

Computer Science Department – Engineering and Information Technology Faculty
Comp233, Discrete Mathematics, Dec 5, 2019
Winter 2019

Winter 2019	
Student Name: Student ID:	
Question 1 (26%):  1) The inverse of function $f(x) = x^3 + 2$ is  a) $f^{-1}(y) = (y-2)^{1/2}$ b) $f^{-1}(y) = (y-2)^{1/3}$ c) $f^{-1}(y) = (y-1)^{1/3}$ d) $f^{-1}(y) = (y-1)$	
2) The function $f(x) = x^3$ is bijection from R to R. Is it True or False?  (a) True (b) False	
3) Which of the following function $f: ZXZ \rightarrow Z$ is not onto? a) $f(a,b) = a + b$ b) $f(a,b) = a$ c) $f(a,b) =  b $ d) $f(a,b) = a - b$	
<ul> <li>4) A function is said to be if and only if f(a) = f(b) implies that a = b for all a and b in the domain of f.</li> <li>a) One - to - many</li> <li>b) One - to - one</li> <li>c) Many - to - many</li> <li>d) Many - to - one</li> </ul>	
5) 4. If the number of binary subsets of a set are 4 then the number of elements in that sets are  a) 1  b) 2  c) 3  4) 4	
<ul> <li>6) Let the set be A = {a, b, c, {a,b}} then which of the following is false</li> <li>a) {a, b} ∈ A</li> <li>b) a ∈ A</li> <li>c) {a} ∈ A</li> <li>d) b, c ∈ A</li> </ul>	

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7) The set containing all the collection of subsets is known as

 a) Subset

      bDPower set
       c) Union set
       d) None of the mentioned
   8) If set A and B have 3 and 4 elements respectively then the number of subsets of set (A X B) is
       a) 1024
       b) 2048
       c) 512
      d) 4096

 If A ⊆ B then A X C ⊆ B X C the given statement is

     (a)True
       b) False
   10) Let A = \{1, 2, 3\} and B = \{x, y, z\}. Consider the relations R = \{(1,x),(2,x)\}
     and S = \{(1,x),(1,y),(2,z),(3,y)\}. The S is
   a) One - to - One
   b) Onto

 c) Correspondence

   d) Not function
       Bonus (I am not obliged to answer the question)
  11) Evaluate the performance of comp233 instructor at this semester?
                                       c)70 - 79% d) 60 - 69% e) Under 60%
   a) 90 - 100%
                      b) 80 - 89 %
  12) What grade you expect at this course?
                       b)80 - 89\%
                                                        d) 60 - 69% e) Under 60%
       a) 90 - 99\%
                                         c)70 - 79\%
  13) How do you evaluate yourself in class attendance?
                                                     d) never
                     b) Noramal
                                     c)rearly
       a)Always
Question 2 (20%):
      I) Suppose A = \{1, 2\} and B = \{2, 3\}. Find each of (\mathcal{P}: is power set)
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the following: (2%) a)  $\mathcal{P}(A)$ 

(3%) b) P (A ∩B)

(5%) c) P (A∪B)



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- 7) The set containing all the collection of subsets is known as
  - a) Subset
  - b Power set
    - c) Union set
    - d) None of the mentioned
- 8) If set A and B have 2 and 5 elements respectively then the number of subsets of set (A X B) is
  - a)1024
    - b) 2048
    - c) 512
    - d) 4096
- 9) If  $A \subseteq B$  then  $A \times C \subseteq B \times C$  the given statement is
  - (a)True
    - b) False
- 10) Let  $A = \{1, 2, 3\}$  and  $B = \{x, y, z\}$ . Consider the relations  $R = \{(1,x),(2,x)\}$  and  $S = \{(1,x),(1,y),(2,z),(3,y)\}$ . The S is
- a) Sirjective
- b) Bijective
- c) Correspondence
- d) Not function

## Bonus (I am not obliged to answer the question)

- 11) Evaluate the performance of comp233 instructor at this semester?
- a) 90 100%
- b) 80 89%
- c)70 79%
- d) 60 69% e) Under 60%
- 12) What grade you expect at this course?
  - a) 90 99%
- b) 80 89%
- c)70 79%
- d) 60 69% e) Under 60%
- 13) How do you evaluate yourself in class attendance?
  - a)Always
- b) Noramal
- c)rearly
- d) never

## Question 2 (20%):

I) Suppose A = {1, 2} and B = {2, 3}. Find each of (P: is power set) the following:

(2%) a) 
$$\mathcal{P}(A) = \{ \phi, \{ i \}, \{ 2 \}, \{ 1, 2 \} \}$$

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II) Let S_i = \left\{ x \in \mathbb{R} \mid 1 < x < 1 + \frac{1}{i} \right\} = (1, 1 + \frac{1}{i}), for each positive integer find:
 a. \bigcup_{i=0}^{4} S_i = ? S_i \cup S_2 \cup S_3 \cup S_4 = (1,2) \cup (1,3/2) \cup (1,4/3) \cup (1,5/4) = (1,2)
 b. \bigcap_{i=2}^{4} S_{i} = ? S_{1} \cap S_{2} \cap S_{3} \cap S_{4} = (1,2) \cap (1,3/2) \cap (1,4/3) \cap (1,5/4)
               = (1,5/4)
 c. \bigcup_{i=1}^{n} S_i = ? S_1 \cup S_2 \cup S_3 \cup S_4 - -- \cup S_n = (1, 2) \cup (1, 3/2) \cup (1, 4/3)
U(1,5/4) -- - U(1,1+1/n)
U(1,5/4) -- - U(1,1+1/n)
Question 3 (30%, 15% each):
U(1,5/4) -- - U(1,1+1/n)
U(1,5/4) -- - U(1,1+1/n)
      Define H: \mathbf{R} \times \mathbf{R} \to \mathbf{R} \times \mathbf{R} as follows:
      H(x,y) = (x+1,2-y) for every (x,y) \in R \times R.
      a. Is H one – to – one? Prove or give a counterexample.
         Yes. His One-te-One function Since.
       Let (x1.54), (x2,152) ERXR Such that
if H(x_1, y_1) = H(x_2, y_2)
we want to show that x_1 = x_2, y_1 = y_2
  Hence, H(x,y,) = H(xyy)
          S (x+1, 2-y,) = (x,+1,2-y2)
            : X,+1 = X2+1 => : [X1=X2]
           & 2-y=2-y2 => (4=32)
     So, H function is One-to One X
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b. Is Honto? Prove or give a counterexample.

Yes, H is Onto function

Let  $(x,y) \in \mathbb{R} \times \mathbb{R}$ . We need  $(r,s) \in \mathbb{R} \times \mathbb{R}$ Such that H(r,s) = (x,y), Hence from

Lefinition, Let us Solve H(r,s) = (x,y) (r+1, 2-5) = (x,y) = (x,y)  $(r+1, 2-5) = (x,y) = (x+1, 2-y) \in \mathbb{R} \times \mathbb{R}$ Since; if we substitute (r,s) = (x-1, 2-y) in H function

we get H(r,s) = (x,y) Hence H is Onto  $\mathbb{R}$ Question 4 (30%, 15% each):

a) Construct an algebraic proof for the given statement.

For all sets A, B, and C,  $(A \cup B) - (C - A) = A \cup (B - C)$ . Cite a property from every step?

b) Use an element argument to prove this statement Assume that all sets are subsets of a universal set U. Justify you each step

For all sets A, B, and C  $(A-B) \cup (C-B) = (A \cup C) - B$ 1) Let x (plac). Such that XE (A-B) U (C-B) We want to show that  $x \in (AUC)-B)$  is true. by definition of subset  $x \in (A-B)$  U(C-B) and by differentian of Union. XEA-B Or XEC-B For: XE A-B (case 1) by differition of difference XEA and x&B By the diffitien of union and using XEA: XEAUC By diffirition of difference, using x ∈ AUC and X & B 30, X∈(AUC)-B Second cure (x ∈ C-B): by difference XEC and X & B. by difinition of anion and using XEC, SO XE AUC. by diffition of difference Using XEAUC and X&B So, [XE(AUG-B] 2) Let  $x \in (AUC) - B$ , we want to show  $x \in (A-B)U(C-B)$ XE (AUC) -B => by def. of dif = XEAUC and X&B by dif of union, (x eA, or XEC) and X&B. First case: XEA, and X&B. by def of dif: XEA-B by def of union X = A-B, so X = (A-B) U(C-B) Second aire: XEC and X&B. by def of dif: XEC-B

by def of union XEC-B, XEA-B)VC-B]

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