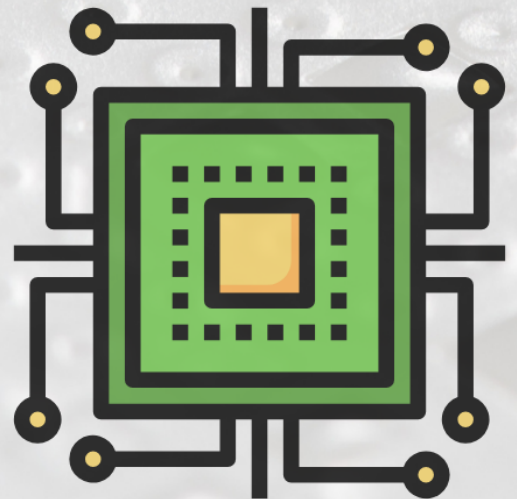
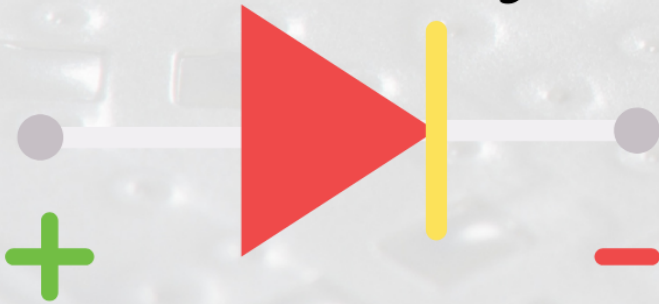


Circuits Analysis

By Rawan Alfares



Introduction

1. **Voltage** : is the energy per unit charge created by the separation, expressed as
 $V = \frac{dw}{dq}$, V is voltage, Volt.
 w is energy, Joule
 q is charge, Coulomb

2. **Electric Current** : is the Rate of charge flow. defined as :-
 $i = \frac{dq}{dt}$, i is current, Ampere.

3. **Power** : is the rate of doing work (energy) per time defined as :
equals the terminal voltage with current
 P : Power (watt).

$$P = I V$$
$$= \frac{dq}{dt} \cdot \frac{dw}{dq} = \frac{dw}{dt}$$

⇒ what's the difference between power and energy :-

Power : is the rate at which energy is used or transferred over time

← معدل استهلاك أو نقل الطاقة خلال فترة زمنية، تبين سرعة استخدام الطاقة أو إنتاجها. (watt)

Energy : is the Capacity to do work or produce heat.

← القدرة على إنجاز عمل أو إنتاج حرارة ونقل كمية العمل الذي يتم تنفيذها خلال فترة زمنية (Joule)

⇒ what's the difference between network and circuits :-

Network : the inter Connection of two or more Simple Circuits element is called electrical network.

Circuit : if the network Contains at least one closed path, it is called electrical Circuits

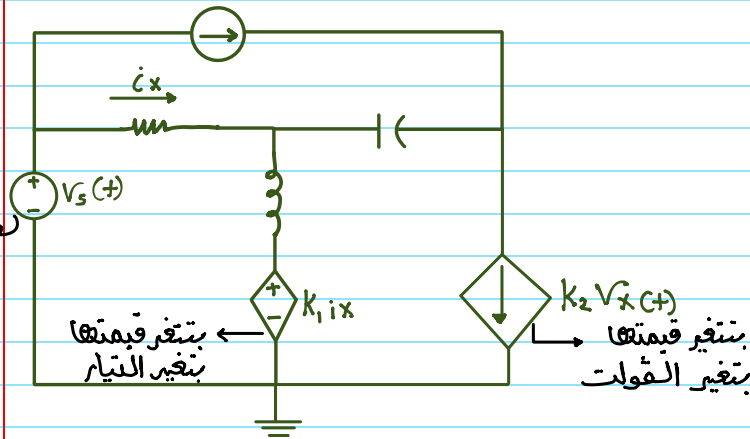
⇒ **Circuit analysis** : given a circuit in which all the components are specified, analysis involves finding such things as the voltage across some elements or the current through another.

* the solution is unique.

⇒ **Circuit design** involves determining the circuit configuration that will meet certain specifications.

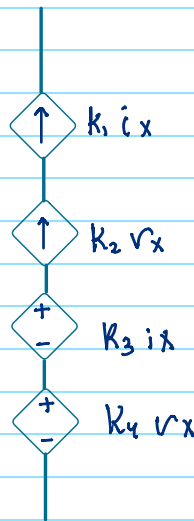
* the solution is not unique.

Ch.2: Circuit Elements



⇒ dependent Source :-

* يعتمد على element في الدارة
* أي تغير في قيمة أحد قيم element
تغير على قيمته.



⇒ Independent Sources :-

like current , voltage.

قيمته ثابتة حتى في حال
تغير قيمة أحد قيم element
في الدارة.

Circuit element :-

1) Active element: Capable of delivering power to some external elements (Sources), ex. voltage source, current source.

2) Passive elements :- Capable only of receiving power.
(R, L, C).

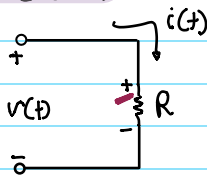
Storage element of current
magnetic field.

Storage element of voltage
(electric field).

Circuit elements can be classified according to the relationship of the current through the element to the voltage across the element.

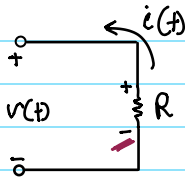
Circuit elements:

1. Resistors:



$$* v(t) = i(t) R$$

$$* i(t) = \frac{1}{R} v(t) = G v(t)$$

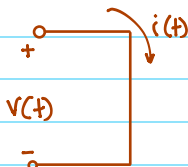


$$* v(t) = -R i(t)$$

* R is called the resistance of the component and is measured in units of Ohm (Ω)

* G is called Conductance of the component and is measured in units of Siemens $S = \Omega^{-1} = V^{-1}$

Two special resistor value :-



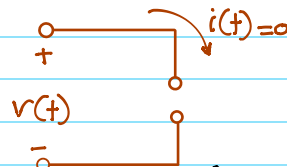
short circuit

$$* v(t) = 0$$

$$* i(t) \rightarrow \text{depend on circuit}$$

$$* R = 0 \Omega$$

$$* G = \infty S$$



open circuit

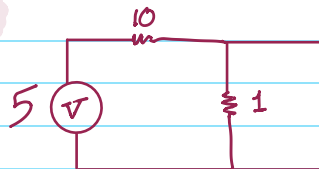
$$* i(t) = 0$$

$$* v(t) = \text{depend on circuit}$$

$$* R = \infty \Omega$$

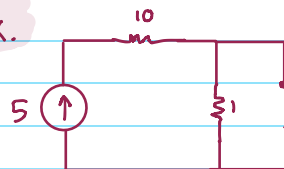
$$* G = 0 S$$

ex.



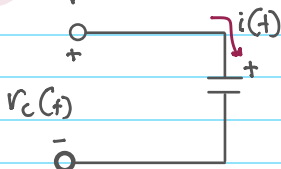
$$I = \frac{5}{10} = 0.5 A$$

ex.

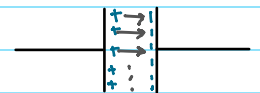


2. Capacitors :

سعة



$$v_C(t) = \frac{1}{C} \int_{-\infty}^t i_C(t) dt$$



electric field.

$$* v_C(t) = v_C(t_0) + \frac{1}{C} \int_{t_0}^t i_C(t) dt, t \geq t_0.$$

the value for the initial value.

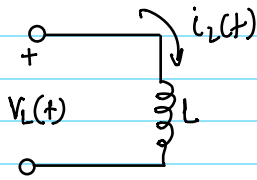
* measured by Farad (F)

$$v_C(t_0) = v_C(t) + \frac{1}{C} \int_t^{t_0} i_C(t) dt$$

$$v_C(0^-) = v_C(0^+)$$

* means that the initial value will be the same magnitude after very tiny time.

3. Inductors :



$$v_L(t) = L \frac{di_L(t)}{dt}$$

$$* i_L(t) = i_L(0^-) + \frac{1}{L} \int_0^t v_L(t) dt$$

$$* i_L(0^-) = i_L(0^+)$$

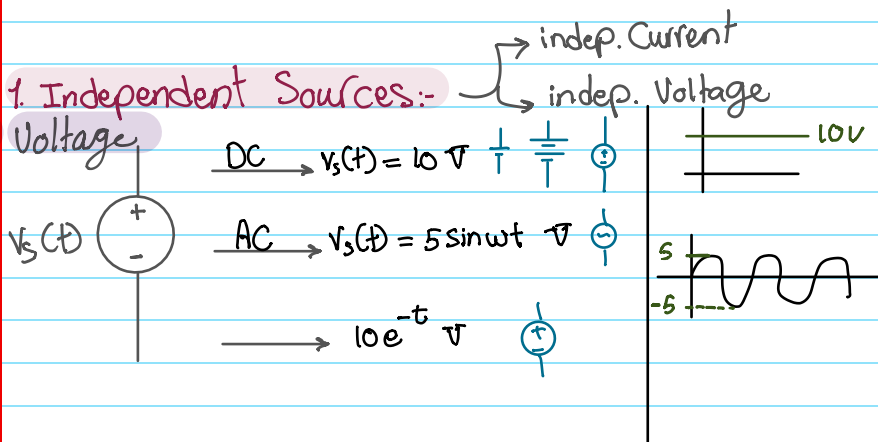
* measured by Henry (H)

Active elements :

- Independent Sources
- Dependent Sources

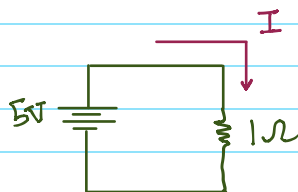
1. Independent Sources:-

1. Voltage

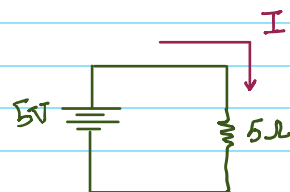


* قيمة ثابتة يعني
النظر عن تغير قيم
المكونات الأخرى في
الدائرة مثل البطارية

example:

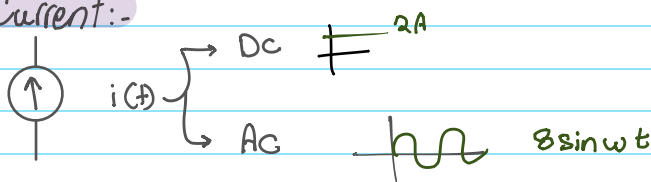


$$I = \frac{5}{1} = 5A$$

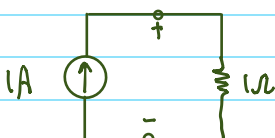


$$I = \frac{5}{5} = 1A$$

2. Current:-



قيمة ثابتة يعني انظر
عن تغير قيمة الفولت

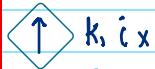


$$V = IR = 1 \times 1 = 1V$$



$$V = IR = 1 \times 5 = 5V$$

2. dependent Sources: are Sources in which the Source Voltage or Current depend on upon a Current or Voltage else where in the Circuit.



$k_1 i_x$

dep. Current Source

Control parameter is Current



$k_3 i_x$

dep. Voltage Source

Control parameter is Current



$k_2 v_x$

dep. Current Source

Control parameter is Voltage



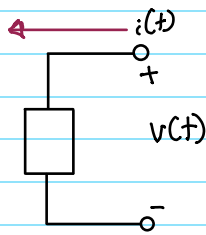
$k_4 v_x$

dep. Voltage Source

Control parameter is Voltage

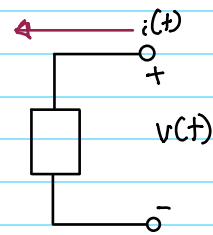
Power and Energy

$$* P(t) = \frac{dw(t)}{dt} \quad \rightarrow \quad p(t) = i(t) v(t)$$



$$p(t) = + v(t) i(t)$$

absorbing



$$p(t) = - v(t) i(t)$$

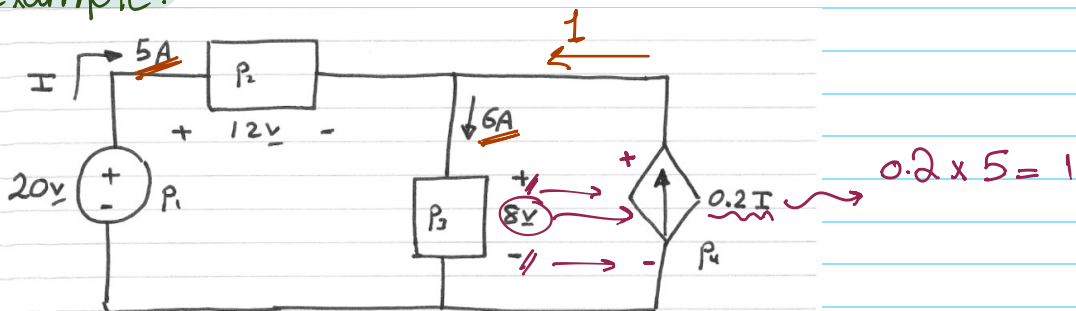
Supplying

$$* \sum P = 0$$

$$\sum P_{\text{supplying}} = \sum P_{\text{absorbing}}$$

the law of Conservation of energy must be obeyed in any electric circuit.

example:



1. $P_1 = -IV = (-20)(5) = -100 \text{ watt}$ Supplied power
2. $P_2 = IV = (5)(12) = 60 \text{ watt}$ absorbing power
3. $P_3 = (8)(6) = 48 \text{ watt}$ absorbing power
4. $P_4 = (-1)(8) = -8 \text{ watt}$ Supplied power

$$\sum P = 0$$

$$= -8 + 48 - 100 + 60 = 0$$

ربنا تقبل منا إِنَّكَ أَنْتَ السَّمِيعُ الْعَلِيمُ