



Faculty of Engineering and Technology

Department of Electrical and Computer Engineering

Control systems

(ENEE4302)

“MATLAB assignment”

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Introduction:

The block diagram of a pitch control system for Unmanned Free-Swimming Submersible Vehicles (UFSS) typically consists of several subsystems working together to control the pitch angle of the vehicle. The aim of the pitch control system is to submerge or rise the vehicle by varying a vertical force.

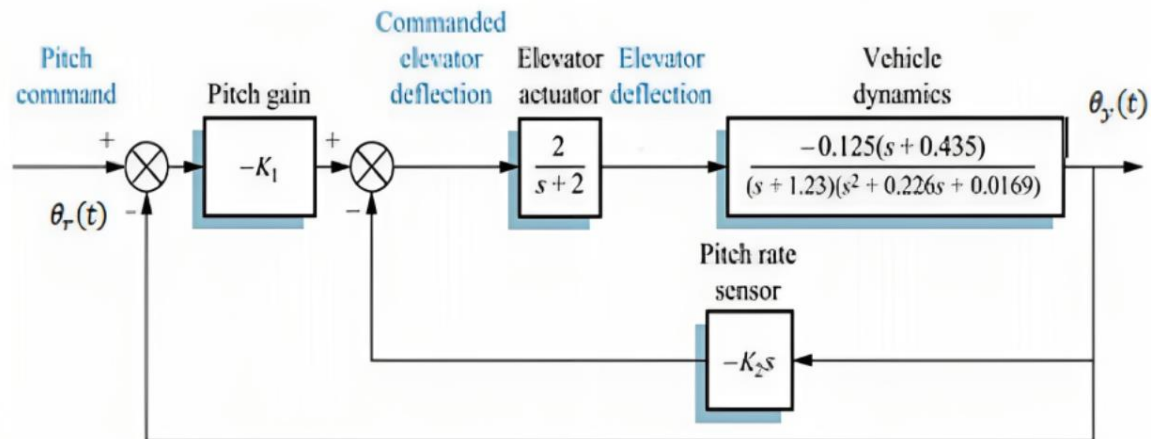


Figure 1 system block diagram

The block diagram consists of a Pitch Gain: This subsystem represents the gain applied to the pitch control system. It determines the sensitivity of the system to changes in the pitch angle. Elevator Actuator: The elevator actuator is responsible for controlling the elevator deflection, which in turn affects the pitch angle of the vehicle. It receives input from the pitch rate feedback and adjusts the elevator deflection accordingly. Vehicle Dynamics: This subsystem represents the dynamics of the UFSS vehicle. It considers factors such as mass, inertia, and hydrodynamic forces that affect the pitch angle of the vehicle. The vehicle dynamics subsystem is typically modeled using transfer functions. Pitch Rate Sensor: The pitch rate sensor provides feedback to the closed-loop system. It measures the rate of change of the pitch angle and provides this information to the elevator actuator for control purposes.

Procedure, Results and Discussion:

(all assignment objectives are here but maybe not in the same order as the assignment)

Part 1: Transfer Function

1- Transfer function in terms using symbolic k_1 , k_2 using math operation

In the below code I used math operations to manually reduce the block diagram into one Transfer Function while using k_1 , k_2 and s as symbolic variables.

When k_1 , k_2 are symbolic:

```
clear all;
syms s k1 k2;
%k1=5;
%k2=8;
g1=-k1;
g2=2/(s+2);
l1=(-0.125)/(s+1.23);
l2=(s+0.435)/(s^2+0.226*s+0.0169);
g3=l1*l2;
g4=(-k2*s);
cas1=g2*g3;%series g2 g3
feedback1=cas1/(1+(cas1*g4));%cas1 g4 feedback
cas2=g1*feedback1;%series g1 feedback1
system_tf=cas2/(1+cas2);%feedback cas2 1
system=simplify(system_tf);
system=(system);
[num,den]=numden(system);
num = simplifyFraction(num,"Expand",true);%expand k1*()
num=num/10^6;
den=den/10^6;
system=num/den;
system=vpa(system);
disp(system);
```

$$\frac{0.10875 k_1 + 0.25 k_1 s}{0.10875 k_1 + 0.610547 s + 0.25 k_1 s + 0.10875 k_2 s + 0.25 k_2 s^2 + 3.20688 s^2 + 3.456 s^3 + s^4 + 0.041574}$$

Figure 2 Transfer function in terms of k_1 , k_2 .

When $k_1 = 5$ and k_2 is symbolic.

If we change the above code and remove k_1 from the 2nd line and removing “%” from the 3rd line therefore transferring it from being a comment into a constant we get the following transfer function.

$$\frac{1.25 s + 0.54375}{1.860547 s + 0.10875 k_2 s + 0.25 k_2 s^2 + 3.20688 s^2 + 3.456 s^3 + s^4 + 0.585324}$$

Figure 3 transfer function using $k_1=5$.

When $k_1 = 5$ and $k_2 = 8$.

Doing the same procedure we can get the transfer function when $k_1 = 5$, $k_2 = 8$.

$$\frac{1.25 s + 0.54375}{s^4 + 3.456 s^3 + 5.20688 s^2 + 2.730547 s + 0.585324}$$

Figure 4 system transfer function $k_1=5$, $k_2=8$.

When k_1 is symbolic and $k_2 = 8$.

$$\frac{0.10875 k_1 + 0.25 k_1 s}{0.10875 k_1 + 1.480547 s + 0.25 k_1 s + 5.20688 s^2 + 3.456 s^3 + s^4 + 0.041574}$$

Figure 5 system transfer function k_1 symbol $k_2=8$

2-Transfer function using Simulink:

1-using the non accurate model

The system in the figure below was built using Simulink but this system isn't an accurate representation of the desired system since the linearization model of the derivative block is $\frac{s}{cs+1}$

Not s .

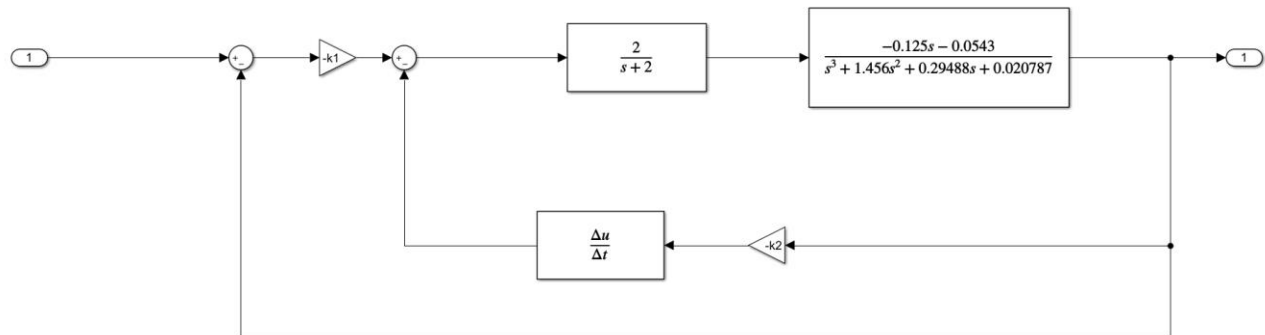


Figure 6 Simulink block diagram

Below is the written code and the transfer function of the system at $k_1=5, k_2=8$.

```
[a,b,c,d]=linmod('block_diagram') %linearized model

a = 4x4
    -1.4560   -0.2949   -0.0208    2.0000
    1.0000     0         0         0
     0         1.0000     0         0
     0        -0.6250   -0.2715   -2.0000

b = 4x1
     0
     0
     0
    -5

c = 1x4
     0   -0.1250   -0.0543     0

d = 0

[num,den]=ss2tf(a,b,c,d)%state space to transfer function

num = 1x5
     0         0         0    1.2500    0.5430

den = 1x5
    1.0000    3.4560    3.2069    1.8605    0.5846

system=tf(num,den)%G(s)=

system =

          1.25 s + 0.543
-----
s^4 + 3.456 s^3 + 3.207 s^2 + 1.861 s + 0.5846

Continuous-time transfer function.
```

Figure 7 non accurate transfer function (code)

2- Accurate Simulink block diagram

Below is manually reduced block diagram so I didn't have to use the derivative block which introduced the error to the previous system.

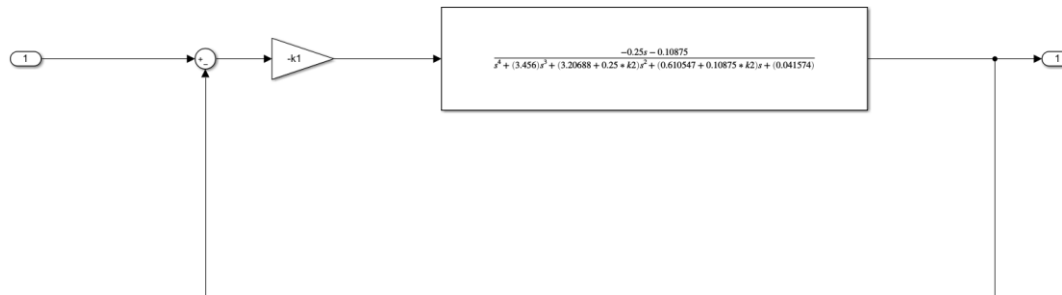


Figure 8 accurate Simulink model

The code used and result Transfer Function:

```
[a,b,c,d]=linmod('block_t'); %linearized model
[num,den]=ss2tf(a,b,c,d);%state space to transfer function
system=tf(num,den);%G(s)=
system=simplify(system)
system =
```

$$\frac{1.25 s + 0.5437}{s^4 + 3.456 s^3 + 5.207 s^2 + 2.731 s + 0.5853}$$

Continuous-time transfer function.

3-Transfer function using control system library in MATLAB:

Here we use the function in control system library such as series, feedback, tf and stepinfo which make the system easier to analyze here is the code I used to get the transfer function.

```
k1=5;
k2=8;
g1=tf([-k1],[1]);
g2=tf([2],[1 2]);
l1=tf([-0.125],[1 1.23]);
l2=tf([1 0.435],[1 0.226 0.0169]);
g3=l1*l2;
g4=tf([-k2 0],[1]);
cas1=series(g2,g3);
feedback1=feedback(cas1,g4);
cas2=series(g1,feedback1);
system_tf=feedback(cas2,1)
```

system_tf =

$$\frac{1.25 s + 0.5437}{s^4 + 3.456 s^3 + 5.207 s^2 + 2.731 s + 0.5853}$$

Continuous-time transfer function.

2-Root locus Plot

Using the function `rlocus(system_tf)` or `rlocusplot(system_tf)`

We can plot the root locus.

1-Variable k_1 and k_2

While using different values of k_1 and k_2 , 3 stable values each

```
k1=[5,10,15] ;%values of k1  
k2=[8,4,1];%values of k2
```

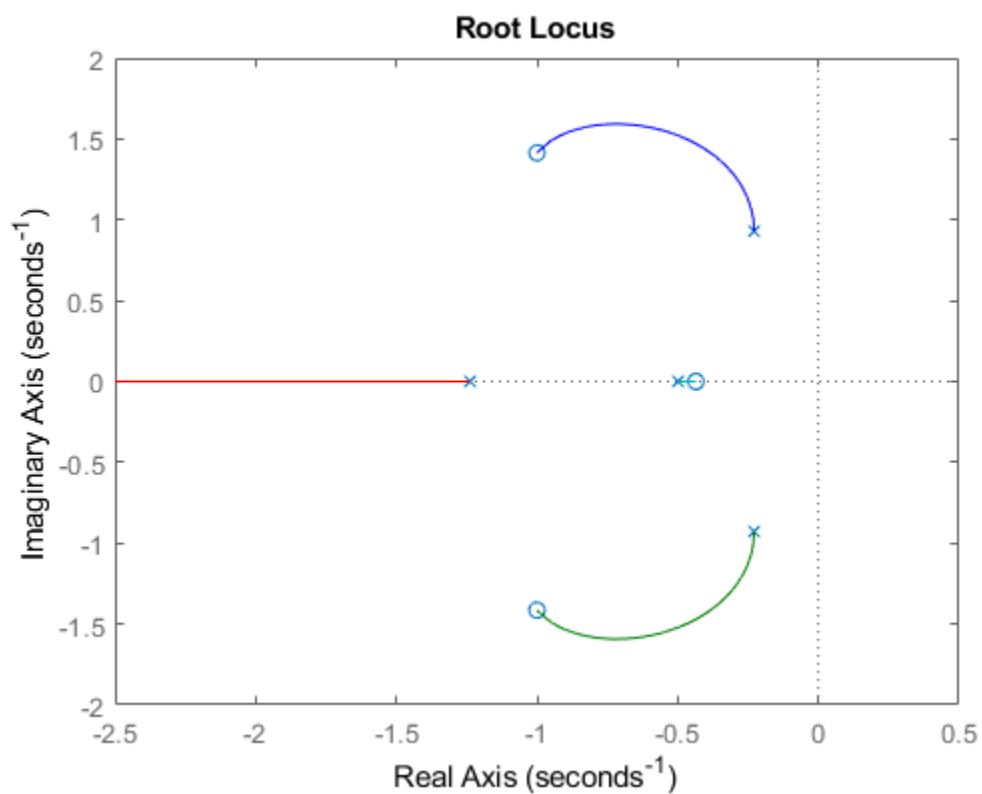


Figure 9 root locus for variable k_1 and k_2

2- Variable k2 fixed k1

Now root locus for $k_1=5$ and different values of k_2

```
k1=5 ;  
k2=[8,4,1];
```

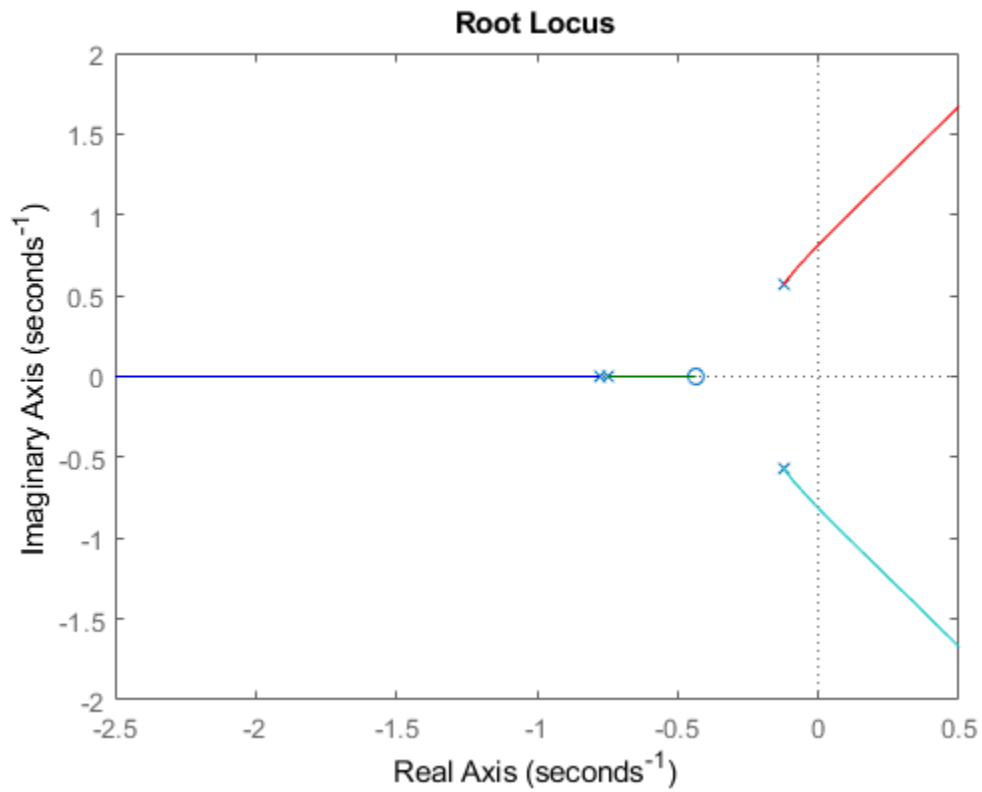


Figure 10 root locus for $k_1=5$ and 3 different values of k_2

3- Variable k1 fixed k2

```
k1=[5,10,15] ;  
k2=8;
```

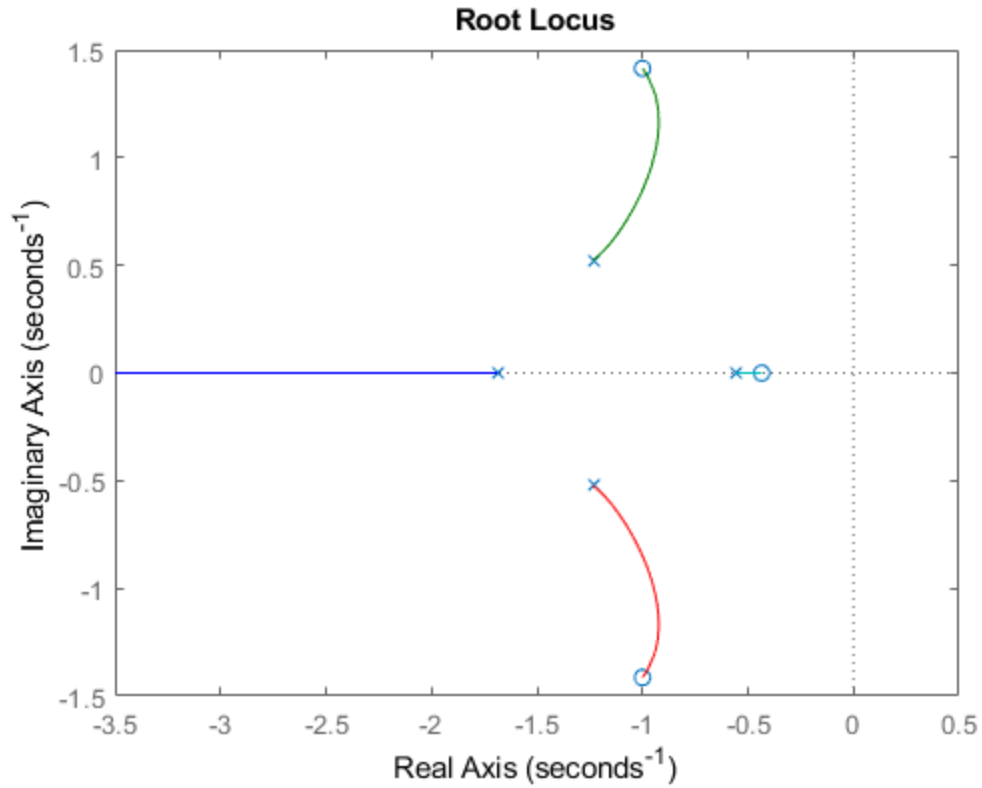


Figure 11 k1 variable k2 =8

4- Constant k_1, k_2

$k_1=5$ $k_2=8$

```
k1=5 ;%values of k1  
k2=8;%values of k2
```

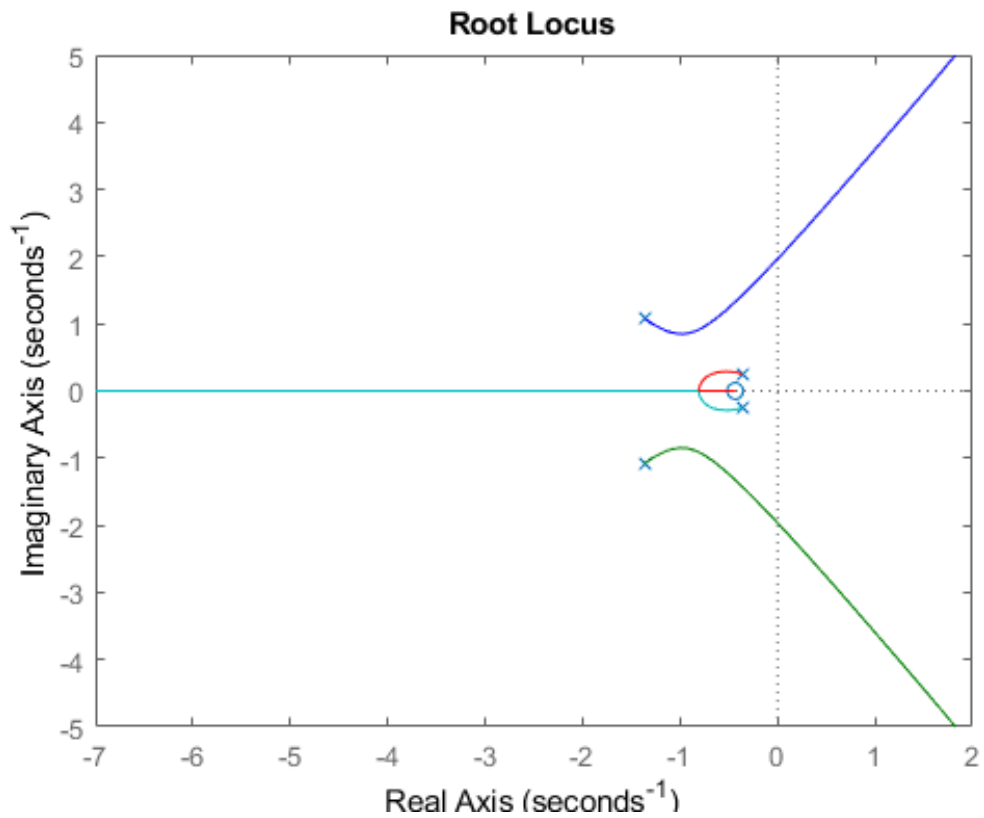


Figure 12 root locus $k_1=5$ $k_2=8$

3- Testing system stability for k1

Using Routh Hurwitz, we can test the system stability based on the change of the signs.

$$\frac{0.10875 k_1 + 0.25 k_1 s}{0.10875 k_1 + 1.480547 s + 0.25 k_1 s + 5.20688 s^2 + 3.456 s^3 + s^4 + 0.041574}$$

Figure 13 Transfer function k2=8

s^4	1	5.20688	0.041574+0.25k1	+
s^3	3.456	1.48+0.25k1		+
s^2	4.778-0.0723k1	0.041574+0.25k1		
s^1	$\frac{-0.018075k_1^2 + 0.2235k_1 + 6.93}{4.778 - 0.0723k_1}$			
s^0	0.041574+0.25k1			

Table 1 Routh Hurwitz table k2=8.

K2=8

K1

$s^3 s^4$ +++++
 s^2 +++++(66.057)-----
 s^1 -----(-6.244)+++++(49.97)-----(-82.47)-----
 s^0 -----(-0.3822)+++++

K2=4

$s^3 s^4$ +++++
 s^2 +++++53.973-----
 s^1 -----(-4.5304)+++++(37.809)-----(-70.49)-----
 s^0 -----(-0.3822)+++++

Stable between [-0.3822,37.809]

K2=1

$s^3 s^4$ ++++++

s^2 ++++++(44.91072)-----

s^1 -----(-3.23)+++++(28.645)----- (61.529)-----

s^0 -----(-0.3822)+++++

4-Step response for different K_1 values along with its transient parameters and root locus plot.

1-Stable oscillatory $k_1 = 25, k_2 = 8$

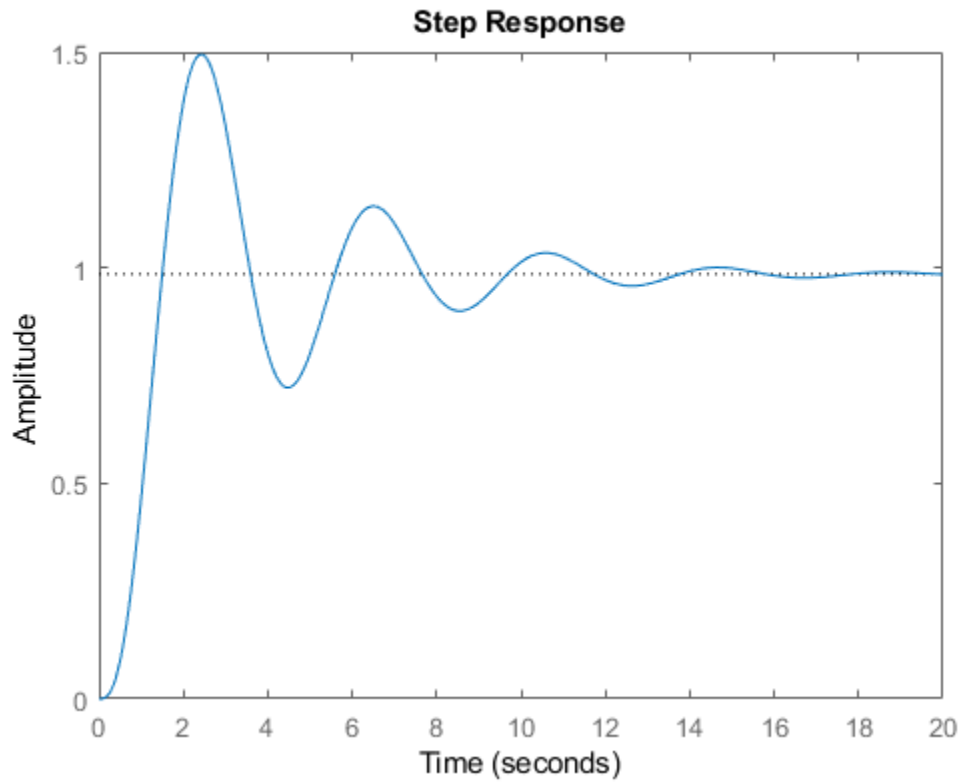


Figure 14 Stable oscillatory

Poles and zeros:

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

-2.4301	+	0.0000i
-0.2814	+	1.5408i
-0.2814	-	1.5408i
-0.4630 + 0.0000i		

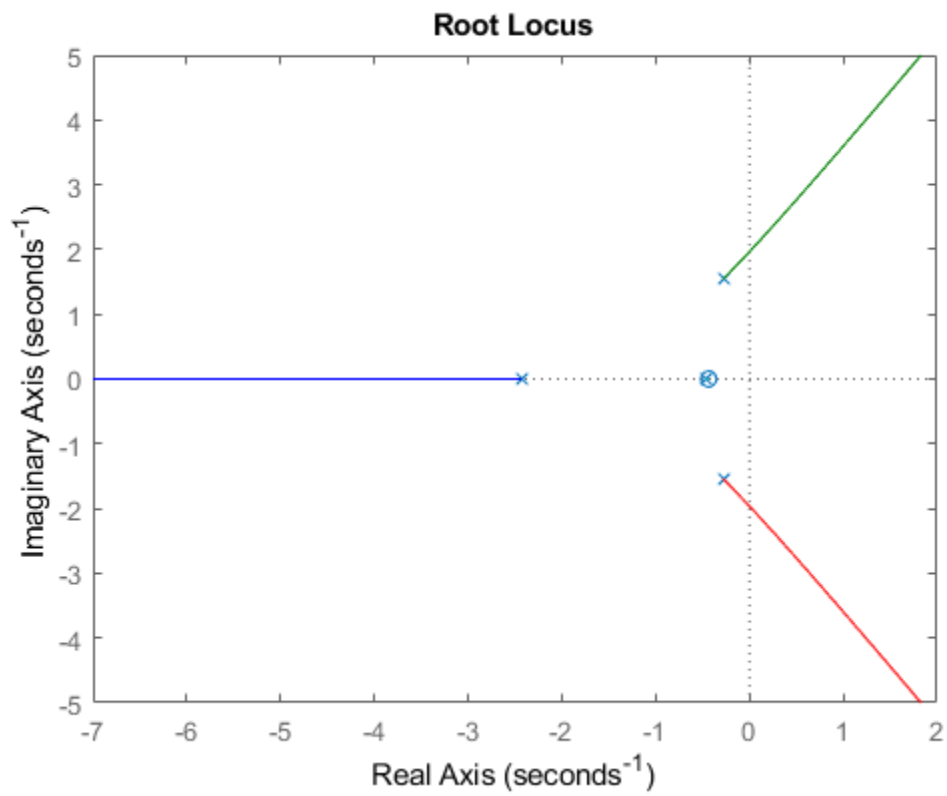


Figure 15 root locus $k_1=25, k_2=8$

Transient parameters:

Notice that since it is oscillatory the settling time is relatively high but the rise time is relatively low which made the overshoot high due to the poles being far from the real axis, also there is no undershoot which is expected of a stable oscillatory system.

```
stepinfo(system_tf)
ans = struct with fields:
    RiseTime: 0.8812
    SettlingTime: 13.1379
    SettlingMin: 0.7217
    SettlingMax: 1.4951
    Overshoot: 51.7937
    Undershoot: 0
    Peak: 1.4951
    PeakTime: 2.4257
```

Steady state error

Using this code we can find the steady state error.

```
[y,tf]=step(system_tf);
sp=1;
ss_error=abs(sp-y(end))
ss_error = 0.0115
```

2-stable non-oscillatory $k_1 = 1, k_2 = 8$

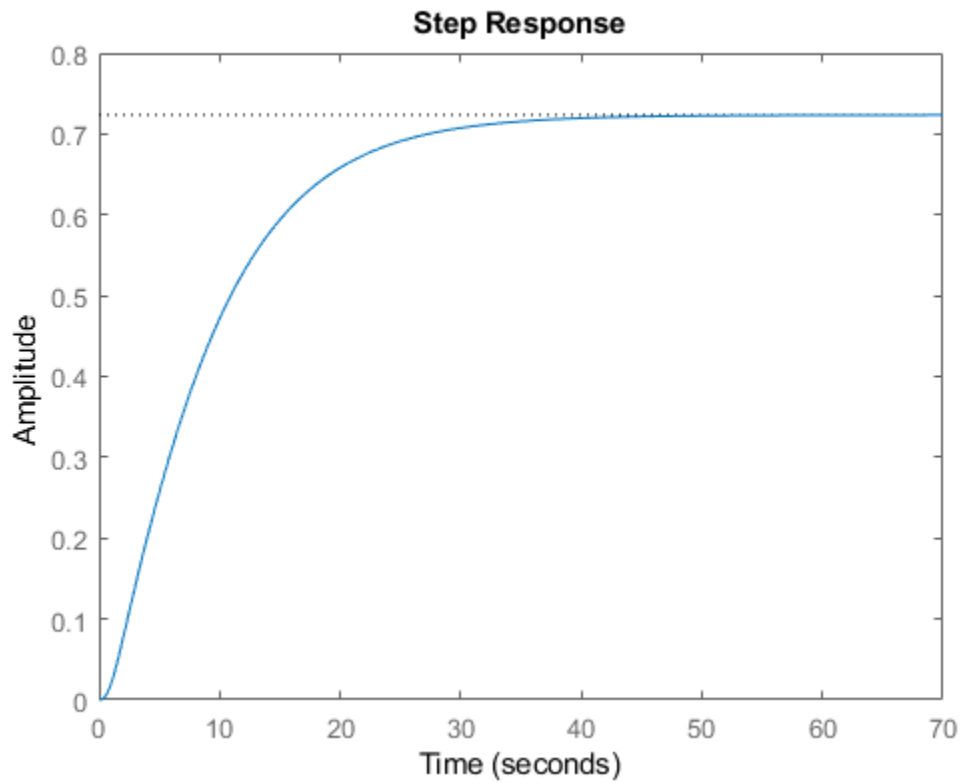


Figure 16 Stable non-oscillatory

Poles and zeros

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

-1.5218	+	1.2639i
-1.5218	-	1.2639i
-0.2701	+	0.0000i
-0.1422 + 0.0000i		

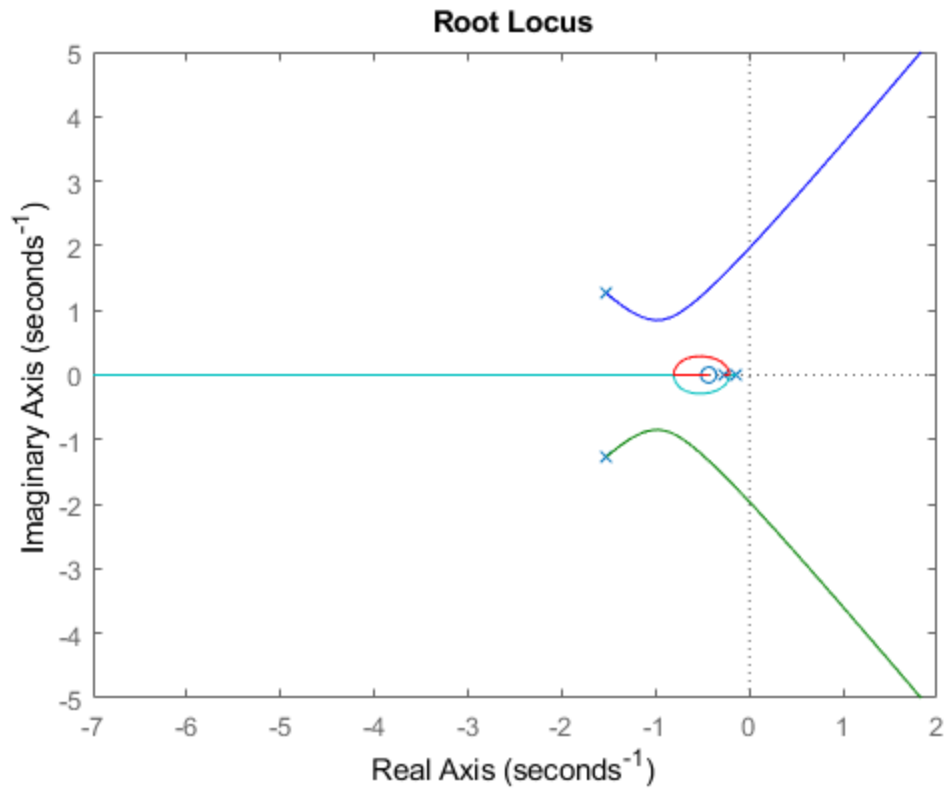


Figure 17 root locus for stable non-oscillatory

Transient parameters

Notice that the rise time is high because the poles are far from the real axis and the settling time is also high because the poles are close to the imaginary axis and because the system is non oscillatory there is no overshoot or under shoot.

```
stepinfo(system_tf)
```

```
ans = struct with fields:
```

RiseTime:	17.3169
SettlingTime:	30.7223
SettlingMin:	0.6529
SettlingMax:	0.7234
Overshoot:	0
Undershoot:	0
Peak:	0.7234
PeakTime:	77.4015

Steady state error

Using this code we can find the steady state error.

```
[y,tf]=step(system_tf);  
sp=1;  
ss_error=abs(sp-y(end))  
ss_error = 0.2766
```

3-unstable $k_1 = 50, k_2 = 8$

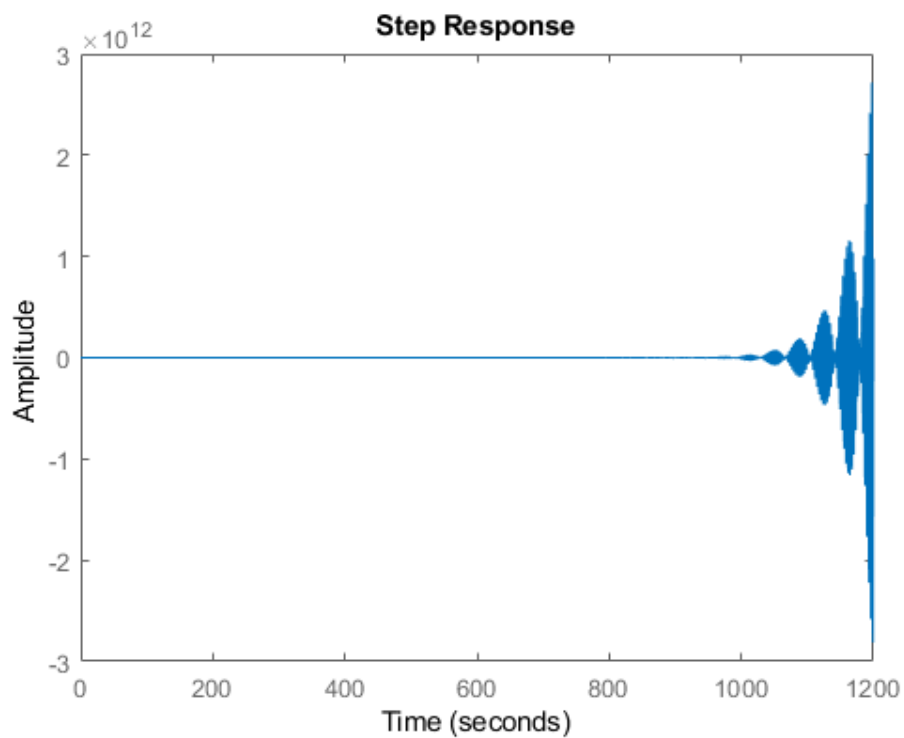


Figure 18 unstable

Poles and zeros

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

-3.0570	+	0.0000i
0.0240	+	2.0020i
0.0240	-	2.0020i
-0.4471 + 0.0000i		

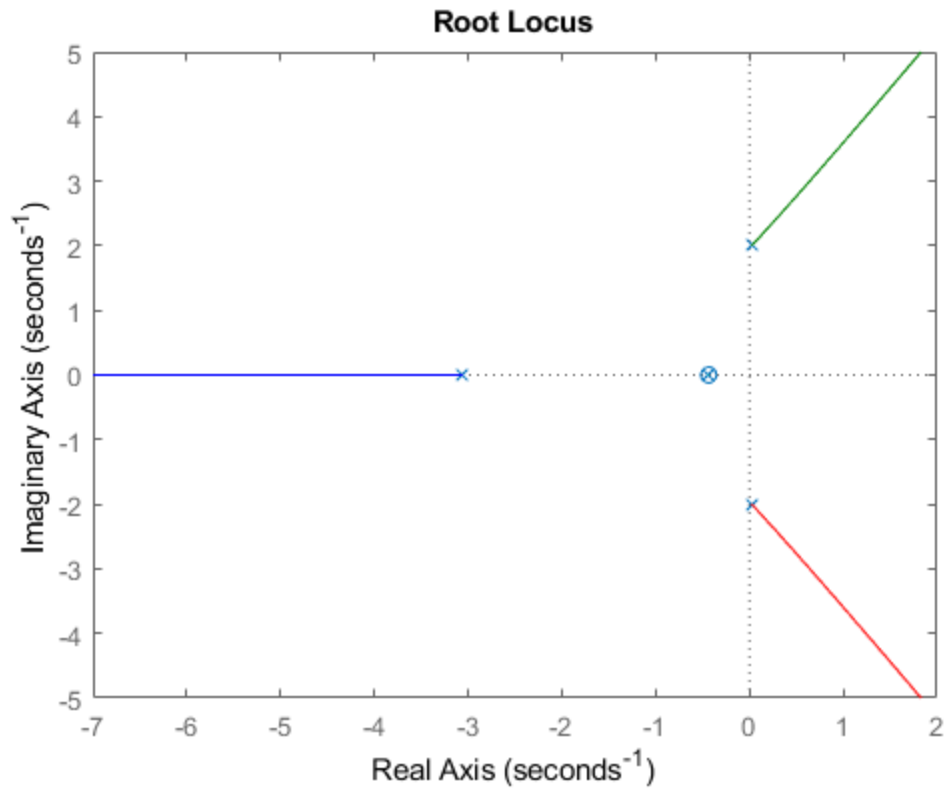


Figure 19 root locus for unstable

Transient parameters

There is no transient parameters for a non-stable system

```
stepinfo(system_tf)
```

```
ans = struct with fields:
```

RiseTime:	NaN
SettlingTime:	NaN
SettlingMin:	NaN
SettlingMax:	NaN
Overshoot:	NaN
Undershoot:	NaN
Peak:	Inf
PeakTime:	Inf

Steady state error

Since this isn't stable there is no steady state error but when using the same code we get this error

Which is huge and indicates that the system isn't stable (if you didn't notice from the poles or the step response).

```
[y,tf]=step(system_tf);  
sp=1;%setpoint  
ss_error=abs(sp-y(end))  
ss_error = 2.8637e+12
```


4-At the limit of stability ($k_1 = 35.196, k_2 = 4$)

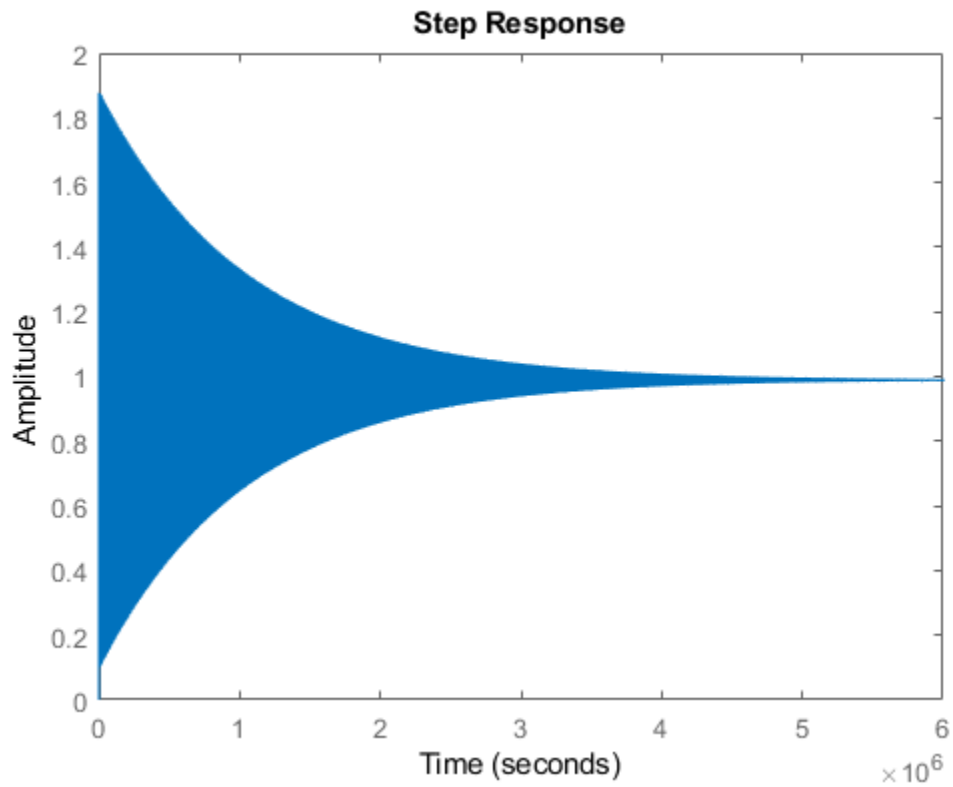


Figure 20 At the limit of stability

Poles and zeros

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

-3.0038	+	0.0000i
-0.0000	+	1.6878i
-0.0000	-	1.6878i
-0.4522 + 0.0000i		

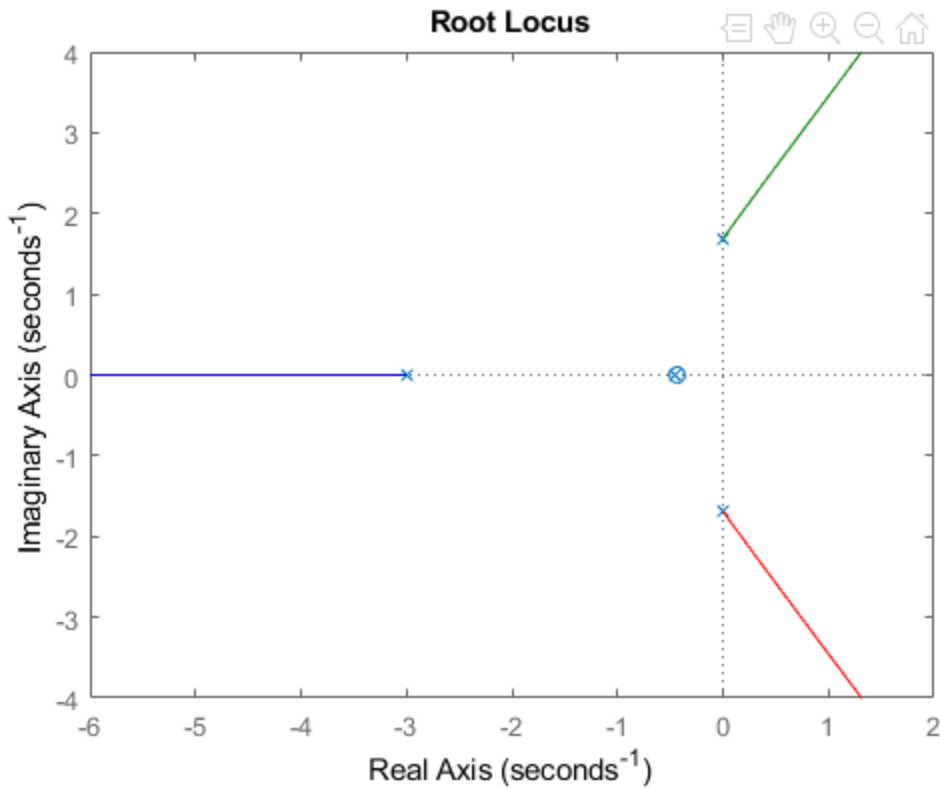


Figure 21 root locus for the limit of stability

Transient parameters

Rise time is high, settling time is so high due to it almost being marginally stable (undamped) but it should have been infinity.

```
stepinfo(system_tf)
```

```
ans = struct with fields:
```

RiseTime:	179.7022
SettlingTime:	3.9899e+06
SettlingMin:	0.0983
SettlingMax:	1.8772
Overshoot:	89.7584
Undershoot:	0
Peak:	1.8772
PeakTime:	579.1197

Steady state error

Using the same code we get a relatively low steady state error.

```
[y,tf]=step(system_tf);  
sp=1;  
ss_error=abs(sp-y(end))  
ss_error = 0.0137
```

5-The desired system ($k_1 = 5, k_2 = 8$)

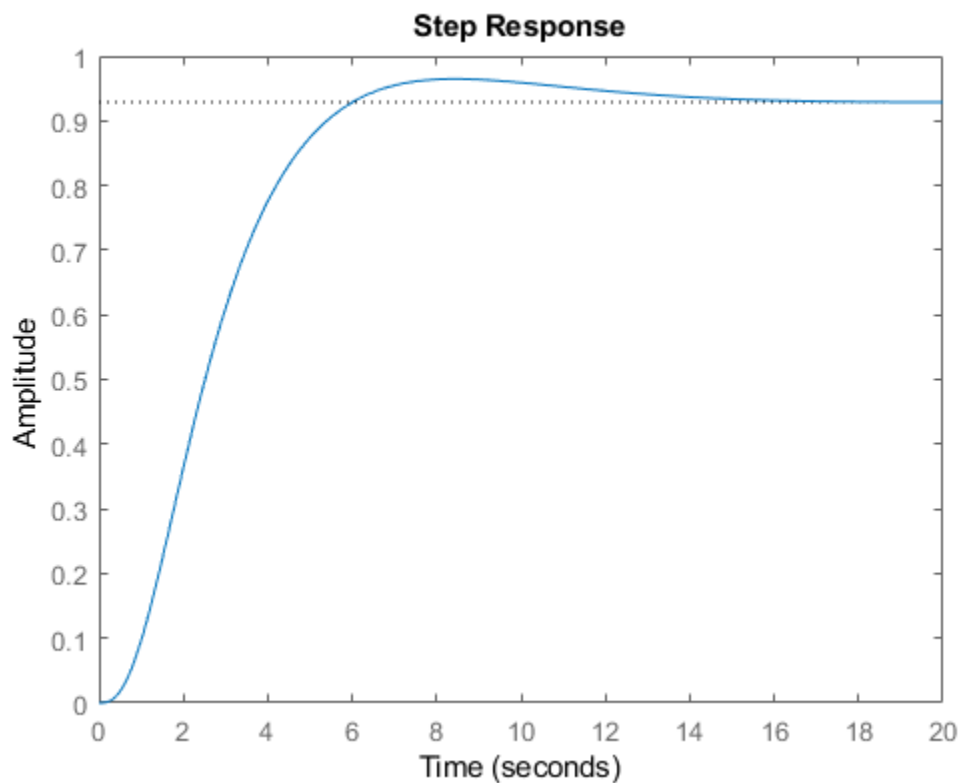


Figure 22 step response $k_1=5$ $k_2=8$

Poles and zeros

```
zeros=zero(system_tf)  
zeros = -0.4350  
poles=pole(system_tf)  
poles = 4x1 complex  
-1.3643 + 1.0805i  
-1.3643 - 1.0805i  
-0.3637 + 0.2469i  
-0.3637 - 0.2469i
```

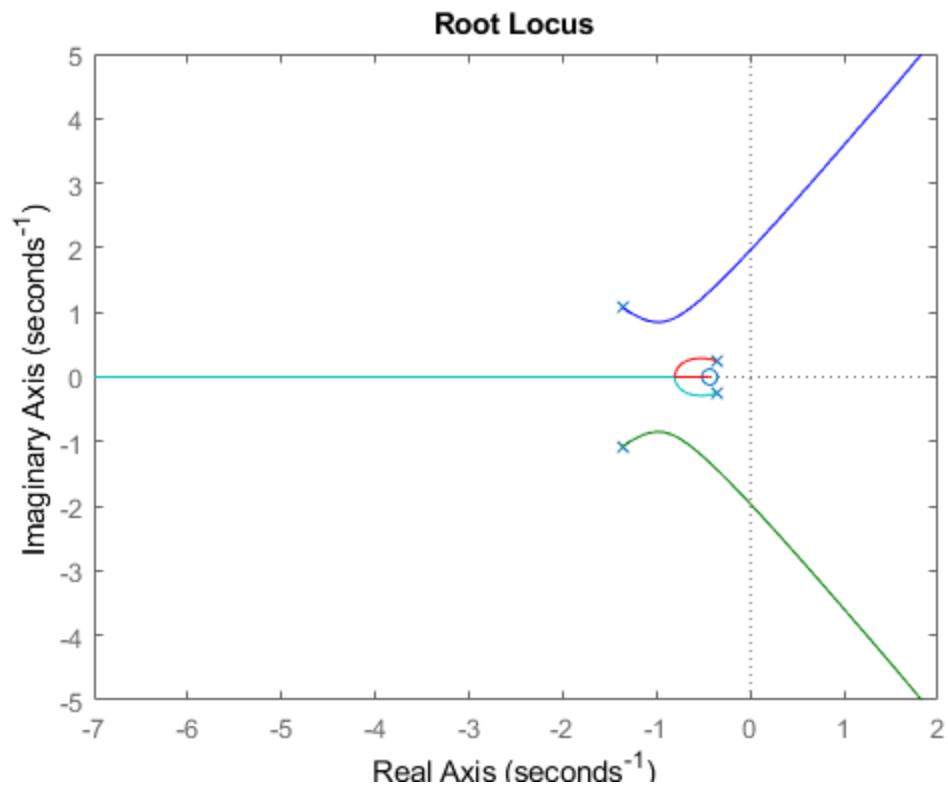


Figure 23 root locus $k_1=5$ $k_2=8$

Transient parameters

```
stepinfo(system_tf)
```

```
ans = struct with fields:
```

```
    RiseTime: 3.5648
    SettlingTime: 11.7887
    SettlingMin: 0.8402
    SettlingMax: 0.9647
    Overshoot: 3.8475
    Undershoot: 0
    Peak: 0.9647
    PeakTime: 8.4388
```

Steady state error

```
[y,tf]=step(system_tf);
sp=1;
ss_error=abs(sp-y(end))
ss_error = 0.0710
```

The effect of turning the controller off ($k_2 = 0$)

1-stable oscillatory $k_1 = 5$

The transfer function would become like this.

```
system_tf =  
  
          1.25 s + 0.5437  
-----  
s^4 + 3.456 s^3 + 3.207 s^2 + 1.861 s + 0.5853
```

the poles and zeros would be

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex  
-2.4007 + 0.0000i  
-0.2239 + 0.5927i  
-0.2239 - 0.5927i  
-0.6074 + 0.0000i
```

The root locus plot:

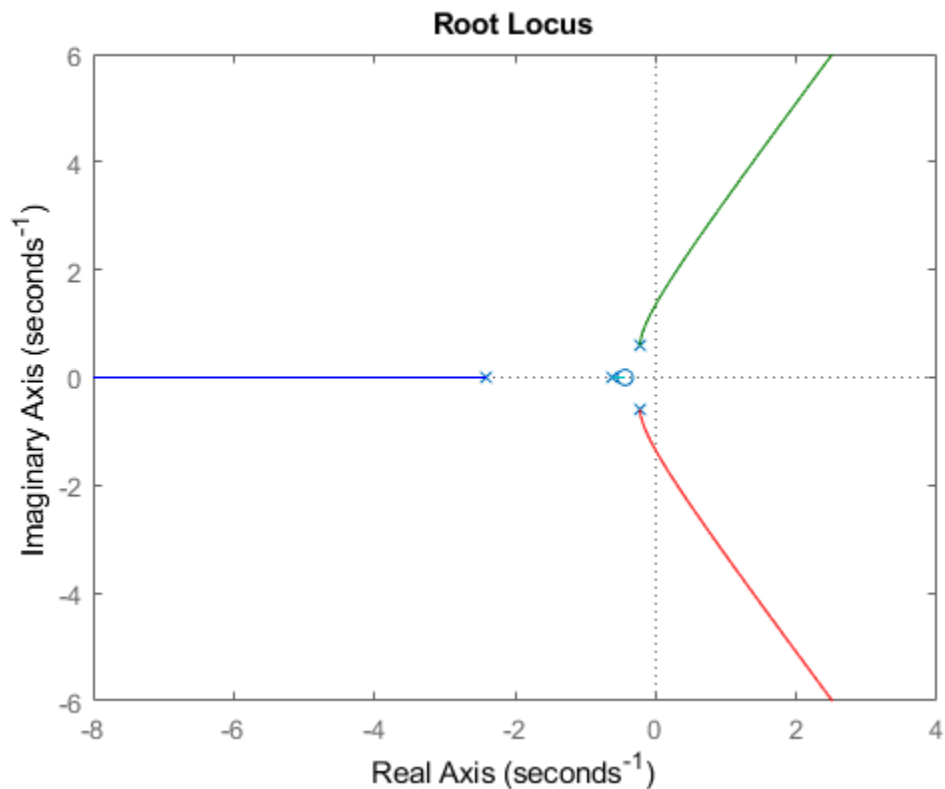


Figure 24 root locus for $k_2 = 0$ $k_1 = 5$

Step response:

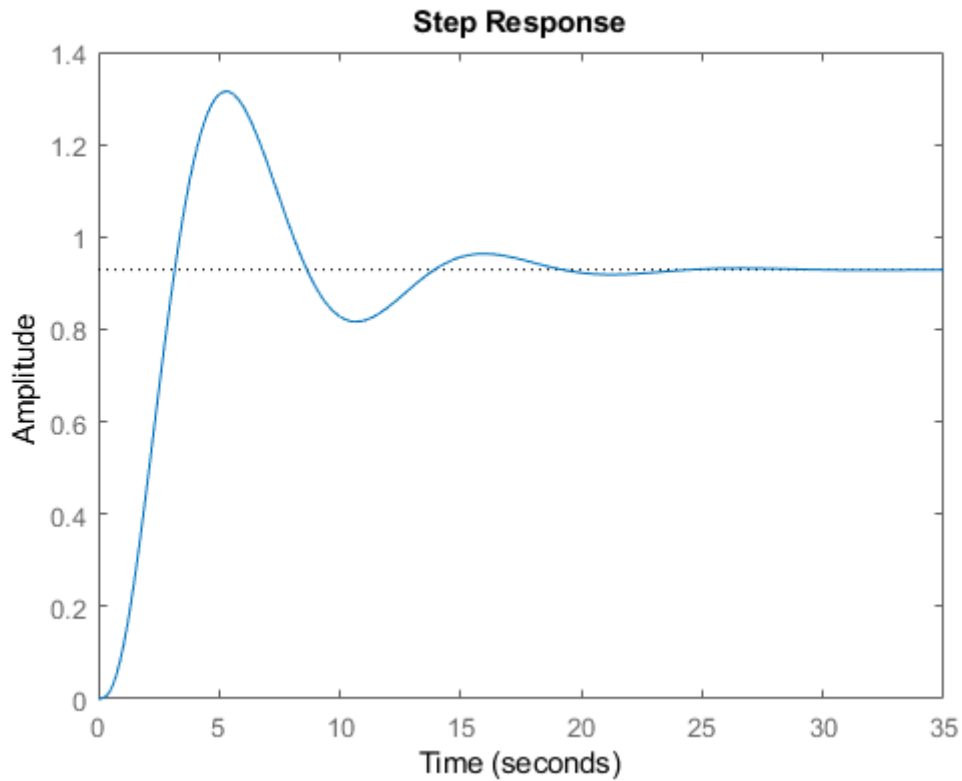


Figure 25 Step response for $k_2=0$ $k_1=5$

Transient parameters:

```
stepinfo(system_tf)
ans = struct with fields:
    RiseTime: 1.9688
    SettlingTime: 17.7732
    SettlingMin: 0.8166
    SettlingMax: 1.3152
    Overshoot: 41.5771
    Undershoot: 0
    Peak: 1.3152
    PeakTime: 5.3071
```

Steady state error

```
[y,tf]=step(system_tf);
sp=1;
ss_error=abs(sp-y(end))
ss_error = 0.0719
```

2-Unstable $k_1 = 50$,

The transfer function would become like this:

system_tf =

$$\frac{12.5 s + 5.438}{s^4 + 3.456 s^3 + 3.207 s^2 + 13.11 s + 5.479}$$

the poles and zeros would be:

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

```
-3.4857 + 0.0000i
```

```
0.2379 + 1.8617i
```

```
0.2379 - 1.8617i
```

```
-0.4462 + 0.0000i
```

The root locus plot:

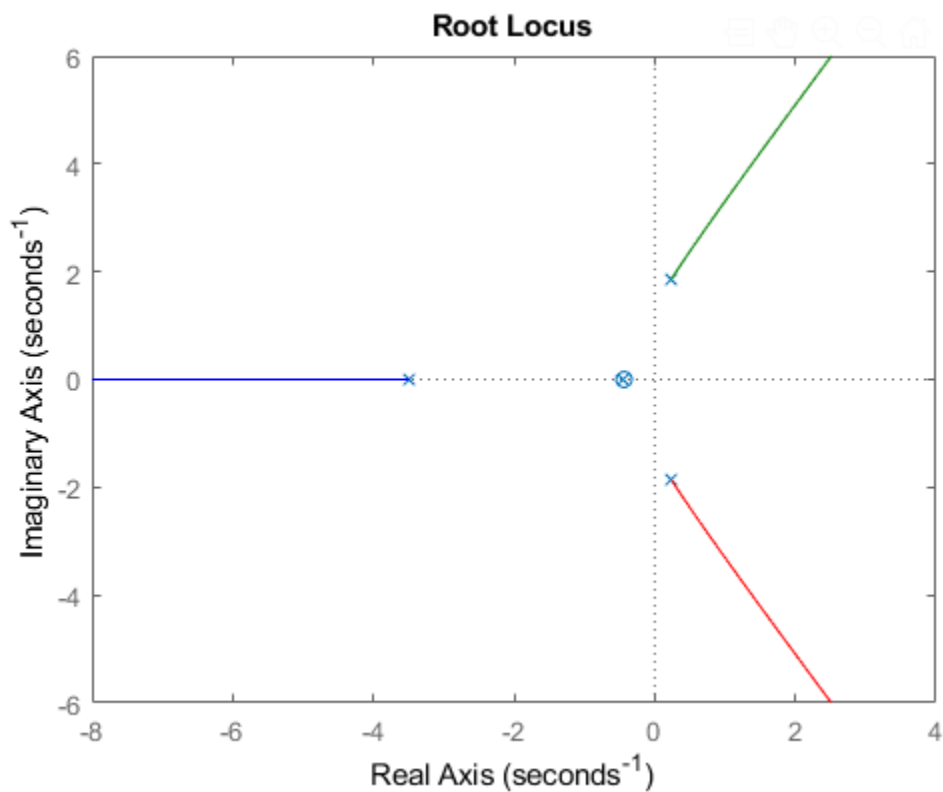


Figure 26 root locus for $k_2 = 0$ $k_1 = 50$ (unstable)

Step response:

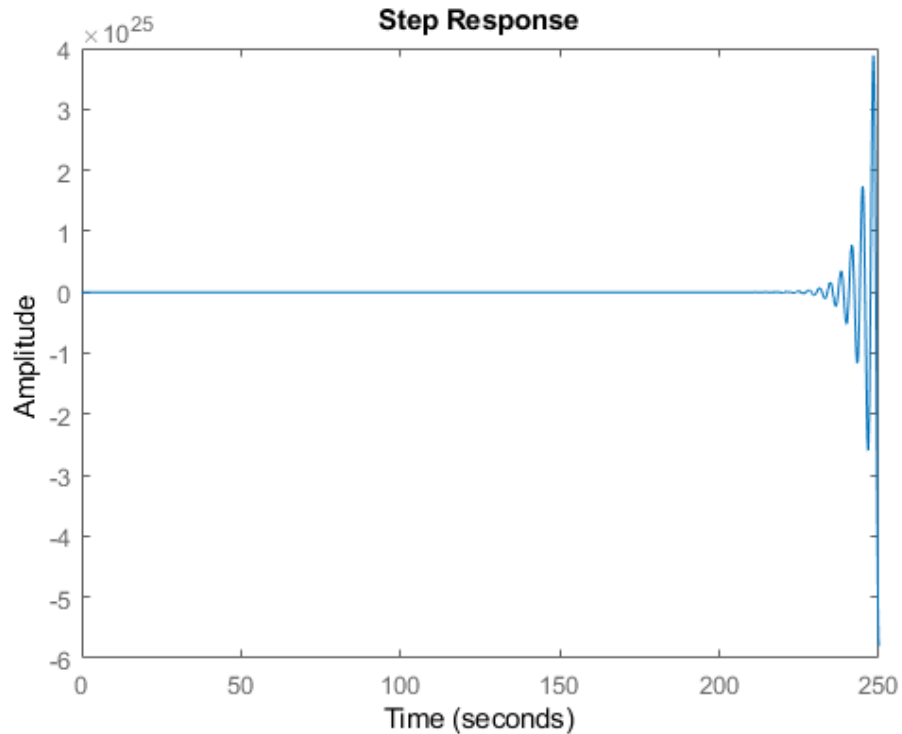


Figure 27 Step response for $k_2=0$ $k_1=50$ (unstable)

Transient parameters:

No info about the transient parameters because its unstable

```
stepinfo(system_tf)
```

```
ans = struct with fields:
```

```
    RiseTime: NaN
    SettlingTime: NaN
    SettlingMin: NaN
    SettlingMax: NaN
    Overshoot: NaN
    Undershoot: NaN
    Peak: Inf
    PeakTime: Inf
```

Steady state error

(no steady state) not stable

```
[y,tf]=step(system_tf);
sp=1;
ss_error=abs(sp-y(end))
ss_error = 2.2096e+24
```


3-stable non oscillatory $k_1 = 0.001$

The transfer function would become like this:

```
system_tf =
```

```
system_tf =
```

$$\frac{0.00025 s + 0.0001088}{s^4 + 3.456 s^3 + 3.207 s^2 + 0.6108 s + 0.04168}$$

the poles and zeros would be:

```
zeros=zero(system_tf)
```

```
zeros = -0.4350
```

```
poles=pole(system_tf)
```

```
poles = 4x1 complex
```

```
-2.0001 + 0.0000i
```

```
-1.2298 + 0.0000i
```

```
-0.1130 + 0.0646i
```

```
-0.1130 - 0.0646i
```

The root locus plot (pole-zero map):

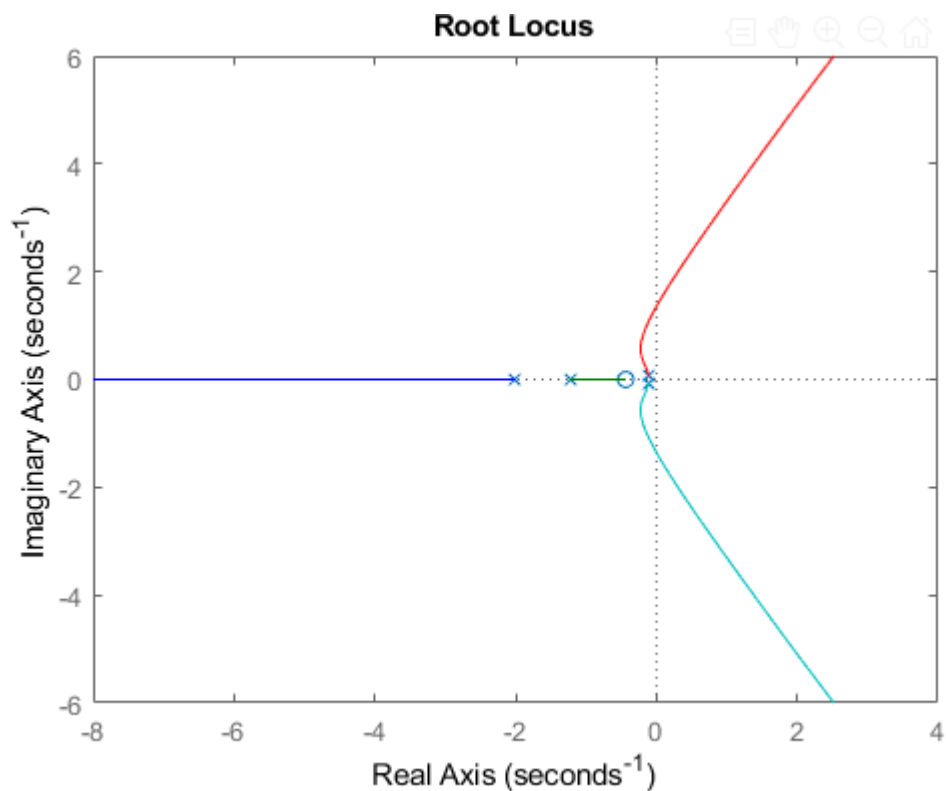


Figure 28 root locus for $k_2 = 0$ $k_1 = 0.001$ (stable non oscillatory)

Step response:

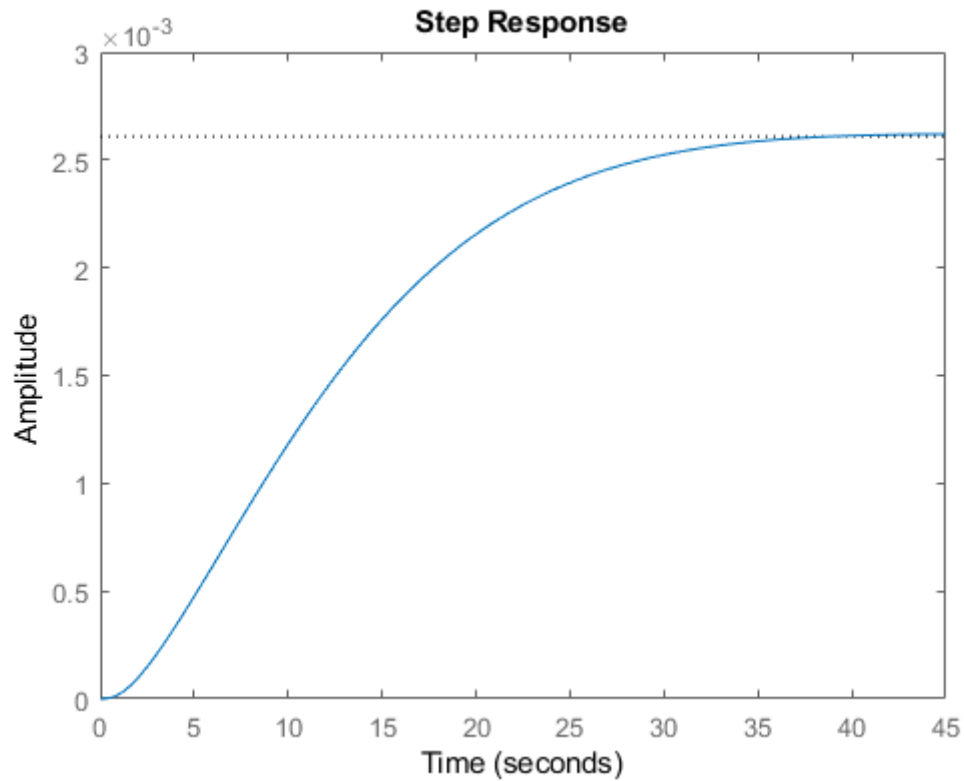


Figure 29 Step response for $k_2=0$ $k_1=0.001$ (stable non oscillatory)

Transient parameters:

```
stepinfo(system_tf)
ans = struct with fields:
    RiseTime: 20.3699
    SettlingTime: 32.1435
    SettlingMin: 0.0024
    SettlingMax: 0.0026
    Overshoot: 0.4327
    Undershoot: 0
    Peak: 0.0026
    PeakTime: 46.8536
```

Steady state error

```
[y,tf]=step(system_tf);
sp=1;
ss_error=abs(sp-y(end))
ss_error = 0.9974
```

5-canonical controller state-space representation of the feedback system

```
[A, B, C, D] = tf2ss(system_tf.num{1}, system_tf.den{1})%controller canonical form
```

A = 4×4

-3.4560	-5.2069	-2.7305	-0.5853
1.0000	0	0	0
0	1.0000	0	0
0	0	1.0000	0

B = 4×1

1
0
0
0

C = 1×4

0	0	1.2500	0.5437
---	---	--------	--------

D = 0