

Discrete Chapter 2 :-

* ch 2.1 :-

Q₁ :

* if all algebraic expressions can be written in prefix notation, then $(a+2b)(a^2-b)$ can be written in prefix notation.

* All algebraic expressions " " " " " notation.
" " " " "

Q₂ : * If all prime numbers are odd, then 2 is odd.

Q₃ * My mind is shot or logic is confusing.

* " " " "

* Therefore, logic is confusing.

Q₄ if this function is polynomial then ---
if this function is diff
" " " " is cont

Q₅ (a) statement (c) statement
(b) sentence (d) sentence

Q₆ S: stocks are increasing
i: interest rates are steady

a) $S \wedge i$

b) $\sim S \wedge \sim i$

Q₇ $m \wedge \sim c$

Q₈ (a) $(h \wedge w) \wedge \sim s$
(b) $\sim w \wedge (h \wedge s)$

(c) $(\sim h \wedge \sim w) \wedge \sim s$

(d) $(\sim w \wedge \sim s) \wedge h$

(e) $w \wedge \sim (h \wedge s)$ (not $w \wedge \sim h \wedge \sim s$)

Q₉ $n \vee k \wedge \sim (n \wedge k)$

Q₁₀

p : DATAENDFlag is off
 q : error equals 0
 r : sum is less than 1000

(a) $p \wedge q \wedge r$

(c) $\sim p \vee (q \wedge r)$

(b) $p \wedge \sim q$

(c) $p \wedge (\sim q \vee \sim r)$

(d) $(\sim p \wedge q) \vee \sim r$

Q₁₁

inclusive, the statement can occur together.

Q₁₂

p	q	$\sim p$	$\sim p \wedge q$
T	T	F	F
T	F	F	F
F	T	T	T
F	F	T	F

Q₁₃

$\sim(p \wedge q) \vee (p \vee q)$

p	q	$(p \wedge q)$	$\sim(p \wedge q)$	$(p \vee q)$	$\sim(p \wedge q) \vee (p \vee q)$
T	T	T	F	T	T
T	F	F	T	T	T
F	T	F	T	T	T
F	F	F	T	F	T

Q₁₄ $p \wedge (q \wedge r)$

p	q	r	$(q \wedge r)$	$p \wedge (q \wedge r)$
T	T	T	T	T
T	T	F	F	F
T	F	T	F	F
T	F	F	F	F
F	T	T	T	F
F	T	F	F	F
F	F	T	F	F
F	F	F	F	F

Q₁₅ $p \wedge (\sim q \vee r)$

p	q	r	$\sim q$	$\sim q \vee r$	$p \wedge (\sim q \vee r)$
T	T	T	F	T	T
T	T	F	F	F	F
T	F	T	T	T	T
T	F	F	T	T	T
F	T	T	F	T	F
F	T	F	F	F	F
F	F	T	T	T	F
F	F	F	T	T	F

$$Q_{16} \quad p \vee (p \wedge q) \equiv p$$

p	q	$p \wedge q$	$p \vee (p \wedge q)$
T	T	T	T
T	F	F	T
F	T	F	F
F	F	F	F

$p \vee (p \wedge q)$ & p are logically eq since they have the same truth values in the truth table.

$$Q_{17} \quad \sim(p \wedge q) \stackrel{?}{=} \sim p \wedge \sim q$$

p	q	$\sim p$	$\sim q$	$(p \wedge q)$	$\sim(p \wedge q)$	$\sim p \wedge \sim q$
T	T	F	F	T	F	F
T	F	F	T	F	T	F
F	T	T	F	F	T	F
F	F	T	T	F	T	T

$\sim(p \wedge q)$ & $\sim p \wedge \sim q$ are not logically eq since they don't have the same truth values in the truth table

Q₁₈ $P \vee t$ and t

P	t	$P \vee t$
T	T	T
F	T	T

they are logically eq since they have the same truth values in the truth table.

Q₁₉ $P \wedge t \stackrel{?}{=} P$

P	t	$P \wedge t$
T	T	T
F	T	F

they're logically eq since they've the same truth values in the truth table

Q₂₀ $P \wedge C$ and $P \vee C$

P	C	$P \wedge C$	$P \vee C$
T	F	F	T
F	F	F	F

↳ they're not logically eq. since they don't have the same truth values in the truth table.

Q₂₁ $(P \wedge Q) \wedge R$ and $P \wedge (Q \wedge R)$

they're logically eq. since they've the same truth values in the truth table.

and Q₂₂ / Q₂₃ aren't logically eq & Q₂₄

Q₂₅ Hal isn't a major or Hal's sister isn't a computer science major.

Q₂₆ Sam isn't an orange belt or Kate isn't a red belt.

Q₂₇ The connector isn't loose and the machine isn't

Q₂₈ The units digits of 4^{67} isn't 4 and it isn't 6.

Q₂₉ This computer " " hasn't " " and it isn't being

Q₃₀ The dollar isn't " " or the stock market isn't " ".

Q₃₁ The train isn't late and my watch isn't ...

$$Q_{32} \quad -2 < x < 7 \Rightarrow \neg((-2 < x) \wedge (x < 7))$$

$$(-2 \geq x) \vee (x \geq 7)$$

$$Q_{33} \quad -10 < x < 2 \Rightarrow \neg((-10 < x) \wedge (x < 2))$$

$$= (-10 \geq x) \vee (x \geq 2)$$

$$Q_{34} \quad \neg(x < 2 \text{ or } x > 5) \Rightarrow x \geq 2 \wedge x \leq 5$$

$$= 2 \leq x \leq 5$$

$$Q_{35} \quad \neg(x \leq -1 \text{ or } x > 1) \Rightarrow x > -1 \wedge x \leq 1$$

$$= -1 < x \leq 1$$

$$Q_{36} \quad \neg(x \geq -3 \wedge x < 1) \Rightarrow (x < -3) \vee (x \geq 1)$$

$$Q_{37} \quad \neg(x \geq -7 \wedge x < 0) \Rightarrow (x < -7) \vee (x \geq 0)$$

$$Q_{38} \sim ((\text{num-orders} > 100 \wedge \text{num-instock} \leq 500) \vee \text{num-in} < 200)$$

$$(\text{num-orders} \leq 100 \text{ or } \text{num-in} > 500) \text{ and } \text{num-in} \geq 200$$

$$Q_{39} (\text{num-orders} \geq 50 \text{ or } \text{num-instock} \leq 300) \text{ and } (50 > \text{num-order} \geq 75 \text{ or } \text{num-instock} \leq 500)$$

$Q_{40} - Q_{43}$ skip

$$Q_{44} \quad x < 2 \text{ or it is not the case that } 1 < x < 3$$

$$\sim (1 < x < 3)$$

$$\sim (1 < x \wedge x < 3)$$

$$(x < 2) \vee (1 \geq x \vee x \geq 3)$$

$$x < 2 \vee 1 \geq x \vee x \geq 3$$

they are logically eq

Q_{45}

- Bob is a double math and computer science major and Ann is a math major, but Ann is not a double math and computer science major.
- It is not the case that both Bob and Ann are double math and computer science majors, but it is the case that Ann is a math major and Bob is a double math and computer science major.

idk
(later)

$$Q_{46} (a) \quad p \oplus q \equiv (p \vee q) \wedge \sim (p \wedge q)$$

$$p \oplus p \equiv (p \vee p) \wedge \sim (p \wedge p)$$

$$\equiv p \wedge \sim p$$

$$\equiv C$$

$$(p \oplus p) \oplus p \equiv c \oplus p \equiv (c \vee p) \wedge \sim(c \wedge p)$$

$$\equiv p \wedge t$$

$$\equiv p$$

$$(b) (p \oplus q) \oplus r \equiv p \oplus (q \oplus r)$$

$\oplus$ is associative $\Rightarrow$ then it's true

(c)

p	q	r	$p \oplus q$	$(p \oplus q) \wedge r$	$p \wedge r$	$q \wedge r$	$(p \wedge r) \oplus (q \wedge r)$
T	T	T	F	F	T	T	F
T	T	F	F	F	F	F	F
T	F	T	T	T	T	F	T
T	F	F	T	F	F	F	F
F	T	T	T	T	F	T	T
F	T	F	T	F	F	F	F
F	F	T	F	F	F	F	F
F	F	F	F	F	F	F	F

$$Q48 (p \wedge \sim q) \vee (p \vee q)$$

$$\equiv p \wedge (\sim q \vee q) \quad \text{Distributive law}$$

$$\equiv p \wedge (q \vee \sim q) \quad \text{Commutative law}$$

$$\equiv p \wedge t \quad \text{Negation law}$$

$$\equiv p \quad \text{identity law}$$

$$Q_{49} \quad (p \vee \sim q) \wedge (\sim p \vee \sim q)$$

$$\equiv (\sim q \vee p) \wedge (\sim q \vee \sim p) \quad \text{commutative law}$$

$$\equiv \sim q \vee (p \wedge \sim p) \quad \text{distributive law}$$

$$\equiv \sim q \vee C \quad \text{negation law}$$

$$\equiv \sim q \quad \text{identity law}$$

$$Q_{50} \quad (p \wedge \sim q) \vee p \equiv p$$

$$\equiv p \vee (p \wedge \sim q) \quad \text{commutative law}$$

$$\equiv p \quad \text{absorption law}$$

$$Q_{51} \quad p \wedge (\sim q \vee p)$$

$$\equiv p \wedge (p \vee \sim q) \quad \text{commutative law}$$

$$\equiv p \quad \text{absorption law}$$

$$Q_{52} \quad \sim(p \vee \sim q) \vee (\sim p \wedge \sim q)$$

$$\equiv (\sim p \wedge \sim(\sim q)) \vee (\sim p \wedge \sim q) \quad \text{De Morgan's law}$$

$$\equiv (\sim p \wedge q) \vee (\sim p \wedge \sim q) \quad \text{double negative law}$$

$$\equiv \sim p \wedge (q \vee \sim q) \quad \text{distributive law}$$

$$\equiv \sim p \wedge t \equiv \sim p \quad \text{negation law}$$

$$\equiv \sim p \quad \text{identity law}$$

$$Q_{53} \quad \sim((\sim p \wedge q) \vee (\sim p \wedge \sim q)) \vee (p \wedge q) \equiv p$$

$$\equiv \sim(\sim p \wedge q) \wedge \sim(\sim p \wedge \sim q) \vee (p \wedge q) \quad \text{De Morgan's law}$$

$$\equiv (\sim \sim p \vee \sim q) \wedge (\sim \sim p \vee \sim \sim q) \vee (p \wedge q) \quad \text{De Morgan's law (X2)}$$

$$\equiv (p \vee \sim q) \wedge (p \vee q) \vee (p \wedge q) \quad \text{double negative law}$$

$$\equiv p \vee (\sim q \wedge q) \vee (p \wedge q) \quad \text{distributive law}$$

$$\equiv p \vee (q \wedge \sim q) \vee (p \wedge q) \quad \text{commutative law}$$

$$\equiv (p \vee c) \vee (p \wedge q) \quad \text{Negation law}$$

$$\equiv p \vee (p \wedge q) \quad \text{identity law}$$

$$\equiv p \quad \text{Absorption law}$$

$$Q_{54} \quad (p \wedge (\sim(\sim p \vee q))) \vee (p \wedge q) \equiv p$$

$$\equiv (p \wedge (\sim \sim p \wedge \sim q)) \vee (p \wedge q) \quad \text{De Morgan's law}$$

$$\equiv (p \wedge (p \wedge \sim q)) \vee (p \wedge q) \quad \text{Double negative law}$$

$$\equiv ((p \wedge p) \wedge \sim q) \vee (p \wedge q) \quad \text{Associative law}$$

$$\equiv (p \wedge \sim q) \vee (p \wedge q) \quad \text{Idempotent law}$$

$$\equiv p \wedge (\sim q \vee q) \quad \text{distributive law}$$

$$\equiv p \wedge (q \vee \neg q)$$

commutative law

$$\equiv p \wedge (t)$$

Negation law

$$\equiv p$$

identity law

*Ch 2.2

Q₁ if the loop doesn't contain a stop or a go to, then it will repeat exactly N times.

Q₂ if I catch the 8:05 bus then I am on time for work.

Q₃ if you don't freeze then I'll shoot

Q₄ If you don't fix my ceiling then I won't pay my rent.

Q₅ $\neg p \vee q \rightarrow \neg q$

p	q	$\neg p$	$\neg q$	$\neg p \vee q$	$\neg p \vee q \rightarrow \neg q$
T	T	F	F	T	F
T	F	F	T	F	T
F	T	T	F	T	F
F	F	T	T	T	T

Q₆ $(p \vee q) \vee (\neg p \wedge q) \rightarrow q$

p	q	$\neg p$	$\neg q$	$(p \vee q)$	$(\neg p \wedge q)$	$(p \vee q) \vee (\neg p \wedge q)$	$(p \vee q) \vee (\neg p \wedge q) \rightarrow q$
T	T	F	F	T	F	T	T
T	F	F	T	T	F	T	F
F	T	T	F	T	T	T	T
F	F	T	T	F	F	F	T

skipped Q₇/8/9/10/11

Q₁₂ $(p \vee q) \rightarrow r \equiv (p \rightarrow r) \wedge (q \rightarrow r)$

if $\underbrace{x > 2}_p$ or $\underbrace{x < -2}_q$, then $\underbrace{x^2 > 4}_r$

if $x > 2$ then $x^2 > 4$ and if $x < -2$ then $x^2 > 4$

Q13 a. $p \rightarrow q \equiv \sim p \vee q$ (Done in the slides)

b. $\sim(p \rightarrow q) \equiv p \wedge \sim q$ (Done too)

Q14 a) $p \rightarrow q \vee r$, $p \wedge \sim q \rightarrow r$ and $p \wedge \sim r \rightarrow q$

$$\sim p \vee q \vee r \equiv \sim p \vee q \vee r \equiv \sim p \vee r \vee q$$

(they are logically eq by logical eq
truth table ~~can~~ exist)

b) if $\underbrace{n \text{ is prime}}_p$, then $\underbrace{n \text{ is odd}}_q$ or $\underbrace{n \text{ is 2}}_r$

$p \wedge \sim q \rightarrow r \Rightarrow$ if n is prime and n isn't odd then n is 2

$p \wedge \sim r \rightarrow q \Rightarrow$ if n is prime and n isn't 2 then n is odd

15 $p \rightarrow (q \rightarrow r)$ $(p \rightarrow q) \rightarrow r$

p	q	r	$q \rightarrow r$	$p \rightarrow (q \rightarrow r)$	$(p \rightarrow q)$	$(p \rightarrow q) \rightarrow r$
T	T	T	T	T	T	T
T	T	F	F	F	T	F
T	F	T	T	T	F	T
T	F	F	T	T	F	T
F	T	T	T	T	T	T
F	F	T	T	T	T	T
F	T	F	F	T	T	F
F	F	F	T	T	T	F

they are not logically
equivalent, since they don't
have the same truth
values in the truth table

Q16 p
 * if you paid full price, you didn't buy it at Crown Books
 * You didn't buy it at crown Books or you paid full price q
 (use truth table)
 $p \rightarrow q$
 $\neg q \wedge p$ they aren't logically eq

Q17
 (use truth table)
 * if 2 is a factor of n and 3 is a factor of n, then 6 is a factor of n.
 2 is not a factor of n or 3 is not a factor of n or 6 is a factor of n.

p: 2 is a factor of n
 q: 3 is a factor of n
 r: 6 is a factor of n
 $(p \wedge q) \rightarrow r \stackrel{?}{=} \neg p \vee \neg q \vee r$
 $\downarrow$
 $= \neg(p \wedge q) \vee r$
 $= \neg p \vee \neg q \vee r = \neg p \vee \neg q \vee r$
 then they are logically eq

Q18
 (use truth table)
 p: walks like a duck
 q: talks like a duck
 r: it is a duck

(1) $\Rightarrow (p \wedge q) \rightarrow r \Rightarrow \neg(p \wedge q) \vee r = \neg p \vee \neg q \vee r$
 (2) $\Rightarrow \neg p \vee \neg q \vee r$ then they're logically eq
 (3) $\Rightarrow (\neg p \wedge \neg q) \rightarrow \neg r$
 $\neg(p \wedge \neg q) \vee \neg r$
 $\neg p \vee \neg q \vee \neg r$ then they're not logically eq.

Q₁₉ False $\Rightarrow$ the negation $\Rightarrow$ Sue is Luiz's mother and Ali isn't his cousin.

Q₂₀ a. P is a square and P isn't a rectangle.

b. today is New Year's eve and tmw isn't january.

c. the decimal expansion of r is terminating and r isn't rational.

d. n is prime and n isn't odd and n isn't 2.

e. x is nonnegative and x isn't positive and x isn't 0

f. Tom is Ann's father and Jim isn't her uncle or Sue isn't her aunt.

g. n is divisible by 6 and n isn't divisible by 2 or n isn't divisible by 3.

Q₂₁ $P \rightarrow Q$ False

$\therefore P$ true

Q false

(a) $\neg P \rightarrow Q \Rightarrow$ true

(b) $P \vee Q \Rightarrow$ true

(c) $Q \rightarrow P \Rightarrow$ true

Q₂₂ (a) if P isn't a rectangle, then P isn't a square.

(b) if tmw isn't January, then today isn't New Year's Eve.

(c) if r isn't rational, then the decimal expansion of r isn't terminating

(d) if n is not odd and n isn't 2 then n isn't prime.

(e) if x isn't positive and x isn't zero then x isn't nonnegative

(f) if Jim isn't Ann's uncle or Sue isn't her aunt then Tom isn't her father.

(g) if n isn't divisible by 2 or n isn't divisible by 3 then n is not divisible by 6.

Q₂₃ (skip)

Q₂₄ $p \rightarrow q \equiv q \rightarrow p$ (24 is true)

p	q	$p \rightarrow q$	$q \rightarrow p$
T	T	T	T
T	F	F	T
F	T	T	F
F	F	T	T

they aren't logically eq since they don't have the same truth values.

Q₂₅

p	q	$p \rightarrow q$	$\sim p$	$\sim q$	$\sim p \rightarrow \sim q$
T	T	T	F	F	T
T	F	F	F	T	T
F	T	T	T	F	F
F	F	T	T	T	T

they're not logically eq since they don't have the same truth values

Q₂₆

p	q	$p \rightarrow q$	$\sim p$	$\sim q$	$\sim q \rightarrow \sim p$
T	T	T	F	F	T
T	F	F	F	T	F
F	T	T	T	F	T
F	F	T	T	T	T

they are logically eq since they have the same truth values

Q₂₇

p	q	$\sim p$	$\sim q$	$q \rightarrow p$	$\sim p \rightarrow \sim q$
T	T	F	F	T	T
T	F	F	T	F	F
F	T	T	F	T	T
F	F	T	T	T	T

they are logically eq since they have the same truth values

Q₂₉ $p \rightarrow (q \vee r) \equiv (p \wedge \neg q) \rightarrow r$

p	q	$\neg q$	$p \wedge \neg q$	$q \vee r$	$p \rightarrow (q \vee r)$	$(p \wedge \neg q) \rightarrow r$	$p \rightarrow (q \vee r) \leftrightarrow (p \wedge \neg q) \rightarrow r$
T	T	F	F	T	T	T	T
T	T	F	F	T	T	T	T
T	F	T	T	T	T	T	T
T	F	T	T	F	F	F	T
F	T	F	F	T	T	T	T
F	T	F	F	F	T	T	T
F	F	T	F	T	T	T	T
F	F	T	F	F	T	T	T

(tautology)

they are logically eq since they have the same truth values

Q₃₀ (سؤال)

Q₃₁ $p \rightarrow (q \rightarrow r) \equiv (p \wedge q) \rightarrow r$

p	q	$\neg q$	$p \wedge q$	$q \rightarrow r$	$p \rightarrow (q \rightarrow r)$	$(p \wedge q) \rightarrow r$	$p \rightarrow (q \rightarrow r) \leftrightarrow (p \wedge q) \rightarrow r$
T	T	F	T	T	T	T	T
T	T	F	T	F	F	F	T
T	F	T	F	T	T	T	T
T	F	T	F	F	T	T	T
F	T	F	F	T	T	T	T
F	T	F	F	F	T	T	T
F	F	T	F	T	T	T	T
F	F	T	F	F	T	T	T

tautology

they are logically eq since they're the same truth values

Q₃₂ if This quadratic eq has two distinct real roots then its discriminant is greater than zero and if this quadratic eq's discriminant is greater than zero then it has two distinct real roots.

Q₃₃ if This integer is even, then it equals twice some integer and if this integer equals twice some integer then it is even.

Q₃₄+35+36 skip

Q37 if a new hearing isn't granted then payment will be made on the fifth

Q38 if it doesn't rain, then Anna 'll go

Q39 If a security code isn't entered, then this door will not open.

Q40 if we catch the 8:05 bus, then we are on time for work

Q41 if a triangle has two 45° angles, then this triangle is a right angle

Q42 if this num isn't divisible by 8 then it isn't divisible by 9
if this num is divisible by 9 then it's divisible by 8.

Q43 if Jim doesn't do his hw regularly then he won't pass the course.

OR If Jim passes the course then he did his hw regularly

Q44 if John's team win the rest of the championship's games then they will win the championship.

Q45 if the computer program doesn't produce error messages during translation then this comp-program is correct.

Q46 if compound x is ^pboiling, then its temp must ^qbe at least 150°C .

(a) $q \rightarrow p$ (false) or not necessarily true

(b) $\sim q \rightarrow \sim p$ (contrapositive) true

(c) $p \rightarrow q$ (true)

(d) $\sim p \rightarrow \sim q$ (false) or not necessarily true

(e) $\sim q \rightarrow \sim p$ (true)

(f) $q \rightarrow p$ (false) or not necessarily true

$$p \rightarrow q \equiv \sim p \vee q \quad / \quad p \leftrightarrow q \equiv (p \rightarrow q) \wedge (q \rightarrow p) \\ (\sim p \vee q) \wedge (\sim q \vee p)$$

$$Q_{47} \quad p \wedge \sim q \rightarrow r$$

$$\equiv \sim(p \wedge \sim q) \vee r$$

$$(a) \equiv \sim p \vee q \vee r \quad \xRightarrow{(b)} \sim(p \wedge \sim q \wedge \sim r)$$

$$Q_{48} \quad (p \vee \sim q) \rightarrow r \vee q$$

$$(a) \quad \sim(p \vee \sim q) \vee (r \vee q)$$

$$\sim(\sim(\sim p \wedge q) \vee \sim(\sim r \wedge \sim q))$$

$$(b) \quad \sim(\sim(\sim p \wedge q) \wedge (\sim r \wedge \sim q))$$

$$Q_{49} \quad (p \rightarrow r) \leftrightarrow (q \rightarrow r)$$

$$(\sim p \vee r) \leftrightarrow (\sim q \vee r)$$

$$(\sim p \vee r) \rightarrow (\sim q \vee r) \wedge (\sim q \vee r) \rightarrow (\sim p \vee r)$$

$$(a) \quad (\sim(\sim p \vee r) \vee (\sim q \vee r)) \wedge (\sim(\sim q \vee r) \vee (\sim p \vee r))$$

$$((p \wedge \sim r) \vee (\sim q \vee r)) \wedge ((q \wedge \sim r) \vee (\sim p \vee r))$$

$$Q_{50} \quad (p \rightarrow (q \rightarrow r)) \leftrightarrow ((p \wedge q) \rightarrow r)$$

$$(p \rightarrow (\sim q \vee r)) \leftrightarrow (\sim(p \wedge q) \vee r)$$

$$\sim p \vee (\sim q \vee r) \leftrightarrow (\sim p \vee \sim q \vee r)$$

$$(\sim p \vee \sim q \vee r) \leftrightarrow (\sim p \vee \sim q \vee r)$$

$$(\sim p \vee \sim q \vee r) \rightarrow (\sim p \vee \sim q \vee r) \wedge (\sim p \vee \sim q \vee r) \rightarrow (\sim p \vee \sim q \vee r)$$

$$(a) \quad \sim(\sim p \vee \sim q \vee r) \vee (\sim p \vee \sim q \vee r) \wedge \sim(\sim p \vee \sim q \vee r) \vee (\sim p \vee \sim q \vee r)$$

$$(b) \sim \left(\sim (p \wedge q \wedge \sim r) \wedge (p \wedge q \wedge \sim r) \right) \wedge \sim \left(\sim (p \wedge q \wedge \sim r) \wedge (p \wedge q \wedge \sim r) \right)$$

Q51 Yes

Ch 2.3

Q₁ $\sqrt{2}$ is not rational

Q₂ $1 - 0.99999\ldots$ is less than every positive real num

Q₃ logic isn't easy.

Q₄ This figure is a quadrilateral.

Q₅ They didn't telephoned.

Q₆

premises		conclusion
p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

critical rows

← false

this argument form is invalid since the conclusion is false at one critical row

Q₇ p
 $p \rightarrow q$

$\neg q \vee r$
 $\therefore r$

premises					conclusion
p	q	r	$\neg q$	$p \rightarrow q$	$\neg q \vee r$
T	T	T	F	T	T
T	T	F	F	T	F
T	F	T	T	F	T
T	F	F	T	F	T
F	T	T	F	T	T
F	T	F	F	T	F
F	F	T	T	T	T
F	F	F	T	T	F

critical row

this argument form is valid since the conclusion is true for the critical row

Q₈

premises				conclusion
p	q	r	$\neg q$	$\neg$
T	T	T	F	T
T	T	F	F	F
T	F	T	T	T
T	F	F	T	F
F	T	T	F	T
F	T	F	F	F
F	F	T	T	T
F	F	F	T	F

critical rows

this argument form is invalid since it has a false conclusion for one critical row.

Q₉ $p \wedge q \rightarrow \sim r$
 $p \vee \sim q$
 $\sim q \rightarrow p$
 $\sim r$

premises						conclusion			
p	q	r	$\sim q$	$\sim r$	$p \wedge q$	$p \wedge q \rightarrow \sim r$	$p \vee \sim q$	$\sim q \rightarrow p$	$\sim r$
T	T	T	F	F	T	F	T	T	F
T	T	F	F	T	T	T	T	T	T
T	F	T	T	F	F	T	T	T	F
T	F	F	T	T	F	T	T	T	T
F	T	T	F	F	F	T	F	F	F
F	T	F	F	T	F	T	F	T	T
F	F	T	T	F	F	T	T	F	F
F	F	F	T	T	F	T	T	T	T

critical rows

This argument form is invalid since the conclusion is false for one critical row

Q₁₀ $p \rightarrow r$
 $q \rightarrow r$
 $p \vee q \rightarrow r$

premises				conclusion
p	q	r	$p \vee q$	$(p \vee q) \rightarrow r$
T	T	T	T	T ✓
T	T	F	T	F
T	F	T	T	T ✓
T	F	F	T	F
F	T	T	T	T ✓
F	T	F	T	F
F	F	T	F	T ✓
F	F	F	F	T ✓

critical rows

this argument form is valid since the conclusion is true for all critical rows

Q11

							premises		conclusion
p	q	r	$\sim q$	$\sim r$	$\sim p$	$q \vee r$	$p \rightarrow q \vee r$	$\sim q \vee \sim r$	$\sim p \vee \sim r$
T	T	T	F	F	F	T	T	F	F
T	T	F	F	T	F	T	T	T	T ✓
T	F	T	T	F	F	F	F	T	F x
T	F	F	T	T	F	F	F	T	T
F	T	T	F	F	T	T	T	F	T ✓
F	T	F	F	T	T	T	T	T	T ✓
F	F	T	T	F	T	T	T	T	T ✓
F	F	F	T	T	T	F	T	T	T ✓

critical rows

This argument is invalid since the conclusion is false for one critical row

Q12 to Q21 skip (in the notes)

↳ check (converse & inverse error)

Q22 Tom on team A: TA

Hua on team B: HB

$\sim TA \rightarrow HB$	TA	HB	$\sim TA$	$\sim HB$	premises		conclusion
$\sim HB \rightarrow TA$					$\sim TA \rightarrow HB$	$\sim HB \rightarrow TA$	$\sim TA \vee \sim HB$
$\sim TA \vee \sim HB$	T	T	F	F	T	T	F x
	T	F	F	T	T	T	T ✓
	F	T	T	F	T	T	T ✓
	F	F	T	T	F	F	T

critical row

This argument is invalid since the conclusion is false for one critical row

Q23

Oleg is math major: OM

Oleg is an Economics major: OE

Oleg is required to take Math362: OR

argument form: - OM $\vee$ OE
OM $\rightarrow$ OR
 $\therefore$ OE $\vee$ $\sim$ OR

$\Rightarrow$ (Do the truth table / it's valid)

Q24 rules solved $\Rightarrow p$
rules obtained answer $2 \Rightarrow q$

$p \rightarrow q$
 q
 $\therefore p$

This argument is invalid (converse error)

Q25 real num is rational : p
" " " irrational : q

argument form:
 $p \vee q$
 $\sim p$
 q

valid argument
(elimination)

Q26 go to movie : M $M \rightarrow \sim HW$
Finish hw : HW $\sim HW \rightarrow \sim E$
do well on exam : E $\therefore M \rightarrow \sim E$

This argument form is valid
(Transitivity)

Q27 num > 2 : N $N \rightarrow S$
 $(num)^2 > 4$: S $\sim N$
 $\therefore \sim S$ (invalid argument) (inverse error)

Q28 there are many rational ... : RN
the set of irrational num is infinite : II

$RN \rightarrow II$
 II (invalid argument)
 RN (converse error)

Q29 2 num divisible by 6 $\Rightarrow N6$
product of two " " $\Rightarrow P6$

$N6 \rightarrow P6$
 $\sim N6$ (invalid argument)
 $\sim P6$ (inverse error)

Q30 Computer prog is correct : CC
produce correct output : CO

$CC \rightarrow CO$
 CO
 $\therefore CC$

this is invalid argument form
(converse error)

Q31 Sandra knows Java : SJ
Sandra knows C++ : SC

$SJ \wedge SC$
 $\therefore SC$

(valid argument)
(specialization)

Q32 Christmas Bonus : CB
 Buy Stereo : BS
 Sell motorcycle : SM

CB $\rightarrow$ BS
 SM $\rightarrow$ BS
 $\therefore (CB \vee SM) \rightarrow BS$

(valid argument
 (proof by division
 into cases)

Q32 - Q35 (skip)

Q26 Undeclared Variable $\Rightarrow$ UV
 Three syntax errors $\Rightarrow$ SE
 missing semi colon $\Rightarrow$ MS
 misspelled Variable Name $\Rightarrow$ MV

UV $\vee$ SE $\rightarrow$ false
 $\downarrow$ SE $\rightarrow (MS \vee MV)$
 $\downarrow$ false
 $\sim MS$
 $\sim MV$
 $\therefore UV$

Q34
 $HL \rightarrow \boxed{\sim KT}$ true
 $\downarrow$ false
 $\boxed{TFY} \rightarrow \boxed{KT}$ false
 $HL \rightarrow$ true
 $\downarrow$ false
 $\boxed{TFY} \vee \boxed{TB}$ true
 $TBY \rightarrow TG$
 $\downarrow$
 $\sim TFX$

$HL \rightarrow \sim KT$
 HL

$\therefore \sim KT$ modus ponens

$TFY \rightarrow KT$
 $\sim KT$

$\therefore \sim TFX$ modus tollens

41. a. $\sim p \vee q \rightarrow r$
 b. $s \vee \sim q$
 c. $\sim t$
 d. $p \rightarrow t$
 e. $\sim p \wedge r \rightarrow \sim s$
 f. $\therefore \sim q$

42. a. $p \vee q$
 b. $q \rightarrow r$
 c. $p \wedge s \rightarrow t$
 d. $\sim r$
 e. $\sim q \rightarrow u \wedge s$
 f. $\therefore t$

43. a. $\sim p \rightarrow r \wedge \sim s$
 b. $t \rightarrow s$
 c. $u \rightarrow \sim p$
 d. $\sim w$
 e. $u \vee w$
 f. $\therefore \sim t$

44. a. $p \rightarrow q$
 b. $r \vee s$
 c. $\sim s \rightarrow \sim t$
 d. $\sim q \vee s$
 e. $\sim s$
 f. $\sim p \wedge r \rightarrow u$
 g. $w \vee t$
 h. $\therefore u \wedge w$

Q41
 ~~$\sim p \vee q \rightarrow \sim$~~
 $s \vee \sim q$
 ~~$\sim t$~~
 ~~$p \rightarrow t$~~
 ~~$\sim p \wedge r \rightarrow \sim s$~~

① $p \rightarrow t$
 $\sim t$
 $\therefore \sim p$
 modus tollens

② $\sim p$
 $\therefore \sim p \vee q$
 Generalization

③ $\sim p \vee q \rightarrow r$
 $\sim p \vee q$
 $\therefore r$ modus ponens

$$\textcircled{4} \quad \begin{array}{c} \sim p \\ r \end{array}$$

$\therefore r \wedge \sim p \Rightarrow$ conjunction rule

$$\textcircled{5} \quad \begin{array}{c} r \wedge \sim p \rightarrow \sim s \\ r \wedge \sim p \\ \hline \therefore \sim s \end{array}$$

$$\textcircled{6} \quad \begin{array}{c} s \vee \sim q \\ \sim s \\ \hline \therefore \sim q \end{array} \quad \begin{array}{l} \text{elimination} \\ \text{rule} \end{array} \Rightarrow \text{conclusion}$$

42. a. ~~$p \vee q$~~
 b. ~~$q \rightarrow r$~~
 c. $p \wedge s \rightarrow t$
 d. ~~r~~
 e. ~~$\sim q \rightarrow u$~~ ~~$\sim s$~~
 f. $\therefore t$

$$\textcircled{1} \quad \begin{array}{c} q \rightarrow r \\ \sim r \\ \hline \therefore \sim q \end{array} \quad \text{modus tollens}$$

$$\textcircled{4} \quad \begin{array}{c} p \vee q \\ \sim q \\ \hline \therefore p \end{array} \quad \text{elimination}$$

$$\textcircled{2} \quad \begin{array}{c} \sim q \rightarrow u \wedge s \\ \sim q \\ \hline \therefore u \wedge s \end{array} \quad \text{modus ponens}$$

$$\textcircled{5} \quad \begin{array}{c} s \\ p \\ \hline \therefore p \wedge s \end{array} \quad \text{conjunction}$$

$$\textcircled{3} \quad \begin{array}{c} u \wedge s \\ \hline \therefore s \end{array} \quad \text{specialization}$$

$$\textcircled{6} \quad \begin{array}{c} p \wedge s \rightarrow t \\ p \wedge s \\ \hline \therefore t \end{array} \quad \text{modus ponens}$$

43. a. ~~$\sim p \rightarrow \sim r$~~ ~~$\sim s$~~
 b. $t \rightarrow s$
 c. ~~$u \rightarrow \sim p$~~
 d. ~~$\sim u$~~
 e. ~~$u \vee \sim w$~~
 f. $\therefore \sim t$

$$\textcircled{1} \quad \begin{array}{c} u \vee w \\ \sim w \\ \hline \therefore u \end{array} \quad \text{by elimination Rule}$$

$$\textcircled{2} \quad \begin{array}{c} u \rightarrow \sim p \\ u \\ \hline \therefore \sim p \end{array} \quad \text{by modus ponens}$$

$$\textcircled{3} \quad \begin{array}{c} \sim p \rightarrow r \wedge \sim s \\ \sim p \\ \hline \therefore r \wedge \sim s \end{array} \quad \text{modus ponens}$$

$$\textcircled{4} \quad \begin{array}{c} r \wedge \sim s \\ \hline \therefore \sim s \end{array} \quad \text{by specialization rule}$$

$$\textcircled{5} \quad \begin{array}{c} t \rightarrow s \\ \sim s \\ \hline \therefore \sim t \end{array} \quad \text{by modus tollens}$$

44. a. $p \rightarrow q$

b. $r \vee s$

c. $\neg s \rightarrow \neg t$

d. $\neg q \vee s$

e. $\neg s$

f. $\neg p \wedge r \rightarrow u$

g. $w \wedge t$

h. $\therefore u \wedge w$

① $\neg s \rightarrow \neg t$

$\neg s$
 $\therefore \neg t$ modus ponens

② $w \vee t$

$\neg t$
 $\therefore w$ elimination Rule

③ $\neg \vee s$

$\neg s$
 $\therefore \neg$ elimination Rule

④ $\neg q \vee s$

$\neg s$
 $\therefore \neg q$ elimination Rule

⑤ $p \rightarrow q$

$\neg q$
 $\therefore \neg p$ modus tollens

⑥ $\neg p$

$\neg$
 $\therefore \neg p \wedge \neg$ conjunction

⑦ $\neg p \wedge \neg \rightarrow u$

$\neg p \wedge \neg$
 $\therefore u$ modus ponens

⑧

u
 w
 $\therefore u \wedge w$ conjunction Rule