

## Chapter 8

## Chapter 8

## - Risk &amp; Return

- Returns  $\rightarrow$  Dividends $\rightarrow$  Appreciation of stock price \$3  $\rightarrow$  \$3.5

- The company should not give dividends when stock is lost, because it will automatically face higher costs with no revenues.

## - Risk Preferences : أنواع

## 1. Risk averse

$\rightarrow$  Rational in decisions, what ever Risk they take they want Return for it.  $\uparrow$  Return  $\uparrow$  Risk.

## 2. Risk neutral

$\rightarrow$  investors choose the investment with higher return regardless of its Risk, I want this much of Return & he wants to reach it 3% from government, individuals... etc

## 3. Risk seekers "lovers"

$\rightarrow$  investors prefer investing with greater risk, even if the expected Return is low.

ex: investing in a country that has war.  $\rightarrow$

- Risk is always uncertain, nothing is stable

Risk = uncertainty.

Risk & Return  $\left\{ \begin{array}{l} \rightarrow \text{Single asset} \\ \rightarrow \text{Portfolio} \end{array} \right.$

- To Reduce Risk  $\rightarrow$   $\rightarrow$  we should do "Diversification"  $\rightarrow$  التنوع

- Returns for single asset

$$= \frac{\text{new } P - \text{old } P}{\text{old } P} = \frac{(P_t - P_{t-1}) + C_t}{P_{t-1}}$$

$C_t \rightarrow$  is Dividend  
Cash flow.

- when they don't give dividend that means  $C_t = \text{Zero}$

Examples:

	Buy	End	Dividend	note:- new is End old is Buy
Apple	411.23	532.17	5.30	
walmart	60.33	68.23	1.59	

$$\begin{aligned} \text{Returns for apple} &= \frac{532.17 - 411.23 + 5.30}{411.23} \\ &= 30\% \end{aligned}$$

$$\begin{aligned} \text{Returns for walmart} &= \frac{68.23 - 60.33 + 1.59}{60.33} \\ &= 15.7\% \end{aligned}$$

1) Range "Risk" = Pessimistic outcome  
- optimistic outcome

	Asset "A"	Asset "B"
Initial investment	\$10,000	10,000
CF <sub>0</sub>		

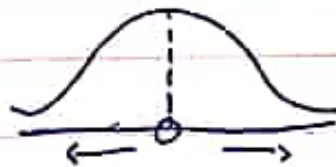
Annual Return

↳ pessimistic	13%	7%
↳ most likely	15%	15%
↳ optimistic	17%	23%

$$\begin{aligned} \text{Range} &= \text{optimistic} - \text{pessimistic} \\ &= 17\% - 13\% \\ &= 4\% \end{aligned} \quad \left. \vphantom{\begin{aligned} \text{Range} &= \text{optimistic} - \text{pessimistic} \\ &= 17\% - 13\% \\ &= 4\% \end{aligned}} \right\} \text{Asset "A"}$$

$$\begin{aligned} \text{Range} &= \text{optimistic} - \text{pessimistic} \\ &= 23\% - 7\% \\ &= 16\% \end{aligned} \quad \left. \vphantom{\begin{aligned} \text{Range} &= \text{optimistic} - \text{pessimistic} \\ &= 23\% - 7\% \\ &= 16\% \end{aligned}} \right\} \text{Asset "B"}$$

2) Probability Distribution



3) Standard deviation

→

4) Beta → شرح على لقدام

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### 3) Standard deviation

- rf for a period

$$\sigma_i = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

- if for a probability

$$\sigma_i = \sqrt{\sum (x_i - \bar{x})^2 \times \text{probability}}$$

$x_i \rightarrow$  Return Asset

$\bar{x} \rightarrow$  Expected Return

"Step one"  $x_i \rightarrow$  Return for single asset.

$$x_i = R_i = \frac{C_{\text{new}} - \text{old})}{\text{old}} + CF_i$$

"Step two"  $\bar{x}_n = \frac{\sum x_i}{n}$   $n \rightarrow$  Period

$$\bar{x}_p = \sum x_i \times \text{probability}$$

$$\bar{R}_p = \sum R_i \times \text{probability}$$

Example 8-

Asset "A"

	Return	Probability	expected Return
pessementric	13%	0.25	$13\% \times 0.25 = 3.25\%$
most likely	15%	0.50	$15\% \times 0.50 = 7.50\%$
optimistic	17%	0.25	$17\% \times 0.25 = 4.25\%$

$$\Sigma = 15\%$$

Asset "B"

	Return	Probability	expected Return
pessementric	7%	0.25	$7\% \times 0.25 = 1.75\%$
most likely	15%	0.50	$15\% \times 0.50 = 7.50\%$
optimistic	23%	0.25	$23\% \times 0.25 = 5.75\%$

$$\Sigma 15\%$$

Both expected Returns are 15%. So it doesn't matter in which asset i invest, "A or B"

$$\sigma_A = \sqrt{\Sigma (X_A - \bar{X})^2 \times \text{probability}} \quad \text{Note: } X_A \rightarrow \text{Return}$$

$\bar{X} \rightarrow \Sigma \text{ expected Ret}$

$X_A$	$\bar{X}$	$X_A - \bar{X}$	$(X_A - \bar{X})^2$	Prob	$(X_A - \bar{X})^2 \times \text{Prob}$
13%	15%	-2%	4%	0.25	1%
15%	15%	0%	0%	0.50	0%
17%	15%	2%	4%	0.25	1%
					$\Sigma 2\%$

$$= \sqrt{2\%} = \sqrt{1.41\%} = \text{Risk.}$$

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$$\sigma = \sqrt{\sum (X_i - \bar{X})^2 \cdot \text{Probability}}$$

$X_i$	$\bar{X}$	$X_i - \bar{X}$	$(X_i - \bar{X})^2$	Prob	$(X_i - \bar{X})^2 \cdot \text{Prob}$
71.	151.	-81.	641.	0.25	161.
151.	151.	01.	01.	0.50	01.
231.	151.	81.	641.	0.25	161.

$\Sigma 321.$

$$\sigma = \sqrt{321.} = \sqrt{5.61.} = \text{Risk}$$

$$\text{Coefficient of Variation} = \frac{\sigma}{\mu} = \frac{5.61.}{10.471.} = 0.525 \approx 0.53$$

in the question she said if the Risk is 0.75 or less shall take it. the Risk is 0.53 so she will make the decision of investing.

\* Note 6  $\rightarrow$  is Risk

Examples

if Return "A"

	Return	Risk
A	15%	1.411.
B	201.	5.61.

$$\text{Coefficient variance "A"} = \frac{\sigma}{R} = \frac{1.411.}{151.}$$

$$= 0.094$$

وحدة القياس بـ 100

$$\text{Coefficient variance "B"} = \frac{\sigma}{R} = \frac{5.61.}{201.} = 0.28$$

Example 8:

Year	Buy P	End P	Dividend
2013	\$ 35	\$36.5	\$ 2.50
2014	\$36.5	\$34.5	\$ 3.50
2015	\$34.5	\$ 35	\$ 4

$$\begin{aligned} \text{Return}_1 &= \frac{(36.5 - 35) + 3.50}{35} = 14.3\% \\ \text{Return}_2 &= \frac{(34.5 - 36.5) + 3.50}{36.5} = 4\% \\ \text{Return}_3 &= \frac{(35 - 34.5) + 4}{34.5} = 13\% \end{aligned}$$

$$\begin{aligned} \sum R &= \bar{X} \\ 14.3 + 4 + 13 \\ &= 10.43\% \end{aligned}$$

$X = \text{Single } R$

Year	$X$	$\bar{X}$	$X - \bar{X}$	$(X - \bar{X})^2$
2013,	14.3%	10.43%	3.9%	15.21%
2014,	4%	10.43%	-6.43%	41.3%
2015,	13%	10.43%	2.57%	6.6%

$$\sum = 63.11\%$$

$$n-1 = 3-1 = 2 \quad \text{Since its period}$$

$$\sqrt{\frac{\sum (X - \bar{X})^2}{n-1}} = \sqrt{\frac{63.11\%}{2}} = 5.62\%$$



Portfolio  $\rightarrow$  Return  
 $\hookrightarrow$  Risk

$$R_{\text{portfolio}} = \sum (w_i \times R_i)$$

-  $w_i \rightarrow$  weighted proportion

-  $R_i \rightarrow$  Return of each single asset.

Examples:-

100 Shares from Walmart  $\rightarrow$  \$55 / per share = \$ 5,500

100 Shares from Cisco system  $\rightarrow$  \$25 / per share = \$ 2,500

$$w_i = \frac{5,500}{8,000} = 68.75\% \quad \text{Total Portfolio} = 8,000$$

$$w_i = \frac{2,500}{8,000} = 31.25\%$$

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- given in question "0.50"

Year	Asset $x_i$	Asset $y_i$	$R_{\text{Portfolio}}$	Expected $R$
2014	8%	16%	$(0.50 \times 8\%) + (0.50 \times 16\%)$	= 12%
2015	10%	14%	$(0.50 \times 10\%) + (0.50 \times 14\%)$	= 12%
2016	12%	12%	$(0.50 \times 12\%) + (0.50 \times 12\%)$	= 12%
2017	14%	10%	$(0.50 \times 14\%) + (0.50 \times 10\%)$	= 12%
2018	16%	8%	$(0.50 \times 16\%) + (0.50 \times 8\%)$	= 12%

$$\bar{R}_p = \frac{\sum R_i}{n} = \frac{12\% + 12\% + 12\% + 12\% + 12\%}{5} = \frac{60\%}{5} = 12\%$$

$$\sigma_p = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{(12\% - 12\%)^2 + \dots \text{5 times}}{5-1}} = \sqrt{\frac{0\%}{4}} = 0\%$$

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Year	$R_y$	$R_x$	$R_{p \& B} \text{ by } x, y$	
2014	8%	8%	$(0.50 \times 8\%) + (0.50 \times 8\%)$	= 8%
2015	10%	10%	$(0.50 \times 10\%) + (0.50 \times 10\%)$	= 10%
2016	12%	12%	$(0.50 \times 12\%) + (0.50 \times 12\%)$	= 12%
2017	14%	14%	$(0.50 \times 14\%) + (0.50 \times 14\%)$	= 14%
2018	16%	16%	$(0.50 \times 16\%) + (0.50 \times 16\%)$	= 16%

$$\bar{R}_p = \frac{8\% + 10\% + 12\% + 14\% + 16\%}{5} = 12\%$$

$$\sigma_{rp} = \sqrt{\frac{(8-12)^2 + (10-12)^2 + (12-12)^2 + (14-12)^2 + (16-12)^2}{5-1}}$$

$$\sigma_{rp} = \sqrt{10\%} = 3.1622 \approx 3.2\%$$

→ Correlation  $\begin{cases} \rightarrow \text{Positive Correlation} \rightarrow \text{Same direction} \\ \rightarrow \text{Negative Correlation} \rightarrow \text{opposite direction} \end{cases}$

→ Correlation Coefficient

- Perfectly Positively Correlation → +1

- Perfectly Negatively Correlation → -1

↳ unCorrelation = zero

There's Risk  $\downarrow$

Example 8

Year	R <sub>top</sub>	R <sub>parallel</sub>	R <sub>parallel</sub>	R <sub>bop, parallel</sub>	R <sub>parallel, parallel</sub>
1	4%	5%	6%	19%	5.3%
2	6%	7.4%	4%	6.6%	6.1%
3	7%	4%	2%	5.2%	3.4%
4	10%	6%	1%	7.6%	4.5%

P<sub>1</sub> → Bop "bank of Palestine" 40%  
 ↳ Parallel 60%

P<sub>2</sub> → Parallel → 70%  
 ↳ parallel → 30%

$$\bar{R}_1 = 9.6\% \quad \bar{R}_2 = 4.825\%$$

$$\sigma_1 = \sqrt{(19\% - 9.6\%)^2 + (6.6\% - 9.6\%)^2 + (5.2\% - 9.6\%)^2 + (7.6\% - 9.6\%)^2}$$

$$\sigma_1 = \sqrt{\frac{85.36 + 9 + 19.36 + 4}{3}} = 6.34\%$$

$$\sigma_2 = \sqrt{\frac{(5.3\% - 4.825\%)^2 + (6.1\% - 4.825\%)^2 + (3.4\% - 4.825\%)^2 + (4.5\% - 4.825\%)^2}{4 - 1}}$$

$$= \sqrt{\frac{0.225 + 1.62 + 2.03 + 0.105}{3}} = \sqrt{\frac{3.98}{3}} = 1.15\%$$

$$- CV_1 = \frac{\sigma}{\bar{R}} = \frac{6.34\%}{9.6\%} = \underline{\underline{0.66}} \quad - CV_2 = \frac{\sigma}{\bar{R}} = \frac{1.15\%}{4.825\%} = \underline{\underline{0.238}}$$

Second for Ratio is the best choice because it has lower G & CV.  
 So → lower Risk.

## Risk & Return

- CAPM → Capital asset pricing method.

$R_s$  = Return of the asset "stock"

Note:  $(R_m - R_f)$  is called  
↳ market Risk premium.

$$R_s = R_f + \text{Beta} \times (R_m - R_f)$$

-  $R_s$  → Return of the asset

-  $R_f$  → Risk Free → treasury bills, treasury bond → بحدود الحكومة  
→ Government bond.

-  $R_m$  → The market index → Al-Duch index

- Beta → Risk

Total Risk = Diversifiable Risk + Nondiversifiable Risk

= Unsystematic Risk + Systematic Risk

= Specific Risk + market Risk

\* Beta only measures the Nondiversifiable Risk

Beta قيمته -2 , 2 بتراوح بين

-2 → Return عكس the market

+2 → Return same direction of the market

Beta for the market = 1

$B = 1.5$  → if the market increase by 1, it will go up by 1.5

$B = -1.5$  → if the market increase by 1, it will go down by 1.5



## Examples

	<u>Beta</u>	<u>Total investment</u>	<u>weighted</u>
Amazon	0.82	50,000	25%
E. bay	0.87	40,000	20%
Walmart	0.99	20,000	10%
Microsoft	1.18	60,000	30%
Yahoo	0.89	<u>30,000</u>	15%
		$\Sigma$ 200,000	

$$\text{Beta Portfolio} = \Sigma (w_i \times \text{Beta}_i)$$

$$= 0.965$$

$$\text{weighted} = \frac{50,000}{200,000} = 25\%$$

$$\frac{20,000}{200,000} = 10\%$$

$$\frac{40,000}{200,000} = 20\%$$

$$\frac{60,000}{200,000} = 30\%$$

$$\frac{30,000}{200,000} = 15\%$$

Example

Portfolio V

Portfolio W

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Asset	Proportion	Beta	Proportion	Beta
1	0.10	1.65	0.10	0.80
2	0.30	1.00	0.10	1.00
3	0.20	1.30	0.20	0.65
4	0.20	1.10	0.10	0.75
5	0.20	1.25	0.50	1.05

Example 3.

$$\text{Beta} = 1.5$$

$$R_z = R_f + \text{Beta} (R_m - R_f)$$

$$R_f = 7\%$$

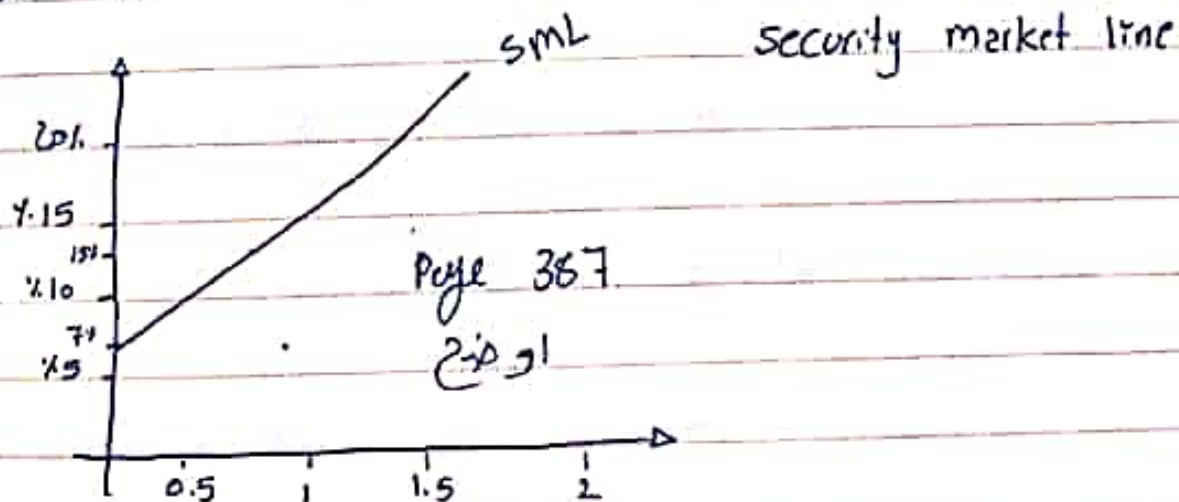
$$= 7\% + 1.5 (11\% - 7\%)$$

$$R_m = 11\%$$

$$= 13\%$$

$$R_z = ??$$

$$R_z = 13\%$$



Δ Risk Free =

"Actual" Nominal Rate = Real rate + Expected inflation

Example page - 208. Problems solution.

**PS-4**

$$A) \text{ Range}_A = \text{optimistic} - \text{pessimistic}$$

$$= 24\% - 16\%$$

$$= 8\%$$

$$\text{Range}_B = 30\% - 10\%$$

$$= 20\%$$

B) project A is less Risky because the range is lower  
 $\text{Range}_A < \text{Range}_B$

C) Project A. Since it's less Risky

D) No Remains the same.

**PS-7**

$$A) -CVA = \frac{6}{r} = \frac{7\%}{20\%} = 0.35$$

$$-CB = \frac{6}{r} = \frac{9.5\%}{20\%} = 0.475$$

$$-CVC = \frac{6}{r} = \frac{6\%}{19\%} = 0.316$$

$$-CA = \frac{6}{r} = \frac{5.5\%}{16\%} = 0.344$$

B) Alternative C because it has less coefficient of variation.



P8-9

CV below 0.9

$$A) R_{12} = \frac{(21.55 - 14.36) + 0}{14.36} = 50\%$$

$$R_{13} = \frac{(64.78 - 21.55) + 0}{21.55} = 200\%$$

$$R_{14} = \frac{(72.38 - 64.78) + 0}{64.78} = 11.73\%$$

$$R_{15} = \frac{(91.8 - 72.38) + 0}{72.38} = 26.8\%$$

B)

Year	Return	Probability	R * P
2012	50%	0.25	12.5%
2013	200%	0.25	50%
2014	11.73%	0.25	2.93%
2015	26.8%	0.25	6.7%
			$\Sigma = 72.13\% \rightarrow \text{expected Return}$

$$C) \bar{R} = \sqrt{\frac{\sum (X_i - \bar{X})^2 \cdot \text{Prob}}{n-1}}$$

$$\bar{R} = \frac{50\% + 200\% + 11.73\% + 26.8\%}{4} = 72.13\%$$

	$R_i - \bar{R}$	4	$(R_i - \bar{R})^2$
2012	22.06%		0.49
2013	1.289%		1.635
2014	-6%		0.365
2015	-45.3%		0.2

$$\sigma = \sqrt{\frac{6.44 + 1.635 + 2.365 + 0.2}{4-1}} = \sqrt{\frac{2.64}{3}} = 0.95$$

D)  $CV = \frac{\sigma}{R} = \frac{0.95}{0.7213} = 1.3$

E) Coefficient of variation is greater than 0.9  
So it is risky.

P 8-21

A)	Asset	B	(b)	(A)	الحال
			lot. ↑	lot. ↓ →	
	w	0.9	0.04% ↑	-0.09 ↓	
	X	-0.6	-0.06 ↓	0.06 ↑	
	Y	1.8	0.18 ↑	-0.18 ↓	
	Z	2.3	0.23 ↑	-0.23 ↓	

C) I would prefer asset (X) because it is moving opposite the market. so the return will increase.

D) I would prefer asset (Z) because it will be increased the most.

## Chapter 6

## Interest Rates & bond valuation

Debt security  
"obligation"

→ Money market security  
"Short term security"

Debt sec. is 1 year

less  
than  
one  
year

\* Treasury bills "T-bills"

→ Risk ↓

issuer is the government

\* Negotiable Certificate of Deposit

→ Risk ↑

issuer is Deposits and Institutions

\* Commercial paper

issuer: high quality corporations

note: its an unsecured promissory.

→ Capital market securities  
"long term"

\* Bonds

- Treasury bond

issuer: government

- Municipal bond

issuer: local government

- Corporate bond

issuer: corporations



Principal (\$)

Interest (%)

Maturity (n)

- Interest Rate
- Coupon Rate
- Discount Rate
- Yield to maturity

عائد نفی اکتف

$$\Rightarrow \text{Nominal interest Rate} = \text{Real interest Rate} + \text{expected inflation}$$

Example 3

ABC bond

Principal "Face value" = \$1000

Interest = 6%

maturity = 3 years

This is for the ones with Risk Free Treasury bonds & Treasury bills

$$\text{Nominal interest rate} = \text{Real interest Rate} + \text{expected inflation}$$

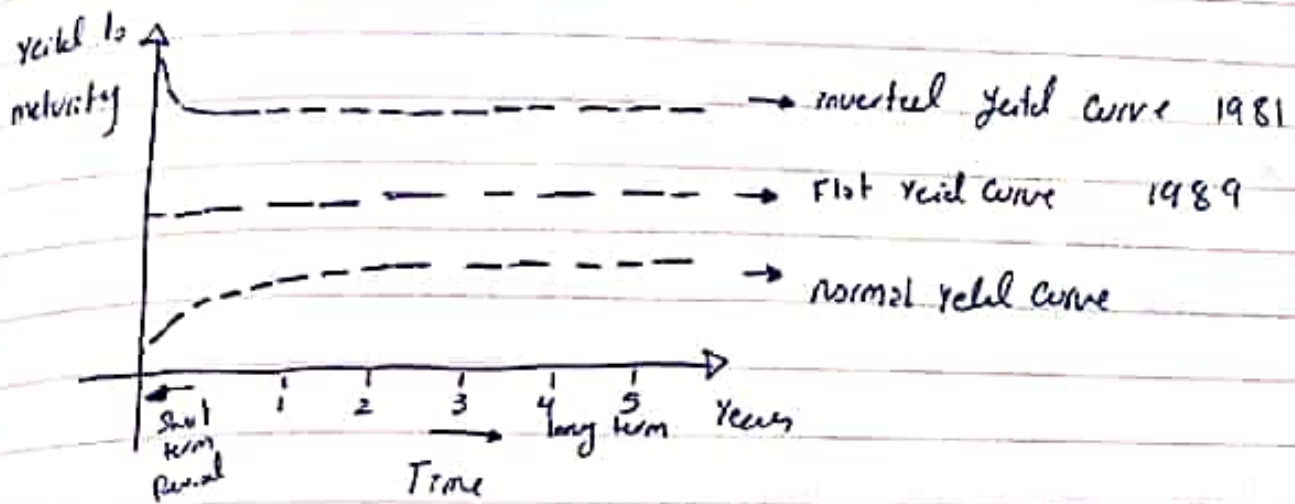
$$4\% = 2\% + 2\%$$

$$\text{Nominal interest rate} = \text{Real interest} + \text{expected inflation} + \text{Risk Premium}$$

$$6\% = 2\% + 2\% + 2\%$$

2

→ Term structure of the interest Rate.



- inverted → yield curve  
interest in short term  $>$  interest in long term / downward

- normal → interest in short term  $<$  interest in long term / upward

- flat → interest in short term = interest in long term

\* why to have normal yield curve

- Expectation Theory.
- Liquidity Preference Theory.
- Market segmentation Theory.

\* Expectation Theory

1 to investor think about Returns

interest Rate in future will increase what do: do now?

1 invest in the short term now until the interest Rate increase

3

2. if i'm an investor :- ~~cost~~ thinks about cost  
i invest in the long term right away

\* liquidity preference theory

گدست بقدر از حمل اصل ال Security واحولها لكاش  
بزيه ال Risk عليه

\* Market Segmentation theory

- insurance  $\rightarrow$  long term  
- Pension

- Banking industry  $\rightarrow$  short term security

في قطاعات استثماريين في long term وفي قطاعات في short term.



\* Default Risk "Credit"

منو احتمالية يكون ال Creditor غير قابل و راجع المال و ال interest  
issuers to gain back the \$ & interest.

\* maturity Risk :

احتمالية التفرغ Risk في فترة الاستحقاق

\* Contractual Provision Risks

بعض شروط ال issuers تجعله اعز في issuers

- Cost of Debt < cost of equity

- Corporate bond

\* Principal "face value"

\* Coupon interest Rate

\* Maturity

- Structured debt provisions

↳ Restrictive covenants

Revenues  
- Cost of goods sold → Common stock holders 13

Gross Profit  
- operating Expenses

EBIT

- Interest Expense → Tax deductible 11  
اول ناس به يقولم هم الالاهول

EBT

- Tax

Earnings after tax

- Preferred Div → Preferred stock holders 12

Earnings available for common stock.

\* Trustee → Bond Holder طرف ثالث بين الشري واد  
بهن حقوق الطرفين

## \* Cost of bond of the issuer

1. Maturity → المدة الزمنية - راجع بعد زعميات التوزيع الشبه على

2. Impact of offering size

حجم المقادير التي تقدم اقترابها "او خضها"

3. Impact of issuer Risk

يعتمد على وضع المقادير الجديد - كل ما كان الوضع احسن  
كل ما يقل Risk

4. Impact of Cost of money

لا Interest Rate - بعضنا يدفعها على القرض

\* خصائص القرض التي يمكن بحملها

### [1.] Conversion feature

→ Stocks → إمكانية تحويل لا Bonds  
Equity → obligation تحويل من  
ownership → Creditors تحويل من  
owners

1. pay Dividends rather than interest ✓

تحويل من Debt → Equity

### [2] Call feature

→ راجع للسند الذي له في السوق

→ حفاظها

#### 1. Call price

→ الكمية التي يدفعها عند راجع ال Bond

2. Call premium → الفرق بين ال Call Price و Par value

→ سعر البيع - سعر الشراء (استرجاع العائد)

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$$\star \text{ Current yield} = \frac{\text{Annual interest payment}}{\text{current price}}$$

$$\text{Yield to maturity} = \text{Cost of Debt "issuer"}$$

- Call yield

\* Example:-

Face value = \$ 1000 } → Annual interest payment

Coupon interest = 8%

Current price = \$ 970

- Current yield

$$\begin{aligned} \text{Current yield} &= \frac{(\text{Face value} \times \text{Coupon interest})}{\text{Current price}} \\ &= \frac{(\$ 1000 \times 0.08)}{\$ 970} = 8.25\% \end{aligned}$$

## \* Types of Bonds :-

- ↳ unsecured bonds
- ↳ Secured bonds

### - unsecured bonds

- Debentures → مدعومة بسمعة الشركة
- Subordinated debentures → ميسند هاء الدين بعدما يندفع للأوائل
- Income bonds → حسب دخل الشركة

بلا ضمان

### - Secured bond

- mortgage bond → مرهونة بأرض أو مبنى
- Collateral trust bond → يتكون مرهونة في السند الثاني
- Equipment trust Certificates → مرهونة في Equipment

- Bonds*
- Zero Coupon bond → خسر فيه Risk
  - junk bond → أعلى Risk عليه
  - Floating Rate bond → حسب سعر الفائدة في السوق

\* High yield bond = junk bond.

\* Foreign bond → يصد في عملتي انا دين ما اروح

\* الأ إذا غلب قوانيني تمنع ذلك

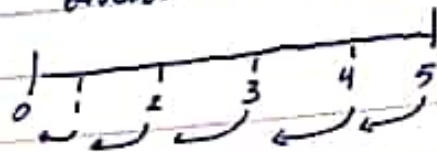
\* Foreign bond → يصد في عملتي الدولة اي انا اراجح عليها



\* Bond valuation &

Discounted  $\rightarrow$  Present value.

Discounted of Future Cash flow



present value annuity  $\rightarrow$

present value single amount  $\rightarrow$  Future is single amount

Bond

\* Principal " Face value \$1000

\* Coupon interest Rate 1.4

\* Maturity 4 years

$$* \text{Bond price} = \text{Bond Value} = \sum_{k=1}^n (PVIFA) + \text{Par value} (PVIF)_{k,n}$$

I  $\rightarrow$  Coupon interest payment = (Coupon interest  $\times$  Face value)  
 (PVIFA)  $\rightarrow$  Present value interest factor of annuity

K  $\rightarrow$  Yield to maturity

n  $\rightarrow$  Period "maturity"

Par value  $\rightarrow$  Face value, principal

(PVIF)  $\rightarrow$  Present value interest factor  $\Rightarrow PV = \frac{FV}{(1+K)^n}$

mixed stream  
 (PVA) =  $\sum_{j=1}^n \frac{FV}{(1+K)^j}$

when we have same payment =  $PMT \left[ \frac{1}{K} - \frac{1}{K(1+K)^n} \right]$



① Example 12:

3 Examples

نائب

122k

نائب

Par Value = \$1000

Coupon interest = 10%

Maturity = 10 years

Yield to maturity = 10%

$$(PVA) = PMT \left[ \frac{1}{k} - \frac{1}{k(1+k)^n} \right]$$

$$= 100 \left[ \frac{1}{10\%} - \frac{1}{10(1+0.10)^{10}} \right] = 614.46$$

$$\text{Par Value} = \frac{FV}{(1+k)^n} = \frac{1000}{(1.1)^{10}} = 385.5$$

$$\begin{aligned} \text{Bond Price} &= 385.5 + 614.46 \\ &= 999.9 \approx \$1000 \end{aligned}$$

② Example 8:

Coupon interest = 10%

Yield of maturity = 12%

$$(PVI\Gamma A) = PMT \left[ \frac{1}{k} - \frac{1}{k(1+k)^n} \right]$$

$$= 100 \left[ \frac{1}{0.12} - \frac{1}{(0.12+1)^{10}} \right] = 565$$

$$\text{Par Value} = \frac{FV}{(1+k)^n} = \frac{1000}{(1.12)^{10}} = 322$$

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$$\text{Bond Price} = 565 + 322 \\ = \$887 \quad \text{Discount}$$

[3] Coupon interest = 10%  
Yield to maturity = 8%

$$PV = PMT \left[ \frac{1}{k} - \frac{1}{k(1+k)^n} \right] \\ = 100 \left[ \frac{1}{0.08} - \frac{1}{0.08(1+0.08)^{10}} \right] = 671$$

$$PVIF = \frac{1000}{(1+0.08)^{10}} = \$463.2$$

$$\text{Bond price} = 671 + 463.2 \\ = 1134.2 \rightarrow \text{Premium}$$

→ Yield to maturity = Coupon interest  
BP "Bond Price" = par value "face value"

→ Yield to maturity > coupon interest  
BP "bond price" = Discount      Bond price < FV

→ Yield to maturity < coupon interest  
BP "bond price" = Premium

Face Value أو قوت

Bond Price > FV

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السعر الحقيقي هو الذي يتغير  
إذا اختلف ما يتغير

File

Problems

P6-3

$$A \frac{100}{25} = 4 \text{ skirts}$$

$$B) PV = \frac{FV}{(1+k)^n} = 100 = \frac{FV}{(1+0.09)^1} = \$109 = FV$$

$$C) PV = \frac{FV}{(1+k)^n} = 25 = \frac{FV}{(1+0.05)^1} = FV = \$26.25$$

D) At the end of the year we have

$$\frac{109}{26.25} = 4.15$$

$$\text{Percentage} = \frac{4.15 - 4}{4} = 0.038$$

3.8% more skirts

E) Real Rate + inflation Rate = Nominal Rate

$$\text{Real} + 5\% = 9\%$$

$$\text{Real} = 4\%$$



D6-8

A) Rate of Return = Real rate + inflation rate  
 $4\% = \text{Real rate} + 2\%$   
 $2\% = \text{Real rate}$

B)	<u>Security</u>	<u>Real Rate</u>	<u>+ inflation Rate</u>	<u>+ Risk Premium</u>	<u>= Nominal</u>
	A	2%	6%	4%	= 12%
	B	2%	5.5%	5%	= 12.5%
	C	2%	5%	2%	= 9%
	D	2%	4.8%	3%	= 9.8%
	E	2%	6%	6%	= 14%

C) Because the mobility security have different maturity.

Chapter 7  
Stock valuation

# Chapter 7

Stock → Equity → Common stock  
"ownership" → Preferred stock

- Differences between Equity & Debt

Equity → "ownership", Return → "Dividends, Appreciation of stock price"  
no maturity, Claim on interest & Asset, Tax treatment

Debt → "obligation", Return → "coupon pmt", maturity, Claim on income & Assets, Tax treatment.

## \* Common Stock & Preferred Stock

- Common Stock

1. Privately owned

↳ owned by private investors. Not publicly traded.

2. Publicly owned (stock)

↳ owned by public investors, Publicly traded.

أب يد يملك مثل ربي الناس ويشتروا stock

3. Closely owned (stock)

↳ individual or small group of investors, Privately owned.

4. Widely owned (stock)

↳ many unrelated individuals or institutional investors.

1

### \* preemptive Rights \*

لا ادعى انزل السهم جديدة الاذلية واي الم حت يتفرون  
م اي حاطب الا مرم الكالية .

### \* Obligation of ownership \*

بزيادة عدد الامم وعدد ساهم فقل لا الساهم و Earnings per share

### \* انواع السهم النرية بتفرم

#### 1. Authorized Shares :- الم طرح به

↳ Shares of common stock that rem allowed to issue.

#### 2. Outstanding Shares :-

↳ issued shares of common stock held by investors.  
it includes both private & public investors.

#### 3. Treasury stock :-

↳ issued shares of common stock held by the firm  
Repurchased shares by the firm.

#### 4. Issued shares:-

↳ Shares of common stock that are put into circulation  
the sum of outstanding shares & Treasury stock.



## \* Preferred Stock

1. No voting Rights

2. Dividends

- % of par value
- Amount \$1 / share.

3. Cumulation

- Cumulative preferred stock.
- Non cumulative preferred stock.

4. other features

- Callable

to Retire shares in a specific period with a specific Price.

- Conversion

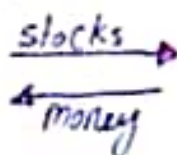
change each share into a stated number of shares of common stock.

- Issuance

- Direct

ABC Company

فردت تصرف الأسهم في الكتاب العام



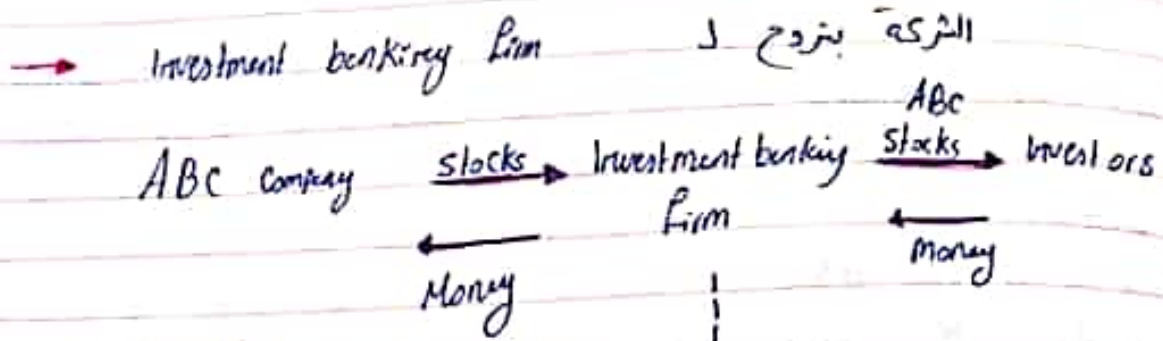
Investors

Could be individuals or institutions.

- Indirect

→ يكون في وسيط باعها ارا الاسم

3



الاتفاقية المسماة  
underwriting agreement.

بناء الشركة في IPO  
↳ Initial public offering

→ Zero growth model

$$P_s = \frac{D_s}{R_s}$$

Example:  $P_s = \frac{\$3}{0.15} = \$20$

$P_s$  → Price of the stock

→ Dividends

→ Required rate of Return.

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# A Constant Growth model

Year	Dividends per share
2019	\$ 1.40
2014	\$ 1.29
2013	\$ 1.20
2012	\$ 1.12
2011	\$ 1.05
2010	\$ 1

$$P_0 = \frac{D_1}{r_s - g}$$

$P_0$  → Price of the stock

$D_1$  → Dividends of the next year

$$D_n = D_0 (1+g)^n$$

$D_0$  → Dividends of the current year

$g$  → Growth of dividends

$r_s$  → Required Rate of Return

$g$  → Growth of dividends.

△ Stock

$$D_{2019} = D_{2010} (1+g)^9$$

$$\frac{\$1.40}{\$1} = \frac{\$1}{\$1} (1+g)^9$$

$$\$1.40 = (1+g)^9$$

$$G = 7\%$$

$$P_0 = \frac{D_1}{r_s - g}$$

$$P_0 = \frac{\$1.40 (1+0.07)}{0.15 - 0.07}$$

$$P_0 = \$18.75 / \text{Shares.}$$

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\* variable growth model.

Rate

<u>t</u>	<u>End of year</u>	<u>Dividend</u>	<u><math>(1+g)^n</math></u>	<u><math>D_t</math></u>
1	2016	\$1.50	$(1+0.10)^1$	= \$1.65
2	2017	\$1.50	$(1+0.10)^2$	= \$1.82
3	2018	\$1.50	$(1+0.10)^3$	= \$2

# step one.

$D_{2016} = \$1.50 / \text{share}$   
 $g_1 = 10\% \text{ (2016, 2017, 2018)}$   
 $\text{End of 2018}$   
 $g_2 = \infty \quad 5\%$   
 $R_s = 15\%$   
 $P_0 = P_{2018} ??$

$$PV = \frac{FV}{(1+R_s)^n}$$

$$= \frac{(1+R_s)^n}{(1+R_s)^n}$$

$$\div (1+0.15)^1 = \$1.150$$

$$\div (1+0.15)^2 = \$1.323$$

$$\div (1+0.15)^3 = \$1.521$$

Discount Dividends

PV Dividends

$$\$1.43$$

$$\$1.57$$

$$\$1.32$$

$$\underline{\underline{\$4.12}}$$

# step 2

$$\begin{aligned}
 R_{2018} &= R_{2018} (1+g)^n \\
 &= \$2 (1+0.05)^1 \\
 &= \$2.10
 \end{aligned}$$

Future  $\rightarrow$  growth rate  
 Discounting process  $\rightarrow$  required rate at future  
 'PV'

$$P_{2018} = \frac{D_{2018}}{R_s - g} = \frac{D_{2018}}{0.15 - 0.05}$$

$$P_{2018} = \frac{\$2.10}{0.10} = \$21$$

$$P_{2018} = \frac{P_{2018}}{(1+0.15)^n} = \frac{\$21}{(1+0.15)^3} = \$13.81 + \$4.12 = \$17.93$$

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→ Free Cash Flow valuation model

Year	FCF <sub>t</sub>	$(1 + 0.09)^t$	PV FCF <sub>t</sub>
2016	\$400,000	$(1 + 0.09)^1$	\$366,972
2017	\$450,000	$(1 + 0.09)^2$	\$378,788
2018	\$520,000	$(1 + 0.09)^3$	\$401,539
2019	\$560,000	$(1 + 0.09)^4$	\$396,718
2020	\$600,000 + 10,300,000	$(1 + 0.09)^5$	\$7,084,252

Step #3

= 10,900,000

VC = \$8,628,232

- $G = 3\%$  Required Rate of Return = 9%
  - Market value of all Debt = 3,100,000
  - Market value of preferred stock = 800,000
  - # of shares GS = 300,000
  - $V_S = VC - V_D - V_P$
- Common stock    Cash flow    Debt    Current profit

معلومات

Step #1

$$FCF_{20-∞} = \frac{FCF_{20}}{0.09 - 0.03} = \frac{600,000 (1 + 0.03)^1}{0.09 - 0.03} = \$10,300,000$$

Vs / share

=  $\frac{\$4,728,232}{300,000}$

= \$15.76

Step #2

$$FCF_{20-∞} = \$600,000 + \$10,300,000 = \$10,900,000$$

Step #4

$V_S = V_C - V_D - V_P$

$V_S = \$8,628,232 - 3,100,000 - 800,000$

$V_S = \$4,728,232$

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$$\begin{aligned} \text{Book Value per share} &= \frac{6,000,000 - 4,500,000}{100,000} \\ &= \$15 \text{ per share} \end{aligned}$$

$$\begin{aligned} \text{Liquidation value per share} &= \frac{\$5,250,000 - \$4,500,000}{100,000} \\ &= \$7.5 \end{aligned}$$

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