

Chapter 25: Electrical potential and Energy

- potential energy: the amount of work needed to put that system together

- Electrical potential energy: the amount of work/energy needed per unit of charge to move the charge from the reference point to a specific point in an electric field.

$$V = \frac{U}{Q}$$

U : the electrical potential energy of charge Q

- Two different charges placed in the same position would have different potential energies, but they would have identical electrical potentials.

- The work and Electrical potential:

→ The work done on the charge by the electric field = to the reduction in electrical potential energy.

$$\Delta U = -W_{\text{elec}}$$

example: if the charge moves to a position where its electrical potential energy is lower, the change in ΔU is negative and the charge has a positive work done on it by the field.

$$\begin{aligned} \rightarrow W_{\text{elec}} &= \text{Force} \times \text{distance} \\ &= F \times \Delta x \end{aligned}$$

$$\rightarrow F = qE$$

$$\therefore W_{\text{elec}} = qE \Delta x$$

$$\Delta U = \frac{Vq}{q}$$

$$\Delta U = -W_{\text{elec}}$$

$$\therefore \frac{\Delta V q}{q} = -qE \Delta x$$

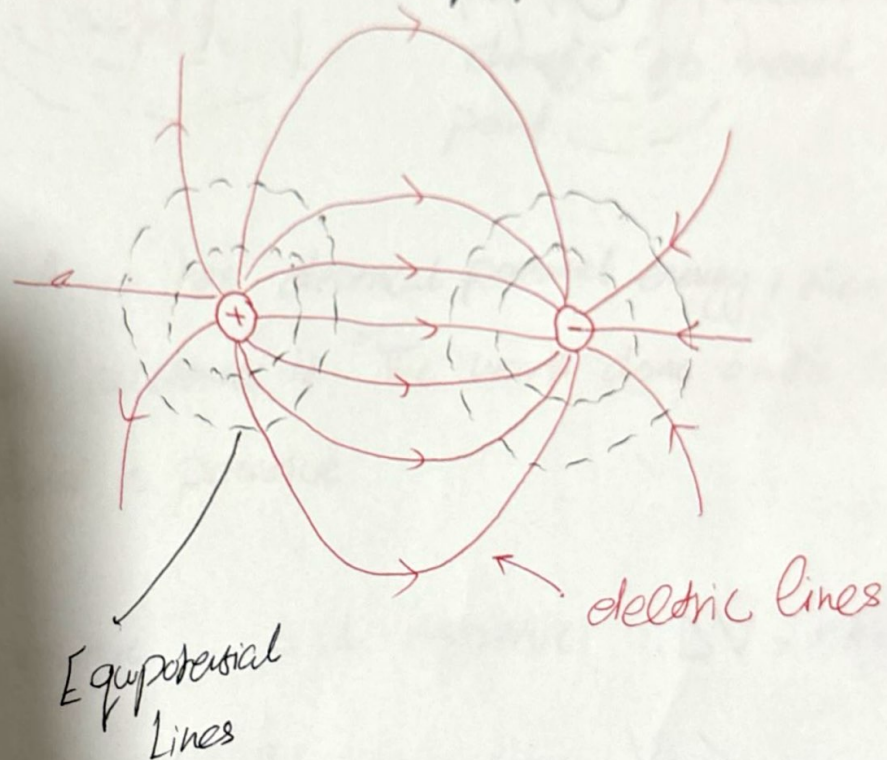
$$\therefore \Delta V = -E \Delta x$$

$$E = - \frac{\Delta V}{\Delta x}$$

see Example 25.1, 25.2

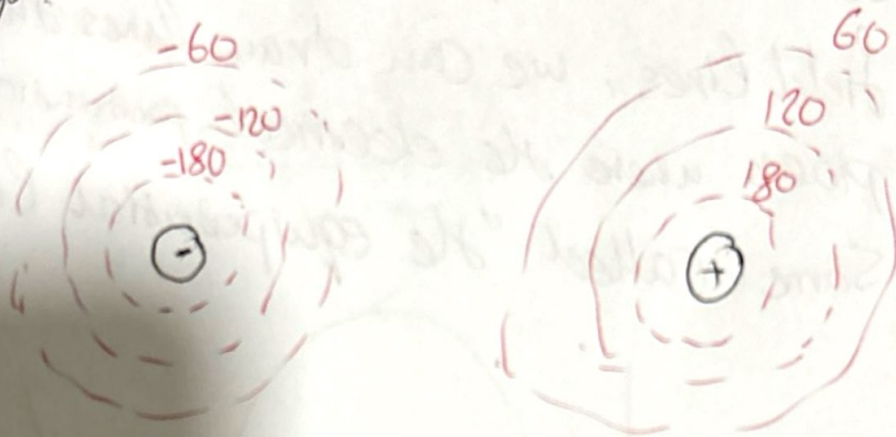
Equipotential and field lines:

- The electrical potential is a scalar quantity. So rather than representing it with vectors or field lines, we can draw lines that show places where the electrical potential is the same. called "the equipotential lines"

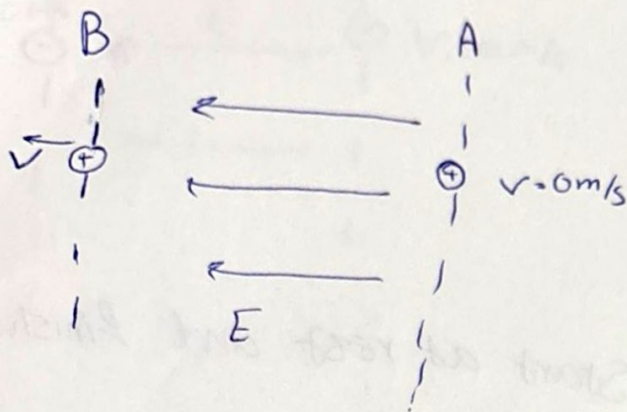


- because any change in position that has a component in the direction of the electric field will result in a change in potential ($\Delta V = E \Delta x$)
equipotential lines are always perpendicular to electric field lines.

it may help to think of the equipotential lines as being like contour lines on a topographic map.



- Positive charge, No External force.



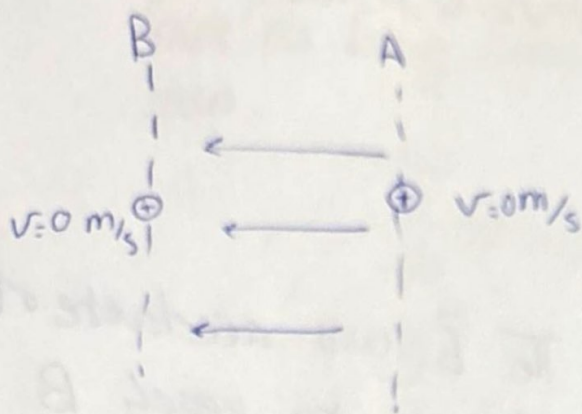
- The $\vec{E}$ will accelerate the charge so reach B point.

at point A it has electrical potential energy, then the $\vec{E}$ field will accelerate it "The work done on the charge by the field is positive"

- if W positive $\therefore \Delta U$ negative $\therefore \Delta V = \text{negative}$

$$\Delta V = V_B - V_A \quad \text{where } V_A > V_B$$

* positive charge, External force



- Start at rest and finishes at B rest.

- So, The work done by the external force "Non-electrical" is negative and equal in magnitude to the work done by the $\vec{E}$ field.

$$K.E_f + U_f = K.E_i + U_i + W_{app}$$

W_{app} : external force

$W_{electrical} = (U_f - U_i) = -\Delta U$: electrical force ($\vec{E}$)

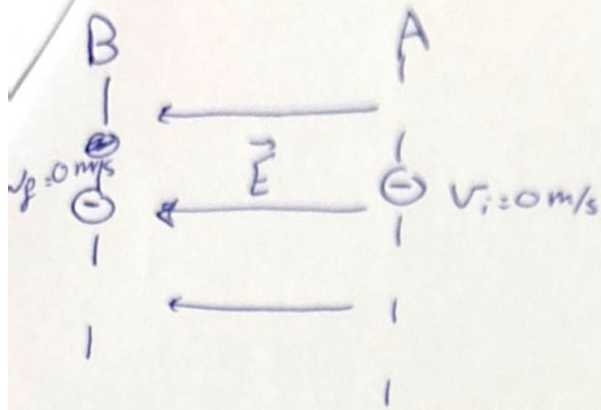
$$\Delta K.E_f = \text{Zero}$$

→ To balance the equation we need to consider the W_{app}

and W_{app} should be negative

$$W_{app} = W_{ele}$$

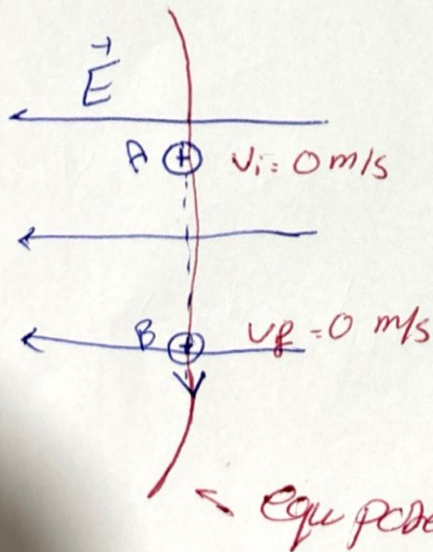
* Negative Change, External Force:



- The work done by $\vec{E}$ on the charge is negative, and equal in magnitude with W_{app} , W_{app} is positive.

$$\Delta U = U_f - U_i \quad \therefore W_{ele} = \text{negative.}$$

* Charge moving perpendicular to the field



- There is no work done by the field on the charge. ? why.

← Equipotential line.

* in this path there is no change in the electrical potential energy. where $V_B = V_A \quad \therefore W = \text{Zero.}$