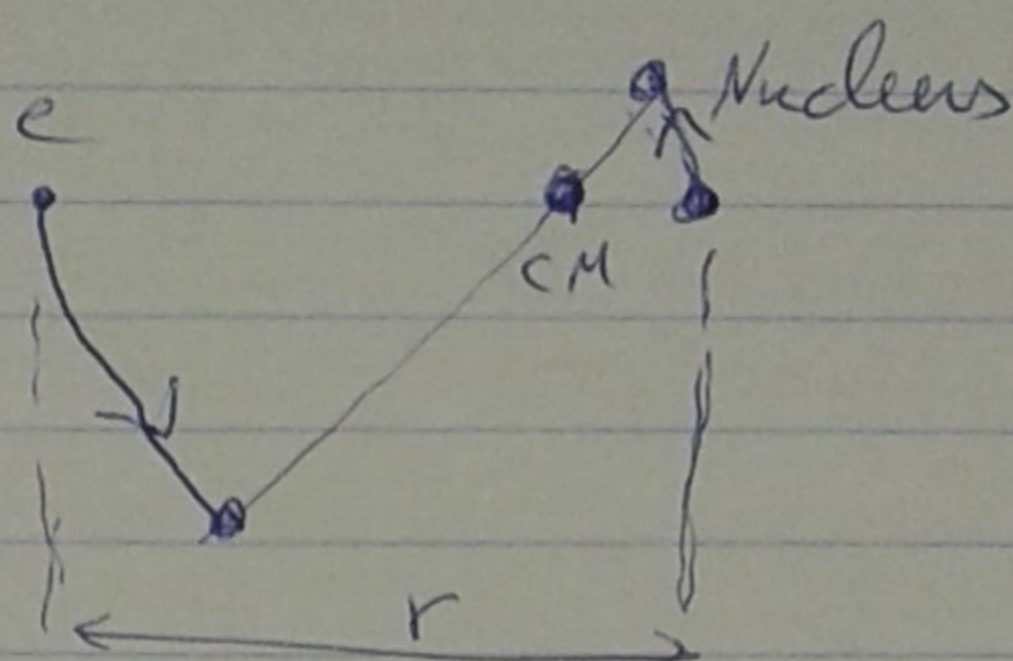


Ch. 4

Problem 32 : The nucleus also moves
The nucleus & electron rotate about CM



replace

$$m_e \text{ by } \mu = \left(\frac{M}{m_e + M} \right) m_e$$

reduced mass

for H atom $E_n \propto m_e$ $E_n = \left(\frac{M}{m_e + M} \right) \frac{-13.6 \text{ eV}}{n^2}$

$E_n \propto \frac{1}{a_0}$ $a_0 \propto \frac{1}{m_e}$

$M = \text{mass of the proton} = 1.007825 \text{ u} = \frac{938.78 \text{ MeV}}{c^2}$

for deuterium : Nucleus = proton + neutron

$M_d = 1876.12 \text{ MeV}/c^2 \leftarrow \text{Masses}$

for Tritium : Nucleus = 1p + 2n $\leftarrow \text{from Appendix B}$

$M_t = 2809.431 \text{ MeV}/c^2$ $\lambda = \left(\frac{m_e + M}{M} \right) \lambda_0$

using m_e $\lambda_0(n=3 \rightarrow n=2) = 656 \text{ nm}$

using μ $\lambda(n=3 \rightarrow n=2) = 656.357 \text{ nm}$ for H

This is how deuterium was discovered (1931) from the shift in λ

$\Delta\lambda = 0.18 \text{ nm} = 1.8 \text{ \AA}$ (can be measured)

$= 656.178 \text{ nm}$ for Deuterium
 $= 656.119 \text{ nm}$ for Tritium