

Birzeit University Faculty of Engineering and Technology Department of Electrical and Computer Engineering Circuit Analysis – ENEE 2304 Quiz #4

1 February 2023	Dr. Jaser Sa'ed	Tir	ne: 10 min
Student Name:		ID Number:	
A 90 Ω resistor, a 32 mH inductor, and a 5 μ F capacitor are connected in series across the terminals of a sinusoidal voltage source, as shown in the Fig. The star de state connection for the series		90 Ω	32 mH

the Fig. . The steady-state expression for the source voltage v_s is 750 cos (5000t + 30°) V.

- a) Construct the frequency-domain equivalent circuit.
- b) Calculate the steady-state current *i* by the phasor method.

Solution

a) From the expression for v_s , we have $\omega = 5000$ rad/s. Therefore the impedance of the 32 mH inductor is

$$Z_L = j\omega L = j(5000)(32 \times 10^{-3}) = j160 \ \Omega,$$

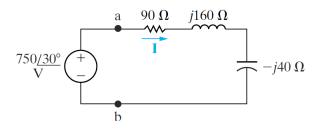
and the impedance of the capacitor is

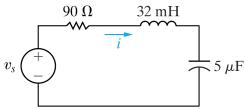
$$Z_C = j \frac{-1}{\omega C} = -j \frac{10^6}{(5000)(5)} = -j40 \ \Omega.$$

The phasor transform of v_s is

$$\mathbf{V}_s = 750 / 30^\circ \,\mathrm{V}.$$

Figure 9.16 illustrates the frequency-domain equivalent circuit of the circuit shown in Fig. 9.15.





b) We compute the phasor current simply by dividing the voltage of the voltage source by the equivalent impedance between the terminals a,b. From Eq. 9.45,

$$Z_{ab} = 90 + j160 - j40$$

= 90 + j120 = 150/53.13° Ω.

Thus

$$\mathbf{I} = \frac{750 \ / \ 30^{\circ}}{150 \ / \ 53.13^{\circ}} = 5 \ / \ -23.13^{\circ} \ \mathbf{A}.$$

We may now write the steady-state expression for *i* directly:

$$i = 5\cos(5000t - 23.13^{\circ})$$
 A.

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