

تجميع قوانين فايننس 2 (FINN2300)

Chapter 8: RISK & RETURN

Total rate of return:

$$r_t = \frac{C_t + P_t - P_{t-1}}{P_{t-1}} \quad (8.1)$$

where

r_t = actual, expected, or required rate of return during period t
 C_t = cash (flow) received from the asset investment in the time period $t - 1$ to t
 P_t = price (value) of asset at time t
 P_{t-1} = price (value) of asset at time $t - 1$

Expected return:

$$\bar{r} = \sum_{j=1}^n r_j \times Pr_j$$

where

r_j = return for the j th outcome
 Pr_j = probability of occurrence of the j th outcome
 n = number of outcomes considered

3. The formula for finding the expected value of return, \bar{r} , when all of the outcomes, r_j , are known and their related probabilities are equal, is a simple arithmetic average:

$$\bar{r} = \frac{\sum_{j=1}^n r_j}{n} \quad (8.2a)$$

where n is the number of observations.

Standard deviation of returns:

The expression for the *standard deviation of returns*, σ_r , is⁴

$$\sigma_r = \sqrt{\sum_{j=1}^n (r_j - \bar{r})^2 \times Pr_j} \quad (8.3)$$

Coefficient of variation:

$$CV = \frac{\sigma_r}{\bar{r}} \quad (8.4)$$

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Portfolio return:

$$r_p = (w_1 \times r_1) + (w_2 \times r_2) + \cdots + (w_n \times r_n) = \sum_{j=1}^n w_j \times r_j \quad (8.5)$$

where

w_j = proportion of the portfolio's total dollar value represented by asset j

r_j = return on asset j

Of course, $\sum_{j=1}^n w_j = 1$, which means that 100 percent of the portfolio's assets must be included in this computation.

Total Security Risk:

$$\text{Total security risk} = \text{Nondiversifiable risk} + \text{Diversifiable risk} \quad (8.6)$$

Portfolio beta:

$$\beta_p = (w_1 \times \beta_1) + (w_2 \times \beta_2) + \cdots + (w_n \times \beta_n) = \sum_{j=1}^n w_j \times \beta_j \quad (8.7)$$

Of course, $\sum_{j=1}^n w_j = 1$, which means that 100 percent of the portfolio's assets must be included in this computation.

The capital asset pricing model (CAPM):

$$r_j = R_F + [\beta_j \times (r_m - R_F)] \quad (8.8)$$

where

r_j = required return on asset j

R_F = risk-free rate of return, commonly measured by the return on a U.S. Treasury bill

β_j = beta coefficient or index of nondiversifiable risk for asset j

r_m = market return; return on the market portfolio of assets

Risk-free rate of return:

$$R_F = r^* + IP \quad (8.9)$$

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Chapter 6: INTEREST RATES AND BOND VALUATION

Nominal rate of interest:

Risk premium:

Risk-free rate:

$$r_1 = \underbrace{r^* + IP}_{\text{risk-free rate, } R_F} + \underbrace{RP_1}_{\text{risk premium}} \quad (6.1)$$

As the horizontal braces below the equation indicate, the nominal rate, r_1 , can be viewed as having two basic components: a risk-free rate of return, R_F , and a risk premium, RP_1 :

$$r_1 = R_F + RP_1 \quad (6.2)$$

For the moment, ignore the risk premium, RP_1 , and focus exclusively on the risk-free rate. Equation 6.1 says that the risk-free rate can be represented as

$$R_F = r^* + IP \quad (6.3)$$

Risky non-Treasury issues:

$$r_1 = \underbrace{r^* + IP}_{\text{risk-free rate, } R_F} + \underbrace{RP_1}_{\text{risk premium}}$$

In words, the nominal rate of interest for security 1 (r_1) is equal to the risk-free rate, consisting of the real rate of interest (r^*) plus the inflation expectation premium (IP), plus the risk premium (RP_1). The *risk premium* varies with specific issuer and issue characteristics.

Value of any asset at time zero:

$$V_0 = \frac{CF_1}{(1+r)^1} + \frac{CF_2}{(1+r)^2} + \cdots + \frac{CF_n}{(1+r)^n} \quad (6.4)$$

where

V_0 = value of the asset at time zero

CF_t = cash flow *expected* at the end of year t

r = appropriate required return (discount rate)

n = relevant time period

We can use Equation 6.4 to determine the value of any asset.

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Basic model for the value:

$$B_0 = I \times \left[\sum_{t=1}^n \frac{1}{(1 + r_d)^t} \right] + M \times \left[\frac{1}{(1 + r_d)^n} \right] \quad (6.5)$$

where

B_0 = value of the bond at time zero

I = *annual* interest paid in dollars

n = number of years to maturity

M = par value in dollars

r_d = required return on the bond

Present value instead of future value:

1. Converting annual interest, I , to semiannual interest by dividing I by 2.
2. Converting the number of years to maturity, n , to the number of 6-month periods to maturity by multiplying n by 2.
3. Converting the required stated (rather than effective)⁶ annual return for similar-risk bonds that also pay semiannual interest from an annual rate, r_d , to a semiannual rate by dividing r_d by 2.

$$B_0 = \frac{I}{2} \times \left[\sum_{t=1}^{2n} \frac{1}{\left(1 + \frac{r_d}{2}\right)^t} \right] + M \times \left[\frac{1}{\left(1 + \frac{r_d}{2}\right)^{2n}} \right] \quad (6.6)$$

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CHAPTER 7: STOCK VALUATION

Basic valuation model for common stock:

$$P_0 = \frac{D_1}{(1 + r_s)^1} + \frac{D_2}{(1 + r_s)^2} + \cdots + \frac{D_\infty}{(1 + r_s)^\infty} \quad (7.1)$$

where

P_0 = value today of common stock

D_t = per-share dividend *expected* at the end of year t

r_s = required return on common stock

Zero-Growth Model:

$$P_0 = D_1 \times \sum_{t=1}^{\infty} \frac{1}{(1 + r_s)^t} = D_1 \times \frac{1}{r_s} = \frac{D_1}{r_s} \quad (7.2)$$

D_1 represent the amount of the annual dividend

Constant-Growth Model:

Gordon growth model:

By letting D_0 represent the most recent dividend, we can rewrite Equation 7.1 as

$$P_0 = \frac{D_0 \times (1 + g)^1}{(1 + r_s)^1} + \frac{D_0 \times (1 + g)^2}{(1 + r_s)^2} + \cdots + \frac{D_0 \times (1 + g)^\infty}{(1 + r_s)^\infty} \quad (7.3)$$

If we simplify Equation 7.3, it can be rewritten as

$$P_0 = \frac{D_1}{r_s - g} \quad (7.4)$$

Value of the stock:

$$P_0 = \underbrace{\sum_{t=1}^N \frac{D_0 \times (1 + g_1)^t}{(1 + r_s)^t}}_{\text{Present value of dividends during initial growth period}} + \underbrace{\left[\frac{1}{(1 + r_s)^N} \times \frac{D_{N+1}}{r_s - g_2} \right]}_{\text{Present value of price of stock at end of initial growth period}} \quad (7.5)$$

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Free cash flow valuation model:

$$V_C = \frac{FCF_1}{(1 + r_d)^1} + \frac{FCF_2}{(1 + r_d)^2} + \dots + \frac{FCF_\infty}{(1 + r_d)^\infty} \quad (7.6)$$

where

V_C = value of the entire company
 FCF_t = free cash flow *expected* at the end of year t
 r_d = the firm's weighted average cost of capital

Find common stock value:

$$V_S = V_C - V_D - V_P \quad (7.7)$$

To find common stock value: V_S , we must subtract the market value of all the firm's debt: V_D , and the market value of preferred stock: V_P from V_C :

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CHAPTER 9: COST OF CAPITAL

Before-tax cost of debt:

$$r_d = \frac{I + \frac{\$1,000 - N_d}{n}}{\frac{N_d + \$1,000}{2}} \quad (9.1)$$

where

I = annual interest in dollars
 N_d = net proceeds from the sale of debt (bond)
 n = number of years to the bond's maturity

After-tax cost of debt:

$$r_i = r_d \times (1 - T) \quad (9.2)$$

where

Tax rate: T

Cost of preferred stock:

$$r_p = \frac{D_p}{N_p} \quad (9.3)$$

where

annual dollar dividend= D_p

net proceeds from the sale of the stock N_p

Gordon growth model:

$$P_0 = \frac{D_1}{r_s - g} \quad (9.4)$$

where

P_0 = value of common stock
 D_1 = per-share dividend *expected* at the end of year 1
 r_s = required return on common stock
 g = constant rate of growth in dividends

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Cost of common stock equity:

$$r_s = \frac{D_1}{P_0} + g \quad (9.5)$$

Required return:

$$r_s = R_F + [\beta \times (r_m - R_F)] \quad (9.6)$$

where

R_F = risk-free rate of return

r_m = market return; return on the market portfolio of assets

Cost of retained earnings:

$$r_r = r_s \quad (9.7)$$

Cost of a new issue of common stock:

$$r_n = \frac{D_1}{N_n} + g \quad (9.8)$$

If we let N_n represent the net proceeds from the sale of new common stock after subtracting underpricing and flotation costs, the cost of the new issue, R_n .

Weighted average cost of capital (WACC):

$$r_a = (w_i \times r_i) + (w_p \times r_p) + (w_s \times r_{s \text{ or } n}) \quad (9.9)$$

where

w_i = proportion of long-term debt in capital structure

w_p = proportion of preferred stock in capital structure

w_s = proportion of common stock equity in capital structure

$w_i + w_p + w_s = 1.0$

R_a = weighted average cost of capital

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Chapter 10 :CAPITAL BUDGETING TECHNIQUES

Net present value (NVP):

The net present value (NPV) is found by subtracting a project's initial investment (CF_0) from the present value of its cash inflows (CF_t) discounted at a rate equal to the firm's cost of capital (r):

NPV = Present value of cash inflows – Initial investment

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+r)^t} - CF_0 \quad (10.1)$$

Profitability index (PI):

$$PI = \frac{\sum_{t=1}^n \frac{CF_t}{(1+r)^t}}{CF_0} \quad (10.2)$$

Internal Rate of Return (IRR):

$$\$0 = \sum_{t=1}^n \frac{CF_t}{(1+IRR)^t} - CF_0 \quad (10.3)$$

$$\sum_{t=1}^n \frac{CF_t}{(1+IRR)^t} = CF_0 \quad (10.3a)$$