Center of Mass The center of mass of a system of particles is the point that moves as though :1-all of the system's mass were concentrated there
2-all experied forces were applied there
Gor a discrete system Diment the location of COM :- Xcom =  $\frac{m_1 X_1 + m_2 X_2}{m_1 + m_2}$ 3 Dime the location of com :- rcom = X i + y i + ZK · for a continuous system (Solid body) uniform objects 3 Dimen -  $\vec{r_{com}} = \frac{\int \vec{r} \, dm}{m_{tot}}$ • A uniform object has a uniform <u>density</u> or <u>mass</u> per unit volume which is: -  $P = M^{-1} man$ T volume PS: the center of Mass closs not necessarily lies within the object : exp: a cloughnuit Orcom · 16 an extremel force acts on a Com Fret = Main acceleration of Com (not the particles) > net force of all external forces that acts on system > introuvel forces are not included Slaa Etaiwi

Sinear Momenten Sof a particle -> · P = my of a parebicle Mass Isvelocity • Fret = dP Venton's 2nd law in terms of momentum enterned dt dt "The time rated of change of the momentum of a porticle is equal to the net fora Pchanges when there acting on the porticle and is in the is a rehelptochal fora direction of that fora " I of a system of particles  $\vec{P} = \vec{P}_1 + \vec{P}_2 \text{ or of particle 2}$  $\vec{P} = \mathcal{M} V_{Com}$ · Fret = JP Collision brief Collision :- in a Small duration  $\vec{P}_i = \vec{P}_f$   $J = \Delta P$ J= AP · in a single Collision :- DP = J n is the number of collisions · in series of Callisions :-Ps: the minus sign indicates that I and sp has oppiste  $J = -n \Delta P$ Favo = n m DV Directions =-AM AV (Am=nm) Alaa Haiwi

Uscanded By Camsoannes

2 impulse A = arear = J Y F(t)  $J = \int_{ci}^{cr} \vec{F}(t) dt \qquad \int_{ci}^{F} (f(t)) dt$ A A A  $\Delta P = J$   $J = Favg \Delta t$ 

Kinetic Energy in cellisions Completely inelastic collision inelastic collision ·K.E Conservered Callisian. · K. F is not Conserved · greatest logs of K.E.  $K.E_i = K.E_{\mathcal{L}}$ 

· the boclies stick together

 $m_{v_{i}} + m_{v_{2}} = (m_{i} + m_{v}) r_{f}$ 

K. E f. # K. Gi

Tos: - Vien is constant before and after a collision because EFFEFERE daa Etaining

. . . . .

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Swe use this

 $(v_{1i} - v_{2i}) = -(v_{1f} - v_{2f})$ 

equation

problems with a projectile and an abject :-• The object (Target) is Stationary :-  $V_{2i} = 0$ • If  $m_1 > m_2 = > m_1$  mores forward • If  $m_1 < m_2 = > m_1$  bounds ( • If  $m_1 < m_2 = > m_1$  bounds ( •  $V_{20}$ stops after collision and body 1 moves with the same relocity as body, 1 • The object (Target) is moviney :- Vzi =0  $(m_1V_1 + m_2V_2)_i = (m_1V_1 + m_2V_2)_f$  $\left(\frac{1}{2}m_{1}V_{1}^{2}+\frac{1}{2}m_{2}V_{2}\right)_{f}$  =  $\left(\frac{1}{2}m_{1}V_{1}^{2}+\frac{1}{2}m_{2}V_{2}^{2}\right)_{f}$ Systems with varying Mass : A Rocket to find a:- RVrel = May => T = Ma Total STRUCTUST positive mass rate = du to find V: - Vp - Vi = Vrel In Mi Alaa Etaiwi

#How to salve Problems Center of Mass Those are The main ideas 1- If the problem is about a system of particles we use Xcom 2 X, m + Xm to finel the position of COM 2-16 the system is a uniform body then it's probably in the center 3- in some question Xcom doesn't change cause there is no horizontal or vertical Force so we put Xcom 20 Dog moves But Frample: PIF Page 231 Xcom 20 4-1f 2 bodies are projected the com will be moving in a projectile motion So we use equation of constant acceleration to find V& for each body and then we can find voom and a com 5 lineau Momentum I- If the problem is about finishing AF Then whind up and 2- in these problems you should Toto pour attention to O's and O'O' Directions, The main trick is in it Maa Etainin

3- in problems with such plats remember that mod Area under (F, F) curve = J= DP 4- in explosions !-AP20  $P_i = P_{g}$ Zm (V) = m,V,+m,V2 -... 5- Sometimes you need to use (R+U)=(K+U). Specaily IP the question is talking about a h or when the question is about releasing a ball in the Or it the question is talking about an spring Them K=U  $\frac{1}{2}my^2 = \frac{1}{2}x^2$ 6- in Rockets problems: you use: Ve-Vii = Vrel In Ui Me or River = Mitor du

Alaa Etaiwi