

# chapter 8

## Speed Regulation

↪ shaft speed  $\omega_m$

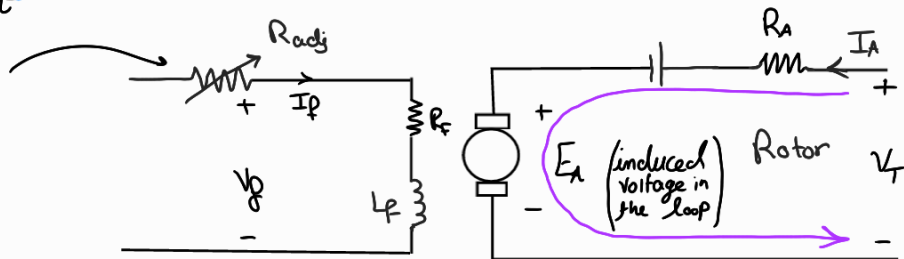
$$SR = \frac{\omega_{m,nl} - \omega_{m,fl}}{\omega_{m,fl}} \times 100\%$$

$$SR = \frac{n_{m,nl} - n_{m,fl}}{n_{m,fl}} \times 100\%$$

- SR should be + but can be negative in **Runaway**: motor لا يوقف
- In this case vibration causes stator to hit Rotor since air gap is small or (see lecture)

## Types of DC motors

1. Permanent magnet
2. Separately excited
3. Shunt
4. Series
5. Compound



$$I_L = I_A$$

$$I_F = \frac{V_F}{R_F + R_{fd}}$$

- If can be controlled

$$e_{ind} = K \phi \omega$$

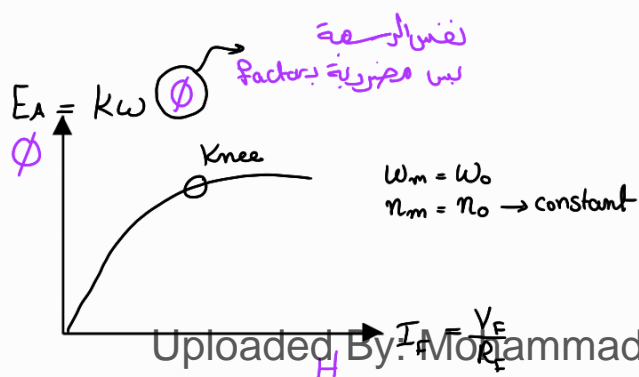
$$\tau_{ind} = K \phi I_A$$

$$V_t + I_A R_A + E_A = 0$$

} Equations needed for Analysis

## Magnetization Curve

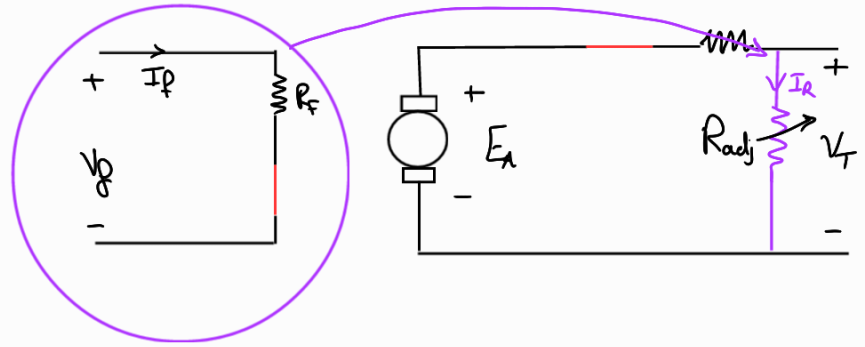
→ we find rated value from if



## Shunt DC motor

At:  $V_f = V_T$

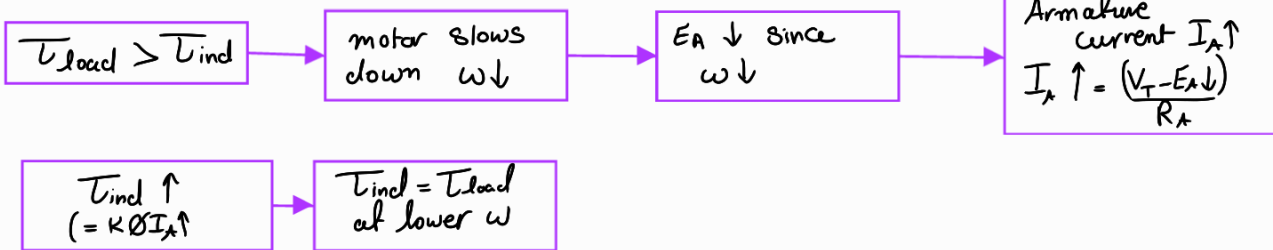
يعني يتصل حالة خاصة من  
separately excited



$I_L = I_A + I_F$

\* How does a shunt DC motor respond to a load?

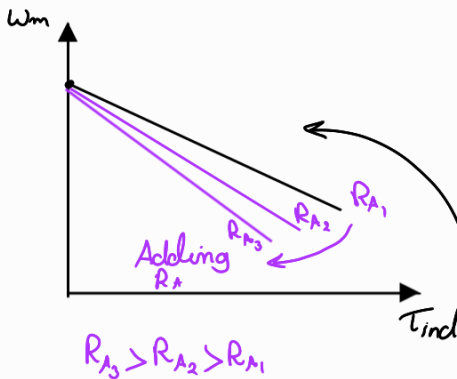
→ If load increased



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The terminal characteristics of a shunt DC motor & separately excited motor

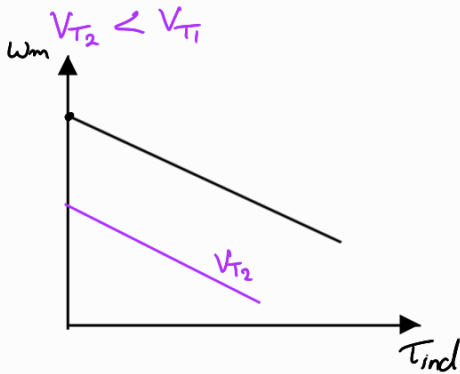
$$\omega = \frac{V_T}{k\phi} - \frac{R_A T_{ind}}{(k\phi)^2}$$



Parameter that controls the DC motor speed

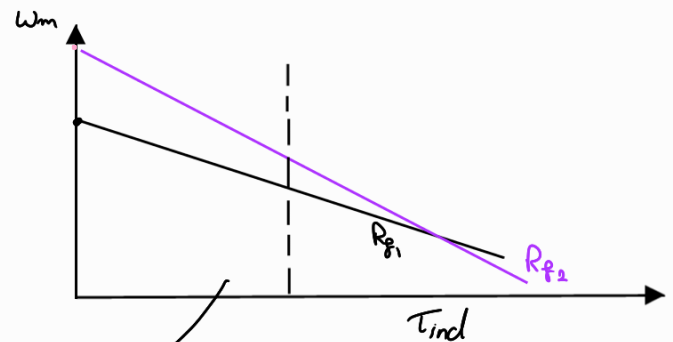
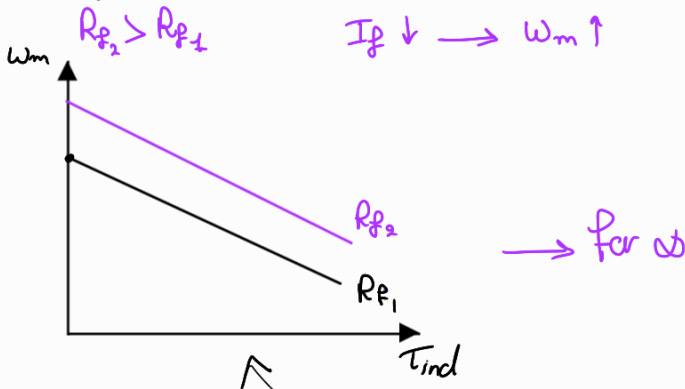
- Terminal voltage of Armature
- Flux by adjusting  $R_f$
- $R_A$  by adding External resistance ( $R_{adj}$  is connected on series) meaning that Electrical losses are increased and energy is less so less common method

Decreasing  $V_T$



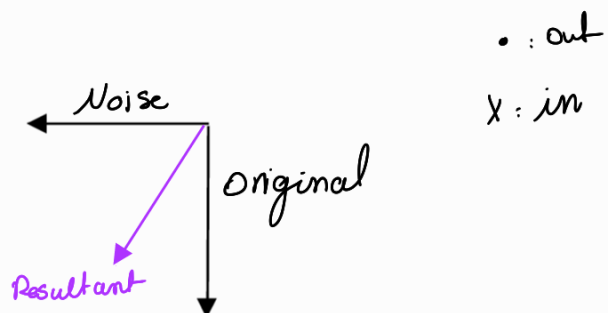
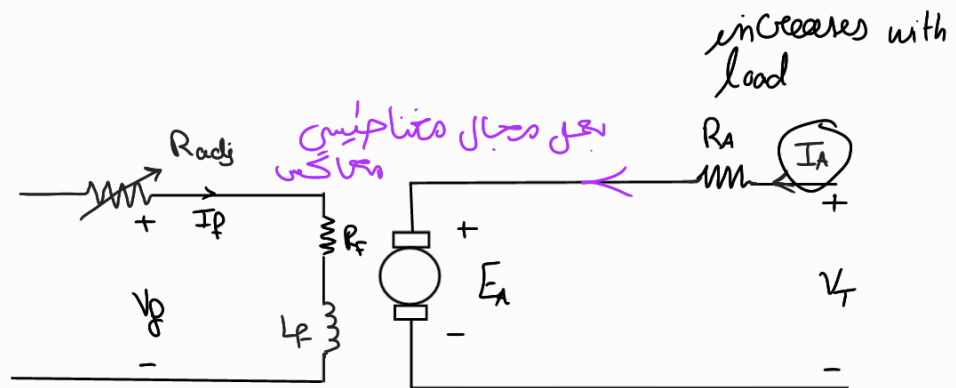
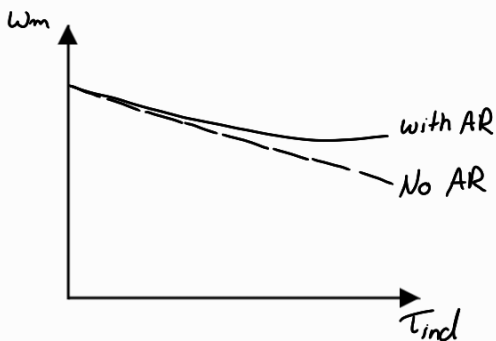
Note: Relation between flux and  $\omega_m$  is not linear

Changing  $\Phi \rightarrow R_f$



Armature Reaction

Noise Magnetic field



- A compensating windings are introduced to reverse the armature windings and so it is neglected

## Changing $R_F$ or $\phi$

1.	Increasing $R_F$ causes $I_F$ to decrease.	$I_F \downarrow = V_T / R_F \uparrow$
2.	Decreasing $I_F$ , $\Rightarrow$ decreases $\phi$	-
3.	Decreasing $\phi$ lowers $E_A$ instantaneously.	$E_A \downarrow = K\phi \downarrow \omega$
4.	Decreasing $E_A$ causes $I_A$ to increase.	$I_A \uparrow = (V_T - E_A \downarrow) / R_A$
5.	Increasing $I_A$ , $\Rightarrow$ increases $\tau_{ind}$ Note: $I_A \uparrow$ predominates over $\phi \downarrow$ .	$\tau_{ind} \uparrow = K\phi \downarrow I_A \uparrow$
6.	Increasing $\tau_{ind}$ causes $\tau_{ind} > \tau_{load}$ hence motor speeds up ( $\omega \uparrow$ ).	-
7.	Since $\omega \uparrow$ , $E_A$ increases again.	$E_A \uparrow = K\phi \omega \uparrow$
8.	Increasing $E_A$ causes $I_A$ to decrease.	$I_A \downarrow = (V_T - E_A \uparrow) / R_A$
9.	Decreasing $I_A$ causes $\tau_{ind}$ to decrease until $\tau_{ind} = \tau_{load}$ at a higher speed $\omega$	$\tau_{ind} \downarrow = K\phi I_A \downarrow$

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بجهد اكتر  
يأثر أكثر

Example 8-1

input current =  $I_L$

$$P_{conv} = E_A I_A = \tau_{ind} \omega_m$$

$$E_{A0} = K\phi\omega_0 \quad , \quad E_{A1} = K\phi\omega_1$$

under no load

At no load  $E_{A0} = V_T$

## Changing terminal voltage

1.	Increasing $V_A$ causes $I_A$ to increase.	$I_A \uparrow = (V_A \uparrow - E_A) / R_A$
2.	Increasing $I_A$ , $\Rightarrow$ increases $\tau_{ind}$	$\tau_{ind} = K\phi I_A \uparrow$
3.	Increasing $\tau_{ind}$ causes $\tau_{ind} > \tau_{load}$ hence motor speeds up ( $\omega \uparrow$ ).	-
4.	Since $\omega \uparrow$ , $E_A$ increases.	$E_A \uparrow = K\phi \omega \uparrow$
5.	Increasing $E_A$ causes $I_A$ to decrease.	$I_A \downarrow = (V_T - E_A \uparrow) / R_A$
6.	Decreasing $I_A$ causes $\tau_{ind}$ to decrease until $\tau_{ind} = \tau_{load}$ at a higher speed $\omega$ .	$\tau_{ind} \downarrow = K\phi I_A \downarrow$

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## Examples solving

### Example 8-3

Rated power = 100 hp

compensating windings  $\rightarrow$  Armature reaction is ignored

line current = 126 A =  $I_L$

If load is changed:  $I_A$  stays constant Special Case

$$1. I_{A1} = I_L - I_F$$

$$= 126 - \frac{250}{41.67} = 120 \text{ A}$$

$$E_{A1} = (R_A)(I_A) + 250$$

$$= 250 - (120)(0.03)$$

$$E_A = 246 \text{ V}$$

$$\text{If } R_F = 50$$

Since  $I_A$  is constant  $\rightarrow E_{A1} = E_{A2} = 246.4$

$$\frac{E_{A1}}{E_{A2}} = \frac{K \Phi_1 n_1}{K \Phi_2 n_2} \rightarrow 1 = \frac{\Phi_1}{\Phi_2} \frac{n_1}{n_2} \rightarrow n_2 = \frac{\Phi_1}{\Phi_2} n_1$$

we need this

In Magnetization curve

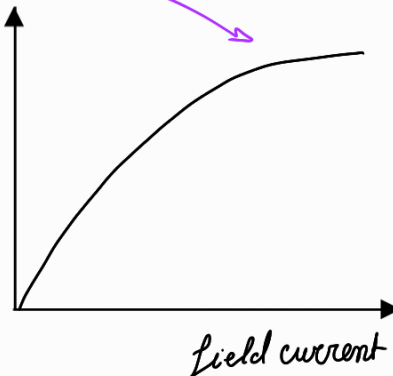
$$\text{At } I_{F1} = 6 \text{ A} \rightarrow E_{A1} = 268 \text{ V}$$

$$\text{At } I_{F2} = 5 \text{ A} \rightarrow E_{A2} = 250 \text{ V}$$

Curve values are at 1200

$$\frac{\Phi_1}{\Phi_2} = \frac{268}{250} = 1.076 \rightarrow \text{neglect 1200 RPM open circuit voltage}$$

$$n_2 = 1.076 (1103) = 1187 \text{ RPM}$$



Note:

$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

For a Motor

$P_{out} = P_{given}$  if

• At Full load conditions

$$P_{out} = P_{conv} - P_{core} - P_{losses}$$

if other conditions

### Example 8-1

$$V_A = 250V$$

$$I_A = 120A$$

$$n = 1103$$

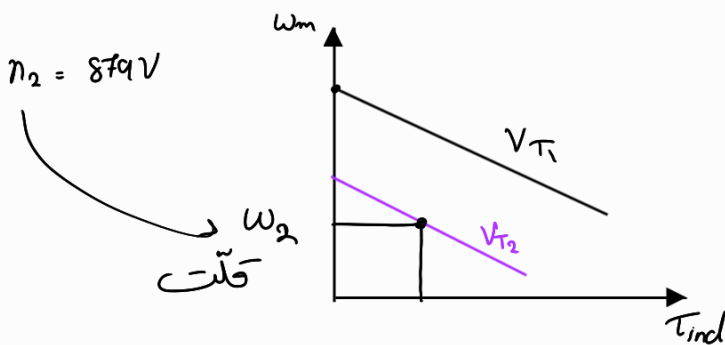
Speed if  $V_A$  is reduced to 200V?

$$E_{A1} = 246.4V \text{ at}$$

$$E_{A2} = 200 - (120)(0.03) = 196.4V$$

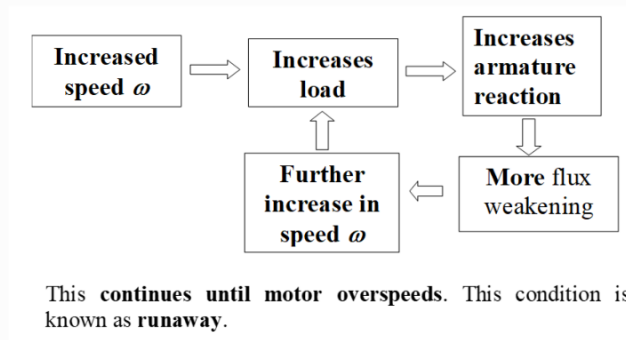
$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

$$n_2 = 879V$$



### Open field circuit

- If field circuit is disconnected → motor speed increases and becomes uncontrollable → **Runaway Condition**



To stop this:

$V_T$  is shut downed or else the motor will be damaged from high current or vibration

### The permanent Magnet DC motor

Disadvantage : I can't control the flux  
Natural magnet losses its properties with time

Advantages: 1. No external field circuit is required → no field circuit  
Copper losses  
2. Smaller because no field circuit

To control speed for this motor:

1. Armature voltage control
2. Armature resistance control

# Torque Speed characteristics of series DC motor

Note

$$P_m = V_T I_L$$

$$V_T = E_A + I_A (R_A + R_S)$$

$$T \propto \omega$$

$$T_{ind} = K \Phi I_A$$

$$\Phi = C I_A$$

$$T_{ind} = K C I_A^2 \quad \text{Non-linear Relationship}$$

$$I_A = \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} \quad \text{اي نفيس في ال current معطى تا حالي}$$

ادل ما اشد معطى تا حالي  
High starting current

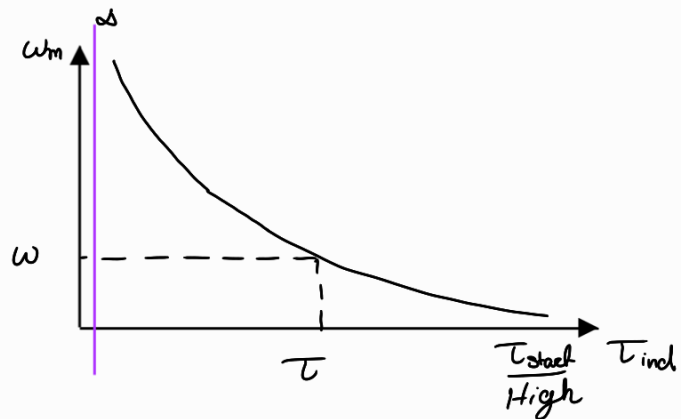
$$V_T = K \Phi \omega + \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)$$

$$\Phi = \frac{\sqrt{C}}{\sqrt{K}} \frac{\sqrt{T_{ind}}}{\sqrt{R_A + R_S}}$$

$$V_T = \frac{\sqrt{K}}{\sqrt{K}} \frac{\sqrt{C} \sqrt{T_{ind}}}{\sqrt{K}} \omega + \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)$$

$$\frac{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}}{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}} \omega = V_T - \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)$$

$$\omega = \frac{V_T}{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}} - \frac{R_A + R_S}{K C}$$



## Disadvantage of this motor

At light load (no load) speed goes to ∞

So we cannot start the motor with no load + can't take load off suddenly

See slide 44 (from lecture)

We control it by changing terminal voltage

### Example 8-5

$$E_A = V_T - I_A (R_A + R_S)$$

$$= 250 - 50(0.08) = 246 \text{ V}$$

$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

$$\text{Magnetomotive force} = 25 \times 50 = 1250$$

$$\text{So } E_{A2} \approx 80$$

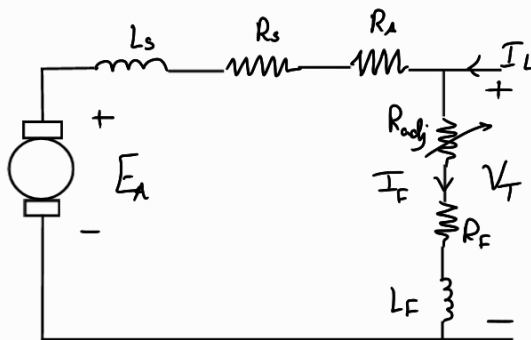
$$n_2 = \left( \frac{246}{80} \right) (1200) = 3690 \text{ RPM}$$

$$\tau_{ind} = \frac{P}{\omega} = \frac{E_A I_A}{\omega} = \frac{(246)(50)}{\frac{3690 \times 2\pi}{60}} = 31.85 \text{ N.m}$$

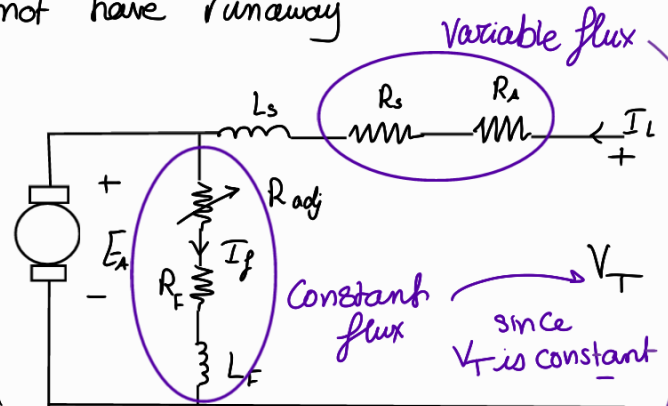


## The compounded DC motor

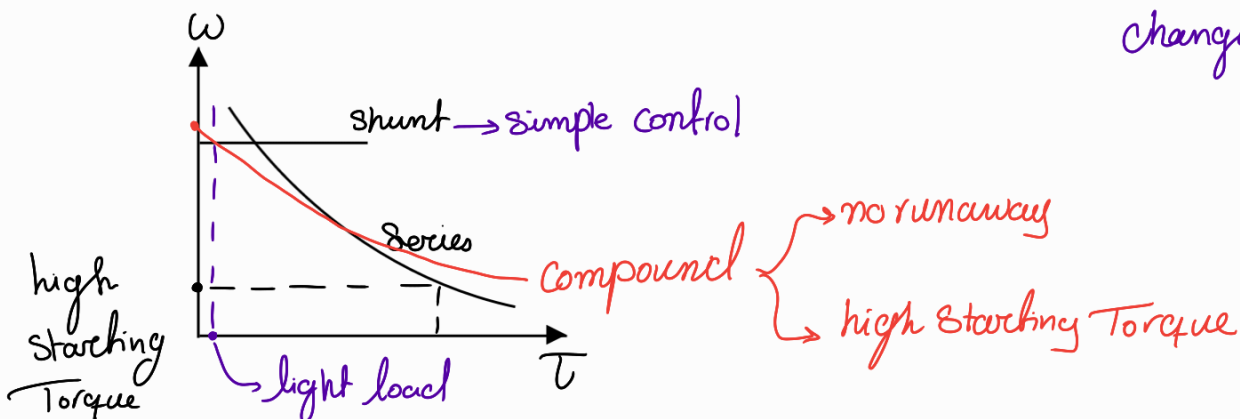
- It has a shunt and a series field and it compounds best features of both shunt & series motors and does not have runaway



Better connection than this  
 Since  $V_T$  is related to field resistance  
 and so relation between  $V_T, I_F$  is simple  
 In the second,  $I_F$  depends on  $I_L$



since  $R_A$  is variable  
 That depends on load  
 $R_A$  changes  $\rightarrow I_A$   
 changes  $\rightarrow \Phi$  changes

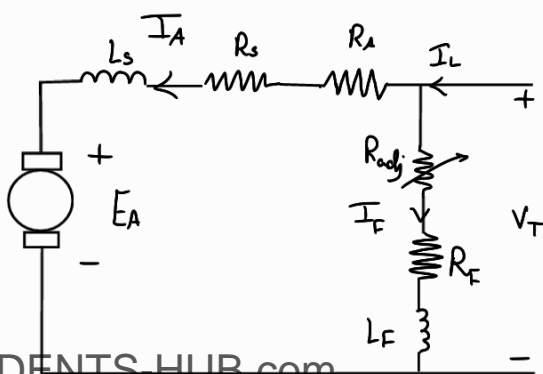
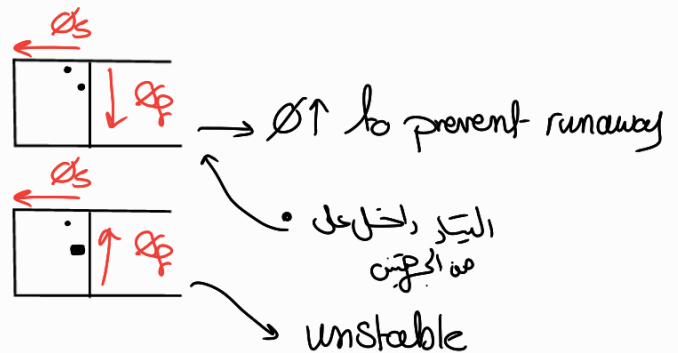


runaway occurs for series (Back)

series  $\rightarrow$  shunt

$$\Phi_{net} = \Phi_s + \Phi_f \quad \text{Cumulatively compounded}$$

$$\Phi_{net} = \Phi_s - \Phi_f \quad \text{Differentially Compounded}$$



$$I_f = \frac{V_T}{R_F} \quad \text{constant}$$

$I_A$  is variable that depends on the load

At light load  $\rightarrow$  shunt اقرب  
 At higher load  $\rightarrow$  series اقرب

Speed control is done by controlling:-

field resistance

Voltage  $V_A$

Armature Resistance  $R_A$

## DC Generator

- Same Structure as motor
  - S.E
  - Shunt
  - Compound

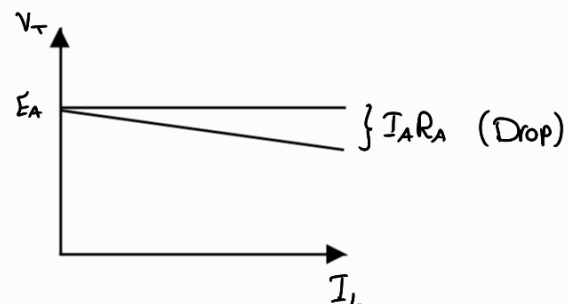
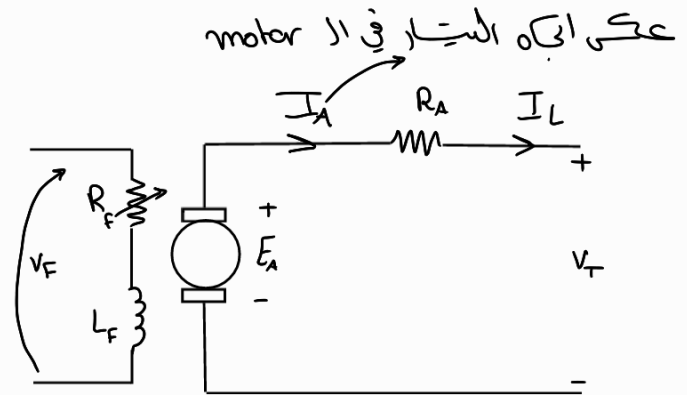
Separately excited DC Generator

$$V_T = E_A - I_A R_A$$

$E_A$  needs to be increased to decrease drop

$$E_A = K \Phi \omega \rightarrow \text{field current}$$

So:  $\Phi$  or  $\omega$  are increased to increase  $E_A$

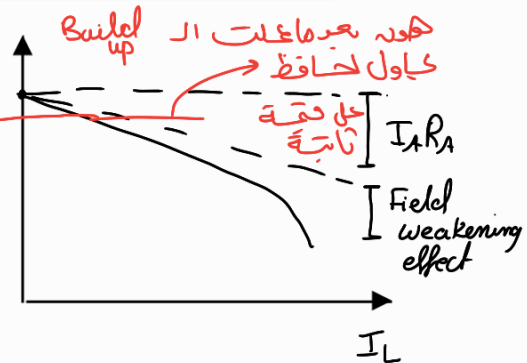


Best type of generator:

Terminal voltage is constant while changing load

Residual gives mechanical energy  $\rightarrow E_A = K \phi_{res} W_m$

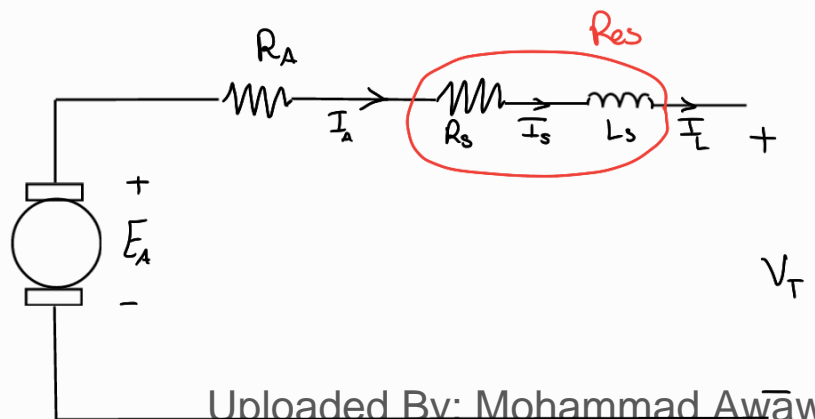
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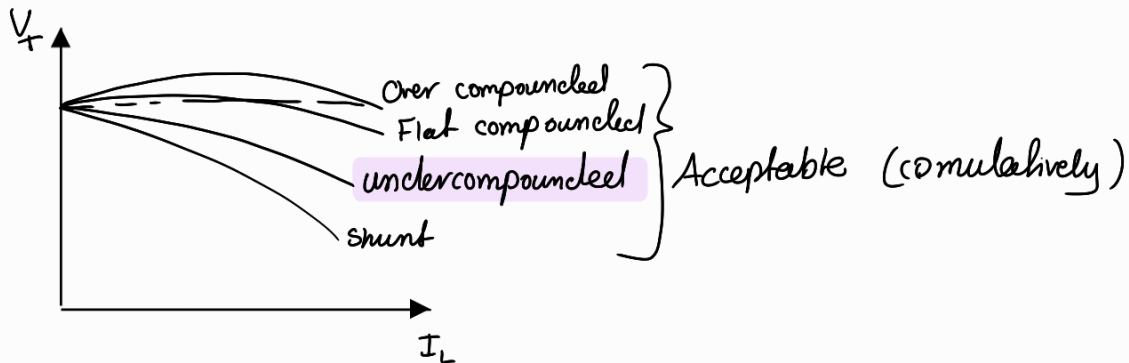
1. Flash the field  $R_A$


$$V_T = E_A - (R_A + R_S) I_A$$

Characteristics are Bad

[illegible]

Compound DC Generators  $\rightarrow$  to control it  $\begin{cases} \omega_m \\ I_F \end{cases}$   
 Cumulatively



Differentially : Bad  $\rightarrow$  Unacceptable

