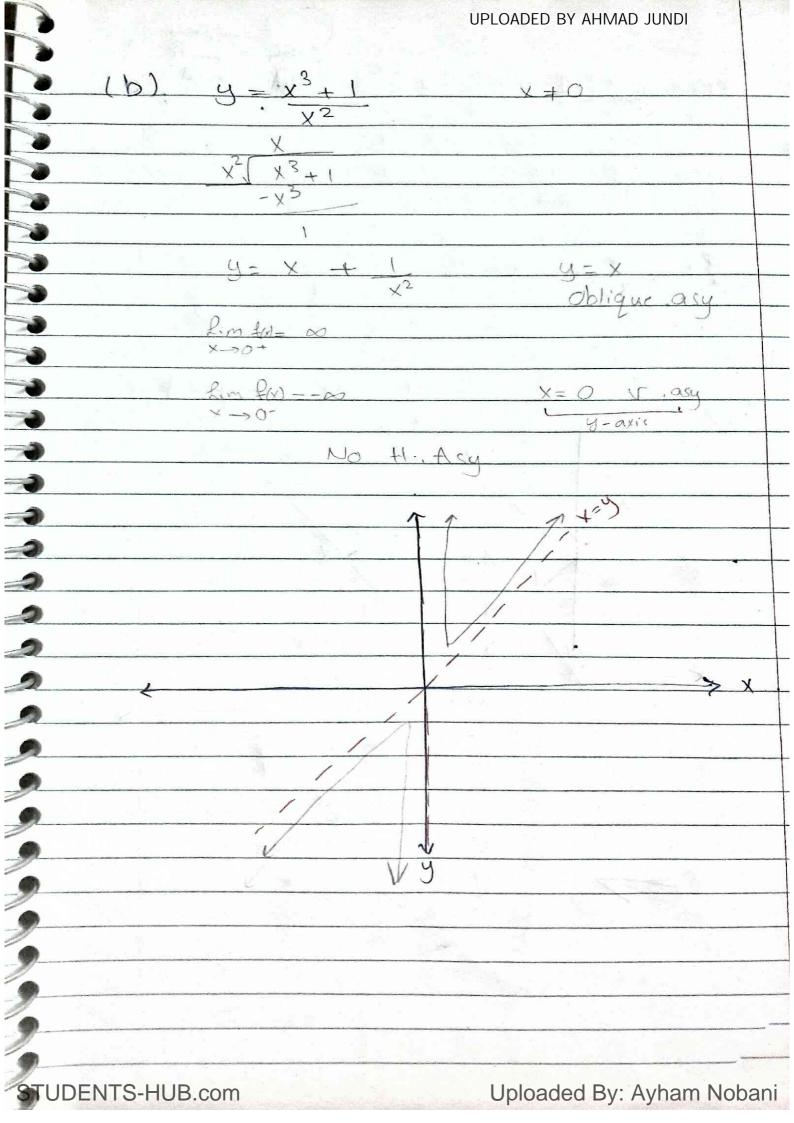


(gof)(x) is even and gux) is odd then.	
1900/1 4/2 0(8/4) 0(8/4)	
f(x) even (gof)(-x) = g(f(-x)) = g(f(-x)) = (gof)(x)	(20) 3
2(x) - 1(-x)	- 1/
2(x) odd) = (-fog) (x)	
f(x) = f(x)x	
	- 1
b) If for even and g(x) odd	
then the is odd.	-0.0
9(x)	
f(x) even -> f(x) - f(-x)	
$g(x)$ odd $\rightarrow g(x) = -g(-x)$	
R(x) = 2(x)	la la
9(x)	I I
$R(-x) - f(x) \rightarrow even - f(x) - P(x)$	
$9(-x) \rightarrow odd - 9(x)$	



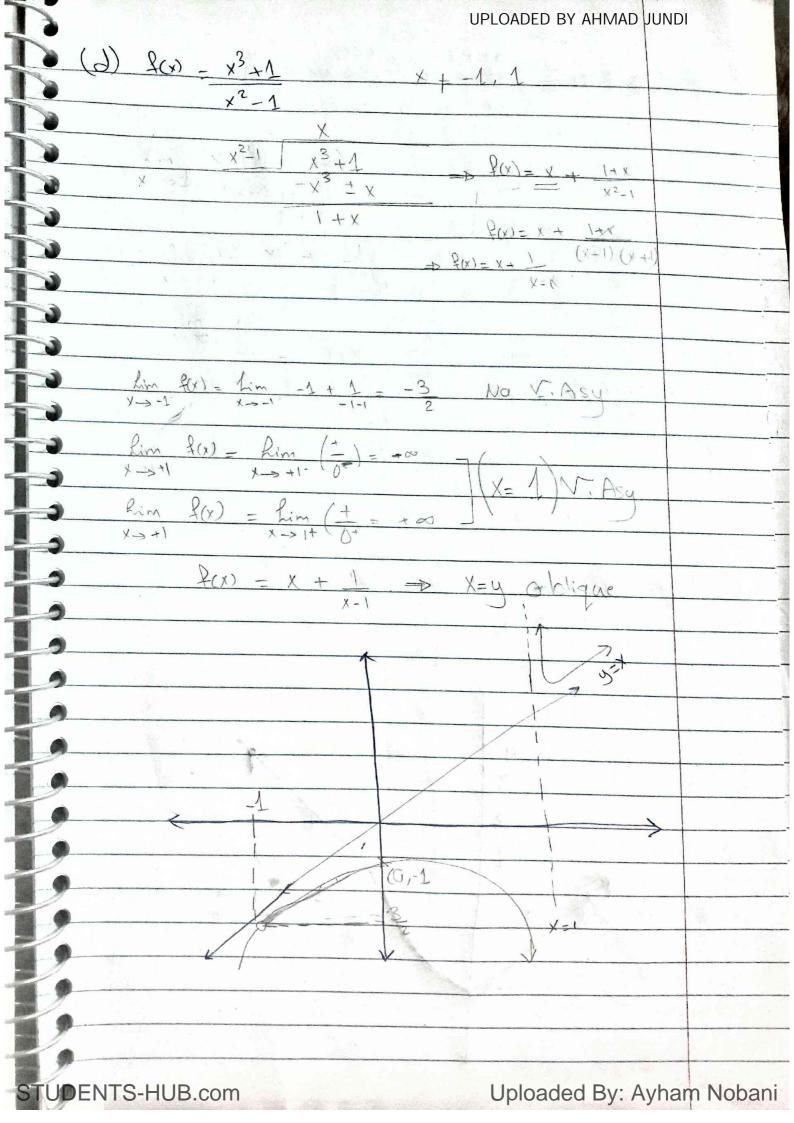


Q2 find the asymptotes of the following Euretion Then Sketch their graphs	15 3
	6
(0) ((1)	6
$(a) f(x) = x+1 \\ x-1 x \neq 1$	6
$\lim_{x \to \infty} f(x) = (+) + \infty$	6
X-> 1*	
$\lim_{x \to \infty} f(x) = (\pm) = -\infty$	
x -31- (0-)	-
Lim f(x)= 1 y=1 H. Asy	4
1 × 1 × 1	6
$0 = \frac{x+1}{x-1} \Rightarrow x+1=0$	
x=-1	6
(-1,0)	
X	
v(0,-1)	
y = 1	

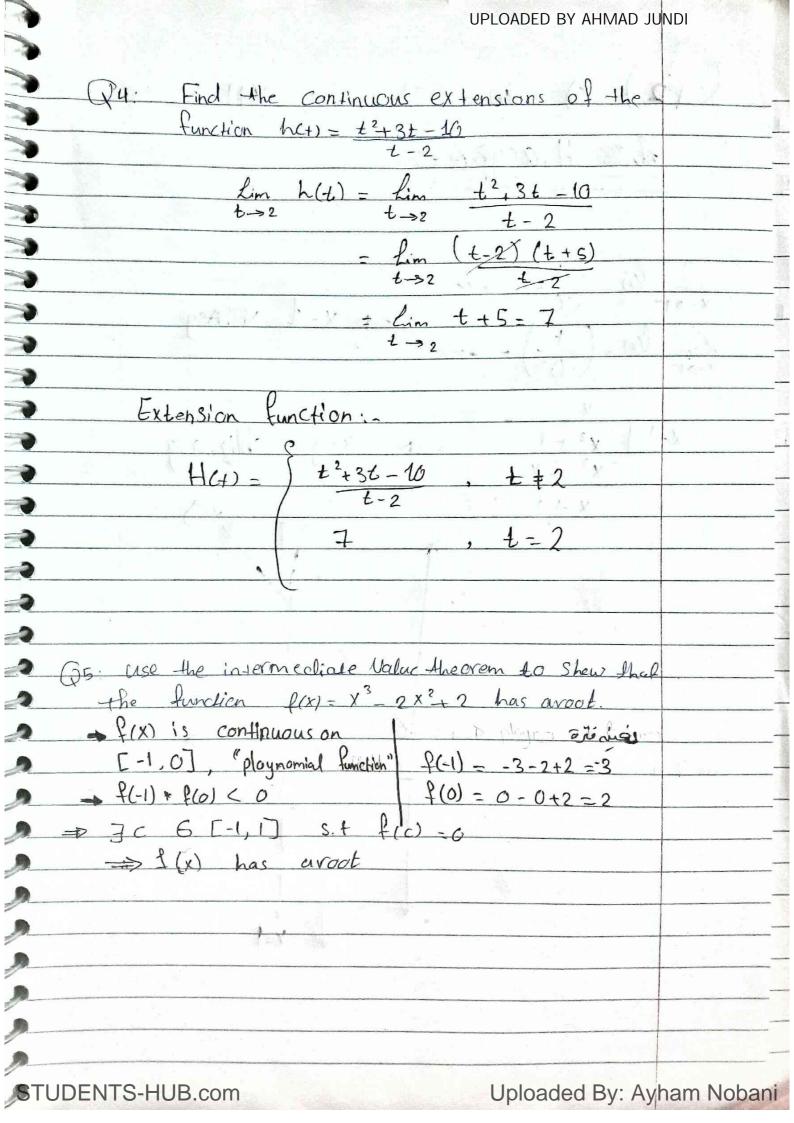


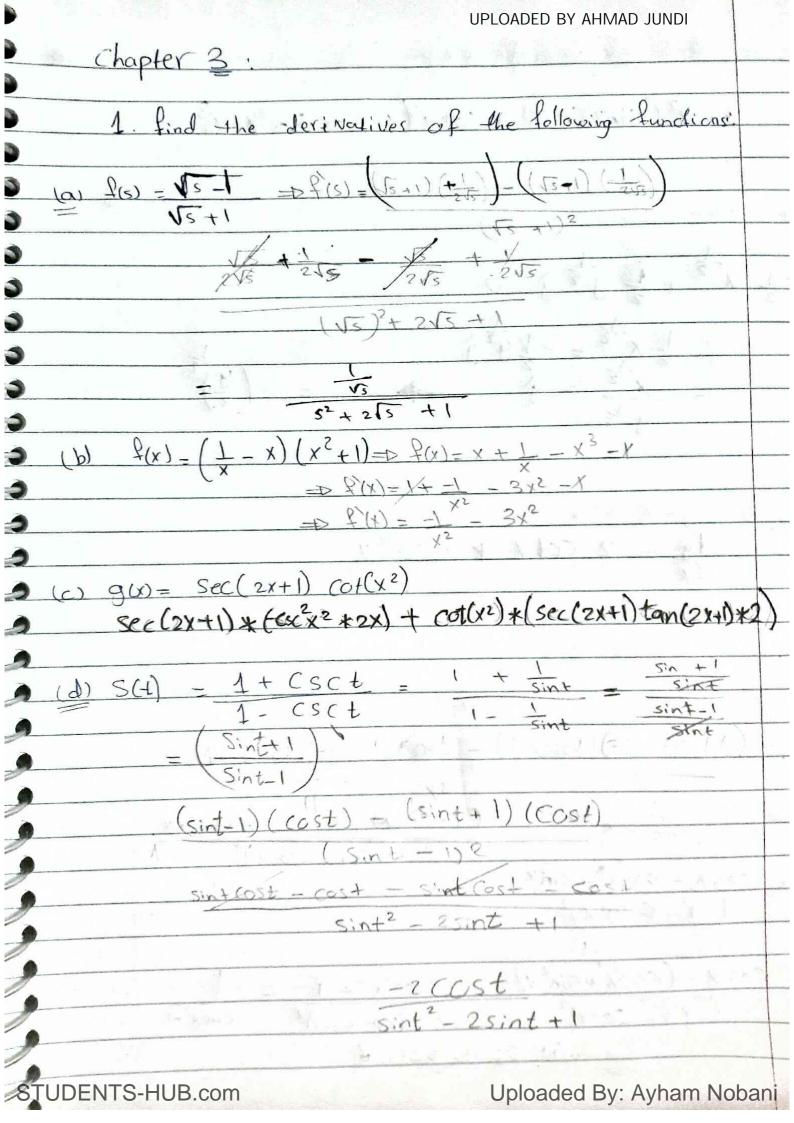
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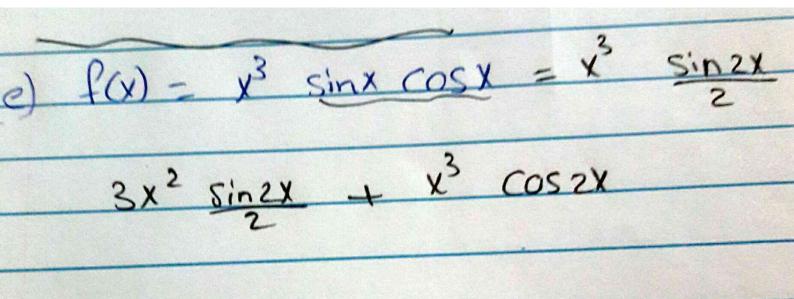
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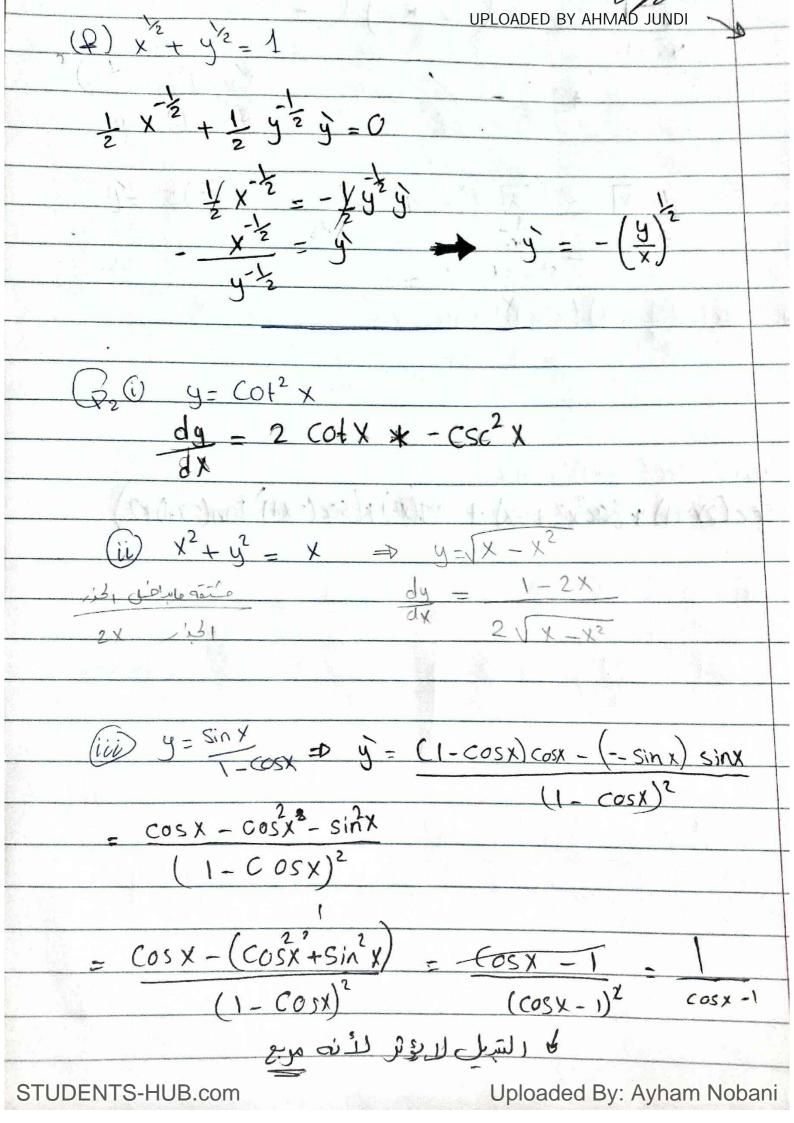


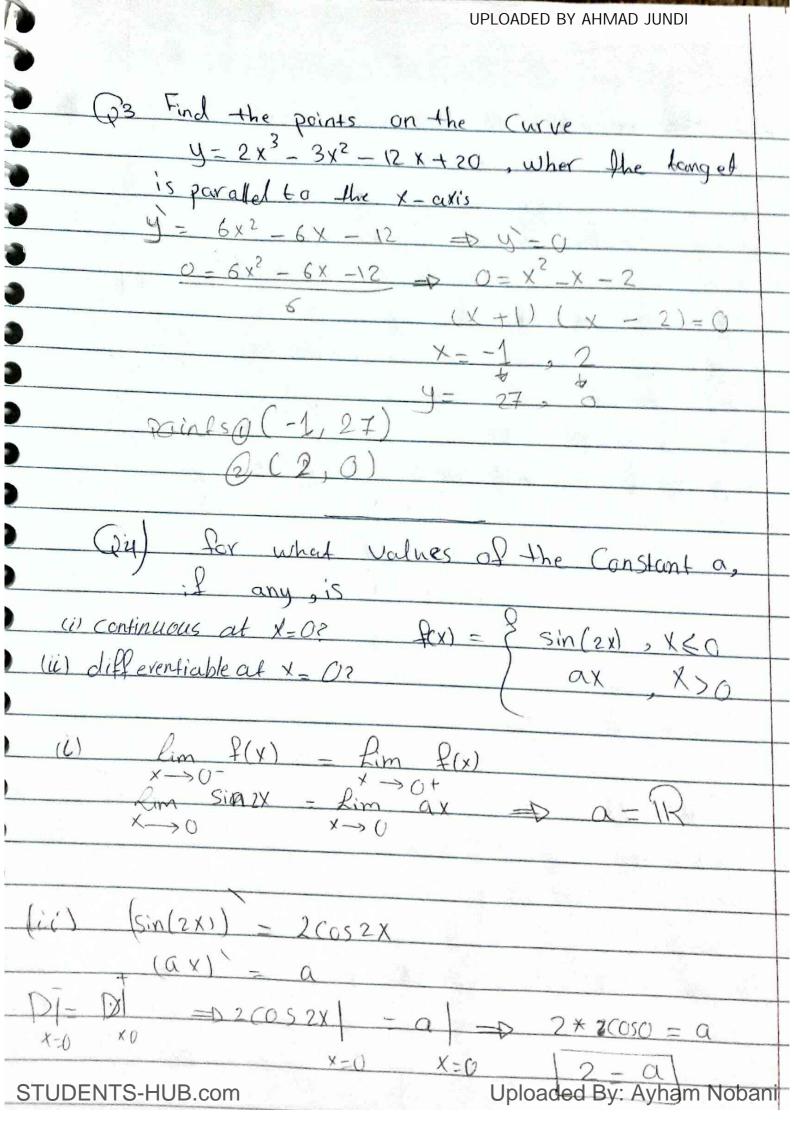
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(35) Find the normals to the curve xy+2x-y=0 that are parallel to the Line 2x+y=0 1 the normals // 2xy=0 Assume tha 2X+9=0 m(normals) = m (-2xzy) urve. m(no(mals) = -22 m(normals) + y (curve) -- 1 -2 * y' = -1 $|3| xy + 2x - y = 0 \rightarrow y = -2x \rightarrow y = (x-1) *2 - 2x$ $|x-1|^2$ y = +2 x = 1 $\frac{1}{2} = \frac{+2}{(x-1)^2}$ $\Rightarrow +4 = x^2 - 2x +1$ $\Rightarrow x^2 - 2x + 3 = 0 \Rightarrow (x + 1)(x - 3) = 0$ x = -1, 3 y = +1, -3two normals -> (x-3) @ y+1=-2(x+1)

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(P6: (a) f(x) = tan x, x = T/4 UPLOADED BY AHMAD JUNDI a= [] f(1) = tan 1 - 1 / f(1) - Sec 1 - 2 $L(x) = f(a) + f'(a)(x-\pi)$ L(x) = 1 + 2(x - T) = 1 + 2x - T(b) $g(x) = \frac{1}{x}$, x=1a=[1] f(i)=[1] f(i)=[-1]L(x) = 1 = 1 (x-1)1 - X + $(c) h(x) = x^2$, x = 0 $a=[0]/h(0)=[0]/h(0)=(x^2+1)2x-(x^2+2x)$ L'(0)=0 L(X) = O + O(X + O)Uploaded By: Ayham Nobani

(d)
$$f(x) = 1 + \cos\theta$$
, $\theta = T$
 $a = TI / f(T_3) = \frac{3}{2} / f(T_3) = -\sqrt{3}$
 $1(x) = \frac{3}{2} + -\sqrt{3}(x - T_3)$
 $= \frac{3}{2} - \sqrt{3}x + T\sqrt{3}$