

# Machine Design 2 ENME 436

**Department of Mechanical and Mechatronics Engineering** 

Dr. Rashad Mustafa





**Fatigue strength** means the property of a design or component, the casual occurrences during the operation elasto-plastic cyclic, quasi-static and sudden loads taking into account the environmental conditions, such as corrosion, and to maintain a high temperature and safe operation for the intended period of use.

#### Requirements for the fatigue strength of components and systems

- Designed for customer-specific operating and operating conditions
- Ensuring the required service life
- Ensuring the lowest possible probability of failure
- Consideration of special events and misuse





Faculty of Engineering and Technology Department of Mechanical and Mechatronics Engineering Machine Design 2 – ENME436

#### **Text Book:**

Mechanical Engineering Design, 10<sup>th</sup> Edition, Joseph E. Shigley & Charles R. Mischke

#### **Course Content:**

- 1. Friction, wear and lubrication; systems of lubrication.
- 2. Design of sliding bearings; journal and thrust bearings.
- 3. Antifriction bearings; types, selection criteria and calculation procedure.
- 4. Power transmission; Prime mover characteristics and types.
- 5. Design of gear drives; Spur gears, helical gears, bevel gears, worm gears.
- 6. Design of belt drives; Flat belts, V-belts.
- 7. Design of chain drives and rope drives.



# Introduction











STUDENTS-HUB.com

Uploaded By: anonymous 5







Introduction

History







Uploaded By: anonymous 7

# Chapter 11: Rolling Contact Bearing Introduction





Ancient Egyptians used timbers for transportation of stones for pyramid building. This was roller bearings start.



STUDENTS-HUB.com

Uploaded By: anonymous 8







Uploaded By: anonymous <sub>9</sub>



The terms "*rolling-contact bearing*", "*antifriction bearing*", and "*rolling bearing*" are all used to describe that class of bearing in which the main load is transferred through elements in rolling contact rather than in sliding contact.

# Types of rolling contact bearing:

Ball bearing













Uploaded By: anonymous<sub>11</sub>

# **Main Components**





# **11.1 Bearing Types**





# **11.1 Classification of Bearing Loads**

- Radial (Carry radial load)
- Thrust, axial contact (carry axial loads)
- Angular-contact (curry axial and radial loads)

Radial load











# **11.1 Ball Bearing Types**





# **11.1 Ball Bearing Types**



# Sealed Bearing





Uploaded By: anonymous  $_{16}$ 

# Shield Bearing





STUDENTS-HUB.com

# **11.1 Ball Bearing Types**



# **External Self-Aligning**

# **Internal Self-Aligning**







# **11.1 Ball Bearing Types**



#### Figure 11-3

Types of roller bearings: (*a*) straight roller; (*b*) spherical roller, thrust; (*c*) tapered roller, thrust; (*d*) needle; (*e*) tapered roller; (*f*) steep-angle tapered roller. (*Courtesy of The Timken Company.*)







Uploaded By: anonymous<sub>18</sub>



# **Bearing system life**



$$C_{10} = F_R = F_D \left(\frac{L_D}{L_R}\right)^{1/a} = F_D \left(\frac{\mathscr{L}_D n_D 60}{\mathscr{L}_R n_R 60}\right)^{1/a}$$



Uploaded By: anonymous<sub>19</sub>



# **Bearing system life: Example:**

Roller bearing is to withstand radial load  $F_r = 4 \text{ kN}$  and have a life  $L_D = 1200 \text{ hr}$  at  $n_D = 600 \text{ rpm}$ . What value of load rating you will select from TimKen Engineering Company catalog



# **11.5 Relating Load, Life, and Reliability**



#### Figure 11-5

Constant reliability contours. Point A represents the catalog rating  $C_{10}$  at  $x = L/L_{10} = 1$ . Point *B* is on the target reliability design line  $R_D$ , with a load of  $C_{10}$ . Point D is a point on the desired reliability contour exhibiting the design life  $x_D = L_D/L_{10}$ at the design load  $F_D$ .





$$C_{10} \approx a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(1 - R_D)^{1/b}} \right]^{1/a} \qquad R \ge 0.90 \qquad (11-10)$$

# 11.5 Relating Load, Life, and Reliability



$$C_{10} \approx a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(1 - R_D)^{1/b}} \right]^{1/a} \qquad R \ge 0.90 \qquad (11-10)$$

| Table 11-6<br>Typical Weibull |              | Ratina Life,                                | Weibull Parameters<br>Rating Lives |               |              |  |
|-------------------------------|--------------|---------------------------------------------|------------------------------------|---------------|--------------|--|
| Parameters for Two            | Manufacturer | Revolutions                                 | <b>X</b> 0                         | θ             | Ь            |  |
| Manufacturers                 | 1<br>2       | 90(10 <sup>6</sup> )<br>1(10 <sup>6</sup> ) | 0<br>0.02                          | 4.48<br>4.459 | 1.5<br>1.483 |  |



Uploaded By: anonymous<sub>22</sub>



#### Application factor and Life should be taken into account in the Bearing application

| Table 11–4                      | Type of Application                                                               |                                                                                                | Life, kh                  |  |  |  |
|---------------------------------|-----------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------|---------------------------|--|--|--|
| Bearing-Life                    | Instruments and apparatus for infrequent use                                      |                                                                                                | Up to 0.5                 |  |  |  |
| Recommendations for             | Aircraft engines                                                                  |                                                                                                | 0.5-2                     |  |  |  |
| Various Classes of<br>Machinery | Machines for short or intermittent operation winterruption is of minor importance | Machines for short or intermittent operation where service interruption is of minor importance |                           |  |  |  |
| 1- Life                         | Machines for intermittent service where reliabl<br>is of great importance         | 8-14                                                                                           |                           |  |  |  |
|                                 | Machines for 8-h service that are not always for                                  | ully utilized                                                                                  | 14–20                     |  |  |  |
|                                 |                                                                                   | 20-30                                                                                          |                           |  |  |  |
|                                 | Machines for continuous 24-h service                                              |                                                                                                | 50-60                     |  |  |  |
|                                 | Machines for continuous 24-h service where re<br>of extreme importance            | eliability is                                                                                  | 100-200                   |  |  |  |
| Table 11–5                      | Type of Application                                                               | Load Factor                                                                                    |                           |  |  |  |
| Load-Application Factors        | Precision gearing                                                                 | 1.0-1.1                                                                                        |                           |  |  |  |
|                                 | Commercial gearing                                                                | 1.1–1.3                                                                                        |                           |  |  |  |
|                                 | Applications with poor bearing seals                                              | 1.2                                                                                            |                           |  |  |  |
| 2 – Application                 | <b>2 – Application</b> Machinery with no impact 1.0–1.2                           |                                                                                                |                           |  |  |  |
| factor                          | Machinery with light impact                                                       |                                                                                                |                           |  |  |  |
| STUDENTS-HUB.com                | Machinery with moderate impact                                                    | 1.5⊎pխaded By                                                                                  | : anonymous <sub>23</sub> |  |  |  |



#### Figure 11-6

The relationship of dimensionless group  $F_e/(VF_r)$  and  $F_a/(VF_r)$  and the straight-line segments representing the data.

$$\frac{F_e}{VF_r} = 1 \qquad \text{when } \frac{F_a}{VF_r} \le e$$
$$\frac{F_e}{VF_r} = X + Y \frac{F_a}{VF_r} \qquad \text{when } \frac{F_a}{VF_r} > e$$

A rotation factor V is defined such that V = 1when the inner ring rotates and V = 1.2 when the outer ring rotates

STUDENTS-HUB.com

 $\frac{F_e}{VF_r}$ 20000000 Slope YX  $\frac{F_a}{VF_r}$ e 0

Uploaded By: anonymous<sub>24</sub>



(11 - 12)

# $F_e = X_i V F_r + Y_i F_a$

#### Table 11-1

Equivalent Radial Load Factors for Ball Bearings

|           |      | $F_a/(VF_r) \leq e$ |                | $F_a/(VF_r) > e$ |                |  |
|-----------|------|---------------------|----------------|------------------|----------------|--|
| $F_a/C_0$ | е    | <b>X</b> 1          | Y <sub>1</sub> | <b>X</b> 2       | Y <sub>2</sub> |  |
| 0.014*    | 0.19 | 1.00                | 0              | 0.56             | 2.30           |  |
| 0.021     | 0.21 | 1.00                | 0              | 0.56             | 2.15           |  |
| 0.028     | 0.22 | 1.00                | 0              | 0.56             | 1.99           |  |
| 0.042     | 0.24 | 1.00                | 0              | 0.56             | 1.85           |  |
| 0.056     | 0.26 | 1.00                | 0              | 0.56             | 1.71           |  |
| 0.070     | 0.27 | 1.00                | 0              | 0.56             | 1.63           |  |
| 0.084     | 0.28 | 1.00                | 0              | 0.56             | 1.55           |  |
| 0.110     | 0.30 | 1.00                | 0              | 0.56             | 1.45           |  |
| 0.17      | 0.34 | 1.00                | 0              | 0.56             | 1.31           |  |
| 0.28      | 0.38 | 1.00                | 0              | 0.56             | 1.15           |  |
| 0.42      | 0.42 | 1.00                | 0              | 0.56             | 1.04           |  |
| 0.56      | 0.44 | 1.00                | 0              | 0.56             | 1.00           |  |

\*Use 0.014 if  $F_a/C_0 < 0.014$ .





#### Table 11-2

Dimensions and Load Ratings for Single-Row 02-Series Deep-Groove and Angular-Contact Ball Bearings

|       |     |        | Fillet  | Shou   | lder           |             | Load Ra        | tings, kN   |         |
|-------|-----|--------|---------|--------|----------------|-------------|----------------|-------------|---------|
| Bore, | OD, | Width, | Radius, | Diamet | er, mm         | Deep 0      | Groove         | Angular     | Contact |
| mm    | mm  | mm     | mm      | ds     | d <sub>H</sub> | <b>C</b> 10 | C <sub>0</sub> | <b>C</b> 10 | Co      |
| 10    | 30  | 9      | 0.6     | 12.5   | 27             | 5.07        | 2.24           | 4.94        | 2.12    |
| 12    | 32  | 10     | 0.6     | 14.5   | 28             | 6.89        | 3.10           | 7.02        | 3.05    |
| 15    | 35  | 11     | 0.6     | 17.5   | 31             | 7.80        | 3.55           | 8.06        | 3.65    |
| 17    | 40  | 12     | 0.6     | 19.5   | 34             | 9.56        | 4.50           | 9.95        | 4.75    |
| 20    | 47  | 14     | 1.0     | 25     | 41             | 12.7        | 6.20           | 13.3        | 6.55    |
| 25    | 52  | 15     | 1.0     | 30     | 47             | 14.0        | 6.95           | 14.8        | 7.65    |
| 30    | 62  | 16     | 1.0     | 35     | 55             | 19.5        | 10.0           | 20.3        | 11.0    |
| 35    | 72  | 17     | 1.0     | 41     | 65             | 25.5        | 13.7           | 27.0        | 15.0    |
| 40    | 80  | 18     | 1.0     | 46     | 72             | 30.7        | 16.6           | 31.9        | 18.6    |
| 45    | 85  | 19     | 1.0     | 52     | 77             | 33.2        | 18.6           | 35.8        | 21.2    |
| 50    | 90  | 20     | 1.0     | 56     | 82             | 35.1        | 19.6           | 37.7        | 22.8    |
| 55    | 100 | 21     | 1.5     | 63     | 90             | 43.6        | 25.0           | 46.2        | 28.5    |
| 60    | 110 | 22     | 1.5     | 70     | 99             | 47.5        | 28.0           | 55.9        | 35.5    |
| 65    | 120 | 23     | 1.5     | 74     | 109            | 55.9        | 34.0           | 63.7        | 41.5    |
| 70    | 125 | 24     | 1.5     | 79     | 114            | 61.8        | 37.5           | 68.9        | 45.5    |



#### Table 11-3

Dimensions and Basic Load Ratings for Cylindrical Roller Bearings

|         |            | 02-Se  | eries       |          | 03-Series |         |                           |                       |  |
|---------|------------|--------|-------------|----------|-----------|---------|---------------------------|-----------------------|--|
| Bore,   | OD,        | Width, | Load Ra     | ting, kN | OD,       | Width,  | Load Ra                   | ting, kN              |  |
| mm      | mm         | mm     | <b>C</b> 10 | Co       | mm        | mm      | <b>C</b> 10               | Co                    |  |
| 25      | 52         | 15     | 16.8        | 8.8      | 62        | 17      | 28.6                      | 15.0                  |  |
| 30      | 62         | 16     | 22.4        | 12.0     | 72        | 19      | 36.9                      | 20.0                  |  |
| 35      | 72         | 17     | 31.9        | 17.6     | 80        | 21      | 44.6                      | 27.1                  |  |
| 40      | 80         | 18     | 41.8        | 24.0     | 90        | 23      | 56.1                      | 32.5                  |  |
| 45      | 85         | 19     | 44.0        | 25.5     | 100       | 25      | 72.1                      | 45.4                  |  |
| 50      | 90         | 20     | 45.7        | 27.5     | 110       | 27      | 88.0                      | 52.0                  |  |
| 55      | 100        | 21     | 56.1        | 34.0     | 120       | 29      | 102                       | 67.2                  |  |
| 60      | 110        | 22     | 64.4        | 43.1     | 130       | 31      | 123                       | 76.5                  |  |
| 65      | 120        | 23     | 76.5        | 51.2     | 140       | 33      | 138                       | 85.0                  |  |
| 70      | 125        | 24     | 79.2        | 51.2     | 150       | 35      | 151                       | 102                   |  |
| 75      | 130        | 25     | 93.1        | 63.2     | 160       | 37      | 183                       | 125                   |  |
| 80      | 140        | 26     | 106         | 69.4     | 170       | 39      | 190                       | 125                   |  |
| 85      | 150        | 28     | 119         | 78.3     | 180       | 41      | 212                       | 149                   |  |
| 90      | 160        | 30     | 142         | 100      | 190       | 43      | 242                       | 160                   |  |
| 95      | 170        | 32     | 165         | 112      | 200       | 45      | 264                       | 189                   |  |
| STODEN- | TS-HUB.com | 34     | 183         | 125      | 215       | 47 Uplo | baded <sup>0</sup> By: an | onymous <sub>27</sub> |  |







#### Figure 11-7: The basic ABMA plan for boundary dimensions.

It shows the variety of bearings that may be obtained with a particular bore



The bearings are identified by a two-digit number called the *dimension-series code*.

- The first number in the code is from the *width series*.
- The second number is from the *diameter series* (outside).

Since the dimension series code does not reveal the dimensions directly, it is necessary to resort to tabulations. Uploaded By: anonymous<sub>29</sub>

### Problem 11-35



The worm shaft shown in part a of the figure transmits 1.2 hp at 500 rev/min. A static force analysis gave the results shown in part b of the figure. Bearing A is to be an angular-contact ball bearing selected from Table 11–2, mounted to take the 555-lbf thrust load. The bearing at B is to take only the radial load, so an 02-series cylindrical roller bearing from Table 11–3 will be employed. Use an application factor of 1.2, a desired life of 30 kh, and a combined reliability goal of 0.99, assuming distribution data from manufacturer 2 in Table 11–6. Specify each bearing.





#### Problem 11-35







Uploaded By: anonymous<sub>31</sub>

# 11.5 Relating Load, Life, and Reliability



$$C_{10} \approx a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(1 - R_D)^{1/b}} \right]^{1/a} \qquad R \ge 0.90 \qquad (11-10)$$

| Table 11–6<br>Typical Weibull |              | Ratina Life,                                | Weibull Parameters<br>Rating Lives |               |              |  |
|-------------------------------|--------------|---------------------------------------------|------------------------------------|---------------|--------------|--|
| Parameters for Two            | Manufacturer | Revolutions                                 | <b>X</b> 0                         | θ             | Ь            |  |
| Manufacturers                 | 1<br>2       | 90(10 <sup>6</sup> )<br>1(10 <sup>6</sup> ) | 0<br>0.02                          | 4.48<br>4.459 | 1.5<br>1.483 |  |



Uploaded By: anonymous<sub>32</sub>



#### Table 11-3

Dimensions and Basic Load Ratings for Cylindrical Roller Bearings

|       |            | 02-Se  | eries       |          | 03-Series |         |                           |                       |  |
|-------|------------|--------|-------------|----------|-----------|---------|---------------------------|-----------------------|--|
| Bore, | OD,        | Width, | Load Ra     | ting, kN | OD,       | Width,  | Load Ra                   | ting, kN              |  |
| mm    | mm         | mm     | <b>C</b> 10 | Co       | mm        | mm      | <b>C</b> 10               | Co                    |  |
| 25    | 52         | 15     | 16.8        | 8.8      | 62        | 17      | 28.6                      | 15.0                  |  |
| 30    | 62         | 16     | 22.4        | 12.0     | 72        | 19      | 36.9                      | 20.0                  |  |
| 35    | 72         | 17     | 31.9        | 17.6     | 80        | 21      | 44.6                      | 27.1                  |  |
| 40    | 80         | 18     | 41.8        | 24.0     | 90        | 23      | 56.1                      | 32.5                  |  |
| 45    | 85         | 19     | 44.0        | 25.5     | 100       | 25      | 72.1                      | 45.4                  |  |
| 50    | 90         | 20     | 45.7        | 27.5     | 110       | 27      | 88.0                      | 52.0                  |  |
| 55    | 100        | 21     | 56.1        | 34.0     | 120       | 29      | 102                       | 67.2                  |  |
| 60    | 110        | 22     | 64.4        | 43.1     | 130       | 31      | 123                       | 76.5                  |  |
| 65    | 120        | 23     | 76.5        | 51.2     | 140       | 33      | 138                       | 85.0                  |  |
| 70    | 125        | 24     | 79.2        | 51.2     | 150       | 35      | 151                       | 102                   |  |
| 75    | 130        | 25     | 93.1        | 63.2     | 160       | 37      | 183                       | 125                   |  |
| 80    | 140        | 26     | 106         | 69.4     | 170       | 39      | 190                       | 125                   |  |
| 85    | 150        | 28     | 119         | 78.3     | 180       | 41      | 212                       | 149                   |  |
| 90    | 160        | 30     | 142         | 100      | 190       | 43      | 242                       | 160                   |  |
| 95    | 170        | 32     | 165         | 112      | 200       | 45      | 264                       | 189                   |  |
|       | rs-HUB.com | 34     | 183         | 125      | 215       | 47 Uplo | baded <sup>0</sup> By: an | onymous <sub>33</sub> |  |



#### Table 11-2

Dimensions and Load Ratings for Single-Row 02-Series Deep-Groove and Angular-Contact Ball Bearings

|       |     |        | Fillet  | Shoulder |                | Load Ratings, kN |        |             |                |
|-------|-----|--------|---------|----------|----------------|------------------|--------|-------------|----------------|
| Bore, | OD, | Width, | Radius, | Diame    | ter, mm        | Deep             | Groove | Angular     | Contact        |
| mm    | mm  | mm     | mm      | ds       | d <sub>H</sub> | <b>C</b> 10      | Co     | <b>C</b> 10 | C <sub>o</sub> |
| 25    | 52  | 15     | 1.0     | 30       | 47             | 14.0             | 6.95   | 14.8        | 7.65           |
| 30    | 62  | 16     | 1.0     | 35       | 55             | 19.5             | 10.0   | 20.3        | 11.0           |
| 35    | 72  | 17     | 1.0     | 41       | 65             | 25.5             | 13.7   | 27.0        | 15.0           |
| 40    | 80  | 18     | 1.0     | 46       | 72             | 30.7             | 16.6   | 31.9        | 18.6           |
| 45    | 85  | 19     | 1.0     | 52       | 77             | 33.2             | 18.6   | 35.8        | 21.2           |
| 50    | 90  | 20     | 1.0     | 56       | 82             | 35.1             | 19.6   | 37.7        | 22.8           |
| 55    | 100 | 21     | 1.5     | 63       | 90             | 43.6             | 25.0   | 46.2        | 28.5           |
| 60    | 110 | 22     | 1.5     | 70       | 99             | 47.5             | 28.0   | 55.9        | 35.5           |
| 65    | 120 | 23     | 1.5     | 74       | 109            | 55.9             | 34.0   | 63.7        | 41.5           |
| 70    | 125 | 24     | 1.5     | 79       | 114            | 61.8             | 37.5   | 68.9        | 45.5           |
| 75    | 130 | 25     | 1.5     | 86       | 119            | 66.3             | 40.5   | 71.5        | 49.0           |
| 80    | 140 | 26     | 2.0     | 93       | 127            | 70.2             | 45.0   | 80.6        | 55.0           |
| 85    | 150 | 28     | 2.0     | 99       | 136            | 83.2             | 53.0   | 90.4        | 63.0           |
| 90    | 160 | 30     | 2.0     | 104      | 146            | 95.6             | 62.0   | 106         | 73.5           |
| 95    | 170 | 32     | 2.0     | 110      | 156            | 108              | 69.5   | 121         | 85.0           |



 $F_e = X_i V F_r + Y_i F_a$ 

| 11 | 1 1 | 1 1 | 2 |
|----|-----|-----|---|
|    |     | _   |   |
| •  |     |     | _ |

| Table 11-1                |           |               | F <sub>a</sub> /(VF, | ) ≤ e          | $F_a/(VF_r) > e$ |                |  |
|---------------------------|-----------|---------------|----------------------|----------------|------------------|----------------|--|
| Equivalent Radial Load    | $F_a/C_0$ | е             | <b>X</b> 1           | Y <sub>1</sub> | <b>X</b> 2       | Y <sub>2</sub> |  |
| Factors for Ball Bearings | 0.014*    | 0.19          | 1.00                 | 0              | 0.56             | 2.30           |  |
|                           | 0.021     | 0.21          | 1.00                 | 0              | 0.56             | 2.15           |  |
| 0.0392                    | 0.028     | <b>2</b> 0.22 | 1.00                 | 0              | 0.56             | 1.99           |  |
|                           | 0.042     | 0.24          | 1.00                 | 0              | 0.56             | 1.85           |  |
|                           | 0.056     | 0.26          | 1.00                 | 0              | 0.56             | 1.71           |  |
|                           | 0.070     | 0.27          | 1.00                 | 0              | 0.56             | 1.63           |  |
|                           | 0.084     | 0.28          | 1.00                 | 0              | 0.56             | 1.55           |  |
|                           | 0.110     | 0.30          | 1.00                 | 0              | 0.56             | 1.45           |  |
|                           | 0.17      | 0.34          | 1.00                 | 0              | 0.56             | 1.31           |  |
|                           | 0.28      | 0.38          | 1.00                 | 0              | 0.56             | 1.15           |  |
|                           | 0.42      | 0.42          | 1.00                 | 0              | 0.56             | 1.04           |  |
|                           | 0.56      | 0.44          | 1.00                 | 0              | 0.56             | 1.00           |  |

\*Use 0.014 if  $F_a/C_0 < 0.014$ .





# Figure 11-9

Plot of  $F^a$  as ordinate and L as abscissa for  $F^aL$  = constant. The linear damage hypothesis says that in the case of load  $F_1$ , the area under the curve from L = 0 to  $L = L_A$  is a measure of the damage  $D = F_1^a L_A$ . The complete damage to failure is measured by  $C_{10}^a L_B$ .



$$F^{a}L = \text{constant} = K$$

(a)



# **11.7 Variable Loading**



# Figure 11-10 $F^a$ A three-part piecewise-<br/>continuous periodic loading<br/>cycle involving loads $F_{e1}$ , $F_{e2}$ ,<br/>and $F_{e3}$ . $F_{eq}$ is the equivalent<br/>steady load inflicting the<br/>same damage when run for<br/> $l_1 + l_2 + l_3$ revolutions, doing<br/>the same damage D per period.

$$D = F_{e_1}^a l_1 + F_{e_2}^a l_2 + F_{e_3}^a l_3$$

$$F_{e1}^{a}$$

$$F_{e3}^{a}$$

$$I_{1}$$

$$I_{2}$$

$$I_{3}$$

$$F_{e3}^{a}$$

$$I_{1}$$

$$I_{2}$$

$$I_{3}$$

$$I_{1}$$

$$I_{2}$$

$$I_{1}$$

$$I_{2}$$

$$D = F_{\rm eq}^a (l_1 + l_2 + l_3)$$



# **11.7 Variable Loading**



Equation 1:

$$D = F_{e_1}^a l_1 + F_{e_2}^a l_2 + F_{e_3}^a l_3$$

Equation 2:

$$D = F_{\rm eq}^a (l_1 + l_2 + l_3)$$

Equating Equation 1 and 2, we get the  $oldsymbol{F_{eq}}$ 

$$F_{\rm eq} = \left[\frac{F_{e1}^a l_1 + F_{e2}^a l_2 + F_{e3}^a l_3}{l_1 + l_2 + l_3}\right]^{1/a} = \left[\sum f_i F_{ei}^a\right]^{1/a}$$



Uploaded By: anonymous<sub>38</sub>

# **11.7 Variable Loading**



$$F_{\rm eq}^{a}L_{\rm eq} = F_{e1}^{a}l_{1} + F_{e2}^{a}l_{2} + F_{e3}^{a}l_{3}$$

and note that

$$K = F_{e1}^a L_1 = F_{e2}^a L_2 = F_{e3}^a L_3$$

and *K* also equals

$$K = F_{e_1}^a l_1 + F_{e_2}^a l_2 + F_{e_3}^a l_3 = \frac{K}{L_1} l_1 + \frac{K}{L_2} l_2 + \frac{K}{L_3} l_3 = K \sum \frac{l_i}{L_i}$$

From the outer parts of the preceding equation we obtain

$$\sum \frac{l_i}{L_i} = 1$$



Uploaded By: anonymous<sub>39</sub>

#### **Problem 11 - 38**



Estimate the remaining life in revolutions of an 02-30 mm angular-contact ball bearing already subjected to 200 000 revolutions with a radial load of 18 kN, if it is now to be subjected to a change in load to 30 kN.



# **Problem 11 - 38**

#### Table 11-3

Dimensions and Basic Load Ratings for Cylindrical Roller Bearings

|         |           | 02-Se  | eries       |                | 03-Series |                   |                           |                  |  |
|---------|-----------|--------|-------------|----------------|-----------|-------------------|---------------------------|------------------|--|
| Bore,   | OD,       | Width, | Load Ra     | ting, kN       | OD,       | Width,            | Load Ra                   | ting, kN         |  |
| mm      | mm        | mm     | <b>C</b> 10 | C <sub>0</sub> | mm        | mm                | <b>C</b> 10               | Co               |  |
| 25      | 52        | 15     | 16.8        | 8.8            | 62        | 17                | 28.6                      | 15.0             |  |
| 30      | 62        | 16     | 22.4        | 12.0           | 72        | 19                | 36.9                      | 20.0             |  |
| 35      | 72        | 17     | 31.9        | 17.6           | 80        | 21                | 44.6                      | 27.1             |  |
| 40      | 80        | 18     | 41.8        | 24.0           | 90        | 23                | 56.1                      | 32.5             |  |
| 45      | 85        | 19     | 44.0        | 25.5           | 100       | 25                | 72.1                      | 45.4             |  |
| 50      | 90        | 20     | 45.7        | 27.5           | 110       | 27                | 88.0                      | 52.0             |  |
| 55      | 100       | 21     | 56.1        | 34.0           | 120       | 29                | 102                       | 67.2             |  |
| 60      | 110       | 22     | 64.4        | 43.1           | 130       | 31                | 123                       | 76.5             |  |
| 65      | 120       | 23     | 76.5        | 51.2           | 140       | 33                | 138                       | 85.0             |  |
| 70      | 125       | 24     | 79.2        | 51.2           | 150       | 35                | 151                       | 102              |  |
| 75      | 130       | 25     | 93.1        | 63.2           | 160       | 37                | 183                       | 125              |  |
| 80      | 140       | 26     | 106         | 69.4           | 170       | 39                | 190                       | 125              |  |
| 85      | 150       | 28     | 119         | 78.3           | 180       | 41                | 212                       | 149              |  |
| 90      | 160       | 30     | 142         | 100            | 190       | 43                | 242                       | 160              |  |
| 95      | 170       | 32     | 165         | 112            | 200       | 45                | 264                       | 189              |  |
| STODENT | S-HUB.com | 34     | 183         | 125            | 215       | <sup>47</sup> Upl | oaded <sup>0</sup> By: an | $ony_{10}^{220}$ |  |



# **Problem 11 - 38**

#### Table 11-2

Dimensions and Load Ratings for Single-Row 02-Series Deep-Groove and Angular-Contact Ball Bearings

|       |     |        | Fillet  | Shoulder |                | Load Ratings, kN |        |             |         |
|-------|-----|--------|---------|----------|----------------|------------------|--------|-------------|---------|
| Bore, | OD, | Width, | Radius, | Diame    | ter, mm        | Deep             | Groove | Angular     | Contact |
| mm    | mm  | mm     | mm      | ds       | d <sub>H</sub> | <b>C</b> 10      | Co     | <b>C</b> 10 | Co      |
| 25    | 52  | 15     | 1.0     | 30       | 47             | 14.0             | 6.95   | 14.8        | 7.65    |
| 30    | 62  | 16     | 1.0     | 35       | 55             | 19.5             | 10.0   | 20.3        | 11.0    |
| 35    | 72  | 17     | 1.0     | 41       | 65             | 25.5             | 13.7   | 27.0        | 15.0    |
| 40    | 80  | 18     | 1.0     | 46       | 72             | 30.7             | 16.6   | 31.9        | 18.6    |
| 45    | 85  | 19     | 1.0     | 52       | 77             | 33.2             | 18.6   | 35.8        | 21.2    |
| 50    | 90  | 20     | 1.0     | 56       | 82             | 35.1             | 19.6   | 37.7        | 22.8    |
| 55    | 100 | 21     | 1.5     | 63       | 90             | 43.6             | 25.0   | 46.2        | 28.5    |
| 60    | 110 | 22     | 1.5     | 70       | 99             | 47.5             | 28.0   | 55.9        | 35.5    |
| 65    | 120 | 23     | 1.5     | 74       | 109            | 55.9             | 34.0   | 63.7        | 41.5    |
| 70    | 125 | 24     | 1.5     | 79       | 114            | 61.8             | 37.5   | 68.9        | 45.5    |
| 75    | 130 | 25     | 1.5     | 86       | 119            | 66.3             | 40.5   | 71.5        | 49.0    |
| 80    | 140 | 26     | 2.0     | 93       | 127            | 70.2             | 45.0   | 80.6        | 55.0    |
| 85    | 150 | 28     | 2.0     | 99       | 136            | 83.2             | 53.0   | 90.4        | 63.0    |
| 90    | 160 | 30     | 2.0     | 104      | 146            | 95.6             | 62.0   | 106         | 73.5    |
| 95    | 170 | 32     | 2.0     | 110      | 156            | 108              | 69.5   | 121         | 85.0    |





#### Figure 11-13

Nomenclature of a tapered roller bearing. Point *G* is the location of the effective load center; use this point to estimate the radial bearing load. (*Courtesy of The Timken Company.*)



STUDENTS-HUB.com



#### Indirect mounting Figure 11-14 а Comparison of mounting $B_c$ $A_{c}$ stability between indirect and direct mountings. (Courtesy of Cone face The Timken Company.) *(a)* facing each 90<sup>6</sup> other Bearing A Bearing B $B'_o$ `A Cone back facing each (b) other $B_c$ $A_c$ a, Direct mounting

STUDENTS-HUB.com

Uploaded By: anonymous<sub>44</sub>

Using  $F_i$  for the induced thrust load from a radial load, Timken provides the equation:









#### Figure 11-16

Direct-mounted tapered roller bearings, showing radial, induced thrust, and external thrust loads.



$$\begin{array}{ll} \mbox{If} & F_{iA} > (F_{iB} + F_{ae}) & \begin{cases} F_{eB} = 0.4F_{rB} + K_B(F_{iA} - F_{ae}) & (11\mbox{-}20a) \\ F_{eA} = F_{rA} & (11\mbox{-}20b) \\ \end{bmatrix} \\ \begin{array}{l} \mbox{STUDENTS-HUB.com} & \mbox{Uploaded By: anonymous}_{46} \end{cases} \end{array}$$

# Example 11-8



The shaft depicted in Fig. 11–18*a* carries a helical gear with a tangential force of 3980 N, a radial force of 1770 N, and a thrust force of 1690 N at the pitch cylinder with directions shown. The pitch diameter of the gear is 200 mm. The shaft runs at a speed of 800 rev/min, and the span (effective spread) between the direct-mount bearings is 150 mm. The design life is to be 5000 h and an application factor of 1 is appropriate. If the reliability of the bearing set is to be 0.99, select suitable single-row tapered-roller Timken bearings.





# Example 11-8





# 11.5 Relating Load, Life, and Reliability



$$C_{10} \approx a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(1 - R_D)^{1/b}} \right]^{1/a} \qquad R \ge 0.90 \qquad (11-10)$$

| Table 11-6<br>Typical Weibull |              | Ratina Life,                                | Weibull Parameters<br>Rating Lives |               |              |  |  |  |
|-------------------------------|--------------|---------------------------------------------|------------------------------------|---------------|--------------|--|--|--|
| Parameters for Two            | Manufacturer | Revolutions                                 | <b>X</b> 0                         | θ             | Ь            |  |  |  |
| Manufacturers                 | 1<br>2       | 90(10 <sup>6</sup> )<br>1(10 <sup>6</sup> ) | 0<br>0.02                          | 4.48<br>4.459 | 1.5<br>1.483 |  |  |  |



Uploaded By: anonymous<sub>49</sub>

# Example 11-8



#### Trail 1

$$C_{10} = (1)(4651) \left[ \frac{2.67}{(4.48)(1 - 0.995)^{2/3}} \right]^{3/10} = 11\,486\,\mathrm{N}$$

From Fig. 11–15, tentatively select type TS 15100 cone and 15245 cup, which will work:  $K_A = 1.67$ ,  $C_{10} = 12$  100 N.

For bearing B, from Eq. (11–10), the catalog entry  $C_{10}$  should equal or exceed

$$C_{10} = (1)2654 \left[ \frac{2.67}{(4.48)(1 - 0.995)^{2/3}} \right]^{3/10} = 6554 \text{ N}$$

Tentatively select the bearing identical to bearing A, which will work:  $K_B = 1.67$ ,  $C_{10} = 12 \ 100 \ \text{N}$ .



Uploaded By: anonymous<sub>50</sub>

# Figure 11 - 15



Catalog entry of single-row straightbore Timken roller bearings

#### SINGLE-ROW STRAIGHT BORE



|                         |                         |                         |                            |                                             |             |                        |              | cone   |                                  |                                        |                                  | cup                 |                               |                         |                                  |                     |
|-------------------------|-------------------------|-------------------------|----------------------------|---------------------------------------------|-------------|------------------------|--------------|--------|----------------------------------|----------------------------------------|----------------------------------|---------------------|-------------------------------|-------------------------|----------------------------------|---------------------|
| bore of                 | outside<br>diameter     | width                   | rat<br>500<br>3000<br>one- | ting at<br>rpm for<br>hours L <sub>10</sub> | fac-<br>tor | eff.<br>load<br>center | part numbers |        | max<br>shaft<br>fillet<br>radius | max<br>shaft<br>fillet width<br>radius | backing<br>shoulder<br>diameters |                     | max<br>hous-<br>ing<br>fillet | width                   | backing<br>shoulder<br>diameters |                     |
| d                       | D                       | Т                       | row<br>radial<br>N<br>lbf  | nrust<br>N<br>lbf                           | K           | a <sup>②</sup>         | cone         | cup    | R①                               | В                                      | d <sub>b</sub>                   | d <sub>a</sub>      | radius<br>r①                  | С                       | D <sub>b</sub>                   | D <sub>a</sub>      |
| <b>25.400</b><br>1.0000 | <b>50.292</b><br>1.9800 | <b>14.224</b><br>0.5600 | <b>7210</b><br>1620        | <b>4620</b><br>1040                         | 1.56        | - <b>3.3</b><br>-0.13  | L44642       | L44610 | <b>3.5</b><br>0.14               | <b>14.732</b><br>0.5800                | <b>36.0</b><br>1.42              | <b>29.5</b><br>1.16 | 1.3<br>0.05                   | <b>10.668</b><br>0.4200 | <b>44.5</b><br>1.75              | <b>47.0</b><br>1.85 |
| <b>25.400</b><br>1.0000 | <b>50.292</b><br>1.9800 | <b>14.224</b> 0.5600    | <b>7210</b><br>1620        | <b>4620</b><br>1040                         | 1.56        | - <b>3.3</b><br>-0.13  | L44643       | L44610 | <b>1.3</b><br>0.05               | <b>14.732</b> 0.5800                   | <b>31.5</b><br>1.24              | <b>29.5</b><br>1.16 | <b>1.3</b><br>0.05            | <b>10.668</b><br>0.4200 | <b>44.5</b><br>1.75              | <b>47.0</b><br>1.85 |
| <b>25.400</b> 1.0000    | <b>51.994</b> 2.0470    | <b>15.011</b><br>0.5910 | <b>6990</b><br>1570        | <b>4810</b><br>1080                         | 1.45        | - <b>2.8</b><br>-0.11  | 07100        | 07204  | <b>1.0</b><br>0.04               | <b>14.260</b><br>0.5614                | <b>30.5</b><br>1.20              | <b>29.5</b><br>1.16 | <b>1.3</b><br>0.05            | <b>12.700</b> 0.5000    | <b>45.0</b><br>1.77              | <b>48.0</b><br>1.89 |
| <b>25.400</b> 1.0000    | <b>56.896</b> 2.2400    | <b>19.368</b><br>0.7625 | <b>10900</b><br>2450       | <b>5740</b><br>1290                         | 1.90        | - <b>6.9</b><br>-0.27  | 1780         | 1729   | <b>0.8</b><br>0.03               | <b>19.837</b><br>0.7810                | <b>30.5</b><br>1.20              | <b>30.0</b><br>1.18 | <b>1.3</b><br>0.05            | 15.875<br>0.6250        | <b>49.0</b><br>1.93              | <b>51.0</b> 2.01    |
| <b>25.400</b><br>1.0000 | <b>57.150</b> 2.2500    | <b>19.431</b><br>0.7650 | <b>11700</b><br>2620       | <b>10900</b><br>2450                        | 1.07        | - <b>3.0</b><br>-0.12  | M84548       | M84510 | 1.5<br>0.06                      | <b>19.431</b><br>0.7650                | <b>36.0</b><br>1.42              | <b>33.0</b><br>1.30 | 1.5<br>0.06                   | 14.732<br>0.5800        | <b>48.5</b><br>1.91              | <b>54.0</b> 2.13    |

# Figure 11 - 15



|                         |                         |                         |                                                        |                      |      |                                 | co           | ne     |                    |                         | cu                  |                     |                    |                         |                     |                     |
|-------------------------|-------------------------|-------------------------|--------------------------------------------------------|----------------------|------|---------------------------------|--------------|--------|--------------------|-------------------------|---------------------|---------------------|--------------------|-------------------------|---------------------|---------------------|
| bore outside diameter   | outside                 |                         | rating at<br>500 rpm for<br>3000 hours L <sub>10</sub> |                      | fac- | fac- eff.<br>tor load<br>center | part numbers |        | max<br>shaft       | midth                   | backing<br>shoulder |                     | max<br>hous-       |                         | backing<br>shoulder |                     |
|                         | widui                   | one-<br>row<br>radial   | thrust                                                 |                      | cone |                                 | cup          | radius | width              | ulani                   |                     | fillet<br>radius    | widui              |                         |                     |                     |
| d                       | D                       | Т                       | N<br>lbf                                               | N<br>lbf             | K    | <b>a</b> ②                      | a@           | cup    | R①                 | В                       | d <sub>b</sub>      | d <sub>a</sub>      | r①                 | С                       | D <sub>b</sub>      | D <sub>a</sub>      |
| <b>25.400</b><br>1.0000 | <b>50.292</b><br>1.9800 | <b>14.224</b> 0.5600    | <b>7210</b><br>1620                                    | <b>4620</b><br>1040  | 1.56 | -3.3<br>-0.13                   | L44643       | L44610 | <b>1.3</b><br>0.05 | <b>14.732</b><br>0.5800 | <b>31.5</b><br>1.24 | <b>29.5</b><br>1.16 | 1.3<br>0.05        | <b>10.668</b><br>0.4200 | <b>44.5</b><br>1.75 | <b>47.0</b><br>1.85 |
| <b>25.400</b><br>1.0000 | <b>51.994</b> 2.0470    | <b>15.011</b><br>0.5910 | <b>6990</b><br>1570                                    | <b>4810</b><br>1080  | 1.45 | - <b>2.8</b><br>-0.11           | 07100        | 07204  | <b>1.0</b><br>0.04 | <b>14.260</b><br>0.5614 | <b>30.5</b><br>1.20 | <b>29.5</b><br>1.16 | <b>1.3</b><br>0.05 | <b>12.700</b> 0.5000    | <b>45.0</b><br>1.77 | <b>48.0</b><br>1.89 |
| <b>25.400</b><br>1.0000 | <b>56.896</b> 2.2400    | <b>19.368</b><br>0.7625 | <b>10900</b><br>2450                                   | <b>5740</b><br>1290  | 1.90 | - <b>6.9</b><br>-0.27           | 1780         | 1729   | <b>0.8</b><br>0.03 | <b>19.837</b><br>0.7810 | <b>30.5</b><br>1.20 | <b>30.0</b><br>1.18 | <b>1.3</b><br>0.05 | <b>15.875</b><br>0.6250 | <b>49.0</b><br>1.93 | <b>51.0</b> 2.01    |
| <b>25.400</b><br>1.0000 | <b>57.150</b> 2.2500    | <b>19.431</b><br>0.7650 | <b>11700</b><br>2620                                   | <b>10900</b><br>2450 | 1.07 | - <b>3.0</b><br>-0.12           | M84548       | M84510 | <b>1.5</b><br>0.06 | <b>19.431</b><br>0.7650 | <b>36.0</b><br>1.42 | <b>33.0</b><br>1.30 | <b>1.5</b><br>0.06 | <b>14.732</b> 0.5800    | <b>48.5</b><br>1.91 | <b>54.0</b><br>2.13 |
| <b>25.400</b><br>1.0000 | <b>58.738</b><br>2.3125 | <b>19.050</b><br>0.7500 | <b>11600</b><br>2610                                   | <b>6560</b><br>1470  | 1.77 | - <b>5.8</b><br>-0.23           | 1986         | 1932   | <b>1.3</b><br>0.05 | <b>19.355</b><br>0.7620 | <b>32.5</b><br>1.28 | <b>30.5</b><br>1.20 | 1.3<br>0.05        | <b>15.080</b><br>0.5937 | <b>52.0</b><br>2.05 | <b>54.0</b> 2.13    |
| <b>25.400</b><br>1.0000 | <b>59.530</b><br>2.3437 | <b>23.368</b><br>0.9200 | <b>13900</b><br>3140                                   | <b>13000</b><br>2930 | 1.07 | - <b>5.1</b><br>-0.20           | M84249       | M84210 | <b>0.8</b><br>0.03 | <b>23.114</b> 0.9100    | <b>36.0</b><br>1.42 | <b>32.5</b><br>1.27 | <b>1.5</b><br>0.06 | <b>18.288</b><br>0.7200 | <b>49.5</b><br>1.95 | <b>56.0</b> 2.20    |
| <b>25.400</b><br>1.0000 | <b>60.325</b> 2.3750    | <b>19.842</b><br>0.7812 | <b>11000</b><br>2480                                   | <b>6550</b><br>1470  | 1.69 | - <b>5.1</b><br>-0.20           | 15578        | 15523  | <b>1.3</b><br>0.05 | 17.462<br>0.6875        | <b>32.5</b><br>1.28 | <b>30.5</b><br>1.20 | 1.5<br>0.06        | <b>15.875</b><br>0.6250 | <b>51.0</b> 2.01    | <b>54.0</b><br>2.13 |
| <b>25.400</b><br>1.0000 | <b>61.912</b><br>2.4375 | <b>19.050</b><br>0.7500 | <b>12100</b><br>2730                                   | <b>7280</b><br>1640  | 1.67 | - <b>5.8</b><br>-0.23           | 15101        | 15243  | <b>0.8</b><br>0.03 | <b>20.638</b><br>0.8125 | <b>32.5</b><br>1.28 | <b>31.5</b><br>1.24 | <b>2.0</b><br>0.08 | <b>14.288</b><br>0.5625 | <b>54.0</b><br>2.13 | <b>58.0</b><br>2.28 |
| <b>25.400</b><br>1.0000 | <b>62.000</b><br>2.4409 | <b>19.050</b><br>0.7500 | <b>12100</b><br>2730                                   | <b>7280</b><br>1640  | 1.67 | - <b>5.8</b><br>-0.23           | 15100        | 15245  | <b>3.5</b><br>0.14 | <b>20.638</b><br>0.8125 | <b>38.0</b><br>1.50 | <b>31.5</b><br>1.24 | 1.3<br>0.05        | <b>14.288</b><br>0.5625 | <b>55.0</b><br>2.17 | <b>58.0</b><br>2.28 |
| <b>25.400</b><br>1.0000 | <b>62.000</b><br>2.4409 | <b>19.050</b><br>0.7500 | <b>12100</b><br>2730                                   | <b>7280</b><br>1640  | 1.67 | - <b>5.8</b><br>-0.23           | 15101        | 15245  | <b>0.8</b> 0.03    | <b>20.638</b><br>0.8125 | <b>32.5</b><br>1.28 | <b>31.5</b><br>1.24 | 1.3<br>0.05        | <b>14.288</b><br>0.5625 | <b>55.0</b><br>2.17 | <b>58.0</b> 2.28    |





#### Trail 2

For bearing A, from Eq. (11–10) the corrected catalog entry  $C_{10}$  should equal or exceed

$$C_{10} = (1)(4938) \left[ \frac{2.67}{(4.48)(1 - 0.995)^{2/3}} \right]^{3/10} = 12\ 195\ \text{N}$$

Although this catalog entry exceeds slightly the tentative selection for bearing A, we will keep it since the reliability of bearing B exceeds 0.995. In the next section we will quantitatively show that the combined reliability of bearing A and B will exceed the reliability goal of 0.99.

For bearing *B*,  $F_{eB} = F_{rB} = 2654$  N. From Eq. (11–10),

$$C_{10} = (1)2654 \left[ \frac{2.67}{(4.48)(1 - 0.995)^{2/3}} \right]^{3/10} = 6554 \text{ N}$$



Uploaded By: anonymous<sub>53</sub>