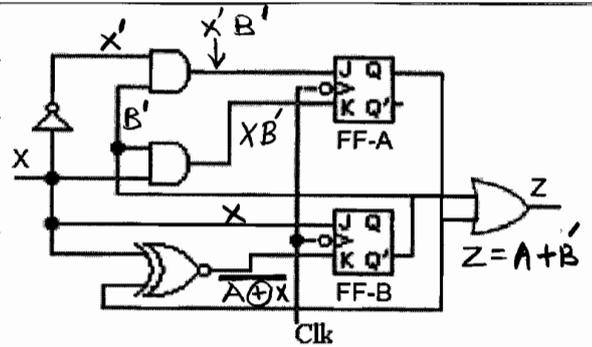


2. a.  $Z = A + B'$   
 → ckt is Moore since external o/p depends on the state only (not affected by the external I/P).



b.  $J_A = X'B'$ ,  $J_B = XB'$   
 $J_B = X$ ,  $J_B = A \oplus X$

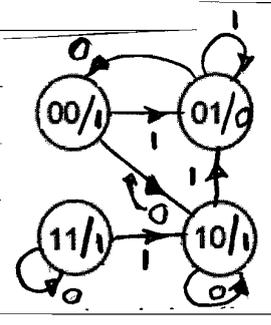
i. present state

| 1-D state Table | present state |   |   | Through CT Table |                | Next state     |                | Ext. o/p Z | Characteristic Table (CT) of JK FF |                |    |        |
|-----------------|---------------|---|---|------------------|----------------|----------------|----------------|------------|------------------------------------|----------------|----|--------|
|                 | A             | B | X | J <sub>A</sub>   | K <sub>A</sub> | J <sub>B</sub> | K <sub>B</sub> |            | A <sup>+</sup>                     | B <sup>+</sup> | JK | Q(t+1) |
| 0               | 0             | 0 | 0 | 1                | 0              | 0              | 1              | 1          | 0                                  | 1              | 1  | Q(t+1) |
| 1               | 0             | 0 | 1 | 0                | 1              | 1              | 0              | 0          | 1                                  | 0              | 0  | Q(t)   |
| 2               | 0             | 1 | 0 | 0                | 0              | 0              | 1              | 0          | 0                                  | 0              | 0  | 0      |
| 3               | 0             | 1 | 1 | 0                | 0              | 1              | 0              | 0          | 1                                  | 0              | 1  | 1      |
| 4               | 1             | 0 | 0 | 1                | 0              | 0              | 0              | 1          | 0                                  | 1              | 1  | Q'(t)  |
| 5               | 1             | 0 | 1 | 0                | 1              | 1              | 1              | 0          | 1                                  | 1              | 1  |        |
| 6               | 1             | 1 | 0 | 0                | 0              | 0              | 0              | 1          | 1                                  | 1              | 1  |        |
| 7               | 1             | 1 | 1 | 0                | 0              | 1              | 1              | 1          | 0                                  | 1              | 1  |        |

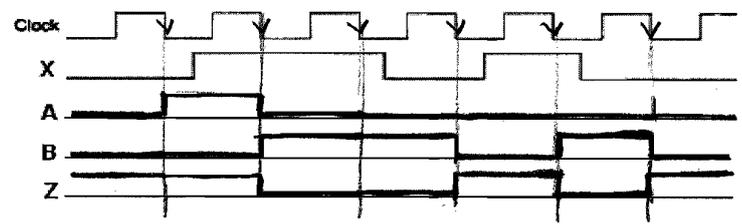
ii. 2-D state Table

| Present state<br>AB | Next state |     | o/p<br>Z |
|---------------------|------------|-----|----------|
|                     | $A^+ B^+$  |     |          |
|                     | x=0        | x=1 |          |
| 00                  | 10         | 01  | 1        |
| 01                  | 00         | 01  | 0        |
| 10                  | 10         | 01  | 1        |
| 11                  | 11         | 10  | 1        |

iii. State Diagram



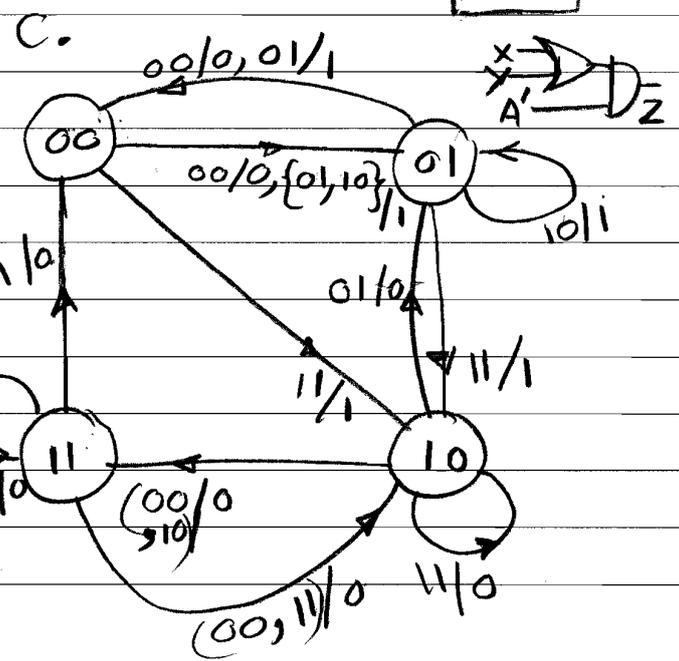
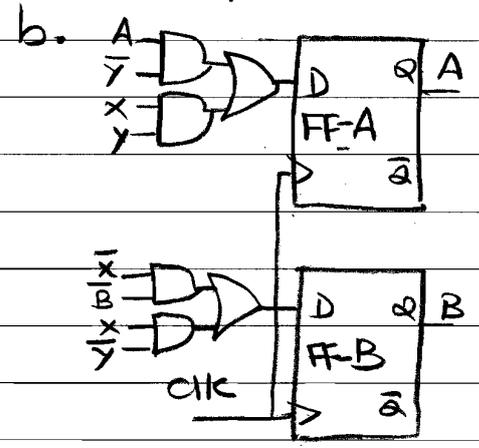
C.



4.  $A(t+1) = Ay' + xy$ ,  $B(t+1) = B'x' + xy'$ ,  $Z = A'(x+y)$

a. Mealy ckt, o/p depends on external i/p's

| pres. state<br>AB | I/p's<br>xy | $D_A = A^+$ | $D_B = B^+$ | $x+y$ | $Z = A'(x+y)$ |
|-------------------|-------------|-------------|-------------|-------|---------------|
| 00                | 00          | 0           | 1           | 0     | 0             |
| 00                | 01          | 0           | 1           | 1     | 1             |
| 00                | 10          | 0           | 1           | 1     | 1             |
| 00                | 11          | 1           | 0           | 1     | 1             |
| 01                | 00          | 0           | 0           | 0     | 0             |
| 01                | 01          | 0           | 0           | 1     | 1             |
| 01                | 10          | 0           | 1           | 1     | 1             |
| 01                | 11          | 1           | 0           | 1     | 1             |
| 10                | 00          | 1           | 1           | 0     | 0             |
| 10                | 01          | 0           | 1           | 1     | 0             |
| 10                | 10          | 1           | 1           | 1     | 0             |
| 10                | 11          | 1           | 0           | 1     | 0             |
| 11                | 00          | 1           | 0           | 0     | 0             |
| 11                | 01          | 0           | 0           | 1     | 0             |
| 11                | 10          | 0           | 0           | 1     | 0             |
| 11                | 11          | 1           | 0           | 1     | 0             |

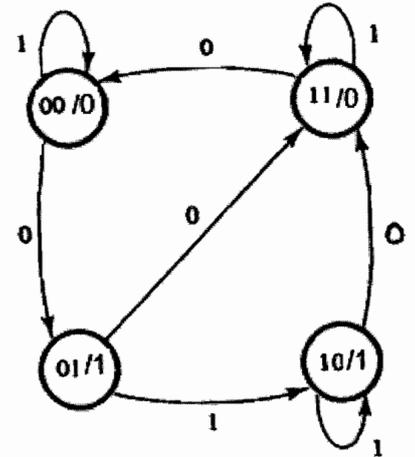


4.

a. Moore, 1 external I/P,  
1 external o/p, 2 state variables,  
2 FFs.

b. 2-D Table

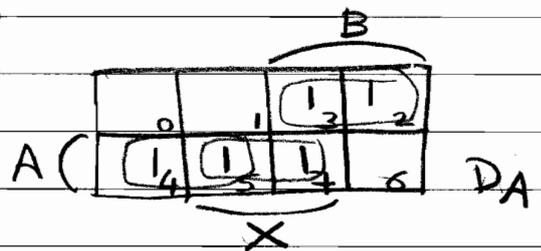
| Present state<br>AB | Next state  |             | output<br>Z |
|---------------------|-------------|-------------|-------------|
|                     | X=0<br>A+B+ | X=1<br>A+B+ |             |
| 00                  | 01          | 00          | 0           |
| 01                  | 11          | 10          | 1           |
| 10                  | 11          | 10          | 1           |
| 11                  | 00          | 11          | 0           |



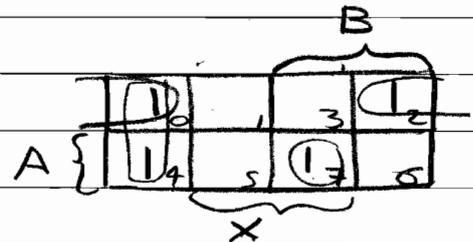
1-D Table

| ABX   | A+  | B+  | Z |
|-------|-----|-----|---|
|       | =DA | =DB |   |
| 0 000 | 0   | 1   | 0 |
| 1 001 | 0   | 0   | 0 |
| 2 010 | 1   | 1   | 1 |
| 3 011 | 1   | 0   | 1 |
| 4 100 | 1   | 1   | 1 |
| 5 101 | 1   | 0   | 1 |
| 6 110 | 0   | 0   | 0 |
| 7 111 | 1   | 1   | 0 |

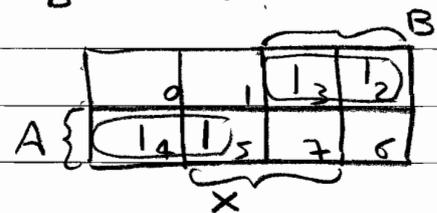
c.



$$D_A = \bar{A}B + AX + A\bar{B}$$



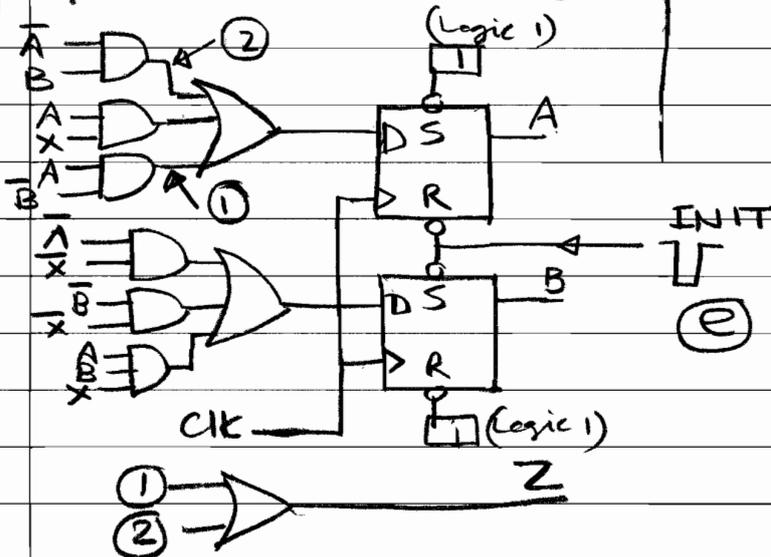
$$D_B = \bar{A}\bar{X} + \bar{B}\bar{X} + ABX$$



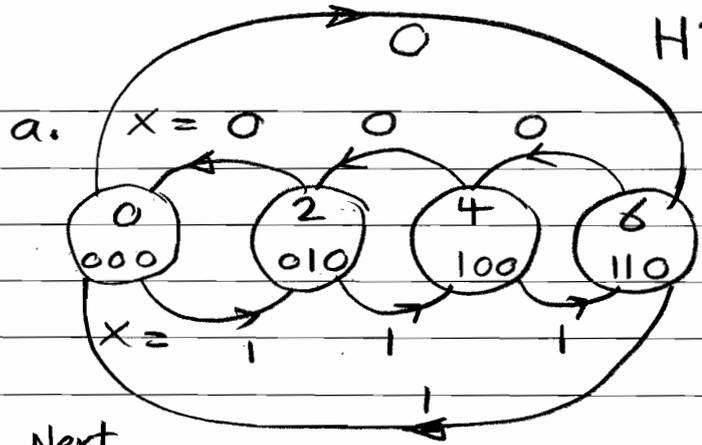
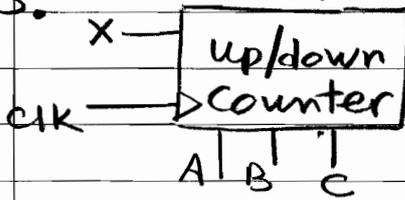
$$Z = A\bar{B} + \bar{A}B$$

f. From the state diagram we need 3 clock pulses to return to state 00.

d.

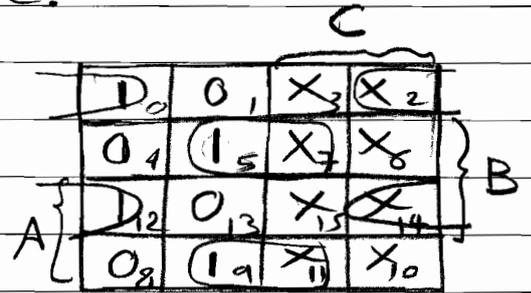


5.  $\begin{cases} X=0 \text{ Down} \\ X=1 \text{ Up} \end{cases}$



b. Present State I/p

|    | A | B | C | X | Next state<br>A <sup>+</sup> B <sup>+</sup> C <sup>+</sup><br>(D <sub>A</sub> ) (D <sub>B</sub> ) D <sub>C</sub> |
|----|---|---|---|---|--|
| 0  | 0 | 0 | 0 | 0 | 0 1 0  |
| 1  | 0 | 0 | 0 | 1 | 0 1 0  |
| 2  | 0 | 0 | 1 | 0 | X X X  |
| 3  | 0 | 0 | 1 | 1 | X X X  |
| 4  | 0 | 1 | 0 | 0 | 0 0 0  |
| 5  | 0 | 1 | 0 | 1 | 1 0 0  |
| 6  | 0 | 1 | 1 | 0 | X X X  |
| 7  | 0 | 1 | 1 | 1 | X X X  |
| 8  | 1 | 0 | 0 | 0 | 0 1 0  |
| 9  | 1 | 0 | 0 | 1 | 1 1 0  |
| 10 | 1 | 0 | 1 | 0 | X X X  |
| 11 | 1 | 0 | 1 | 1 | X X X  |
| 12 | 1 | 1 | 0 | 0 | 1 0 0  |
| 13 | 1 | 1 | 0 | 1 | 0 0 0  |
| 14 | 1 | 1 | 1 | 0 | X X X  |
| 15 | 1 | 1 | 1 | 1 | X X X  |

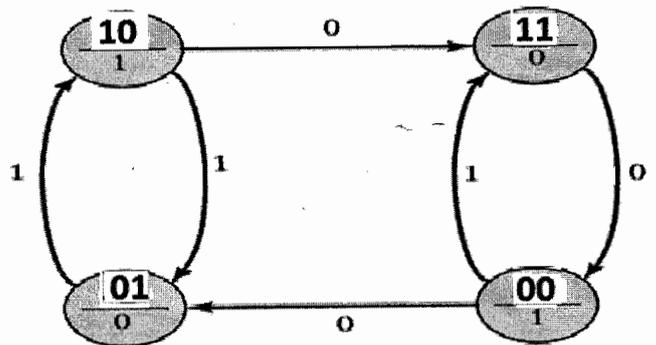


DA map

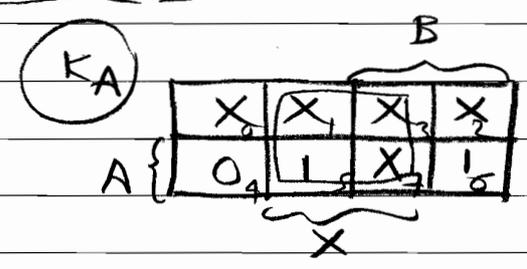
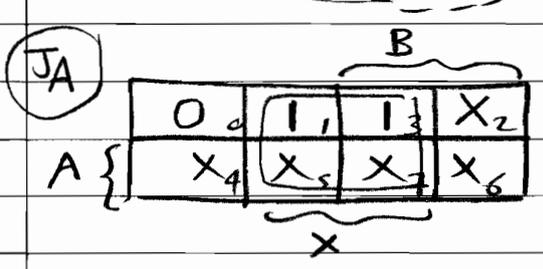
$$D_A = \bar{A}\bar{B}\bar{X} + \bar{A}B\bar{X} + A\bar{B}\bar{X} + AB\bar{X}$$

6. JK FF Excitation Table

| Q(t) | Q(t+1) | J | K |
|------|--------|---|---|
| 0    | 0      | 0 | X |
| 0    | 1      | 1 | X |
| 1    | 0      | X | 1 |
| 1    | 1      | X | 0 |

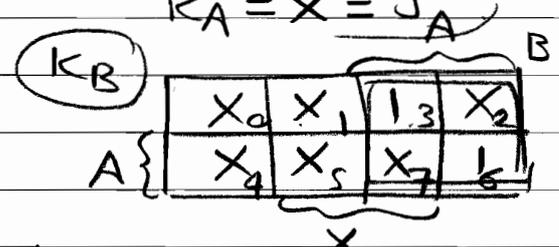
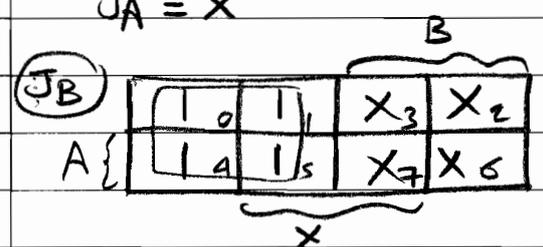


|   | 6, contd. Present |   |   | Next  |       |   | $J_A$ $K_A$ |   | $J_B$ $K_B$ |   |
|---|-------------------|---|---|-------|-------|---|-------------|---|-------------|---|
|   | A                 | B | X | $A^+$ | $B^+$ | Z |             |   |             |   |
| 0 | 0                 | 0 | 0 | 0     | 1     | 1 | 0           | X | 1           | X |
| 1 | 0                 | 0 | 1 | 1     | 1     | 1 | 1           | X | 1           | X |
| 2 | 0                 | 1 | 0 | X     | X     | 0 | X           | X | X           | X |
| 3 | 0                 | 1 | 1 | 1     | 0     | 0 | 1           | X | X           | 1 |
| 4 | 1                 | 0 | 0 | 1     | 1     | 1 | X           | 0 | 1           | X |
| 5 | 1                 | 0 | 1 | 0     | 1     | 1 | X           | 1 | 1           | X |
| 6 | 1                 | 1 | 0 | 0     | 0     | 0 | X           | 1 | X           | 1 |
| 7 | 1                 | 1 | 1 | X     | X     | 0 | X           | X | X           | X |



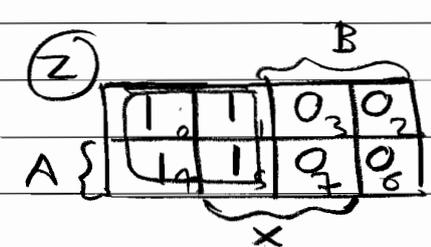
$J_A = X$

$K_A = X = J_A$



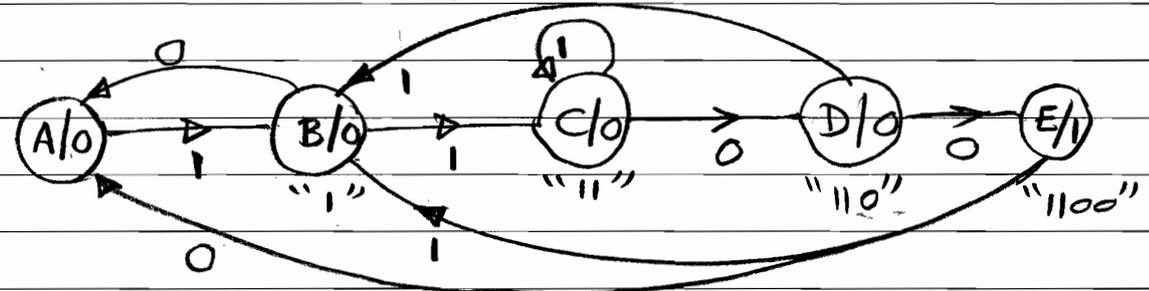
$J_B = \bar{B}$

$K_B = B$



$Z = \bar{B}$

7. a.



- b.
- 5 states
  - 3 state variables
  - 3 FFs
  - $2^3 - 5 = 3$  unused states