

ASIL SHAAR (CORPORATE FINANCE(FINN3300))

CHAPTER 4

Chapter 4
Hurdle Rate

Hurdle Rate = WACC weighted average cost of Capital

objective ^{بمعيار} maximize firm value

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graph TD; A[Maximize firm value] --> B[Investment]; A --> C[Financing]; A --> D[Dividend]
```

Assets = liabilities + owners equity

↓ Investment

Source of financing

Sources of Capital:

- ① debt
- ② preferred equity
- ③ common equity

→

$$WACC = W_d * K_d + W_p * K_p + W_s * K_s$$

↓
Cost of debt
↓
Cost of Preferred stock
↓
Cost of common equity

Calculating Cost of Common equity

$$CAPM \rightarrow E(r) = R_F + b [E(r_m) - R_F]$$

Risk premium

نقصد Cost of equity
بإجمالي العائد المتوقع

In order to use CAPM we need to determine the following:

- ① R_F ② beta ③ Market risk premium

* Risk free Rate

↳ rate of return on a risk free assets

For an assets to be risk free two condition must be:

- ① NO default risk
- ② NO uncertainty about investment rate

Estimating risk free rate:

R_F → rate of return on long-term governmental bond

Risk free rate should be in the same currency in which cash flows are estimated.

Risk free rate: default free governments

$$R_f = r^* + IP$$

real rate
of interest

inflation
premium

* If bonds were issued by different governments that are Aaa rated, there will be differentiation the risk free rates due to expected inflation.

Risk free rate: governments have default risk

* If the government issues long term bond in the local currency, then we should adjust the government bond rate by the estimated default spread to arrive at a risk less local currency rate.

* Risk-free Rate: No local currency government bonds. لا يوجد سندات حكومية بالعملة المحلية

(a) Build up approach

$$R_F = r^* + IP$$

↓ ↓
real rate of interest inflation premium

↳ rate on inflation index x Treasuries

⇒ These treasuries offer a guaranteed real rate of return.

(b) Differential inflation approach

We start with a risk-free rate in the US dollar and add the differential between expected inflation in the average in question

Ex: $R_F \text{ Brazil} = ?$ ten year treasury bond

$R_F \text{ USA} = 2.75\%$

Inflation US higher than Brazil by 3%

$$R_F \text{ Brazil} = 2.75\% + 3\% = 5.75\%$$

$$E(r) = \underline{R_F} + b [E(r_m) - R_F]$$

↓
rate on a long
term government
bond.

market risk premium = equity

risk premium (ERP) To estimate

ERP we can use any of the following
approaches:

- ① Survey approach
- ② historical approach.
- ③ Implied ERP approach.

* Market risk premium > 0

Risk preference:

- ① Risk averse
- ② Risk seekers
- ③ Risk neutral

* market risk premium increases if the degree of
the risk aversion of investors increases.

* Market risk premium increases if the risk of
the average risk investment increases.



(i) survey approach :

limitations:

- (a) There are no constraints on reasonability
- (b) survey approach used to calculate ERP reflects the past and not the future.
- (c) survey to be short term.

ex : (1) R_f 4%

(2) mutual fund \rightarrow return is uncertain

a. less than 4%

b. between 4% - 6%

c. between 6% & 8%

d. between 8% - 10%

e. between 10% - 12%

f. more than 12%

\Rightarrow

② Historical approach.

- ① Determine the time period used.
- ② choose the risk free security (long-term government of bond).

③ Arithmetic versus geometric averages.

$$\text{Expected ERP} = \text{Arithmetic average (market return)} - \text{Arithmetic average } R_f$$

Arithmetic average = $\frac{\sum x}{n}$

$$\text{geometric average} = ?$$

$$\text{terminal value} = (1+r_1)(1+r_2)(1+r_3)\dots(1+r_n)$$

$$\text{geometric average} = \left(\text{terminal value} \right)^{\frac{1}{n}} - 1$$

limitations:

- ① It assume that the degree of risk aversion of investors has not change ^{across} over time



- ② It assumes that the riskiness of average risk investment has not changed over time.

A modified ERP in emerging markets.

$$ERP = ERP_{\text{for a}} + \text{Country premium.}$$

Using the historical approach
mature market

To estimate the Country premium, we can use of the following approach:

① use the Country bond default spread.

The Country's bond default spread will be used as a measure of the Country premium.

$$ERP_x = ERP_{\text{US}} + \text{default spread}_x$$

Examples

$$ERP_{\text{us}} = 4.2\%$$

$$\text{default spread index} = 2.25\%$$

$$\text{Brazil} = 2\%$$

$$ERP_{\text{Brazil}} = 4.2\% + 2\%$$

$$= 6.2\%$$

$$ERP_{\text{index}} = 4.2\% + 2.25\%$$

$$= 6.45\%$$

ERP Brazil??

ERP index??

⑥ Relative standard deviation.

relative standard deviation = measure of Country premium.

$$\text{relative S.D} = \frac{6_X(\text{stock price})}{6_{US}(\text{stock price})}$$

$$ERP_X = ERP_{US} * \text{relative SD}$$

$$ERP_X = ERP_{US} * \frac{6_X(\text{stock price})}{6_{US}(\text{stock price})}$$

Example 8

$$ERP_{US} = 4.2\%$$

$$ERP_{\text{Brazil}} = ??$$

$$SD_{US} = 15\%$$

$$SD_{\text{Brazil}} = 21\%$$

$$ERP_{\text{Brazil}} = ERP_{US} * \frac{6_{\text{Brazil}}}{6_{US}} = 4.2\% * \frac{21\%}{15\%} = \boxed{5.88\%}$$

$$\begin{aligned} \text{Country premium} &= ERP_{\text{Brazil}} - ERP_{US} \\ &= 5.88\% - 4.2\% \\ &= \boxed{1.68\%} \end{aligned}$$

© Default spread + relative standard deviation. 8

$$\text{Country premium} = \frac{\text{Country default spread}}{\frac{\beta_{\text{Block price}}}{\beta_{\text{bond price}}}}$$

Example:

$$\text{ERP}_{\text{US}} = 4.2\%$$

$$\text{ERP}_{\text{Brazil}} = ??$$

$$\beta_{\text{equity Brazil}} = 21\%$$

$$\beta_{\text{bond Brazil}} = 14\%$$

$$\text{default Brazil} = 2\%$$

$$\text{Country premium} = 2\% * \frac{21\%}{14\%} = 3\%$$

$$\text{ERP}_{\text{Brazil}} = \text{ERP}_{\text{US}} + \text{Country premium}$$

$$4.2\% + 3\% = \boxed{7.2\%}$$

③ Implied ERP approach

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Standard and Poor₅₀₀ index = 1,756.54

Total annual cash flow = 82.35 = $CF_0 = D_0$

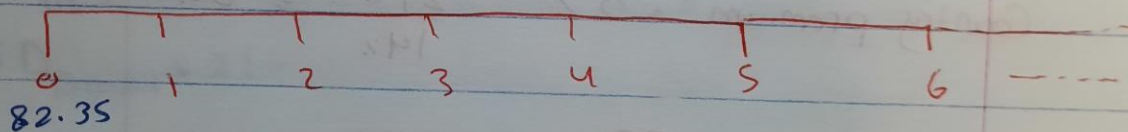
$g_1 = 5.59\%$ for the first five years.

and $g_2 = R_f = 2.55\%$ thereafter

$r = ? = E(r_m) = ?$

Implied ERP?

Price = \sum PV of expected cash flows.



$$CF_1 = CF_0 (1 + g_1) = 82.35 (1 + 5.59\%) = 86.96$$

$$CF_2 = CF_1 (1 + g_1) = 86.96 (1 + 5.59\%) = 91.82$$

$$CF_3 = CF_2 (1 + g_1) = 91.82 (1 + 5.59\%) = 96.95$$

$$CF_4 = CF_3 (1 + g_1) = 96.95 (1 + 5.59\%) = 102.38$$

$$CF_5 = CF_4 (1 + g_1) = 102.38 (1 + 5.59\%) = 108.1$$

$$CF_6 = CF_5 (1 + g_2) = 108.1 (1 + 2.55\%)$$

$$= 110.86$$

$$1756.54 = \frac{86.96}{(1+r)^1} + \frac{91.82}{(1+r)^2} + \frac{96.95}{(1+r)^3} + \frac{102.38}{(1+r)^4} + \frac{108.1}{(1+r)^5} + \left(\frac{110.86}{r - 2.55\%} \cdot \frac{1}{(1+r)^5} \right)$$

$$r = 8.04\%$$

$$\text{Implied ERP} = 8.04\% - 2.55\%$$

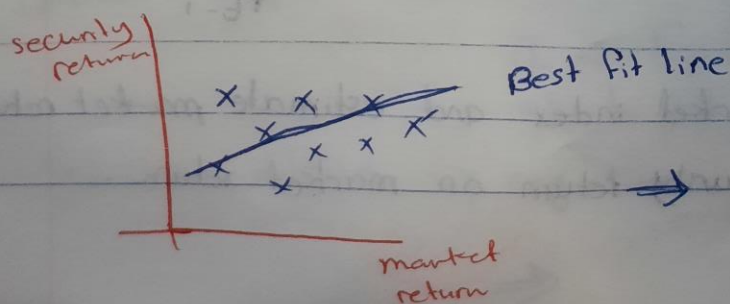
$$= \boxed{5.49\%}$$

$$E(r) = \underbrace{R_f}_{\text{risk-free rate}} + \underbrace{b^a}_{\text{beta}} \cdot \text{ERP}$$

- ① regression beta (historical beta)
- ② Bottom-up beta
- ③ Accounting beta

Y = Dependent variable
X = independent variable.

simple regression: a tool that is used to estimate a relationship between a single dependent variable and a single independent variable.



$$Y = mX + C$$

\downarrow slope \downarrow y-intercept

Revenue US
Total Revenue

J S i o J u p

$$\text{ERP Disney} = 82.01\% \times 5.5\% + 11.64\% \times 6.72\% + 6.02\% \times 7.27\% + 0.33\% \times 9.44\%$$

$$= \boxed{5.76\%}$$

market model

Dependent variable R_i = $\underbrace{a}_{\text{y-intercept constant term}} + \underbrace{b}_{\text{slope regression beta}} R_m$ independent variable

parameters coefficients

To estimate regression beta:

- ① Decide on the estimation period.
- ② Frequency of data = monthly.
- ③ Estimate return on the security $r = \frac{P_t - P_{t-1} + \text{Div}}{P_{t-1}}$

- ④ Choose a market index and estimate market return
- ⑤ regress security return on market return.

67% confidence interval

$$[B - SE^*1, B + SE^*1]$$

95% confidence interval

$$[B - SE^*2, B + SE^*2]$$

confidence interval

$$R_i = a + b^* R_m$$

→ market model

practical model

CAPM → theoretical model

CAPM

$$E(R_i) = R_F + b^* [E(R_m) - R_F]$$

$$E(R_i) = R_F + b^* E(R_m) - b^* R_F$$

$$E(R_i) = R_F - b^* R_F + b^* E(R_m)$$

$$E(R_i) = \underbrace{R_F(1-b)}_{\text{intercept}} + \underbrace{b^*}_{\text{slope}} E(R_m)$$

Theory

Jensen's alpha

↓

$$= \underline{a} - (R_F(1-b))$$

Jensen's alpha → positive

$a > R_F(1-b) \Rightarrow$ the stock did better than expected.

$a < R_F(1-b) \Rightarrow$ the stock did worse than expected.

Jensen's alpha → negative

→

* $\alpha = R_F(1-b) \Rightarrow$ the stock did as expected
 \Rightarrow o Jensen's alpha.

* Bottom up beta (fundamental beta)

Determinants of beta:

(1) Type of product

(2) Degree of operating leverage (higher leverage)
 higher risk

القيمة التي يتغير مع تغير
 Cost ~~Fixed Cost~~ rent ~~Variable~~ risk

Operating Leverage: the use of fixed operating cost to magnify the effect of the change in Sales on the firm's EBIT

Examples

	A	B	A	B
Revenue	100	100	120	120
F.C	10	80	10	80
V.C	80	10	96	12
EBIT	10	10	14	28

If sales increase 20%

EBIT = ??

$$100(1+0.2) = 120$$

(A) $80(1+0.2) = 96$ (B) $10(1+0.2)$

(A)

$$\% \Delta \text{ in Sales} = 20\%$$

$$\% \Delta \text{ in EBIT} = ?$$

$$\frac{14 - 10}{10} = \boxed{40\%}$$

(B)

$$\% \Delta \text{ in Sales} = 20\%$$

$$\% \Delta \text{ in EBIT} = ?$$

$$\frac{28 - 10}{10} = \boxed{180\%}$$

$$\text{DOL} = \frac{\% \Delta \text{ in EBIT}}{\% \Delta \text{ in Sales}} = \frac{40\%}{20\%} = 2 > 1$$

degree of operating leverage exists

$$\text{DOL} = \frac{180\%}{20\%} = 9$$

Higher operating leverage \rightarrow higher cash flow volatility \rightarrow higher risk \rightarrow higher beta.

(3) Degree of financial leverage

* Financial leverage : the use of fixed financing (debt, preferred stock) to magnify the effect of the change in EBIT on the firm's EPS

* The higher the financial leverage \rightarrow the higher the risk \rightarrow the higher the beta.

* Regression beta = beta levered = equity beta → shows the impact of the three determinants of beta which are type of product, operating leverage and financial leverage.

* Beta unlevered = asset beta → shows the impact of the determinants of beta which are type of product and operating leverage.

$$\begin{array}{ccccccc}
 & \textcircled{3} & & \textcircled{2} & & \textcircled{1} & \\
 B_L & = & B_u & * & \left(1 + (1-t) * \frac{D}{E} \right) \\
 \downarrow & & \downarrow & & \downarrow & & \downarrow \\
 \text{Beta levered} & & \text{beta unlevered} & & \text{tax rate} & & \frac{\text{Debt}}{\text{equity}}
 \end{array}$$

$$\boxed{B_L = B_u \text{ only if } \frac{D}{E} = 0}$$

no financial leverage

Effect of financial leverage on beta

<u>Debt to Capital</u>	<u>D/E</u>	<u>beta</u>	<u>Diseny</u>
0	0	1.11	$B_L = 1.25$
10%	$\frac{10}{90} = 11.11\%$	1.19	tax rate = 36.1%
20%			$\frac{D}{E} = 0.1944$
...			$\frac{D}{E} = 19.44\%$
90%			$B_U ??$

$$1.25 = B_U * (1 + (1 - 36.1\%) * 19.44\%)$$

$$\frac{1.25}{1.124} = B_U * \frac{1.124}{1.124}$$

$$\boxed{B_U = 1.11}$$

$$\text{Debt to Capital} = \frac{\text{Debt}}{\text{Capital}} = \frac{\text{Debt}}{\text{Debt} + \text{equity}}$$

$$B_L = 1.11 * (1 + (1 - 36.1\%) * \frac{10}{90})$$

$$\frac{\text{Debt}}{\text{Capital}} = \frac{\text{Debt}}{\text{Debt} + \text{equity}} = \frac{10}{100}$$

$$\therefore \text{Debt} = \boxed{10} \quad \text{equity} = \boxed{90}$$

مبلغ الدين
القسط

$$R^2 = 39.4\%$$

$$1 - R^2 = 60.6\% \rightarrow \text{firm specific risk}$$

$R^2 \rightarrow$ market risk

$1 - R^2 \rightarrow$ firm specific risk

	beta	R^2
Diseny	1.25	0.73
Amgen	1.25	0.25

Undiversified, ~~tip~~ Desing
Diversified indifferent

properties of beta:

Beta could be a weighted average.

Example b_V ?

portfolio V

<u>Assets</u>	<u>beta</u>	<u>proportion (weight)</u>
A	1.5	20%
B	1	50%
C	0.8	30%
		<u>100%</u>

$$b_v = \sum w_{\text{each asset}} * b_{\text{each asset}}$$

$$b_v = 0.2 * 1.5 + 0.5 * 1 + 0.3 * 0.8 = \boxed{1.04}$$

Calculating beta for a Combined firm:

Step 1: Calculate beta unlevered for each company

$$B_L = B_u * \left(1 + (1-t) * \frac{D}{E} \right) \quad \text{tax rate} = 36.1\%$$

Bu Disney? Bu Capital Cities?



$$1.15 = B_u * \left(1 + (1 - 36.1\%) * 0.1 \right)$$

$$1.15 = B_u * 1.0639$$

$$\boxed{B_u = 1.08}$$

Capital Cities

$$0.95 = B_u * \left(1 + (1 - 36.1\%) * 0.1 \right)$$

$$\boxed{B_u = 0.93}$$



Step 2 : Calculate beta unlevered for the Combined firm (weighted average)

$$\beta_{u, \text{Disney}} = 1.08$$

$$\beta_{u, \text{Capital Cities}} = 0.93$$

$$* W_{\text{Disney}} = \frac{\text{Value of Disney}}{\text{Value of combined firm}} = \frac{34,286 \text{ m}}{53,401 \text{ m}} = \boxed{0.64}$$

$$\begin{aligned} \text{Value combined firm} &= 34,286 \text{ m} + 19,115 \text{ m} \\ &= \$53,401 \text{ million} \end{aligned}$$

$$* W_{\text{Capital Cities}} = \frac{\text{Value of Capital Cities}}{\text{Value of combined firm}} = \frac{19,115 \text{ m}}{53,401 \text{ m}} = \boxed{0.36}$$

$$\beta_u = 0.64 * 1.08 + 0.36 * 0.93 = 1.02$$

$$\beta_{u, \text{combined}} = \sum \underset{\substack{\uparrow \\ \text{each} \\ \text{company}}}{w} * \underset{\substack{\downarrow \\ \text{each} \\ \text{company}}}{\beta_u}$$



Step 3 : Calculate beta levered for the combined firm under 3 scenarios

S₁ : If Desing bought Capital Cities with all equity

Diseny (Pre acquisition)	Capital Cities (Pre acquisitions)
Debt 3,186m	Debt 615m
Equity 31,100m	Equity 18,500m
34,286m	\$19,115m

Combined firm

$$\text{Debt} = 3,186 \text{ m} + 615 \text{ m} = \$ 3,801 \text{ m}$$

$$\text{Equity} = 31,100 \text{ m} + 18,500 = \$ 49,600 \text{ m}$$

$$\begin{aligned} B_L \text{ Combined} &= B_U * (1 + (1 - t) * \frac{D}{E}) \\ &= 1.02 * (1 + (1 - 36.1\%) * \frac{3,801 \text{ m}}{49,600 \text{ m}}) \\ &= 1.07 \end{aligned}$$

لنقل لـ 3 مائة دولار في السوق
التي كانت تساوي 100 دولار

~~1.49~~
S₂: If Disney bought Capital Cities with all debt

<u>Combined firm</u>	
Debt	$3,186 \text{ m} + 615 \text{ m} + 18,500 \text{ m}$ $= 22,301 \text{ m } \$$
Equity	$31,100 \text{ m}$

Disney will
pay 1.49
out of mkt
value

$$B_L = 1.02^{\alpha} \left(1 + (1 - 36.1\%) \times \frac{22,301 \text{ m}}{31,100 \text{ m}} \right)$$

$$\boxed{B_L = 1.49}$$

S₃: If Disney used a mixed debt & equity to buy Capital Cities

Debt = \$ 10 billion = 10,000 million

The rest = equity

<u>Combined firm</u>	
Debt	$3,186 \text{ m} + 615 \text{ m} + 10,000 \text{ m}$ $= 13,801 \text{ m } \$$
Equity	$31,100 \text{ m} + 8,500 \text{ m}$ \downarrow $(18,500 - 10,000)$ $= 39,600 \text{ m } \$$

$$B_2 = 1.02 \left(1 + (1 - 36.1\%) \times \frac{13,801m}{39,600m} \right)$$

$$B_2 = 1.25$$

② Bottom up beta

In order to calculate bottom-up beta we have to the following:

① Determine the firm's business divisions

Example : ① Media

Disney ② Parks

③ Consumer products

④ studio entertainment

⑤ Interaction

② For each business division we should do the following:

① Find Comparable Firms , The more Firms the better.

example : Studio entertainment division 10 comparable firms (US Firms that produces movies)



- (b) Get levered beta (regression beta) for each firm of the comparable firms.
- (c) Collect data on equity and debt and tax rate for each of the comparable firms.
- (d) Calculate the average and the median of the levered beta.
- (e) Calculate debt to equity ratio for each of the comparable firm.
- (f) Calculate the average and the median of the debt to equity ratio.
- (g) Calculate the average tax rate or the median.

(h) unlever the beta:

$$B_L = B_U * \left(1 + \left(1 - \frac{\text{tax rate}}{\text{average or median}} \right) * \frac{D}{E} \right)$$

average
median
average
or median
average / median

وکیل میڈیون و average وکیل میڈیون
 ۱۸۱ وکیل میڈیون

③ Calculate ~~beta~~ unlevered for all business operations:

$$B_u = \sum_{\substack{\text{each} \\ \text{division}}} w * \boxed{B_u} = \text{weighted average.}$$

for all business operations

↓
each division

↓
each division

$$\text{Weight for each division} = \frac{\text{Revenue from each division}}{\text{Total revenues.}}$$

OR

$$\text{weight for each division} = \frac{\text{Value of each division}}{\text{Total firm value.}}$$

④ Estimate beta levered for all business operations and cost of equity.

⑤ Estimate beta levered for each division and cost of equity for each division

$$\text{Cost of equity} = R_F + b^* E^* R_P$$

Median
average

$$B_L = B_U \left(1 + (1 - t) \frac{D}{E} \right)$$

$$1.24 = B_U \times (1 + (1 - 0.4)^* 0.2706)$$

$$B_U = 1.06$$

→ each business
division

Calculating bottom up beta for an unlisted firm (private):

- ① Get Comparable firms
- ② Get levered beta for each of comparable firms and calculate the average or median of beta levered
- ③ Get $\frac{D}{E}$ ratio for each of the comparable firms and calculate the average or median of $\frac{D}{E}$ ratio
- ④ Calculate the average or the median of the marginal tax rate
- ⑤ unlever the beta using the following formula:
$$B_L = B_U \left(1 + (1 - t) \frac{D}{E} \right)$$
- ⑥ Calculate beta levered for the private company of interest using the ~~average~~ ^{average} _{median} $\frac{D}{E}$ ratio for the

⇒

Whole industry the company operates in.

Calculating bottom up beta for an unlevered firm:

$$\text{Beta}_{L, \text{median}} = 0.81 \quad r^2_{\text{median}} = 0.26$$

$$\text{tax rate}_{\text{median}} = 0.4$$

$$\text{D/E ratio}_{\text{median}} = 0.2141$$

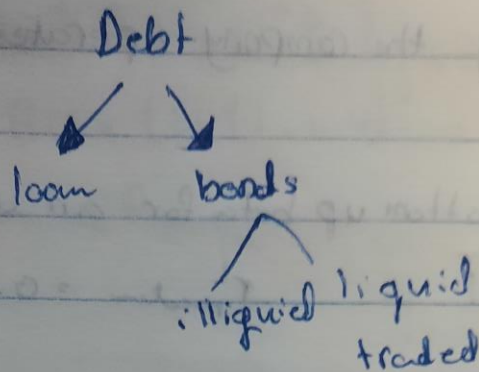
$$B_L = B_U \times (1 + (1 - t) \times \frac{D}{E})$$

$$0.81 = B_U \times (1 + (1 - 0.4) \times 0.2141)$$

$$B_U = 0.72$$

$$\begin{aligned} B_{L, \text{Brookscope}} &= 0.72 (1 + (1 - 0.4) \times 0.2141) \\ &= 0.81 \end{aligned}$$

$$\frac{B}{\sqrt{R^2}} = \frac{0.81}{\sqrt{0.26}}$$



Calculating Cost of debt:

- (a) If the firm issued bonds & they are liquid & traded, then:

$$P_B = \frac{I}{r} \left(1 - \frac{1}{(1+r)^n} \right) + \frac{\text{par}}{(1+r)^n}$$

\downarrow
 YTM

Expected Cash flows for bonds:

- ① interest payment
- ② par value

pre-tax Cost of debt $K_d = \text{YTM}$
 yield to maturity

تدکیر
 کا پیش

after tax cost of debt = pre tax cost of debt $\times (1 - t)$

- (b) If the firm issued bonds but illiquid, then look at the issuer's rating (rating done by Credit agencies)

pre tax cost of debt = R_f + default spread
 (associated with the firm's rating)

© If the firm is not rated or it has not issued bonds then:

① look at the last loan received by the firm:

The interest on the loan = pre-tax cost of debt.

② Do a synthetic rating for the firm:

pre-tax cost of debt = R_f + default spread (associated with the rating done)

Synthetic rating:

$$\text{time interest earned ratio} = \frac{\text{interest coverage ratio}}{\text{ratio}} = \frac{\text{EBIT}}{\text{Interest expense}}$$

Example

$$R_f = 5.5\%$$

$$5.5\% + 0.4\% = \boxed{5.9\%}$$

Calculating Cost of preferred stock:

$$D_0 = D_1 = D_2 = D_3 = \dots = D_N$$

price $\leftarrow P = \frac{D}{r}$ \rightarrow dividends
 \rightarrow required rate of return



present value of a perpetuity.

$$r = \frac{D}{P}$$

$$\boxed{r = KP}$$



$$WACC = w_d * k_d + w_p * k_p + w_s * k_s$$

pretax
cost of
debt

(1-t)

$$k_p = \frac{D}{P}$$

after tax

CAPM
after tax

- X+M
- R_f + default spread
- interest on the loan.

weights:

① Book Value weights

② Market Value weights

Calculating book value weights:

$$w_d = \frac{\text{Debt}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

$$w_p = \frac{\text{Preferred equity}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

$$w_s = \frac{\text{Common equity}}{\text{Debt} + \text{Preferred equity} + \text{Common equity}}$$

$$\text{ERP} = \text{market risk premium} = 5.5\%$$

$$\text{tax rate} = 40\%$$

page

$$156 \quad [1] \quad b = 0.95$$

$$\text{Treasury bill rate} = 5.8\%$$

$$\text{Treasury bond rate} = 6.4\%$$

$$\text{Debt} = \$1.7 \text{ billion}$$

$$\text{Equity} = \$1.5 \text{ billion}$$

$$\text{tax rate} = 36\%$$

$$[a] \text{ ERP} = 8.76\%$$

short term investor

$$E(r_i) = R_F + b * \text{ERP}$$

$$5.8\% + 0.95 * 8.76\% = 14.12\%$$

[b] long term investor

$$\begin{aligned} E(r_i) &= R_F + b * \text{ERP} \\ &= 6.4\% + 0.95 * 5.5\% \\ &= 11.63\% \end{aligned}$$

Cost of equity

$$[c] \text{ Cost of equity} = 11.63\%$$

⇒

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prop [2] Debt = \$1.7 billion

Equity = \$1.5 billion

tax rate = 36%

(a) $B_L = 0.95$

B_u ?

$$B_L = B_u * (1 + (1 - t) * \frac{D}{E})$$

$$0.95 = B_u * (1 + (1 - 0.36) * \frac{1.7 \text{ billion}}{1.5 \text{ billion}})$$

$$B_u = 0.55$$

(b) $\frac{0.55}{0.95} = 0.58$

↳ business risk

$$1 - 0.58 = 0.42 \rightarrow \text{Financial Risk}$$

[3] $b = 1.7$

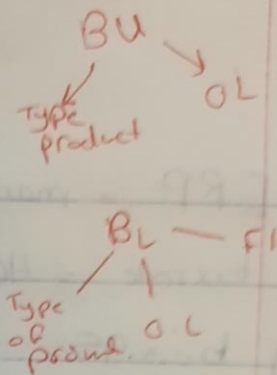
(a) Debt = 0

$$R_F = 6.4\%$$

$$ERP = 5.5\%$$

$$E(r) = 6.4\% + 1.7 * 5.5\%$$

$$K_S = 15.75\%$$



- (b) R_f زادت من 6.4 لـ 7.5
يعني اسعار تزداد ، فإذا لم
اعرف كم زاد بعوض في المعادلة

$$K_s = 7.5\% + 1.7 * 5.5\%$$

$$K_s = 16.75\%$$

- (c) فاينانسيال ريسك business risk
All risk is business risk 100%. $B_L = B_U$

- (15) Frequency of data = monthly

$$R_{\text{stock}} = 3.28\% + 1.65 R_m$$

$$\text{Treasury bill rate} = 4.8\%$$

$$\text{Treasury bond rate} = 6.4\%$$

$$\text{no. of share} = 265 \text{ million shares}$$

$$P = \$30 \text{ per share}$$

$$(a) = E(r) = ?$$

short-term

$$E(r) = R_f + b * ERF$$

$$= 4.8\% + 1.65 * 8.76\%$$

$$E(r) = 19.25\%$$

$$R_i = a + b R_m$$

$$R^2 = 0.2$$

long-run

$$ERP = 5.5\%$$

$$\text{short-run } ERP = 8.76\%$$

$$\textcircled{b} \quad E(r) = R_F + b^* \text{ERP}$$

long-run $6.4\% + 1.65 * 5.5\% = 15.47\%$

\textcircled{c} Jensen's alpha = Intercept - $(1 - \beta)R_F$
 51.1% better than expected.
 annually during the period of the regression
 annualized $R_F = ?$
 monthly $R_F = ?$

monthly overperformance = $(1 + 51.1\%)^{\frac{1}{12}} - 1$
 $= 3.5\%$
 or Jensen's alpha

$$R^2 = 0.2 \quad - (1 - 1.65)$$

$$\frac{3.5\%}{0.22} = \frac{3.28\%}{0.22} + 0.65 R_F$$

$$\frac{0.22\%}{0.65} = \frac{0.65 R_F}{0.65}$$

monthly $R_F = 0.338\%$
 annualized $R_F = (1 + 0.338\%)^{12} - 1$
 $= \boxed{4.1\%} \Rightarrow$

$$\textcircled{a} \frac{D}{E} = 0.03$$

tax rate = 40%

they will acquire a new business will

Sell debt = \$2 billion

b
↓
Combined firm

$$B_L = B_U \times \left(1 + (1 - \text{tax}) \times \frac{D}{E}\right)$$

$$1.65 = B_U \times (1 + (1 - 0.4) \times 0.03)$$

$$B_U = 1.62$$

pre acquisition

$$\text{equity} = 265 \text{m} \times 30 = 7,950 \text{ million}$$

$$\frac{\text{Debt}}{\text{equity}} = 0.03$$

$$\frac{\text{Debt}}{7,950} = 0.03$$

$$\text{Debt} = 238.5 \text{ million}$$

Combined firm

$$\text{Debt} = 238.5 \text{m} + 2000 \text{ million} = 2238.5 \text{m}$$

$$\text{Equity} = 265 \text{m} \times 30 = 7,950 \text{ million}$$

$$B_L = 1.62 \times \left(1 + (1 - 0.4) \times \frac{2238.5 \text{m}}{7,950 \text{m}}\right)$$

$$B_L = 1.89$$

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(17) $B = 1.61$

Debt = 10 billion دولار

Equity = 10 billion \$

tax rate = 40%

(a) BU?

$$B_L = B_U \left(1 + (1 - t) \times \frac{D}{E} \right)$$

$$1.61 = B_U \left(1 + (1 - 0.4) \times \frac{10 \text{ billion}}{10 \text{ billion}} \right)$$

$$\boxed{B_U = 1.01}$$

(b) Debt ratio 10%

$$\text{Debt ratio} = \text{Debt to Capital} = \frac{\text{Debt}}{\text{Debt} + \text{equity}}$$

قبل 10%
Current debt ratio = $\frac{10 \text{ billion}}{10 \text{ billion} + 10 \text{ billion}} = \frac{10 \text{ billion}}{20 \text{ billion}} = \boxed{\frac{1}{2}}$

after 1 year

$$\text{debt ratio} = \frac{50}{100} = \frac{10}{100} = 0.1$$

$$\text{Debt ratio} = \frac{\text{Debt}}{\text{Debt} + \text{equity}} = \frac{40}{100}$$

$$\text{Debt} = 40$$

$$\text{Equity} = 100 - 40 = 60 \quad \therefore \frac{D}{E} = \frac{40}{60}$$

Debt to Capital = 40%

$$B_L = B_U \times \left(1 + (1 - \text{tax}) \times \frac{D}{E} \right)$$

$$1.01 \times \left(1 + (1 - 0.4) \times \frac{40}{60} \right)$$

$$\boxed{B_L = 1.41}$$

year 2

30% debt ratio 10% coupon rate

$$\text{new debt ratio} = \frac{40}{100} - \frac{10}{100} = \boxed{30\%} = 0.3$$

$$\text{Debt ratio} = \frac{\text{Debt}}{\text{Debt} + \text{equity}} = \frac{30}{100}$$

debt = 30 equity = 70

$$\frac{D}{E} = \frac{30}{70}$$

$$B_L = B_U \times \left(1 + (1 - t) \times \frac{D}{E} \right)$$

$$1.01 \times \left(1 + (1 - 0.4) \times \frac{30}{70} \right) \quad \boxed{B_L = 1.27}$$

market value weights:

$$\text{market value of C.S.} = \frac{\text{market share}}{\text{price}} \times \text{no of Common stock}$$

$$\text{market value of P.S.} = \frac{\text{market share}}{\text{price}} \times \text{no of P.S.}$$

بند ٥٥ من الجدول ٥٥

market value of debt = ?

$$\text{market value of debt} = \frac{I}{r} \left(1 - \frac{1}{(1+r)^n} \right) + \frac{par}{(1+r)^n}$$

(the sum of time due amount of debt) \times (weight of each amount of debt) = duration \rightarrow n years

amount of debt \rightarrow Total debt

pre tax cost of debt $\rightarrow r$ years

weight \times time due = $\frac{\text{market value of debt}}{\text{total market value}} \rightarrow$ duration

$$\text{market value wd} = \frac{\text{market value of debt}}{\text{MV of C.S.} + \text{MV of P.S.} + \text{M.V of debt}}$$

$$\text{market value wp} = \frac{\text{market value of P.S.}}{\text{MV of C.S.} + \text{MV of P.S.} + \text{M.V of debt}}$$

$$\text{market value of WS} = \frac{\text{market value of C.S.}}{\text{M.V. of C.S.} + \text{M.V. of P.S.} + \text{M.V. of debt}}$$

Problem 23:

$$\text{Regression Beta} = 0.75$$

$$B_u (\text{average of comparable firm}) = 1.15$$

a) $D/E = 0.20$, tax = 40%, Beta based on the comparable firms?
(Bottom up beta)

$$B_L = B_u \left(1 + (1 - \text{tax}) \frac{D}{E} \right)$$

$$B_L = 1.15 \left(1 + (1 - 0.4) (0.2) \right)$$

$$B_L = 1.288$$

b) %95 confidence Interval Beta Regression?

$$\%95 \text{ CI} = [B \pm SE(b)(\text{Critical value})]$$

$$[0.75 \pm (0.5)(2)] = [-0.25, 1.75]$$

⇒

[c] أقل
 Bottom up
 Better
 more accurate

[d] Calculate WACC?
 Hurdle Rate

← Given

Treasury bond = 6.5%

Tiffany's bond default spread = 1%

ERP = 5.5%

preferred stock

$$WACC = w_d * K_d + w_s * K_s$$

$$\text{Cost of common equity} = R_F + b * ERP$$

↓

$$= 6.5\% + (1.29)(5.5\%)$$

debt rate

$$K_s = 13.59\%$$

$$\text{Cost of debt} = R_F + \text{default spread}$$

$$= 6.5\% + 1\%$$

$$\text{pre tax } K_d = 7.5\%$$

$$\text{After tax } K_d = (1 - 0.4) * 7.5\%$$

$$K_d = 4.5\%$$



$$\frac{D}{E} = \frac{20}{100}$$

Debt = 20 , equity = 100

$$\text{Total Capital} = \text{Debt} + \text{equity} = 120$$

$$w_d = \frac{20}{120}$$

$$w_s = \frac{100}{120}$$

$$w_{ACC} = \left(\frac{20}{120}\right)(4.5\%) + \left(\frac{100}{120}\right)(13.59\%)$$

$$w_{ACC} = 12.075\%$$