

لجاء

Experiment 2

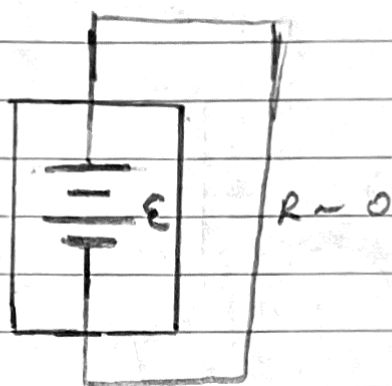
Source internal Resistance, Loading problems and circuit impedance matching.

* electromotive force ($\mathcal{E}$) القوة الدافعة الكهربائية: it is the open circuit voltage difference between its terminals, or it is the voltage difference between terminals of an open circuit.

* An ideal voltage source connected to a short circuit ($R \sim 0$) should according to Ohm's law be able to provide an almost infinite current

ohm's law

$$I = \frac{\mathcal{E}}{R} \approx \infty \quad (R \sim 0)$$



ideal battery or source

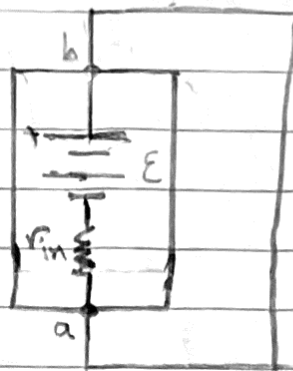
* In real circuits - a voltage source connected to a short circuit can neither maintain its emf) as a voltage difference across its terminals nor can it provide the circuit with unlimited current
في الدارات الحقيقية ان توتر المصدر لا يمكنه ان يحافظ على توتره عند اقترانها بدارة قصر (R ~ 0)

لا يستطيع المصدر الحفاظ على القوة الدافعة الكهربائية \mathcal{E} عند اقترانها بدارة قصر
ولذلك لا يستطيع ان يزود الدارة بتيار لا محدود

⇒ Therefore, each real voltage is assigned an internal resistance (r_{in})

②

Fig 2.1



real battery or real source
↓
has an internal resistance

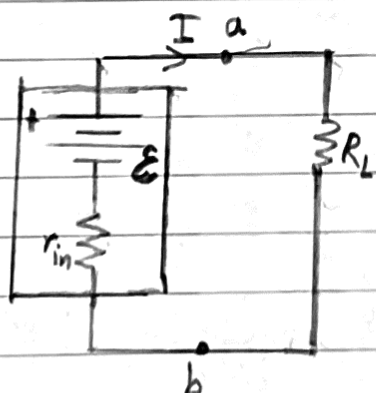
$V_{ab} \approx \mathcal{E}$ for small r_{in}

⇒ Fig gives more realistic representation of a voltage source

- The voltage sources with small internal resistance can maintain most of their emf as a voltage difference between their terminals
- ⇒ So provide circuit with higher current values than would the ones with high internal resistance.

↳ Load: any component which consumes electrical power to produce useful work i.e. ...
⇒ and the resistance of such a component is called load resistance (R_L)

* Loading happens when r_{in} is comparable to R_L



The current passing through the simple series circuit is ⇒

$$I = \frac{\mathcal{E}}{R_L + r_{in}}$$

(3)

Ex 2.1
The voltage difference between the source terminals is :

$$V_{ab} = V_{RL} = I R_L$$

$$\Rightarrow \boxed{V_{RL} = \frac{\mathcal{E} R_L}{(R_L + r_{in})}}$$

* If $R_L \gg r_{in}$ then $R_L + r_{in} \approx R_L$ then

$$V_{RL} \approx \frac{\mathcal{E}}{\cancel{R_L}} \cancel{R_L}$$

$\Rightarrow \boxed{V_{RL} \approx \mathcal{E}} \Rightarrow$ the source delivers most of its emf as a voltage difference across its terminals.

* If R_L is comparable

* If R_L is comparable to r_{in} ($R_L \approx r_{in}$) then

$$V_{RL} \approx \frac{\mathcal{E}}{(R_L + R_L)} R_L$$

$$V_{RL} \approx \frac{\mathcal{E}}{2R_L} R_L$$

$\Rightarrow \boxed{V_{RL} \approx \frac{\mathcal{E}}{2}}$ in this case considerable amount of power is consumed inside the source and converted to ~~un~~useful heat energy. ^{مفق / ضائع} this case is said to be loaded.

* In practical circuits we want to avoid loading the source so we choose $R_L \geq 10 r_{in}$

Impedance Matching (Maximum Power Transfer)

* In real circuits, power consumed in the load produce useful work $\Rightarrow$ therefore we seek to consume the maximum available power there

* The power consumed in the load resistor is

$$P = I^2 R_L$$

$$= \left(\frac{\mathcal{E}}{R_L + r_{in}} \right)^2 R_L$$

$$\Rightarrow P = \frac{\mathcal{E}^2}{(R_L + r_{in})^2} R_L$$

$\rightarrow$ represents the power consumed in the load as a function of the load resistance itself.

* The function $P(R_L)$ has a maximum value which can be obtained by setting $\frac{dP}{dR_L} = 0$

$\Rightarrow R_L = r_{in} \Rightarrow$ the condition for transferring maximum power to the load resistance

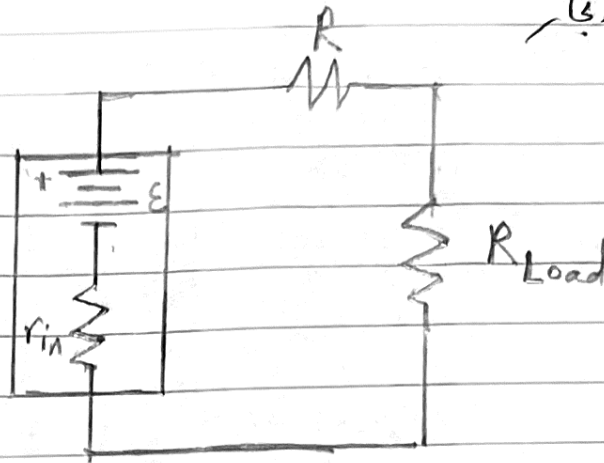
$\rightarrow$ This choice of load resistance is called impedance matching.

• To achieve this condition without avoiding loading problem additional resistance R is added

$\Rightarrow$ this R helps in avoiding loading problem and fulfilling the condition of impedance matching for large load values.

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- The only disadvantage is that this additional resistance R consumes part of the power delivered to the circuit by the source.

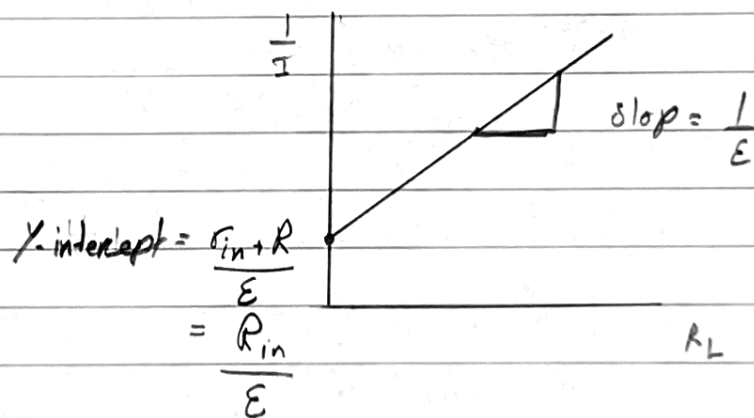


$$I = \frac{\epsilon}{r_{in} + R + R_L}$$

$$\frac{1}{I} = \frac{r_{in} + R + R_L}{\epsilon}$$

$$\frac{1}{I} = \frac{R_L}{\epsilon} + \frac{r_{in} + R}{\epsilon} \rightarrow r_{in} + R = R_{in}$$

plotting $\frac{1}{I}$ vs R_L on a linear graph



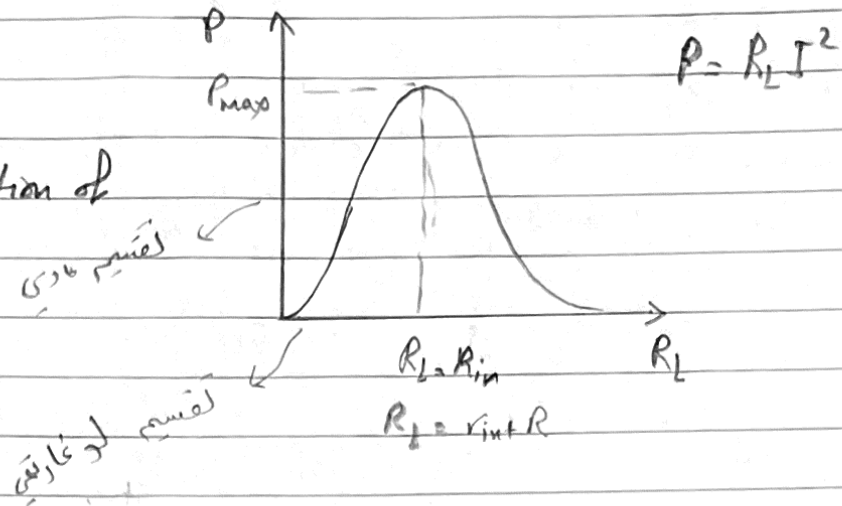
Find ϵ , R_{in} knowing $R = 1\text{ k}\Omega \Rightarrow$ you can find r_{in}

DM ان لفظ في كتابي
حيث يكون كذا 983

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Plotting P vs R_L on a semi-log graph paper

Find R_L that satisfies the condition of max power.

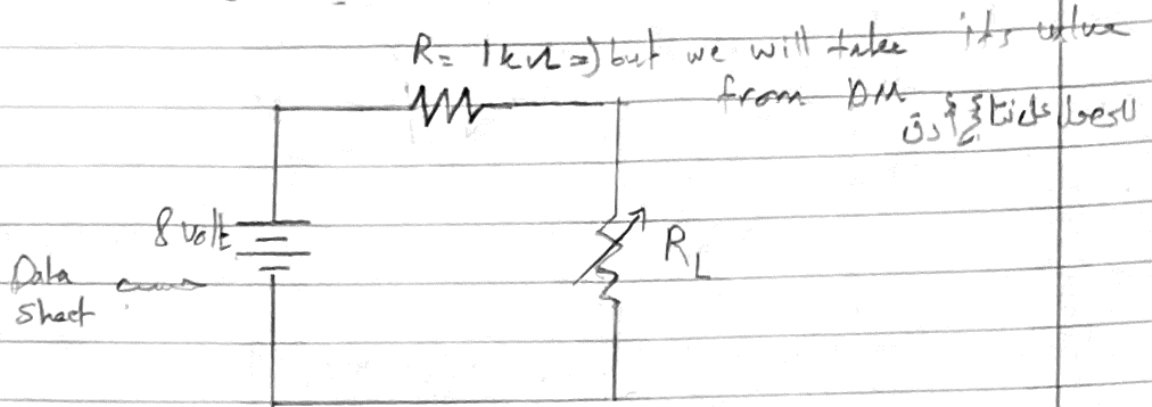


سأدعى

خطوات العمل

a) Connect the circuit as in Fig

نقوم بوصل الدارة كما في الشكل



b) change R_L and record the value of current each time

غير قيم R_L وتسجل كل مرة في data sheet و سجل قيمة التيار المار في R_L في كل مرة

c) Draw $1/I$ vs R_L on a linear graph to find the value of r_{in} and $\mathcal{E}$

y intercept = $\frac{R + r_{in}}{\mathcal{E}}$, $R = 1k\Omega$, $\mathcal{E}$: جهد المصدر

slope = $\frac{1}{\mathcal{E}}$

مع قراءة الجهد
عوضنا
983 mV

d) compute P for all values of $I \Rightarrow (P = R_L I^2)$

e) plot P vs R_L on a semi-log paper

At $P_{max} \Rightarrow R_L = R_{in} = r_{in} + R$

$\Rightarrow$ You can find R_L that satisfies the condition of maximum power transfer.

$r_{in} = R_L - R$

تقريباً بالقيمة
بالقيمة DM
التي حتمتها P_{max}

للوصول على نتائج