Modern Control Theory. The modern trend in engineering systems is toward greater complexity, due mainly to the requirements of complex tasks and good accuracy. Complex systems may have multiple inputs and multiple outputs and may be time varying. Because of the necessity of meeting increasingly stringent requirements on the performance of control systems, the increase in system complexity, and easy access to large scale computers, modern control theory, which is a new approach to the analysis and design of complex control systems, has been developed since around 1960. This new approach is based on the concept of state. The concept of state by itself is not new, since it has been in existence for a long time in the field of classical dynamics and other fields.

Modern Control Theory Versus Conventional Control Theory. Modern control theory is contrasted with conventional control theory in that the former is applicable to multiple-input, multiple-output systems, which may be linear or nonlinear, time invariant or time varying, while the latter is applicable only to linear time-invariant single-input, single-output systems. Also, modern control theory is essentially time-domain approach and frequency domain approach (in certain cases such as H-infinity control), while conventional control theory is a complex frequency-domain approach. Before we proceed further, we must define state, state variables, state vector, and state space.

Modern Control

A Cinear Sys + nonlinersys

A it Can dead with SISO Sys: - Single input

SISO, SI MO, MISO Single output

and MIMO Sys.

Wes Sys Siso

Wes Sys Siso

Wes Single output

Wes Single outp

Moder Control * time domai, n Con ventional Conta * S-Domin (root boos Freq Domain * LTI - linear

LTV: - linear time

LTV: - lineur time Vousient \$885. 5

LTT

rocket

x it can deal with

LTJ

EF=mix

mix + Kx=FE

where

Where

Kit Constants

with uncertainty

State. The state of a dynamic system is the smallest set of variables (called *state variables*) such that knowledge of these variables at $t = t_0$, together with knowledge of the input for $t \ge t_0$, completely determines the behavior of the system for any time

Note that the concept of state is by no means limited to physical systems. It is applicable to biological systems, economic systems, social systems, and others.

State Variables. The state variables of a dynamic system are the variables making up the smallest set of variables that determine the state of the dynamic system. If at

least n variables $x_1, x_2, ..., x_n$ are needed to completely describe the behavior of a dynamic system (so that once the input is given for $t \ge t_0$ and the initial state at $t = t_0$ is specified, the future state of the system is completely determined), then such n variables are a set of state variables.

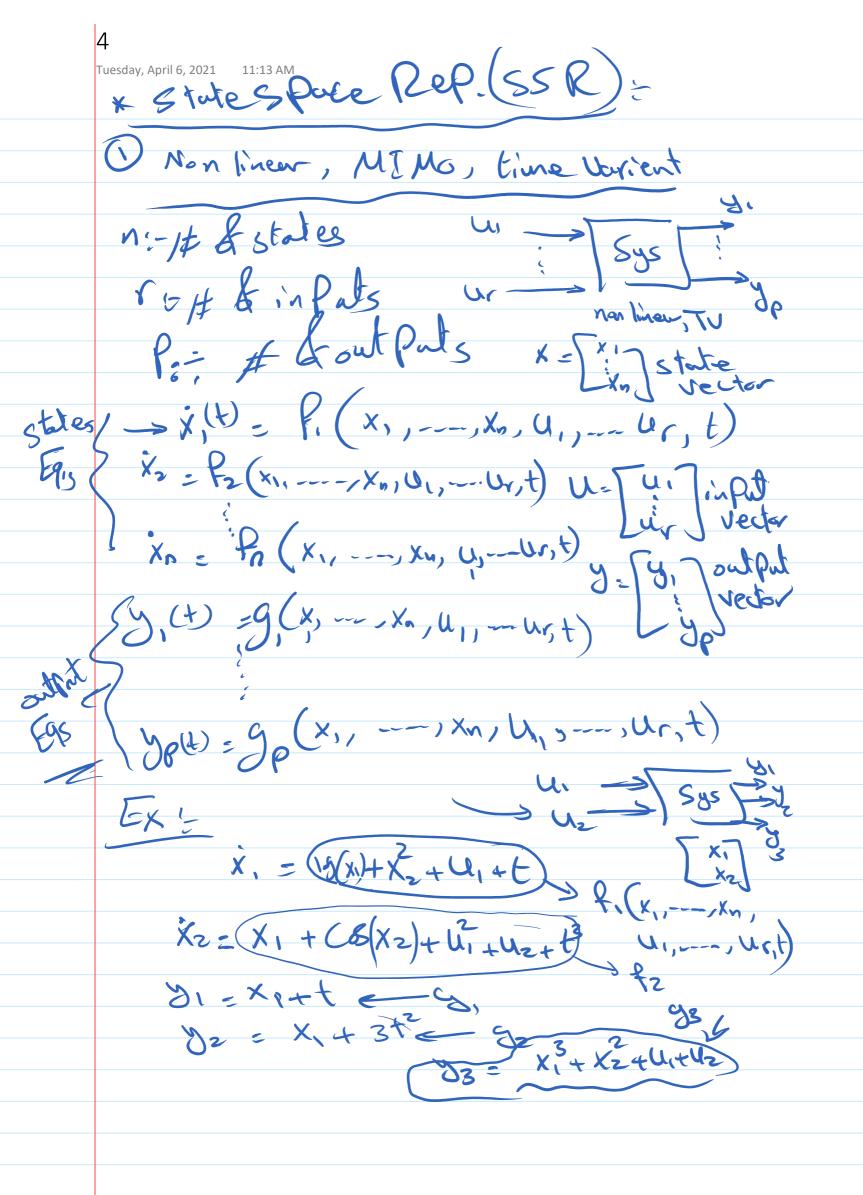
States

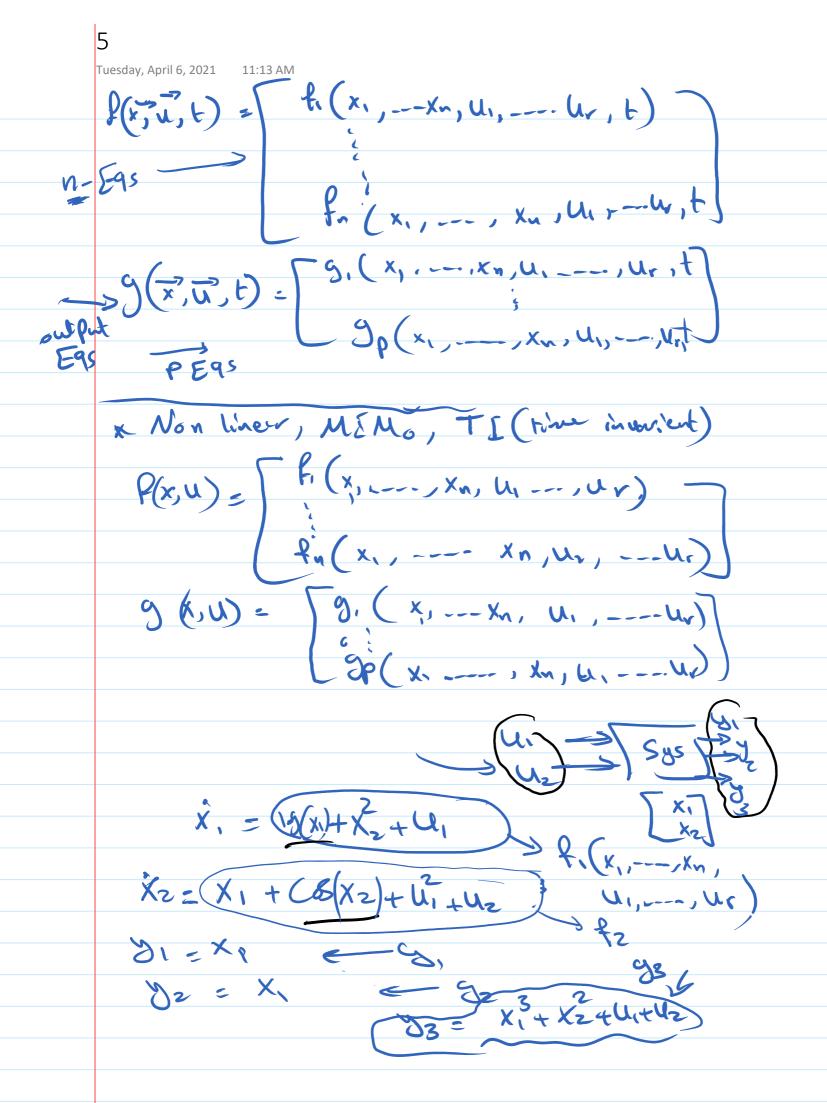
State Vector. If n state variables are needed to completely describe the behavior of a given system, then these n state variables can be considered the n components of a vector \mathbf{x} . Such a vector is called a *state vector*. A state vector is thus a vector that determines uniquely the system state $\mathbf{x}(t)$ for any time $t \ge t_0$, once the state at $t = t_0$ is given and the input u(t) for $t \ge t_0$ is specified.

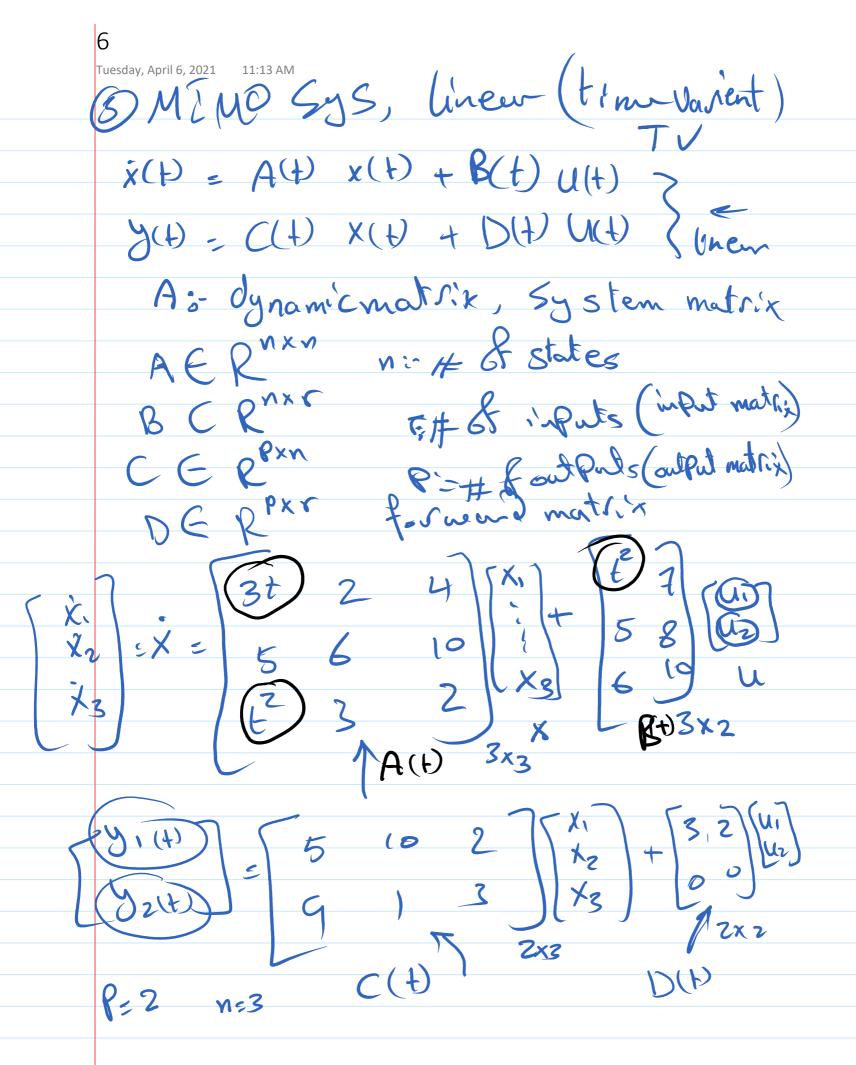
State Space. The *n*-dimensional space whose coordinate axes consist of the x_1 axis, x_2 axis, ..., x_n axis, where $x_1, x_2, ..., x_n$ are state variables, is called a *state space*. Any state can be represented by a point in the state space.

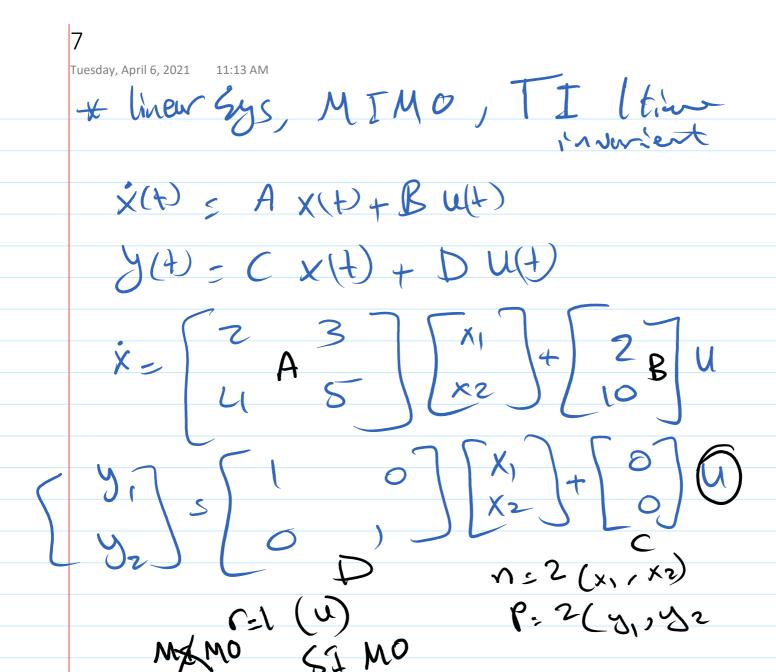
State-Space Equations. In state-space analysis we are concerned with three types of variables that are involved in the modeling of dynamic systems: input variables, out put variables, and state variables. As we shall see in Section 2–5, the state-space representation for a given system is not unique, except that the number of state variables is the same for any of the different state-space representations of the same system.

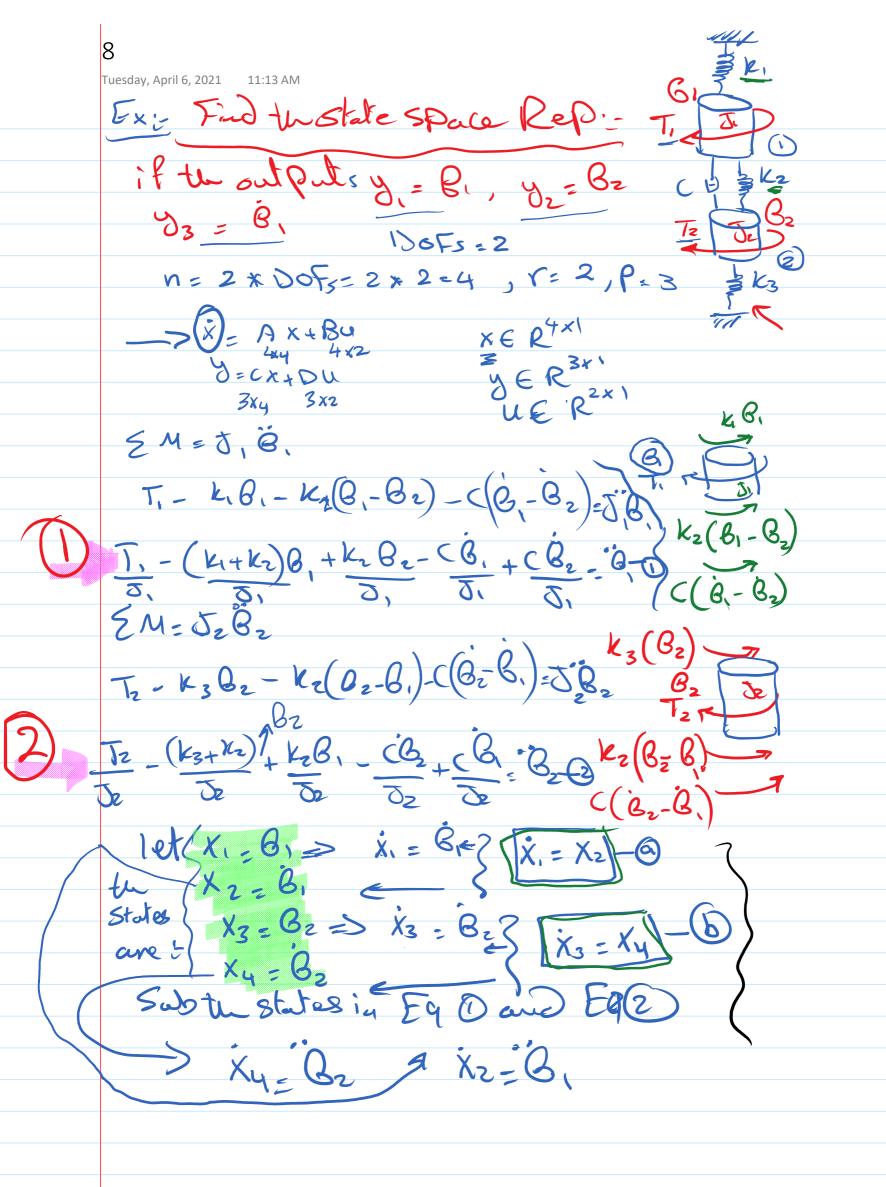
The dynamic system must involve elements that memorize the values of the input for $t \ge t_1$. Since integrators in a continuous-time control system serve as memory devices, the outputs of such integrators can be considered as the variables that define the internal state of the dynamic system. Thus the outputs of integrators serve as state variables. The number of state variables to completely define the dynamics of the system is equal to the number of integrators involved in the system.

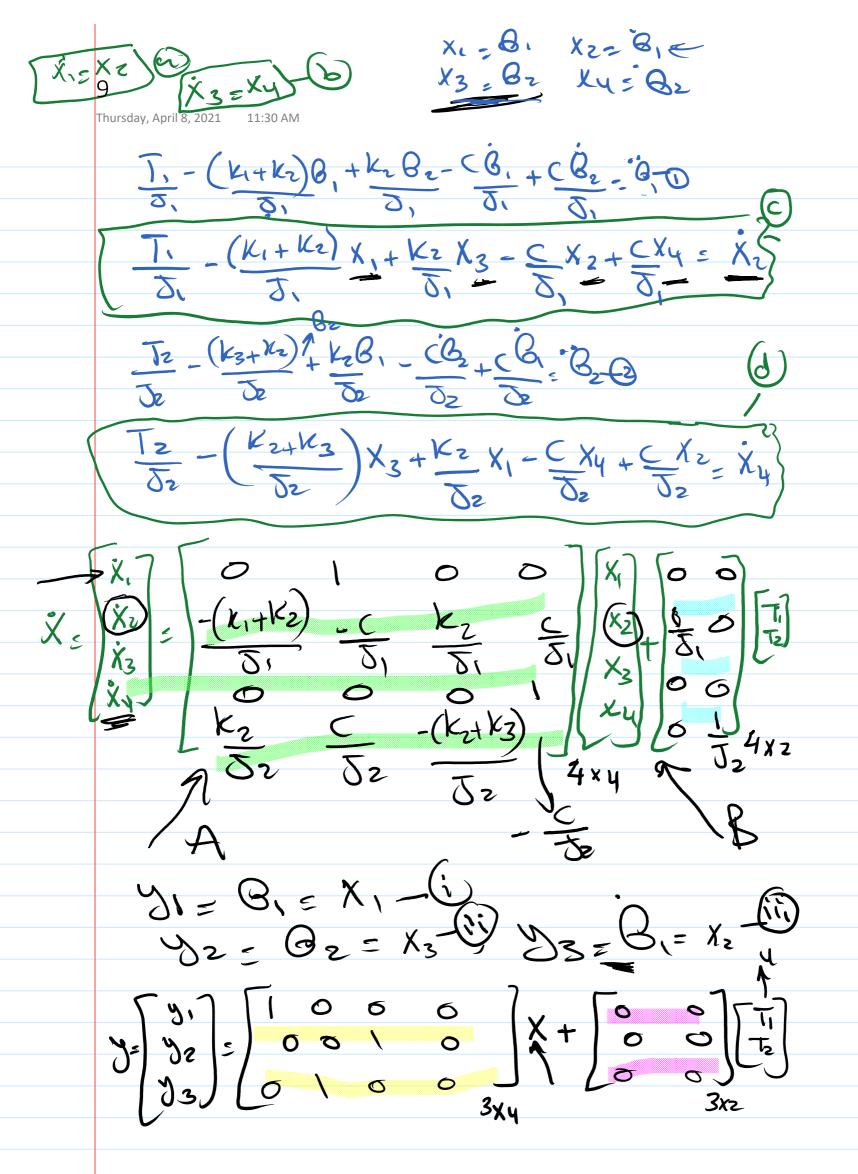


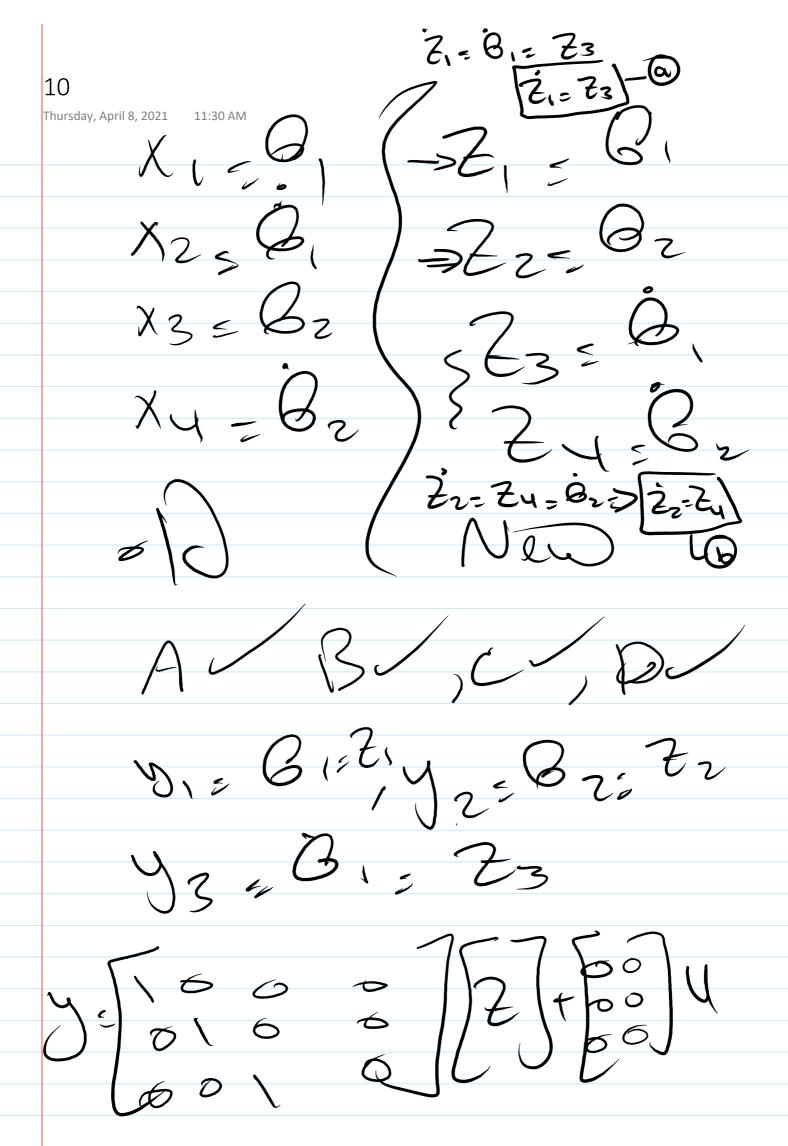


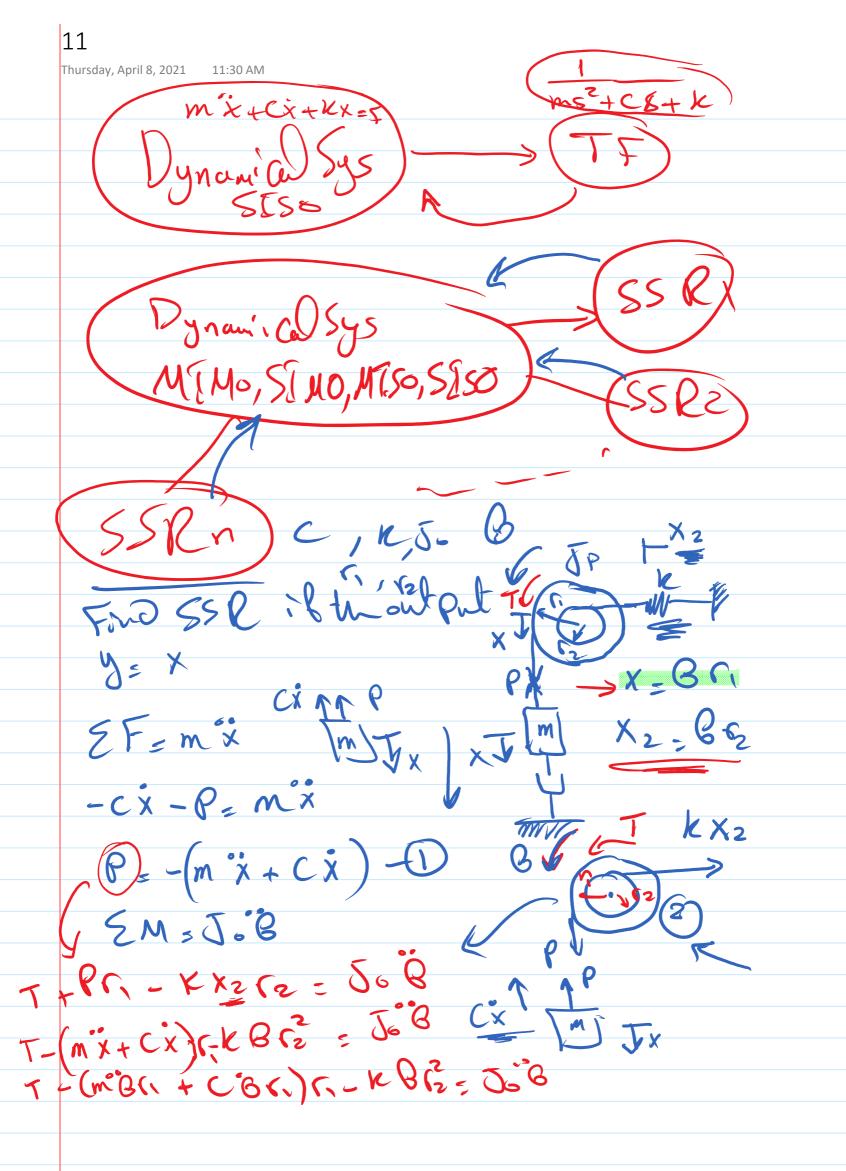


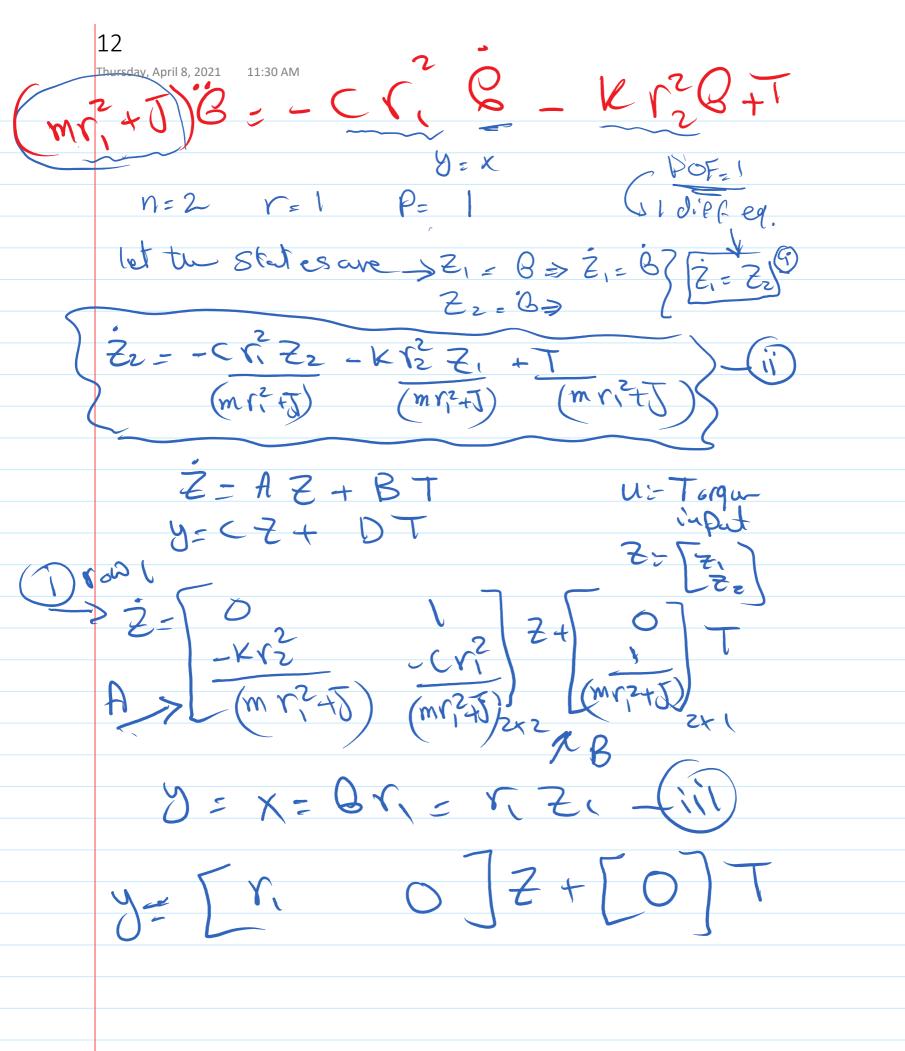


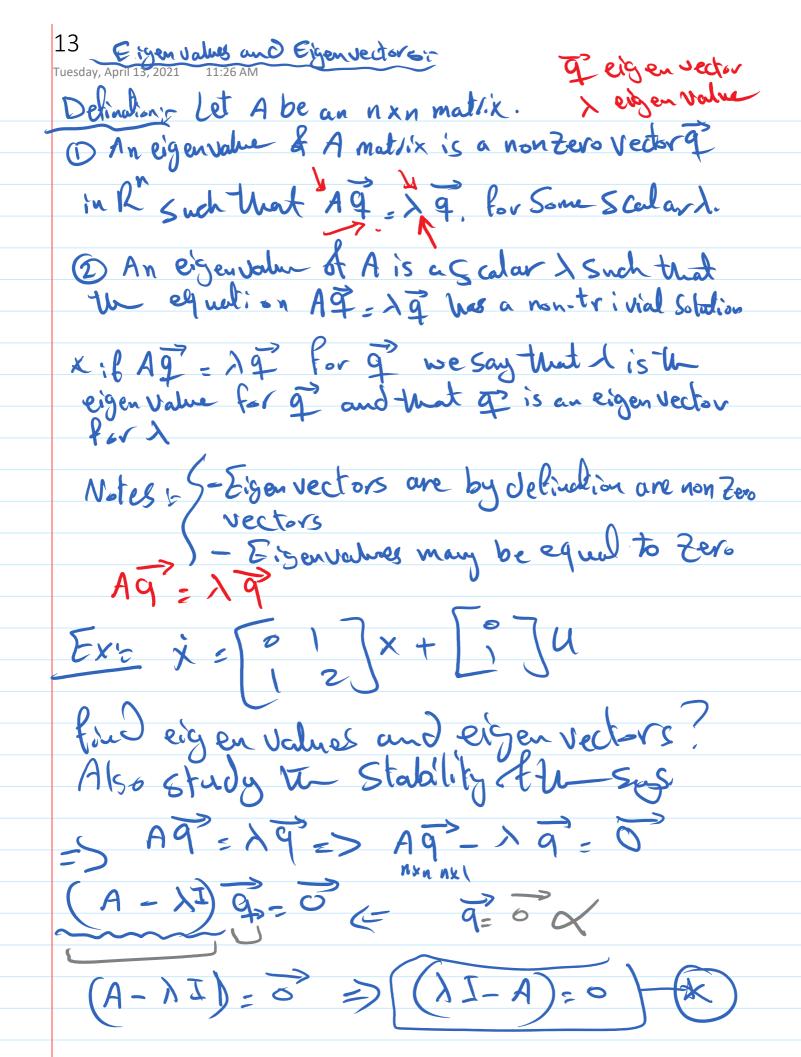


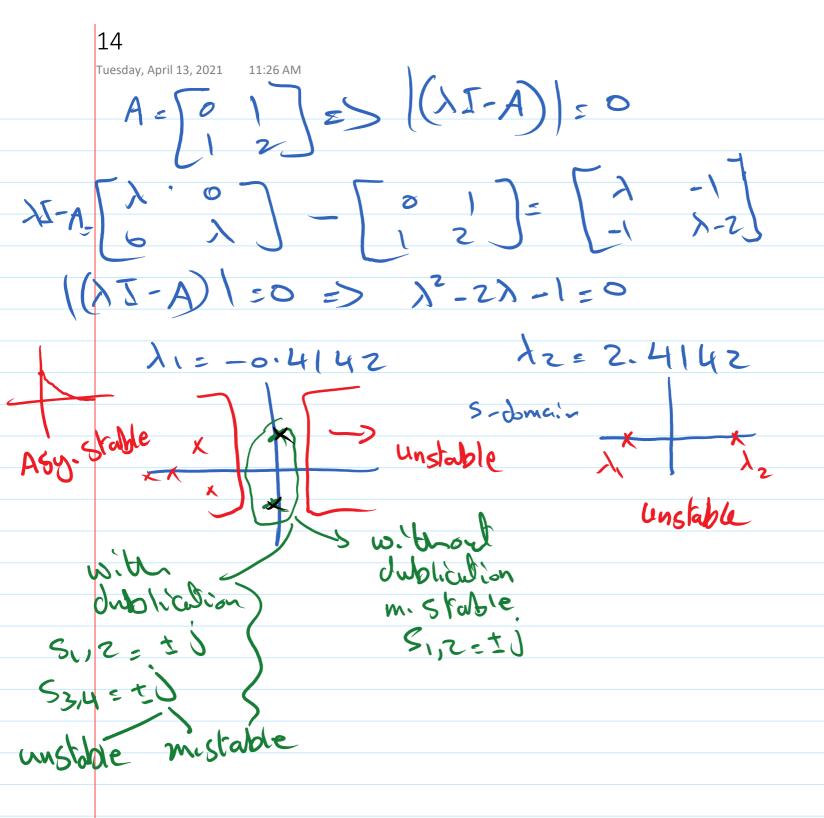


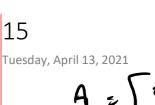


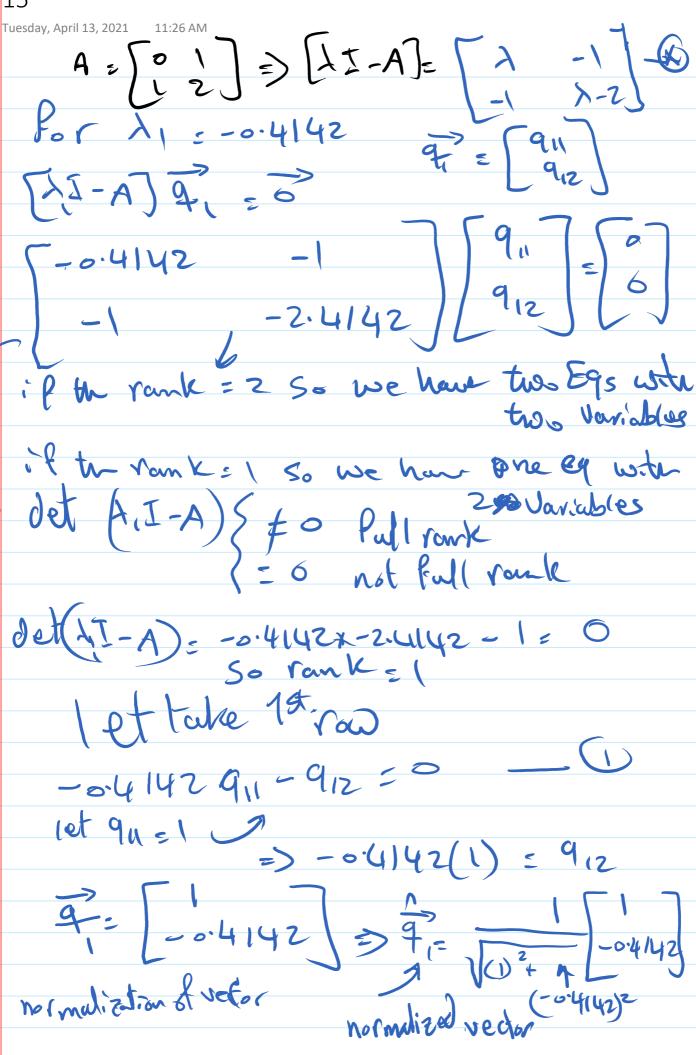


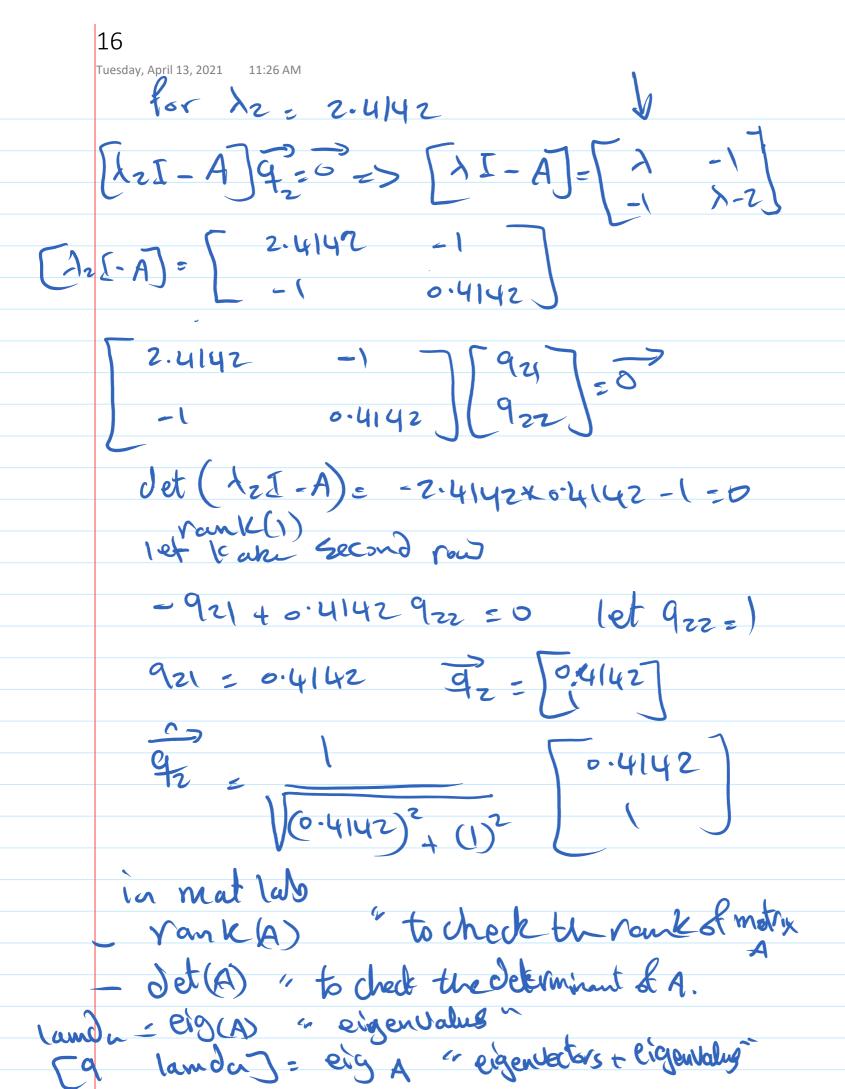












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