

## Question 1

Correct

Mark 1 out of 1

🚩 Flag question

The general solution of the differential equation  $y'' - 6y' + 9y = 0$  is

Select one:

- This choice was deleted after  the attempt was started.

The correct answer is:

$$y(t) = c_1 e^{3t} + c_2 t e^{3t}$$

## Question 2

Correct

Mark 1 out of 1

🚩 Flag question

The solution of the initial value problem  $y'' + 4y = 0$ ,  $y(0) = 2$ ,  $y'(0) = 1$  is

Select one:

- This choice was deleted after the attempt was started. ❌

The correct answer is:

$$y(t) = 2 \cos(2t) + \frac{1}{2} \sin(2t)$$

### Question 3

Correct

Mark 1 out of 1

🚩 Flag question

The value of  $\alpha$  for which the solution of the initial value problem

$$y'' + y' - 2y = 0, y(0) = \alpha, \\ y'(0) = 3 \text{ approaches } 0 \text{ as } t \rightarrow \infty$$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $-\frac{3}{2}$

### Question 4

Correct

Mark 1 out of 1

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The function

$y(t) = e^{2t} \cos(t) + e^{2t} \sin t$  is a solution of the differential equation

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$y'' - 4y' + 5y = 0$$

### Question 5

Correct

Mark 1 out of 1

🚩 Flag question

The general solution of the differential equation  $y'' - 2y' + 3y = 0$  is

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$y(t) = c_1 e^t \cos(\sqrt{2}t) + c_2 e^t \sin(\sqrt{2}t)$$

## Question 6

Incorrect

Mark 0 out of 1

🚩 Flag question

Given that  $W(y_1, y_2)(t) = t^4$ ,  
 $y_1(t) = t^2$ , then a possible function  
of  $y_2(t)$  is

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $t^3 + 2t^2$

## Question 7

Incorrect

Mark 0 out of 1

🚩 Flag question

The longest interval in which a unique solution of the initial value problem  $t(\ln t)y'' + ty' + y = \csc t$ ,  $y(2) = 1$ ,  $y'(2) = 1$  is certain to exist is

Select one:

- This choice was deleted after the attempt was started. ❌

The correct answer is:  $(1, \pi)$

### Question 8

Correct

Mark 1 out of 1

🚩 Flag question

The general solution of the differential equation  $2y'' + y' - y = 0$  is

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$y(t) = c_1 e^{-t} + c_2 e^{t/2}$$

## Question 9

Correct

Mark 1 out of 1

▼ [Flag question](#)

The function  $y_1(x) = x$  is a solution of the differential equation

$$(1 - x^2)y'' + 2xy' - 2y = 0,$$

$x \in (-1, 1)$ . Using the method of reduction of order, a second solution  $y_2(x)$  is

Select one:

- This choice was deleted after  the attempt was started.

The correct answer is:  $1 + x^2$

## Question 10

Incorrect

Mark 0 out of 1

🚩 Flag question

The Wronskian of any solutions  $y_1$  and  $y_2$  of the differential equation  $((x + 1)y')' + 2y = 0, x > -1$  is

Select one:

- This choice was deleted after  the attempt was started.

The correct answer is:  $C(x + 1)^{-1}$

## Question 1

Incorrect

Mark 0 out of 1

🚩 Flag question

Using the method of undetermined coefficients, let  $Y(t)$  be a particular solution of the differential equation  $y^{(4)} - y^{(3)} = -24t$ , then  $Y(-1) =$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $-3$

## Question 2

Correct

Mark 1 out of 1

🚩 Flag question

The general solution of the differential equation

$$y^{(4)} + 2y^{(3)} + 4y'' - 2y' - 5y = 0$$

is

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$y(y) = c_1 e^t + c_2 e^{-t} + c_3 e^{-t} \cos(2t) + c_4 e^{-t} \sin(2t)$$

### Question 3

Incorrect

Mark 0 out of 1

🚩 Flag question

The general form of a particular solution of the differential equation  $y^{(4)} + 2y'' + y = t \cos t$  is

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$Y(t) = (At^3 + Bt^2) \cos t + (Ct^3 + Dt^2) \sin t$$

#### Question 4

Correct

Mark 1 out of 1

🚩 Flag question

A particular solution of the differential equation  $y'' - 2y' + y = \frac{e^t}{t}$ ,  $t > 0$ , has the form

$Y(t) = v_1(t)e^t + v_2(t)te^t$  where  $v_2(t) =$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $\ln t$

## Question 5

Correct

Mark 1 out of 1

🚩 Flag question

Using the method of undetermined coefficients, let  $Y(t)$  be a particular solution of the differential equation  $y''' - y = e^t$ , then  $Y(2) =$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $\frac{2}{3}e^2$

## Question 6

Correct

Mark 1 out of 1

🚩 Flag question

The general form of a particular solution of the differential equation  $y^{(4)} + 2y^{(3)} + y'' = 1 + t \sinh t$

Select one:

- This choice was deleted after ✘ the attempt was started.

The correct answer is:

$$Y(t) = At^2 + (Bt + C)e^t + (Dt^3 + Et^2)e^t$$

## Question 7

Incorrect

Mark 0 out of 1

🚩 Flag question

Using the method of undetermined coefficients, let  $Y(t)$  be a particular solution of the differential equation  $y'' + y' = t^2$ , then  $Y(1) =$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:  $\frac{4}{3}$

## Question 8

Incorrect

Mark 0 out of 1

🚩 Flag question

The general form of a particular solution of the differential equation

$$y'' - y' = te^t \text{ is}$$

Select one:

- This choice was deleted after ✘ the attempt was started.

The correct answer is:

$$Y(t) = (At^2 + Bt)e^t$$

### Question 9

Correct

Mark 1 out of 1

🚩 Flag question

A particular solution of the differential equation  $y'' + y = \sec^2 t$  has the form

$$Y(t) = u_1(t) \cos t + u_2(t) \sin t$$

where  $u_2(t) =$

Select one:

- This choice was deleted after the attempt was started.

The correct answer is:

$$\ln |\sec t + \tan t|$$

## Question 10

Correct

Mark 1 out of 1

🚩 Flag question

If  $Y_1 = 1 + 2t$ ,  $Y_2(t) = 1 + t + e^t$  are solutions of a second order nonhomogeneous differential equation then one of the following is a solution of the corresponding homogeneous equation

Select one:

- This choice was deleted after the attempt was started. ❌

The correct answer is:  $t - e^t$

## Question 1

Correct

Marked out of 2.00

🚩 Flag question

The **inverse Laplace transform**

$\mathcal{L}^{-1}\left\{\frac{s}{s^2+6s+10}\right\}$  equals

Select one:

- $e^{2t}(\cos 2t + \sin 2t)$
- $e^{3t}(\cos t + 3 \sin t)$
- $e^{-2t}(\cos 2t - \sin 2t)$
- $e^{-3t}(\cos t - 3 \sin t)$  ✓
- $e^{3t}(\cos t + 3 \sin t)$

The correct answer is:

$e^{-3t}(\cos t - 3 \sin t)$



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The correct answer is:

$$e^{-3t} (\cos t - 3 \sin t)$$

### Question 2

Correct

Marked out of 2.00

Flag question

Given the initial value problem:

$$x^2 y'' + 3xy' - 3y = 0, \quad x > 0 \quad y(1) = 0, \quad y'(1)$$

Then  $y(-1) =$

Select one:

- $\frac{15}{8}$   
 0  
 2  
  $-\frac{15}{8}$   
 -2

Handwritten note:

$$y'(1) = 4$$



The correct answer is: 0



### Question 3

Correct

### Question 3

Correct

Marked out of 2.00

Flag question

The Laplace transform of the solution of the IVP:

$$f''(t) - f'(t) + f(t) = 1, \quad f(0) = f'(0) = 0$$

satisfies:

Select one:

- $F(s) = \frac{1}{s(s^2+s-1)}$
- $F(s) = \frac{1}{s(s^2-s+1)}$  ✓
- $F(s) = \frac{1}{s(s^2-s-1)}$
- $F(s) = \frac{1}{s(s^2+s+1)}$
- $F(s) = \frac{1}{s^2(s^2-s-1)}$

The correct answer is:

$$F(s) = \frac{1}{s(s^2-s+1)}$$

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Use the table of Laplace transforms or the formula:

$$\mathcal{L}\{t^n f(t)\} = (-1)^n \frac{d^n}{ds^n} (\mathcal{L}\{f(t)\})$$

to determine the following expressions.

$$\mathcal{L}\{t \sin 2t\}$$

- $\frac{2s}{(s^2+1)^2}$   
  $\frac{s^2-9}{(s^2+9)^2}$   
  $\frac{s^2-4}{(s^2+4)^2}$   
  $\frac{4s}{(s^2+4)^2}$  ✓  
  $\frac{s^2-1}{(s^2+1)^2}$   
  $\frac{6s}{(s^2+9)^2}$

The correct answer is:  $\frac{4s}{(s^2+4)^2}$

$$\mathcal{L}\{t^2 \sin 2t\}$$

- $\frac{2s(s^2-27)}{(s^2+9)^3}$   
  $\frac{2(3s^2-1)}{(s^2+1)^3}$   
  $\frac{4(3s^2-4)}{(s^2+4)^3}$  ✓  
  $\frac{2s(s^2-12)}{(s^2+4)^3}$   
  $\frac{2s(s^2-3)}{(s^2+1)^3}$   
  $\frac{18(s^2-3)}{(s^2+9)^3}$



Use the table of Laplace transforms or the formula:

$$\mathcal{L}^{-1}\left\{\frac{d^n}{ds^n}(F(s))\right\} = (-t)^n \mathcal{L}^{-1}\{F(s)\}$$

to determine the following expressions.

$$\mathcal{L}^{-1}\{-4(s^2 - 4)^{-1}\}$$

- $-2 \sinh(t)$
- $-2 e^t \sinh(4 t)$
- $2 e^{-t} \sinh(4 t)$
- $-2 e^{4t} \sinh(t)$
- $-2 \sinh(2 t)$  ✓
- $2 e^{-4t} \sinh(t)$

The correct answer is:  
 $-2 \sinh(2 t)$

$$\mathcal{L}^{-1}\left\{\ln\left(\frac{s+2}{s-2}\right)\right\}$$

- $\frac{2e^{4t} \sinh(t)}{t}$
- $\frac{2 \sinh(2 t)}{t}$  ✓
- $\frac{2 \sinh(t)}{t}$
- $\frac{2e^{-4t} \sinh(t)}{t}$
- $\frac{2e^{-t} \sinh(4 t)}{t}$
- $\frac{2e^t \sinh(4 t)}{t}$

The correct answer is:  $\frac{2 \sinh(2 t)}{t}$

## Question 1

Correct

Marked out of 1.50

🚩 Flag question

The order of the differential equation

$$y^6 y'' + y^3 y' = \sin t$$

Select one:

- 5
- 4
- 2 ✓
- 3
- 8

The correct answer is: 2

## Question 2

Incorrect

Marked out of 2.00

Flag question

An **integrating factor** for the differential equation

$$-2y' - \frac{1}{x}y = e^x, \quad x > 0$$

Select one:

$x^{-1/2}$  ✘

$x^{1/2}$

$-\frac{1}{x}$

$\frac{1}{x}$

$x^{-2}$

The correct answer is:  $x^{1/2}$

### Question 3

Incorrect

Marked out of 2.00

▼ [Flag question](#)

The values of  $m$  for which  $y = x^m$  is a solution of  $x^2y'' - 7xy' + 12y = 0$  are

Select one:

- 3 and  $-4$  ✘
- $-2$  and  $-6$
- 3 and 4
- $-3$  and 4
- 2 and 6

The correct answer is: 2 and 6

### Question 4

Incorrect

Marked out of 3.00

🚩 Flag question

The solution of the I.V.P.

$$xy \frac{dy}{dx} = x^2 + y^2, y(1) = 1 \text{ is}$$

Select one:

- $2 \ln |x| = \left(\frac{y}{x}\right)^2 - 1$
- $\ln |x| = \left(\frac{y}{x}\right)^2 - 1$
- $2 \ln |x| = \left(\frac{y}{x}\right)^2 - 4$
- $2 \ln |x| = \left(\frac{y}{x}\right)^2 + 4$
- $-2 \ln |x| = \left(\frac{y}{x}\right)^2 - 1$  ✘

The correct answer is:

$$2 \ln |x| = \left(\frac{y}{x}\right)^2 - 1$$

Question **5**

Correct

Marked out of 1.50

🚩 Flag question

The differential equation

$$t^2 y' + y^2 = ty$$

Select one:

- nonlinear separable equation
- first order linear homogeneous equation
- first order nonlinear homogeneous equation ✔
- first order linear equation
- linear separable equation

The correct answer is: first order nonlinear homogeneous equation

## Question 6

Correct

Marked out of 2.00

🚩 Flag question

If all solutions of the differential equation  $y' = ay + b$  converge to  $-2$  then possible values for  $a$  and  $b$  are

Select one:

- $a = -1, b = -2$  ✓
- $a = -1, b = 2$
- $a = 1, b = -2$
- $a = 1, b = 2$

The correct answer is:

$$a = -1, b = -2$$

An **integrating factor** that makes the differential equation

$$2ye^x dx + (y + e^x)dy = 0 \text{ exact is}$$

Select one:

- $\sqrt{y}$
- $e^y$
- $e^x$
- $\frac{1}{\sqrt{y}}$  ✓

The correct answer is:  $\frac{1}{\sqrt{y}}$

## Question 2

Incorrect

Marked out of 2.00

▼ Flag question

According to the **Existence and Uniqueness Theorem**, the IVP

$\frac{dy}{dx} = \frac{\sqrt{y^2-4}}{x}$ ,  $y(\alpha) = \beta$  has a unique solution if

Select one:

- $\alpha = 0, \beta = 0$
- $\alpha = 1, \beta = -1$  ✘
- $\alpha = 0, \beta = 1$
- $\alpha = 1, \beta = 3$

The correct answer is:  $\alpha = 1, \beta = 3$

### Question 3

Incorrect

Marked out of 2.00

🚩 Flag question

Using the substitution  $v = y^{-1}$ , the differential equation  $y' - y = x^2 y^2$ ,  $x > 0$  can be written as

Select one:

- $v' - \frac{1}{x}v = -x$
- $v' - v = -x^2$  ✖
- $v' + \frac{1}{x}v = -x$
- $v' + v = -x^2$

The correct answer is:  $v' + v = -x^2$



### Question 4

Correct

Marked out of 2.00

Flag question

If the differential equation

$$\left(x^2y + \frac{y}{x} + \sec y + y\right)dx + \left(\frac{1}{3}x^3 + \ln x + xS(y)\right)dy$$

is exact, then  $S(y) =$

Select one:

- $1 + \sec y$
- $\tan y$
- $\sec y \tan y$  ✓
- $\sec y$

$$\left(x S(y) + x\right) dy$$

$$= 0$$

The correct answer is:  $\sec y \tan y$

## Question 5

Correct

Marked out of 2.00

▼ [Flag question](#)

The **largest interval** in which a

solution of the IVP

$$y' + (\ln t)y = \tan t, \quad y\left(\frac{\pi}{4}\right) = 1 \text{ is}$$

certain to exist is

Select one:

- $(1, \infty)$
- $(0, 1)$
- $(0, \frac{\pi}{2})$  ✓
- $(0, \pi)$

The correct answer is:  $(0, \frac{\pi}{2})$

## Question 6

Correct

Marked out of 2.00

🚩 Flag question

A small metal bar is dropped into a large container of boiling water (that is the temperature of the medium around the metal bar  $100^{\circ}C$ ). Initially the temperature of the bar is measured to be  $20^{\circ}C$ . After  $t = 1$  second, the temperature of the bar increases to  $60^{\circ}C$ . The temperature of the bar at  $t = 4$  equals

Select one:

- $95^{\circ}C$  ✓
- $110^{\circ}C$
- $105^{\circ}C$
- $90^{\circ}C$

The correct answer is:  $95^{\circ}C$

## Question 1

Correct

Marked out of 2.00

🚩 Flag question

The solution of the IVP

$$y'' - 2ky' + k^2y = 0, \quad k > 0, \quad y(0) = 1, \quad y'(0)$$

is

Select one:

- $y = (1 - kt)e^{kt}$
- $y = (1 + t)e^{kt}$
- $y = te^{kt} + 1$
- $y = (1 - kt)e^{kt}$  ✓

$y'(0) = 0$

The correct answers are:

$$y = (1 - kt)e^{kt}$$
$$, y = (1 - kt)e^{kt}$$

## Question 2

Correct

Marked out of 2.00

🚩 Flag question

Consider the IVP  $y' = t^2 - y$ ,  
 $y(0) = 0$ . Using **Picard's method**

Select one:

- $\phi_2(t) = \frac{t^3}{3} - \frac{t^4}{4!}$
- $\phi_2(t) = \frac{t^3}{3!} - \frac{t^4}{4!}$
- $\phi_2(t) = \frac{t^3}{3} - \frac{t^4}{12}$  ✓
- $\phi_2(t) = \frac{t^3}{3!} - \frac{t^4}{12}$

The correct answer is:

$$\phi_2(t) = \frac{t^3}{3} - \frac{t^4}{12}$$

### Question 3

Correct

Marked out of 2.00

🚩 Flag question

The general solution of the differential equation  $y'' = (y')^2$  is

Select one:

- $y(t) = -\ln |t + c_1| + c_2$  ✓
- $y(t) = c_1 e^t + c_2 e^{-t}$
- $y(t) = \ln |t + c_1| + c_2$
- $y(t) = c_1 e^t + c_2$

The correct answer is:

$$y(t) = -\ln |t + c_1| + c_2$$

#### Question 4

Correct

Marked out of 2.00

🚩 Flag question

A second order linear homogeneous differential equation with constant coefficients has  $r_1 = -1 + 2i$ ,  $r_2 = -1 - 2i$  as roots of its auxiliary equation. Then this differential equation is

Select one:

- $y'' + 3y = 0$
- $y'' - 2y' + 5y = 0$
- $y'' - 3y' + 4y = 0$
- $y'' + 2y' + 5y = 0$  ✓

The correct answer is:

$$y'' + 2y' + 5y = 0$$

## Question 5

Correct

Marked out of 2.00

🚩 Flag question

The solution of the  
IVP  $y'' + y = 0$ ,  $y(0) = 0$ ,  $y'(0) = 1$   
is

Select one:

- $y(t) = \sin t$  ✓
- $y(t) = \sinh t$
- $y(t) = e^t - 1$
- $y(t) = \cosh t$

The correct answer is:  $y(t) = \sin t$

## Question 6

Correct

Marked out of 2.00

🚩 Flag question

Given that  $y_1(t) = e^t$  is a solution of the differential equation  $y'' - y' = 0$ . If  $y(t) = u(t)e^t$  is a second solution, then the function  $u(t)$  satisfies the differential equation:

Select one:

- $u'' + u = 0$
- $u'' + 2u' = 0$
- $u'' + 2u = 0$
- $u'' + u' = 0$  ✓

The correct answer is:  $u'' + u' = 0$