Nodal and Mesh Analysis As Circuits get more Complicated, we need an organized method of applying KVL, KCL, and Ohm's Nodal analysis a ssigns voltager to each node then we apply KCL Mesh analysis assigns Currents to each mesh, and then we apply KVL \_62-

# **Nodal Analysis**

Steps to Determine **Node Voltages**: 1. Select a node as the **reference node**. Assign voltage V1, V2, ...  $V_{n-1}$  to the remaining n-1 nodes. The voltages are referenced with respect to the reference node.

2. Apply **KCL** to each of the *n*-1 nonreference nodes. Use Ohm's law to express the branch currents in terms of node voltages.

3. Solve the resulting simultaneous equations to obtain the unknown node voltages.

The Nodal Analysis Method assign voltages to every node relative to a référence node. 12 52 Is Apply KCL to node 1 = I1 + I2 3  $=\frac{N_1}{2}+\frac{N_1-N_2}{5}$  $= 0.7 V_1 - 0.2 V_2$ 3 Apply KCL to node 2  $2 + I_2 = I_3$ I3 - I2 2 - 63 -

 $2 = \frac{N_2}{1} - \frac{N_1 - N_2}{5}$  $2 = -0.2 N_1 + 1.2 N_2$ \_ 0 Solving equations D and D, we get  $V_1 = 5V$  $V_2 = 2.5 V$ -64-STUDENTS-HUB.com Uploaded By: sondos hammad

1.  $\sqrt{2}$ R Is, Is. Applying Kelto node D  $I_{S_1} = I_1 + I_2$  $I_{S_1} = \frac{\lambda_1}{R_1} + \frac{\lambda_1 - \lambda_2}{R_1}$  $I_{S_1} = \left(\frac{1}{R_2} + \frac{1}{R_1}\right) V_1 - \frac{1}{R_1} V_2$  $I_{S_1} = (G_{2+}G_1)V_1 - G_1V_2$ Self Conductance = G2+G1 mutual Conductance = - Gi . 65\_ Uploaded By: sondos hammad STUDENTS-HUB.com

Applying KCL to node 2  $I_{S2} + I_2 = I_3$  $T_{s_2} = T_3 - T_2$  $I_{S2} = \frac{N_2}{R_3} - \frac{N_1 - N_2}{R_1}$  $I_{s2} = -\frac{1}{R_1} V_1 + \left(\frac{1}{R_2} + \frac{1}{R_1}\right) V_2$  $I_{s2} = -G_{1} \vee (G_{2} + G_{1}) \vee 2$ Self Conductance of node 2 = (G3+G1) mutual Conductance between nodes () and () = - 61 \_66\_

Writing Nodal equations by inspection 3<sub>A</sub> 175 52 3 8F KCL at node ():  $7V_{1} - 3V_{2} - 4V_{3} = -11$ KCL at node 2 :  $-3N_1+6N_2-2N_3=3$ KCL at node 3:  $-4N_{1}-2V_{2}+11N_{3}=25$ Solving :  $\lambda_1 = | Y , \lambda_2 = 2V, \lambda_3 = 3Y$ \_67\_ Uploaded By: sondos hammad STUDENTS-HUB.com

# Nodal Analysis with Voltage Sources

**Case 1:** The voltage source is connected between a non reference node and the reference node: The non reference node voltage is equal to the magnitude of voltage source and the number of unknown non reference nodes is reduced by one.

**Case 2:** The voltage source is connected between two non referenced nodes: a generalized node (**supernode**) is formed.

## Nodal Analysis with Voltage

### Sources

A circuit with a **supernode**.



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Voltage Sources and the supernode 6V V. ₹ 6k J ZIZK mA 6mA Constrain equation : N1-N2 = 6  $\dot{\mathbf{U}}$ KCL at node () :  $GmA = I_1 + I_s$  $6mA = \frac{N_1}{6\kappa} + Is$ (2) KCL at node @ :  $T_s = T_{2+} + MA$ 4mA = Is - I2 -70-Uploaded By: sondos hammad STUDENTS-HUB.com

 $4 mA = I_{5} - \frac{N_{2}}{12k}$ (2 Subtracting 3 from 2  $2mA = \frac{N_1}{6\kappa} + \frac{N_2}{12\kappa}$ - 4 This is the supernode equation Solving () and () Weget  $V_1 = 10 Y$ 12 = 4 1 -71-

Supernode equation by inspection  $\checkmark$ Nz 6mA SIZK 6K I,  $6 \text{mA} = \text{I}_1 + \text{I}_2 + 4 \text{mA}$  $2mA = I_1 + I_2$  $2mA = \frac{N_1}{6\kappa} + \frac{N_2}{12\kappa}$ .72

Noltage Sources and the supernode 22~ 13 125 8A Constrain equation :  $\sqrt{3} - \sqrt{2} = 22$ KCL at node () : 74-312-473 = -11 Supernode equation : - 7V1 + 4N2+ 9N3 = 28 Solving for NI = - 4.5Y -73 -STUDENTS-HUB.com Uploaded By: sondos hammad

Supernode equation by inspection 42  $\sqrt{3}$ 12 3. 125 86  $25+3 = (1+3)V_2 + (5+4)V_3 - (3+4)V_1$  $28 = 4V_2 + 9V_3 - 7V_1$ .74\_ Uploaded By: sondos hammad STUDENTS-HUB.com

Circuits with dependent sources \$ 12K 335 2mA KCL at node 1  $2I_{o} = \left(\frac{1}{12\kappa} + \frac{1}{6\kappa}\right)V_{1} - \frac{1}{6\kappa}$  $\sqrt{2}$  $T_{0} = \frac{V_{2}}{3\kappa}$  $= \left(\frac{1}{12\kappa} + \frac{1}{6\kappa}\right)^{1} + \left(\frac{2}{3\kappa} - \frac{1}{6\kappa}\right)^{1}$ KCL at node 2:  $2mA = -\frac{1}{6\kappa} \sqrt{1 + \left(\frac{1}{3\kappa} + \frac{1}{6\kappa}\right)} \sqrt{2}$ Solving for VI and V2, we get  $= -\frac{24}{5} \times \frac{12}{5} \times \frac{12}{$  $\neg$ .75. Uploaded By: sondos hammad STUDENTS-HUB.com

and the second second

Nodal Analysis : Supernode <u> 3 N</u> VI 42 SIR 22 IOA KCL at Supernode 1,2 :  $\left(\frac{1}{2}+\frac{1}{3}\right)V_{1}+\frac{1}{6}V_{2}-\frac{1}{6}V_{3}-\frac{1}{3}V_{4}$ 10 KCL at supernode 34 :  $= \left(\frac{1}{4} + \frac{1}{6}\right)^{1/3} + \left(\frac{1}{1} + \frac{1}{3}\right)^{1/3} - \frac{1}{6} \sqrt{2} - \frac{1}{3} \sqrt{1}$ Constrain equation : N1-N2 = 20 -76-Uploaded By: sondos hammad STUDENTS-HUB.com

Constrain equation: -13-14 = 3Vx = N1- V4 1×  $0 = 3V_{1} - V_{3} - 2V_{4}$ What is the current through the independent voltage Source ? \_77 Uploaded By: sondos hammad STUDENTS-HUB.com