

ASIL SHAAR (CORPORATE FINANCE(FINN3300))

CHAPTER 4

Chapter 4
Hurdle Rate

Hurdle Rate = WACC weighted average cost of Capital

objective ^{بهدف} Maximize firm value

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graph TD; A[Maximize firm value] --> B[Investment]; A --> C[Financing]; A --> D[Dividend];
```

Assets = liabilities + owners equity

↓ Investment ↘ Source of financing

Sources of Capital:

- ① debt
- ② preferred equity
- ③ common equity

→

$$WACC = W_d * K_d + W_p * K_p + W_s * K_s$$

↓
↓
↓

Cost of debt Cost of Preferred stock Cost of Common equity

Calculating Cost of Common equity

$$CAPM \rightarrow E(r) = R_F + b [E(r_m) - R_F]$$

Risk premium.

تسمى Cost of
بتحتمل الشركة.

In order to use CAPM we need to determine the following:

- ① R_F
- ② beta
- ③ Market risk premium.

* Risk free Rate

↳ rate of return on a risk free assets.

For an assets to be risk free two condition must be:

- ① NO default risk
- ② NO uncertainty about investment rate.

Estimating risk free rate:

R_f → rate of return on long-term governmental bond

Risk free rate should be in the same currency in which cash flows are estimated.

Risk free rate: default free governments

$$R_f = r^* + IP$$

real rate
of interest

inflation
premium

* If bonds were issued by different governments that are Aaa rated, there will be differentiation the risk free rates due to expected inflation.

Risk free rate: governments have default risk

* If the government issues long term bond in the local currency, then we should adjust the government bond rate by the estimated default spread to arrive at a risk less local currency rate.

* Risk-free Rate: No local currency government bonds. لا يوجد سندات حكومية بالعملة المحلية.

(a) Build up approach

$$R_F = r^* + IP$$

↓ ↓
real rate of interest inflation premium

↳ rate on inflation index treasuries

⇒ These treasuries offer a guaranteed real rate of return.

(b) Differential inflation approach

We start with a risk-free rate in the US dollar and add the differential between expected inflation in the average in question

Ex: R_F Brazil = ? ten year treasury bond

$$R_F \text{ USA} = 2.75\%$$

Inflation US higher than Brazil by 3%

$$R_F \text{ Brazil} = 2.75\% + 3\% = 5.75\%$$

$$E(r) = \underline{R_F} + b [E(r_m) - R_F]$$

↓
rate on a long
term government
bond.

market risk premium = equity

risk premium (ERP) To estimate

ERP we can use any of the following

approaches:

① survey approach

② historical approach.

③ Implied ERP approach.

* Market risk premium > 0

Risk preference:

① Risk averse

② Risk seekers

③ Risk neutral

* market risk premium increases if the degree of
the risk aversion of investors increases.

* Market risk premium increases if the risk of
the average risk investment increases.

→

(i) survey approach :

limitations:

- (a) There are no constraints on reasonability
- (b) survey approach used to calculate ERP reflects the past and not the future.
- (c) survey to be short term.

ex : (1) R_f 4%

(2) mutual fund \rightarrow return is uncertain

a. less than 4%

b. between 4% - 6%

c. between 6% & 8%

d. between 8% - 10%

e. between 10% - 12%

f. more than 12%

\Rightarrow

② Historical approach.

- ① Determine the time period used.
- ② choose the risk free security (long-term government of bond).

③ Arithmetic versus geometric averages.

$$\text{Expected ERP} = \text{Arithmetic average (market return)} - \text{Arithmetic average } R_F$$

Arithmetic average = $\frac{\sum x}{n}$
x

$$\text{geometric average} = ?$$

$$\text{terminal value} = (1+r_1)(1+r_2)(1+r_3)\dots(1+r_n)$$

$$\text{geometric average} = \left(\frac{\text{terminal value}}{\text{initial value}} \right)^{\frac{1}{n}} - 1$$

limitations:

- ① It assume that the degree of risk aversion of investors has not change ^{increase} over time



② It assumes that the riskiness of average risk investment has not changed over time.

A modified ERP in emerging markets.

$$ERP = ERP_{\text{for a}} + \text{Country premium.}$$

Using the mature market historical approach

To estimate the Country premium, we can use of the following approach:

① use the Country bond default spread.

The Country's bond default spread will be used as a measure of the Country premium.

$$ERP_x = ERP_{\text{US}} + \text{default spread}_x$$

Examples

$$ERP_{\text{us}} = 4.2\%$$

$$\text{default spread india} = 2.25\%$$

$$\text{Brazil} = 2\%$$

$$ERP_{\text{Brazil}} = 4.2\% + 2\%$$

$$= 6.2\%$$

$$ERP_{\text{india}} = 4.2\% + 2.25\%$$

$$= 6.45\%$$

ERP Brazil??

ERP india??

(b) Relative standard deviation.

relative standard deviation = measure of Country premium.

$$\text{relative s.d.} = \frac{\sigma_x(\text{stock price})}{\sigma_{US}(\text{stock price})}$$

$$ERP_x = ERP_{US} * \text{relative SD}$$

$$ERP_x = ERP_{US} * \frac{\sigma_x(\text{stock price})}{\sigma_{US}(\text{stock price})}$$

Examples

$$ERP_{US} = 4.2\%$$

$$ERP_{\text{Brazil}} = ??$$

$$SD_{US} = 15\%$$

$$SD_{\text{Brazil}} = 21\%$$

$$ERP_{\text{Brazil}} = ERP_{US} * \frac{\sigma_{\text{Brazil}}}{\sigma_{US}} = 4.2\% * \frac{21\%}{15\%} = \boxed{5.88\%}$$

$$\begin{aligned} \text{Country premium} &= ERP_{\text{Brazil}} - ERP_{US} \\ &= 5.88\% - 4.2\% \\ &= \boxed{1.68\%} \end{aligned}$$

© Default spread + relative standard deviation.

$$\text{Country premium} = \frac{\text{Country default spread}}{\beta_x (\text{bond price})} * \frac{\beta_x (\text{stock price})}{\beta_x (\text{bond price})}$$

Example:

$$\text{ERP}_{\text{US}} = 4.2\%$$

$$\text{ERP}_{\text{Brazil}} = ??$$

$$\beta_{\text{equity}}_{\text{Brazil}} = 21\%$$

$$\beta_{\text{bond}}_{\text{Brazil}} = 14\%$$

$$\text{default Brazil} = 2\%$$

$$\text{Country premium} = 2\% * \frac{21\%}{14\%} = 3\%$$

$$\text{ERP}_{\text{Brazil}} = \text{ERP}_{\text{US}} + \text{Country premium}$$

$$4.2\% + 3\% = \boxed{7.2\%}$$

3 Implied ERP approach

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Standard and Poor₅₀₀ index = 1,756.54

Total annual cash flow = 82.35 = $CF_0 = D_0$

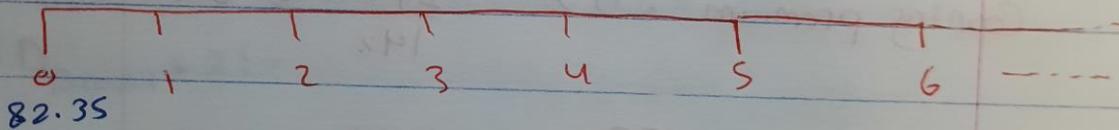
$g_1 = 5.59\%$ for the first five years.

and $g_2 = R_f = 2.55\%$ thereafter

$r = ? = E(r_m) = ?$

Implied ERP?

Price = \sum PV of expected cash flows.



$$CF_1 = CF_0 (1 + g_1) = 82.35 (1 + 5.59\%) = 86.96$$

$$CF_2 = CF_1 (1 + g_1) = 86.96 (1 + 5.59\%) = 91.82$$

$$CF_3 = CF_2 (1 + g_1) = 91.82 (1 + 5.59\%) = 96.95$$

$$CF_4 = CF_3 (1 + g_1) = 96.95 (1 + 5.59\%) = 102.38$$

$$CF_5 = CF_4 (1 + g_1) = 102.38 (1 + 5.59\%) = 108.1$$

$$CF_6 = CF_5 (1 + g_2) = 108.1 (1 + 2.55\%)$$

$$= 110.86$$

$$1756.54 = \frac{86.96}{(1+r)^1} + \frac{91.82}{(1+r)^2} + \frac{96.95}{(1+r)^3} + \frac{102.38}{(1+r)^4} + \frac{108.1}{(1+r)^5} + \left(\frac{110.86}{r - 2.55\%} \cdot \frac{1}{(1+r)^5} \right)$$

$$r = 8.04\%$$

$$\text{Implied ERP} = 8.04\% - 2.55\%$$

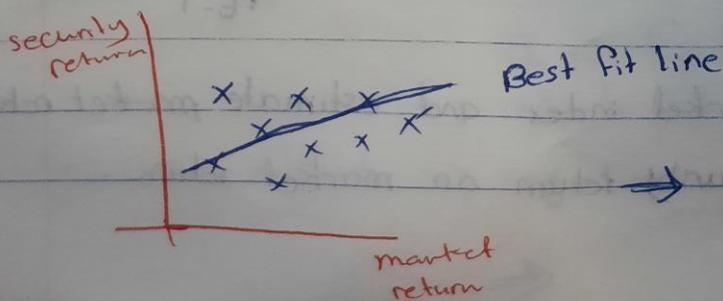
$$= \boxed{5.49\%}$$

$$E(r) = R_f + b^a \text{ ERP}$$

- ① regression beta (historical beta)
- ② Bottom-up beta
- ③ Accounting beta.

Y = Dependent variable
X = independent variable.

simple regression: a tool that is used to estimate a relationship between a single dependent variable and a single independent variable.



$$Y = mX + C$$

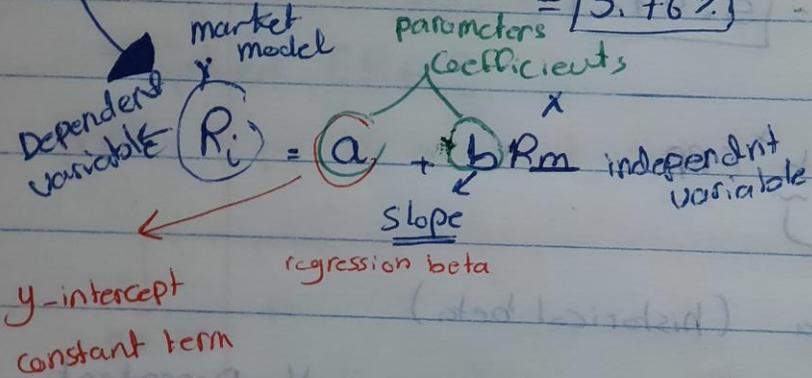
\downarrow slope \downarrow y-intercept

Revenue US
Total Revenue

Jiskoo Joo

$$ERP_{Disney} = 82.01\% \cdot 5.5\% + 11.64\% \cdot 6.72\% + 6.02\% \cdot 7.27\% + 0.33\% \cdot 9.44\%$$

$$= \boxed{5.76\%}$$



To estimate regression beta:

- ① Decide on the estimation period.
- ② Frequency of data = monthly.
- ③ Estimate return on the security $r = \frac{P_t - P_{t-1} + Div}{P_{t-1}}$
- ④ Choose a market index and estimate market return
- ⑤ regress security return on market return.

67% Confidence interval

95% Confidence interval

$$[B - SE^*1, B + SE^*1]$$

$$[B - SE^*2, B + SE^*2]$$

confidence interval

$$R_i = a + b^* R_m$$

practical model

CAPM

theoretical model

↳ market model

CAPM

$$E(R_i) = R_f + b^* [E(R_m) - R_f]$$

$$E(R_i) = R_f + b^* E(R_m) - b^* R_f$$

$$E(R_i) = R_f - b^* R_f + b^* E(R_m)$$

$$E(R_i) = \underbrace{R_f(1-b)}_{\text{intercept}} + \underbrace{b^*}_{\text{slope}} E(R_m)$$

Theory

Jensen's alpha

↓

$$= \underline{a} - (R_f(1-b))$$

Jensen's alpha → positive

$a > R_f(1-b) \Rightarrow$ the stock did better than expected.

$a < R_f(1-b) \Rightarrow$ the stock did worse than expected.

Jensen's alpha → negative

→

* $\alpha = R_F(1-b) \Rightarrow$ the stock did as expected
 \Rightarrow o Jensen's alpha.

* Bottom up beta (fundamental beta)

Determinants of beta:

- (1) Type of product
- (2) Degree of operating leverage (higher leverage)
 higher risk

الكلفة التي تتغير مع تغير
 Cost \leftarrow rent \leftarrow Fixed Cost \leftarrow risk
 Variable \rightarrow

Operating Leverage: the use of fixed operating cost to magnify the effect of the change in Sales on the firm's EBIT

Examples

	A	B	A	B
Revenue	100	\$100	\$120	\$120
F.C	\$10	\$80	\$10	\$80
V.C	\$80	\$10	\$96	\$12
EBIT	\$10	\$10	\$14	\$28

If sales increase 20%

EBIT = ??

$100(1+0.2) = 120$
 (A) $80(1+0.2) = 96$ (B) $10(1+0.2)$

(A)

$$\% \Delta \text{ in Sales} = 20\%$$

$$\% \Delta \text{ in EBIT} = ?$$

$$\frac{14-10}{10} = \boxed{40\%}$$

(B)

$$\% \Delta \text{ in Sales} = 20\%$$

$$\% \Delta \text{ in EBIT} = ?$$

$$\frac{28-10}{10} = \boxed{180\%}$$

$$\text{DOL} = \frac{\% \Delta \text{ in EBIT}}{\% \Delta \text{ in Sales}} = \frac{40\%}{20\%} = 2 > 1$$

degree of operating leverage exists

$$\text{DOL} = \frac{180\%}{20\%} = 9$$

B)

Higher operating leverage \rightarrow higher cash flow volatility \rightarrow higher risk \rightarrow higher beta.

(3) Degree of financial leverage

* Financial leverage: the use of fixed financing (debt, preferred stock) to magnify the effect of the change in EBIT on the firm's EPS

* The higher the financial leverage \rightarrow the higher the risk \rightarrow the higher the beta.

* Regression beta = beta levered = equity beta → shows the impact of the three determinants of beta which are type of product, operating leverage and financial leverage.

* Beta unlevered = asset beta → shows the impact of the determinants of beta which are type of product and operating leverage.

$$\begin{array}{ccccccc}
 & & \textcircled{3} & & \textcircled{2} & & \textcircled{1} \\
 & & \downarrow & & \downarrow & & \downarrow \\
 \text{Beta levered} & = & B_u & * & \left(1 + (1-t) * \frac{D}{E} \right) \\
 \downarrow & & \downarrow & & \downarrow & & \downarrow \\
 \text{Beta levered} & & \text{beta} & & \text{tax rate} & & \frac{\text{Debt}}{\text{equity}} \\
 & & \text{unlevered} & & & &
 \end{array}$$

$$\boxed{B_L = B_u \text{ only if } \frac{D}{E} = 0}$$

no financial leverage

$$R^2 = 39.4\%$$

$$1 - R^2 = 60.6\% \rightarrow \text{firm specific risk}$$

$R^2 \rightarrow$ market risk

$1 - R^2 \rightarrow$ firm specific risk

	beta	R^2
Disney	1.25	0.73
Amgen	1.25	0.25

Undiversified, ~~high~~ Disney
Diversified, indifferent

properties of beta:

Beta could be a weighted average.

Example b_V ?

portfolio V

<u>Assets</u>	<u>beta</u>	<u>proportion (weight)</u>
A	1.5	20%
B	1	50%
C	0.8	30%
		<hr/> 100%

$$b_v = \sum w_{\text{each asset}} * b_{\text{each asset}}$$

$$b_v = 0.2 * 1.5 + 0.5 * 1 + 0.3 * 0.8 = \boxed{1.04}$$

Calculating beta for a Combined firm:

Step 1: Calculate beta unlevered for each company

$$B_L = B_u * \left(1 + (1-t) * \frac{D}{E} \right) \quad \text{tax rate} = 36.1\%$$

B_u Disney? B_u Capital Cities?



$$1.5 = B_u * \left(1 + (1 - 36.1\%) * 0.1 \right)$$

$$1.5 = B_u * 1.0639$$

$$\boxed{B_u = 1.08}$$

Capital Cities

$$0.95 = B_u * \left(1 + (1 - 36.1\%) * 0.1 \right)$$

$$\boxed{B_u = 0.93}$$



Step 2 : Calculate beta unlevered for the Combined firm (weighted average)

$$B_u \text{ Disney} = 1.08$$

$$B_u \text{ Capital Cities} = 0.93$$

$$* W_{\text{Disney}} = \frac{\text{Value of Disney}}{\text{Value of Combined firm}} = \frac{34,286 \text{ m}}{53,401 \text{ m}} = \boxed{0.64}$$

$$\begin{aligned} \text{Value Combined firm} &= 34,286 \text{ m} + 19,115 \text{ m} \\ &= \$53,401 \text{ million} \end{aligned}$$

$$* W_{\text{Capital Cities}} = \frac{\text{Value of Capital Cities}}{\text{Value of Combined firm}} = \frac{19,115 \text{ m}}{53,401 \text{ m}} = \boxed{0.36}$$

$$B_u = 0.64 * 1.08 + 0.36 * 0.93 = 1.02$$

$$B_{u \text{ Combined}} = \sum \underset{\substack{\downarrow \\ \text{each} \\ \text{company}}}{w} * \underset{\substack{\downarrow \\ \text{each} \\ \text{company}}}{b_u}$$



Step 3 : Calculate beta levered for the combined firm under 3 scenarios

S_1 : If Disney bought Capital Cities with all equity.

Disney (Pre acquisition)	Capital Cities (Pre acquisitions)
Debt 3,186m	Debt 615m
Equity 31,100m	Equity 18,500m
<u>34,286m</u>	<u>\$19,115m</u>

Combined firm

$$\text{Debt} = 3,186 \text{ m} + 615 \text{ m} = \$ 3,801 \text{ m}$$

$$\text{Equity} = 31,100 \text{ m} + 18,500 = \$ 49,600 \text{ m}$$

$$\begin{aligned} \beta_{L \text{ Combined}} &= \beta_{U} * \left(1 + (1 - t) * \frac{D}{E} \right) \\ &= 1.02 * \left(1 + (1 - 0.361) * \frac{3,801 \text{ m}}{49,600 \text{ m}} \right) \\ &= 1.07 \end{aligned}$$

لقد تم حساب بيتا المذلل للقرض للشركة المدمجة
 باستخدام صيغة بيتا المذلل للقرض مع الأخذ في الاعتبار
 نسبة الدين إلى حقوق الملكية.

~~1.49~~

S₂: IF Disney bought Capital Cities with all debt

Combined firm	
Debt	3,186 m + 615 m + 18,500 m = 22,301 m \$
Equity	31,100 m

Disney will
0.416
out of m
Capital

$$B_L = 1.02^{\alpha} \left(1 + (1 - 36.1\%) \frac{22,301 \text{ m}}{31,100 \text{ m}} \right)$$

$$B_L = 1.49$$

S₃: IF Disney used a mixed debt & equity to buy Capital Cities

Debt = \$ 10 billion = 10,000 million

The rest = equity

Combined firm

Debt	3,186 m + 615 m + 10,000 m = 13,801 m \$
Equity	31,100 m + 8,500 m ↓ (18,500 - 10,000) = 39,600 \$

$$B_2 = 1.02 \left(1 + (1 - 36.1\%) \frac{13,801m}{39,600m} \right)$$

$$B_2 = 1.25$$

② Bottom up beta

In order to calculate bottom-up beta we have to do the following:

① Determine the firm's business divisions.

Example : ① Media

Disney ② Parks

③ Consumer products

④ Studio entertainment

⑤ Interaction

② For each business division we should do the following:

a) Find comparable firms. The more firms the better.

example : Studio entertainment division 10 comparable firms (US firms that produces movies)



- (b) Get levered beta (regression beta) for each firm of the comparable firms.
- (c) Collect data on equity and debt and tax rate for each of the comparable firms.
- (d) Calculate the average and the median of the levered beta.
- (e) Calculate debt to equity ratio for each of the comparable firm.
- (f) Calculate the average and the median of the debt to equity ratio.
- (g) Calculate the average tax rate or the median.

(h) unlever the beta:

$$B_L = B_U * \left(1 + \left(1 - \frac{\text{tax rate}}{\text{rate}} \right) * \frac{D}{E} \right)$$

average
median
average
or median
average / median

و ایا میانگین و میانگین را به کار ببرید

③ Calculate ~~beta~~ unlevered for all business operations:

$$\beta_u = \sum w * \beta_u = \text{weighted average.}$$

for all business operations

each division

each division

Weight for each division = $\frac{\text{Revenue from each division}}{\text{Total revenues}}$.

OR

weight for each division = $\frac{\text{Value of each division}}{\text{Total firm value}}$.

④ Estimate beta levered for all business operations and cost of equity.

⑤ Estimate beta levered for each division and cost of equity for each division

$$\text{Cost of equity} = R_F + b^* E \cdot R_P$$

Median
average

$$B_L = B_U \left(1 + (1 - t) \frac{D}{E} \right)$$

$$1.24 = B_U \times (1 + (1 - 0.4)^* 0.2706)$$

$$B_U = 1.06$$

→ each business
division

Calculating bottom up beta for an unlisted firm
(private):

- ① Get comparable firms
- ② Get levered beta for each of comparable firms and calculate the average or median of beta levered
- ③ Get $\frac{D}{E}$ ratio for each of the comparable firms and calculate the average or median of $\frac{D}{E}$ ratio
- ④ Calculate the average of the median of the marginal tax rate
- ⑤ unlever the beta using the following formula:
$$B_L = B_U \left(1 + (1 - t) \frac{D}{E} \right)$$
- ⑥ Calculate beta levered for the private company of interest using the average $\frac{D}{E}$ ratio for the median

⇒

Whole industry the company operates in.

Calculating bottom up beta for an unlevered firm:

$$\text{Beta}_{L \text{ median}} = 0.81 \quad r^2_{\text{median}} = 0.26$$

$$\text{tax rate}_{\text{median}} = 0.4$$

$$\text{D/E ratio}_{\text{median}} = 0.2141$$

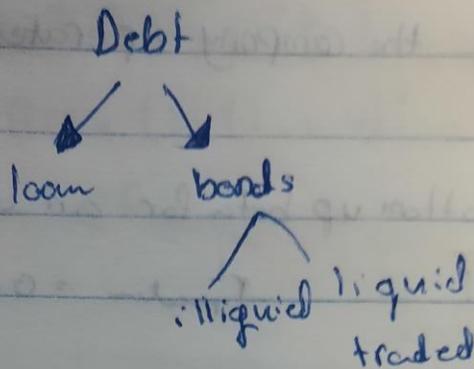
$$B_L = B_U \left(1 + (1-t) \frac{D}{E} \right)$$

$$0.81 = B_U \left(1 + (1-0.4) \times 0.2141 \right)$$

$$B_U = 0.72$$

$$\begin{aligned} B_{L \text{ Bookscope}} &= 0.72 \left(1 + (1-0.4) \times 0.2141 \right) \\ &= 0.81 \end{aligned}$$

$$\frac{B}{\sqrt{R^2}} = \frac{0.81}{\sqrt{0.26}}$$



Calculating Cost of debt:

(a) If the firm issued bonds & they are liquid & traded, then:

$$P_B = \frac{I}{r} \left(1 - \frac{1}{(1+r)^n} \right) + \frac{\text{par}}{(1+r)^n}$$

\downarrow
 YTM

Expected Cash flows for bonds:

- ① interest payment
- ② par value

pre-tax Cost of debt $K_d = \text{YTM}$
 yield to maturity

تدکیرین
 کا یقین

after tax Cost of debt = pre tax Cost of debt * (1-t)

(b) If the firm issued bonds but illiquid, then look at the issuer's rating (rating done by Credit agencies)

pre tax Cost of debt = R_f + default spread
 (associated with the firm's rating)

© If the firm is not rated or it has not issued bonds then:

① look at the last loan received by the firm:

The interest on the loan = pre-tax cost of debt.

② Do a synthetic rating for the firm:

$$\text{pre tax cost of debt} = R_f + \text{default spread} \left(\begin{array}{l} \text{associated with} \\ \text{the rating done} \end{array} \right)$$

Synthetic rating =

$$\text{time interest earned ratio} = \frac{\text{interest coverage ratio}}{\text{interest expense}} = \frac{\text{EBIT}}{\text{Interest expense}}$$

Example

$$R_f = 5.5\%$$

$$5.5\% + 0.4\%$$

$$= \boxed{5.9\%}$$

Calculating Cost of preferred stock:

$$D_0 = D_1 = D_2 = D_3 = \dots = D_N$$

$$\text{price } P = \frac{D}{r}$$

→ dividends
→ required rate of return

$$r = \frac{D}{P}$$

present value of a perpetuity.

$$\boxed{r = KP}$$

$$WACC = w_d * k_d + w_p * k_p + w_s * k_s$$

\swarrow pre tax cost of debt $(1-t)$

\downarrow $k_p = \frac{D}{P}$ after tax

\downarrow CAPM after tax

- YTM
- R_f + default spread
- interest on the loan.

weights:

① Book value weights

② Market Value weights

Calculating book value weights:

$$w_d = \frac{\text{Debt}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

$$w_p = \frac{\text{Preferred equity}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

$$w_s = \frac{\text{Common equity}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

ERP = market risk premium = 5.5%

tax rate = 40%

page

156 [1] $b = 0.95$

Treasury bill rate = 5.8%

Treasury bond rate = 6.4%

Debt = \$1.7 billion

Equity = \$1.5 billion

tax rate = 36%

[a] ERP = 8.76%

short term investor

$$E(r_i) = R_F + b * ERP$$

$$5.8\% + 0.95 * 8.76\% = 14.12\%$$

[b] long term investor

$$E(r_i) = R_F + b * ERP$$

Cost of equity \swarrow

6.4% + 0.95 * 5.5%

= 11.63%

5.5% (with Arabic note: *معدل مخاطر السوق*)

[c] Cost of equity = 11.63%

\Rightarrow

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prop [2] Debt = \$1.7 billion

Equity = \$1.5 billion

tax rate = 36%

(a) $B_L = 0.95$

B_U ?

$$B_L = B_U \left(1 + (1 - t) \times \frac{D}{E} \right)$$

$$0.95 = B_U \left(1 + (1 - 0.36) \times \frac{1.7 \text{ billion}}{1.5 \text{ billion}} \right)$$

$$B_U = 0.55$$

(b) $\frac{0.55}{0.95} = 0.58$

↳ business risk

$$1 - 0.58 = 0.42 \rightarrow \text{Financial Risk}$$

[3] $b = 1.7$

(a) Debt = 0

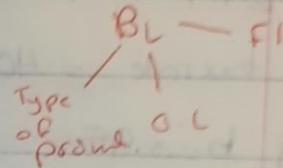
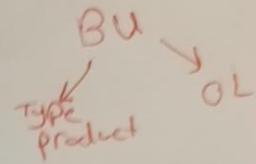
$$R_F = 6.4\%$$

$$ERP = 5.5\%$$

$$E(r) = 6.4\% + 1.7 \times 5.5\%$$

$$k_s = 15.75\%$$

→



(b) R_f زادت من 6.4 لـ 7.5
 يعني اسعار تزداد ، طالما لم ي
 اعرف كم زاد بعوض في المعادلة

$$K_s = 7.5\% + 1.7 * 5.5\%$$

$$K_s = 16.75\%$$

(c) ما في علم دين وما في
 financial risk يعني
 All risk is business risk 100%. $B_L = B_U$

(15) frequency of data = monthly

$$R_{\text{stock}} = 3.28\% + 1.65 R_m$$

Treasury bill rate = 4.8%

Treasury bond rate = 6.4%

no. of share = 265 million shares

price per share = \$30

$$(a) = E(r) = ?$$

short-term

$$E(r) = R_f + b * ERF$$

$$= 4.8\% + 1.65 * 8.76\%$$

$$E(r) = 19.25\%$$

$$R_i = a + b R_m$$

$$R^2 = 0.2$$

long-run

$$ERP = 5.5\%$$

$$\text{short-run } ERP = 8.76\%$$

(b) $E(r) = R_F + b \cdot ERP$
 long-run $6.4\% + 1.65 \cdot 5.5\% = 15.47\%$

(c) Jensen's alpha = Intercept - (1 - B) R_F
 51.1% better than expected.
 annually during the period of the regression
 annualized $R_F = ?$
 monthly R_F

monthly $= (1 + 51.1\%)^{\frac{1}{12}} - 1$
 overperformance $= 3.5\%$
 or Jensen's alpha

$R^2 = 0.2$ $-(1 - 1.65)$

$\frac{3.5\%}{0.22} = \frac{3.28\%}{0.22} + 0.65 R_F$

$\frac{0.22\%}{0.65} = \frac{0.65 R_F}{0.65}$

monthly $R_F = 0.338\%$
 annualized $R_F = (1 + 0.338\%)^{12} - 1 = 4.1\% \Rightarrow$

$$\textcircled{a} \frac{D}{E} = 0.03$$

tax rate = 40%

they will acquire a new business will

Sell debt = \$2 billion

b
↓
Combined firm

$$B_L = B_U \times \left(1 + (1 - \text{tax}) \times \frac{D}{E}\right)$$

$$1.65 = B_U \times \left(1 + (1 - 0.4) \times 0.03\right)$$

$$B_U = 1.62$$

pre acquisition:

$$\text{equity} = 265 \text{m} \times 30 = 7,950 \text{ million}$$

$$\frac{\text{Debt}}{\text{equity}} = 0.03$$

$$\frac{\text{Debt}}{7950} = 0.03$$

$$\text{Debt} = 238.5 \text{ million}$$

Combined firm

$$\text{Debt} = 238.5 \text{m} + 2000 \text{ million} = 2238.5 \text{m}$$

$$\text{Equity} = 265 \text{m} \times 30 = 7950 \text{ million}$$

$$B_L = 1.62 \times \left(1 + (1 - 0.4) \times \frac{2238.5 \text{m}}{7950 \text{m}}\right)$$

$$B_L = 1.89$$

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$$(17) \beta = 1.61$$

$$\text{Debt} = 10 \text{ billion } \text{دولار}$$

$$\text{Equity} = 10 \text{ billion } \$$$

$$\text{tax rate} = 40\%$$

(a) B_U ?

$$B_L = B_U \left(1 + (1-t) \frac{D}{E} \right)$$

$$1.61 = B_U \left(1 + (1-0.4) \frac{10 \text{ billion}}{10 \text{ billion}} \right)$$

$$\boxed{B_U = 1.01}$$

(b) Debt ratio 10%

$$\text{Debt ratio} = \text{Debt to Capital} = \frac{\text{Debt}}{\text{Debt} + \text{equity}}$$

قبل 10%

$$\text{Current debt ratio} = \frac{10 \text{ billion}}{10 \text{ billion} + 10 \text{ billion}} = \frac{10 \text{ billion}}{20 \text{ billion}} = \boxed{\frac{1}{2}}$$

after 1 year

$$\text{debt ratio} = \frac{50}{100} = \frac{10}{100} = 0.1$$

$$\text{Debt ratio} = \frac{\text{Debt}}{\text{Debt} + \text{equity}} = \frac{40}{100}$$

$$\text{Debt} = 40$$

$$\text{Equity} = 100 - 40 = 60 \quad \therefore \frac{D}{E} = \frac{40}{60}$$

Debt to Capital = 40/100

$$B_L = B_U \left(1 + (1 - \text{tax}) \times \frac{D}{E} \right)$$

$$1.01 \left(1 + (1 - 0.4) \times \frac{40}{60} \right)$$

$$B_L = 1.41$$

Year 2

30% debt, 70% equity

$$\text{new debt ratio} = \frac{40}{100} - \frac{10}{100} = 30\% = 0.3$$

$$\text{Debt ratio} = \frac{\text{Debt}}{\text{Debt} + \text{equity}} = \frac{30}{100}$$

debt = 30, equity = 70

$$\frac{D}{E} = \frac{30}{70}$$

$$B_L = B_U \left(1 + (1 - t) \times \frac{D}{E} \right)$$

$$1.01 \left(1 + (1 - 0.4) \times \frac{30}{70} \right) \quad B_L = 1.27$$

market value weights:

$$\text{market value of C.S} = \frac{\text{market share}}{\text{price}} \times \text{no of Common stock}$$

$$\text{market value of P.S} = \frac{\text{market share}}{\text{price}} \times \text{no of P.S}$$

market value of debt = ?

$$\text{market value of debt} = \frac{I}{r} \left(1 - \frac{1}{(1+r)^n} \right) + \frac{par}{(1+r)^n}$$

(the sum of time due amount of debt) \times (weight of each amount of debt) = duration of debt $\leftarrow n$ \times $\leftarrow r$ \times \leftarrow pre tax cost of debt

weight \times time due = $\frac{\text{market value of debt}}{\text{market value of debt}}$ \rightarrow duration

$$\text{market value wd} = \frac{\text{market value of debt}}{\text{M.V of C.S} + \text{M.V of P.S} + \text{M.V of debt}}$$

$$\text{market value wp} = \frac{\text{market value of P.S}}{\text{M.V of C.S} + \text{M.V of P.S} + \text{M.V of debt}}$$

$$\text{market value of WS} = \frac{\text{market value of C.S.}}{\text{M.V. of C.S.} + \text{M.V. of P.S.} + \text{M.V. of debt}}$$

Problem 23:

$$\text{Regression Beta} = 0.75$$

$$\text{B}_u (\text{average of comparable firm}) = 1.15$$

a) $D/E = 0.20$, tax = 40%, Beta based on the comparable firms?
(Bottom up beta)

$$B_L = B_u \left(1 + (1 - \text{tax}) \frac{D}{E} \right)$$

$$B_L = 1.15 \left(1 + (1 - 0.4) (0.2) \right)$$

$$B_L = 1.288$$

b) %95 confidence Interval Beta Regression?

$$\%95 \text{ CI} = [B \pm SE(b)(\text{Critical value})]$$

$$[0.75 \pm (0.5)(2)] = [-0.25, 1.75]$$

⇒

[c] ^{جعل} ^{المستوى} Bottom up ^{المستوى} Beta
 more accurate

[d] Calculate wACC?
 Hurdle Rate

← Given

Treasury bond = 6.5%

Tiffany's bond default spread = 1%

ERP = 5.5%

preferred stock

$$WACC = w_d \cdot K_d + w_s \cdot K_s$$

$$\text{Cost of common equity} = R_F + b \cdot ERP$$

↓ ^{مستوى}

$$= 6.5\% + (1.29)(5.5\%)$$

Debt rate

$$K_s = 13.59\%$$

$$\text{Cost of debt} = R_F + \text{default spread}$$

$$= 6.5\% + 1\%$$

$$\text{pre tax } K_d = 7.5\%$$

$$\text{After tax } K_d = (1 - 0.4) \cdot 7.5\%$$

$$K_d = 4.5\%$$



$$\frac{D}{E} = \frac{20}{100} \quad \text{Debt} = 20, \text{ equity} = 100$$

$$\text{Total Capital} = \text{Debt} + \text{equity} = 120$$

$$w_d = \frac{20}{120}$$

$$w_s = \frac{100}{120}$$

$$wACC = \left(\frac{20}{120}\right)(4.5\%) + \left(\frac{100}{120}\right)(13.59\%)$$

$$wACC = 12.075\%$$