

Lecture

7.5

15, 58, 67

Discussion

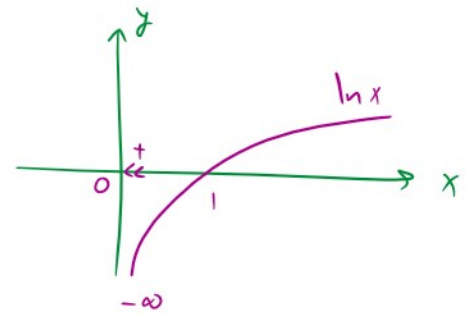
12, 16, 27, 33, 38, 41, 46, 52, 56, 60, 68, 72

Indeterminate forms: $\frac{0}{0}, \frac{\infty}{\infty}, \infty \cdot 0, \infty - \infty, 0^0, 1^\infty, \infty^0$

$\lim f(x) = \lim e$

$$(33) \lim_{x \rightarrow 0^+} \frac{\ln(x^2 + 2x)}{\ln x}$$

$$\frac{\ln 0^+}{\ln 0^+} = \frac{-\infty}{-\infty} = \frac{\infty}{\infty}$$

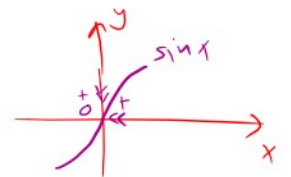


$$\lim_{x \rightarrow 0^+} \frac{\frac{2x+2}{x^2+2x}}{\frac{1}{x}} = \lim_{x \rightarrow 0^+} \frac{2x^2+2x}{x^2+2x} = \frac{0}{0}$$

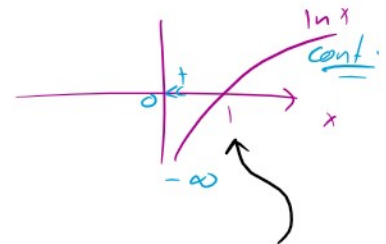
$$= \lim_{x \rightarrow 0^+} \frac{4x+2}{2x+2} = \frac{0+2}{0+2} = \frac{2}{2} = 1$$

$$(38) \lim_{x \rightarrow 0^+} (\ln x - \ln \sin x)$$

$$\ln 0^+ - \ln 0^+ = -\infty - (-\infty) = \infty - \infty$$



$$\lim_{x \rightarrow 0^+} \ln \frac{x}{\sin x}$$



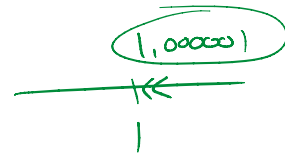
$$\ln \left(\lim_{x \rightarrow 0^+} \frac{x}{\sin x} \right) = \ln \lim_{x \rightarrow 0^+} \frac{1}{\cos x} = \ln 1 = 0$$

$$= \ln 1 = \boxed{0}$$

52 $\lim_{x \rightarrow 1^+} \frac{\frac{1}{x-1}}{x}$

$\frac{1}{\text{small}^+} = \infty$

$f(x)$



$$\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^+} e^{\ln f(x)} = \lim_{x \rightarrow 1^+} e^{\ln \frac{1}{x-1}} = \lim_{x \rightarrow 1^+} e^{\frac{1}{x-1} \ln x}$$

$$= \lim_{x \rightarrow 1^+} e^{\frac{\ln x}{x-1}}$$

$$= e^{\lim_{x \rightarrow 1^+} \frac{\ln x}{x-1}}$$

$\frac{0}{0}$

$$= e^{\lim_{x \rightarrow 1^+} \frac{\frac{1}{x}}{1}} = e^1 = \boxed{e}$$

