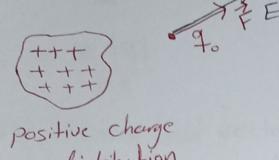
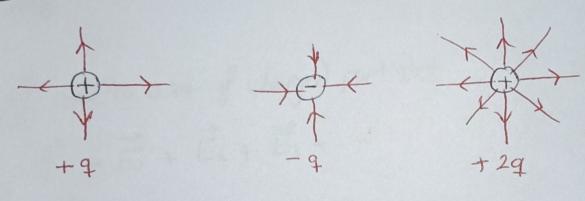
Chapter 22: Electric Fields

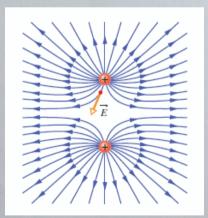
The electric field \vec{E} at any point is defined in terms of the electro
Static fire \vec{F} that would be exerted on a positive test charge \vec{q} .

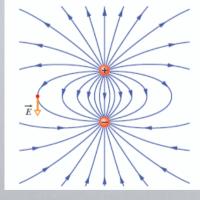
Placed there. $\vec{E} = \vec{F}$ $\vec{E} = \vec{F}$

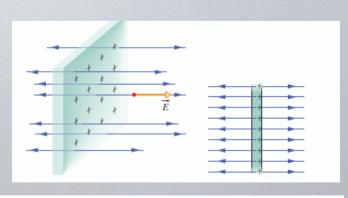


& Electric field lines :









Very large, non-conducting sheet with uniform positive charge on one side

$$E = \frac{k |q|}{r^2}$$

=> The electric field vectors set up by a positively charged particle all point directly away from the particles. Those set up by a negatively charged particles all point directly toward the particle.

$$\vec{z} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3 + \cdots$$

22-32] the four particles are fixed in place and have charges

$$9 = 9 = +5e$$
, $9 = +3e$, and $9 = -12e$. Distance $0 = 8.0 \, \text{Mm}$

What is the magnitude of the net electric held at point P due to

the particles P

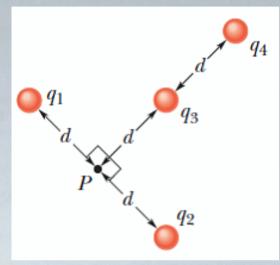
•
$$E_1 = E_2 \Rightarrow \vec{E}_1 + \vec{E}_2 = Zero$$

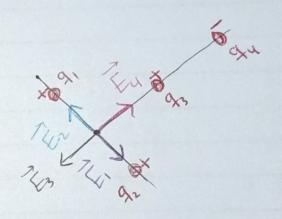
$$E_3 = \frac{k \, 4_3}{J^2} = \frac{9 \times 10^9 \times 3 (1.6 \times 10^{-19})}{(8 \times 10^{-6})^2}$$

$$E_3 = 67.5 \text{ N/C}$$

•
$$E_{4} = \frac{k q_{4}}{(2d)^{2}} = \frac{9 \times 10^{9} (12) (1.6 \times 10^{-19})}{(16 \times 10^{-6})^{2}}$$

$$\Rightarrow$$
 $\vec{E}_1 = Zero$





. The electric field due to a dipole:

> An electric dipole consists of two particles with charges of equal magnitude q but opposite signs, seperated by a small distance d.

•
$$\vec{p}$$
 = Electric dipole moment
 $p = qd$ "from negative to positive"

$$E_{+} = \frac{kq}{r_{+}^{2}} \quad "upward"$$

$$E_{-} = \frac{kq}{r^{2}}$$
 "downward"

$$r_{+} = Z - \frac{d}{2} = Z - \alpha ; \alpha = \frac{d}{2}$$

$$r_{-} = Z + \frac{1}{2} = Z + \alpha$$

$$E = E_{+} - E_{-} = \frac{kq}{(z-\alpha)^{2}} - \frac{kq}{(z+\alpha)^{2}}$$

$$= k9 \left[\frac{1}{(z-a)^2} - \frac{1}{(z+a)^2} \right] = k9 \left[\frac{(z+a)^2 - (z-a)^2}{(z-a)^2 (z+a)^2} \right]$$

$$E = kq \left[\frac{Z^2 + 2aZ + a^2 - Z^2 + 2aZ - a^2}{(Z^2 - a^2)^2} \right] = kq \left[\frac{4aZ}{(Z^2 - a^2)^2} \right]$$

For
$$Z\gg d$$
; $Z\gg a$; $E=kq + aZ=4kqa$

$$Z''$$

$$Z^3$$

we
$$a = \frac{d}{2}$$
; $E = \frac{4kq}{2z^3} = \frac{2kp}{z^3}$

$$E = \bot P y ward'$$
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Z is the distance between the dipole center and the point that we calculated the electric field at

Up here the +qfield dominates. 22-55 Electric dipole V2 0 (12 + (2)2 E(b) = ?? E- PO) By symmetric Ex Concelled 1 cos6 = d/2 Ey+ = K9 (050) $= \frac{K4d}{2[r^2 + (2]^2]^{3/2}}$ Ey+ = Ey- $\vec{E}(P) = -\frac{kqd}{\int r^2 + (\frac{d}{2})^2 \int_{-3/2}^{3/2} \int_{-3/2}^{3/2}$ $r>>d \Rightarrow \vec{E} = - K7d \hat{j}$ Uploaded By: batool Hmaid STUDENTS-HUB.com

3 È due to a continuous charge distribution => Integration 7 = linear charge density C/m

T = surface charge density C/m² P = Volume charge density C/m3

 $dE = \frac{de}{dE}$ $dE = \frac{dq}{r^2} \Rightarrow E = \int dE$

de Jamestion I symmetry allows us to cancel out any of the components. of the fields, to simplify the integration.

[22-13] A non-Conducting rad of length L= 8.15 cm has a charge -q = -4.23 fC uniformly distributed along its length. (a) what is the linear change density of the rod? What are the (b) magnitude and (c) clirection (relative to the positive direction of the Xaxis) of the electric held produced at point Pat distance a = 6.00 cm from the rod? What is the electric field magnitude produced at distance a = 50m by (d) the rod and (e) a particle of charge -9 = -4.23 fC that we use to replace the rod? (At that distance, the rod "looks" like a particle?

(a)
$$\lambda = \frac{9}{L} = \frac{-4.32 \times 10^{-15}}{8.15 \times 10^{-2}} = -5.19 \times 10^{-14} \text{ m}$$

(b)
$$dE = \frac{k}{\lambda} \frac{dq}{\chi^2}$$
; $dq = \lambda dx$

$$dE = k \frac{\lambda}{\lambda} \frac{dx}{\chi^2}$$

"The charge extends from
$$X_1 = \alpha + \delta X_2 = L + \alpha$$
"

$$E = \int k \lambda \frac{dx}{x^2} = k \lambda \int_{x^2}^{L+\alpha} dx = k \lambda \left[-\frac{1}{x} \right]_{\alpha}^{L+\alpha}$$

$$E = k\lambda \left[-\frac{1}{1+a} + \frac{1}{a} \right] = k\lambda \left[-\frac{a+1+a}{a(1+a)} \right]$$

$$E = \frac{k \pi L}{a(L+a)} = \frac{k q}{a(L+a)}$$

$$\vec{E}_{p} = \frac{k}{a} \frac{q}{(L+a)} \hat{l}$$
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$$E_{p} = \frac{k}{a} \frac{9}{(L+a)} \hat{l}$$
use $9 = 4.23 \times 10^{15} \text{C}$

$$A = 6.00 \times 10^{2} \text{m}$$

$$L = 8.15 \times 10^{-2} \text{m}$$
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dq dE

$$\vec{E}_{p} = -\frac{kq}{a(L+a)} = 1.52 \times 10^{-8} \text{ M/c} \hat{c}$$

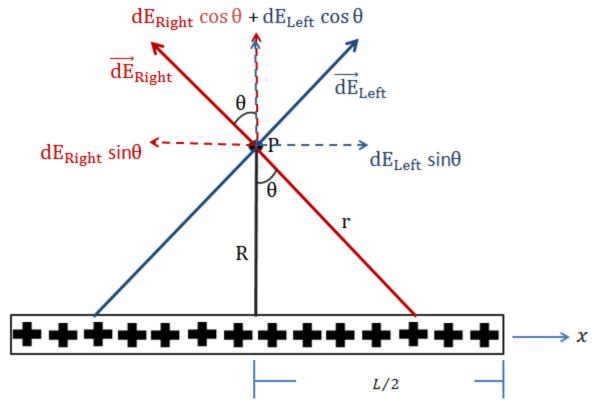
$$E = k \frac{q}{r^2} = \frac{9 \times 10^9 \times 4.23 \times 10^{-15}}{(50)^2}$$

$$a(L+a) = a^2 \implies \text{ The rod treats as a particle.}$$

$$E = \frac{kq}{\alpha^2}$$

50m -9 = X Problem 22-10: Positive charge (q = $9.25 \, \text{pC} = 9.25 \times 10^{-12} \, \text{C}$) is spread uniformly along a thin non-conducting rod of length (L = $16.0 \, \text{cm} = 0.16 \, \text{m}$). What is the electric field produced at point P, at distance (R = $6.00 \, \text{cm} = 0.06 \, \text{m}$) from the rod along its perpendicular bisector?

$$\overrightarrow{dE} = \frac{k \ dq}{r^2} \hat{r}$$



 $dE_{Left} = dE_{Right}$ (both have same magnitude)

 $dE_x = -dE_{Right} \sin\theta \ \hat{\imath} + dE_{Left} \sin\theta \ \hat{\imath} = zero.$ (by symmetric)

$$\vec{E} = \int dE_y = \int dE \cos \theta \hat{j} = \int \frac{k \, dq}{r^2} \cos \theta \hat{j}$$

Using $q = \lambda x$; linear charge density. $dq = \lambda dx$

$$r^2 = (R^2 + x^2)$$
 and $\cos \theta = \frac{R}{r} = \frac{R}{(R^2 + x^2)^{1/2}}$

$$\vec{E} = \int \frac{k \, dq}{r^2} \cos \theta \hat{j} = \int_{-L/2}^{L/2} \frac{k \, \lambda \, dx}{(R^2 + x^2)} \frac{R}{(R^2 + x^2)^{1/2}} \hat{j}$$

$$= k \, \lambda \, R \, \hat{j} \int_{-L/2}^{L/2} \frac{dx}{(R^2 + x^2)^{3/2}} = 2 \, k \, \lambda \, R \, \hat{j} \int_{0}^{L/2} \frac{dx}{(R^2 + x^2)^{3/2}}$$

$$\begin{cases} take \tan \theta = \frac{x}{R}, x = R \tan \theta \to dx = R \sec^2 \theta \, d\theta \\ (R^2 + x^2)^{3/2} = (R^2 + R^2 \tan^2 \theta)^{3/2} = (R^2 \sec^2 \theta)^{3/2} = R^3 \sec^3 \theta \end{cases}$$

$$\vec{E} = 2 \, k \, \lambda \, R \, \hat{j} \int \frac{R \sec^2 \theta \, d\theta}{R^3 \sec^3 \theta} = \frac{2 \, k \, \lambda}{R} \hat{j} \int \frac{d\theta}{\sec \theta} = \frac{2 \, k \, \lambda}{R} \hat{j} \int \cos \theta \, d\theta$$

$$= \frac{2 \, k \, \lambda}{R} \hat{j} \sin \theta$$

Use $\sin \theta = \frac{x}{(R^2 + x^2)^{1/2}}$

$$\Rightarrow \vec{E} = \left[\frac{2 k \lambda}{R} \frac{x}{(R^2 + x^2)^{1/2}} \hat{j} \right]_0^{L/2} = \frac{k}{R} \frac{\lambda L}{(R^2 + (L/2)^2)^{1/2}} \hat{j}$$

Substituted q = 9.25 pC = 9.25 \times 10⁻¹² C = λ L, L = 16.0 cm = 0.16 m and R = 6.00 cm = 0.06 m.

$$\vec{E} = 13.86 N/C \hat{\jmath}$$

· È due to a ring of uniform positive charge

⇒ E at point on a perpendicular axis to the ring plane.

$$dE = k \frac{\partial q}{r^2} = k \frac{\lambda}{r^2} \frac{ds}{R^2 + Z^2}$$

By the symmetry the components perpendiculu to the Z-cixis cancel.

$$\frac{E_{\text{ring}}}{R^2 + Z^2} = \int dE \cos \Theta = \frac{k \pi ds}{R^2 + Z^2} \frac{Z}{(Z^2 + R^2)^2}$$

$$= \frac{k Z \lambda}{(Z^2 + R^2)^{3/2}} \int_{0}^{2\pi R} ds$$

$$E = k \pi Z 2\pi R$$

$$(Z^2 + R^2)^{3/2}$$

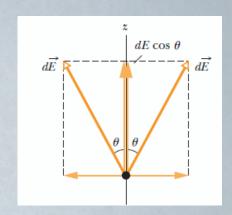
total charge of the ring $q = \lambda(2\pi R)$

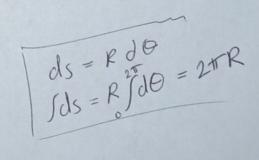
$$E = \frac{k q Z}{(Z^2 + R^2)^{3/2}}$$

$$\vec{E} = + \frac{kqZ}{(Z^2 + R^2)^{3/2}} \hat{k}$$

$$Z\gg R \Rightarrow E = \frac{kq}{Z^2}$$
 "like charged point particle"

 $\frac{z}{\theta}$





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- Electric field due to a charged disk
- ⇒ A disk of radius R and uniform positive charge

. Take a ring on the disk has radius r; r < R, then integrate from the center of the disk to its rim $\rightarrow (0 \rightarrow R)$

$$dE = \frac{d9}{4\pi\epsilon_0} \frac{Z}{(Z^2 + r^2)^{3/2}} \left(\frac{\text{in the positive}}{\text{direction of the}} \right)$$
use $dQ = T I \Lambda$

use dq = TdA = T (2Trdr)

$$E = \int dE = \frac{\nabla Z}{4E_0} \int_{0}^{R} (Z^2 + r^2)^{-3/2} 2r dr$$

Use
$$\int X^{m} dX = \frac{X^{m+1}}{m+1} \Rightarrow \begin{cases} X = Z^{2} + r^{2} \\ m = -3/2 \\ dX = 2rdr \end{cases}$$

$$E = \frac{\nabla Z}{46} \left[\frac{(Z^2 + r^2)^{-\frac{1}{2}}}{-\frac{1}{2}} \right]_0^{-\frac{1}{2}}$$

$$= \frac{\nabla Z}{46} \left[\frac{(Z^2 + R^2)^{-\frac{1}{2}}}{-\frac{1}{2}} - \frac{Z^{-1}}{2} \right]$$

$$E = \frac{\nabla}{2\epsilon_0} \left[1 - \frac{7}{\sqrt{2^2 + R^2}} \right]$$

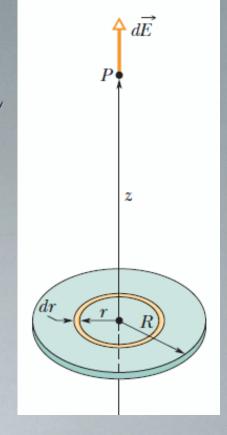
If the electric field due to acharged chisk at point on the central

$$E = \frac{1}{2\epsilon_0} \left[1 - \frac{Z}{Z^2 + R^2} \right]$$

· R -> w ; infinite sheet STUDENTS-HUB.com.

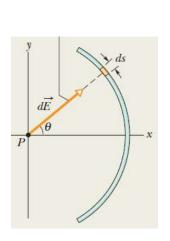
1. Positive charged disk => Electric I hield lines trands away from the disk $E = \frac{Z}{2E_0} \left[1 - \frac{Z}{Z^2 + R^2} \right]$ o negative charged disk \Rightarrow Electric

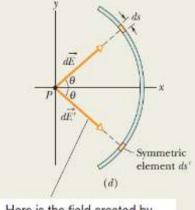
I held lines tends toward the disk

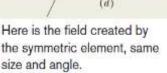


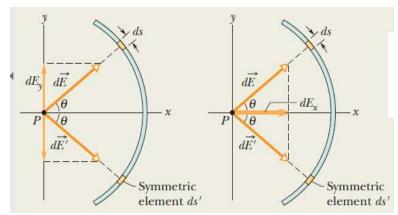
Sample Problem 22.03 Electric field of a charged circular rod

Figure 22-13a shows a plastic rod with a uniform charge -Q. It is bent in a 120° circular arc of radius r and symmetrically paced across an x axis with the origin at the center of curvature P of the rod. In terms of Q and r, what is the electric field \vec{E} due to the rod at point P?









$$dE_x = dE \cos \theta = \frac{1}{4\pi\epsilon_0} \frac{\lambda}{r^2} \cos \theta \, ds.$$

$$E = \int dE_x = \int_{-60^\circ}^{60^\circ} \frac{1}{4\pi\varepsilon_0} \frac{\lambda}{r^2} \cos\theta \, r \, d\theta$$

$$= \frac{\lambda}{4\pi\varepsilon_0 r} \int_{-60^\circ}^{60^\circ} \cos\theta \, d\theta = \frac{\lambda}{4\pi\varepsilon_0 r} \left[\sin\theta \right]_{-60^\circ}^{60^\circ}$$

$$= \frac{\lambda}{4\pi\varepsilon_0 r} \left[\sin 60^\circ - \sin(-60^\circ) \right]$$

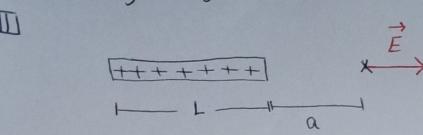
$$=\frac{1.73\lambda}{4\pi\varepsilon_0 r}.$$

$$\lambda = \frac{\text{charge}}{\text{length}} = \frac{Q}{2\pi r/3} = \frac{0.477Q}{r}.$$

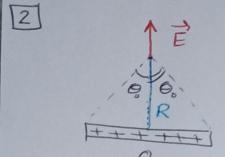
$$E = \frac{(1.73)(0.477Q)}{4\pi\varepsilon_0 r^2}$$
$$= \frac{0.83Q}{4\pi\varepsilon_0 r^2}.$$

$$\vec{E} = \frac{0.83Q}{4\pi\varepsilon_0 r^2}\hat{\mathbf{i}}.$$

· Uniformly charged rod



$$E = \frac{9}{4\pi\epsilon_0 a(L+a)}$$



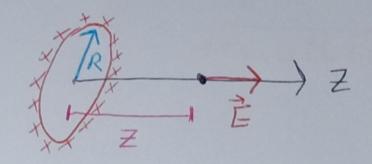
$$\boxed{3}$$
 $\stackrel{?}{\to}$ due to an infinite line of charge very Long wire $L \to \infty$ $\Theta_0 \to \pi/2$

$$E = \frac{1}{2\pi \epsilon_R} \sin(\pi/2)$$

$$/E = \frac{\lambda}{2\pi GR}$$
 For very long line of charge $/$ L>>>> R

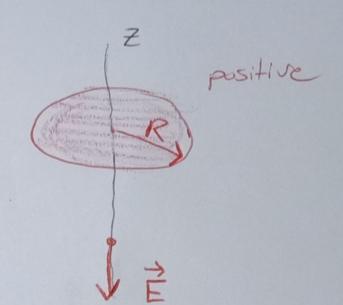
[4] Uniformly charged circular arc

$$E = \frac{9Z}{4\pi\epsilon_{o}(Z^{2}+R^{2})^{3/2}}$$



[6] Uniformly charged disk

$$E = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{Z}{\sqrt{Z^2 + R^2}} \right]$$



. A Point charge in an Electric field

If a particle with charge q is placed in an external electric field E, on

electrostatic force F acts on the particle

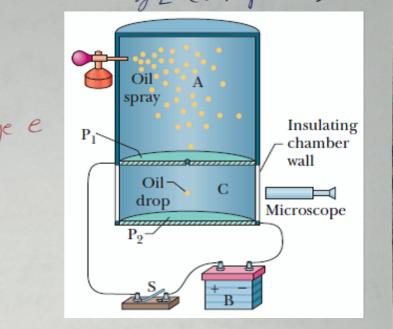
$$\overrightarrow{F} = \overrightarrow{q} \overrightarrow{E}$$

. Millikan's oil-drop experiment

 \Rightarrow if q is positive $\rightarrow \overrightarrow{F}$ in the same direction \overrightarrow{gE} (Parallel)

if q is negative $\rightarrow \overrightarrow{F}$ in the Opposite direction \overrightarrow{fE} (anti-parallel)

For measuring the elementary charge e



· A negatively charged oil drop is suspended between the plates

Suspended between the plates

The oil drop is at rest under the influence of two forces => \ Fe, Upward

Foildrop = Zero => qE = mg

example In Millikan's experiment, an oil drop of radius 1,64 Mm and density 0.851 g/cm3 is suspended in champer C of higure (22-16) when a downward electric held of 1.92 × 105 N/C is applied. Find the charge on the drop in terms of e? The oil drop is suspended $9 = \frac{mg}{E}$, $m = PV = P(\frac{4}{3}\pi r^3) = 851 \frac{kg}{m^3} (\frac{4}{3}\pi) \frac{1.64 \times 10^6}{m^3}$ $m = 1.572 \times 10^{-14} kg$ F= qE+mg= Zero $9 = \frac{mg}{E} = \frac{(1.572 \times 10^{-14})(9.8)}{1.92 \times 10^{5}} = 8.02 \times 10^{-19} \text{C}$ $n = \frac{q}{e} = \frac{8.02 \times 10^{-19} \text{ C}}{1.6 \times 10^{-19} \text{ C}} \qquad \boxed{n = 51} \quad q = 5e$ [22-60 | An alpha particle (the nucleus of a helium atom) has a mass of 6.64 X10-27 kg and a charge of + 2e. What are the (a) magnitude (b) and direction of the electric field that will balance the gravitational force on the particle? (c) if the beld magnitude is then doubled, what is the magnitude of the particle's acceleration? $m = 6.64 \times 10^{-27} \text{kg}$ An alpha particle $\Rightarrow q = +2e = +3.2 \times 10^{-19} \text{C}$ E must be upward $E = mg/q = 6.64 \times 10^{-27} (9.8)/3.2 \times 10^{-19} = 2.03 \times 10^{7} \text{ N/c}$ upward (c) E is doubled, $E = 4.06 \times 10^{7} \text{ N/C}$ upward Fret = $9\vec{E} + m\vec{g} \iff m\alpha = 9\vec{E} - mg$ $\alpha = \frac{9\vec{E} - mg}{m} = \frac{(3.2 \times 10^{-19})(4.06 \times 10^{-7}) - (6.64 \times 10^{-27})(9.8) mg}{6.64 \times 10^{-27}}$ DENTS-HUB. com 9 77

STUDENTS-HUB.com 9.77 m/s² upward Uploaded By: batool Hmaid

122-38 | An electron enters a region of uniform electric field with an initial velocity of 30 km/s in the same direction as the electric field, which has magnitude E = 50N/C. (a) What is the speed of the electron 1.5 ns after entering this region? How far does the electron travel during the 1.5 ns interval?

$$\vec{v}_i = \vec{v}_i + \vec$$

$$\vec{v}_{i} = \vec{v}_{i} + \vec{\alpha} t$$

$$\vec{v}_{i} = +30 \text{ km/s}$$

$$\vec{v}_{i} = 30 \text{ km/s}$$

$$\overrightarrow{E} = +50 \text{ N/C } \widehat{c} \text{ (right ward)}$$

$$\overrightarrow{F} = 9 \overrightarrow{E} \iff m_e \overrightarrow{a} = -e \overrightarrow{E} \iff |a_X = -e \overrightarrow{E}|$$

$$a_x = -\frac{eE}{me} = \frac{(-1.6 \times 10^{19} \text{ c})(50 \text{ d})}{9.11 \times 10^{-31} \text{ kg}} = \frac{8.78 \times 10^{12} \text{ m}}{52}$$

$$\frac{1}{3} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times 10^{3} \text{ m}}{1.5 \times 10^{3} \text{ m}} = \frac{1.64 \times$$

(b)
$$\Delta X = ?$$
 $\Delta X = \frac{1}{12} \times 1 + \frac{1}{2} \cos^2 \frac{1}{2}$
 $= (3 \times 10^4)(1.5 \times 10^{-9}) + \frac{1}{2} (-8.78 \times 10^{12})(1.5 \times 10^{-9})^2$
 $\Delta X = 3.51 \times 10^{-5} \text{m}$

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· A dipole in An electric field

$$\vec{r} = \vec{r} \times \vec{F}$$

$$\vec{r}_{+} = -\frac{1}{2} \cancel{q} E \sin \theta \text{ "clock wise"}$$

$$\vec{r}_{-} = -\frac{1}{2} \cancel{q} E \sin \theta \text{ "clock wise"}$$

$$\vec{r}_{-} = -\frac{1}{2} \cancel{q} E \sin \theta \text{ "clock wise"}$$

$$\vec{r}_{-} = -\frac{1}{2} \cancel{q} E \sin \theta \text{ "clock wise"}$$

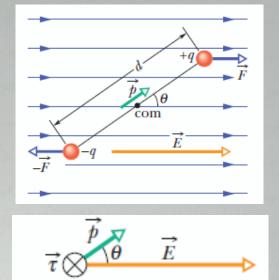
$$= - 4d E \sin 0$$

$$= - 7d E \sin 0$$

$$= -$$

H G

P = electric clipale moment P=qd



• A potential energy U is associated with the crientedion of the clipple moment in the field $|U = -\vec{p} \cdot \vec{E}|$

$$V = \int PE (greatest \ value), \ \vec{P} \ and \ \vec{E} \ antiparallel (\Theta = 180°)$$

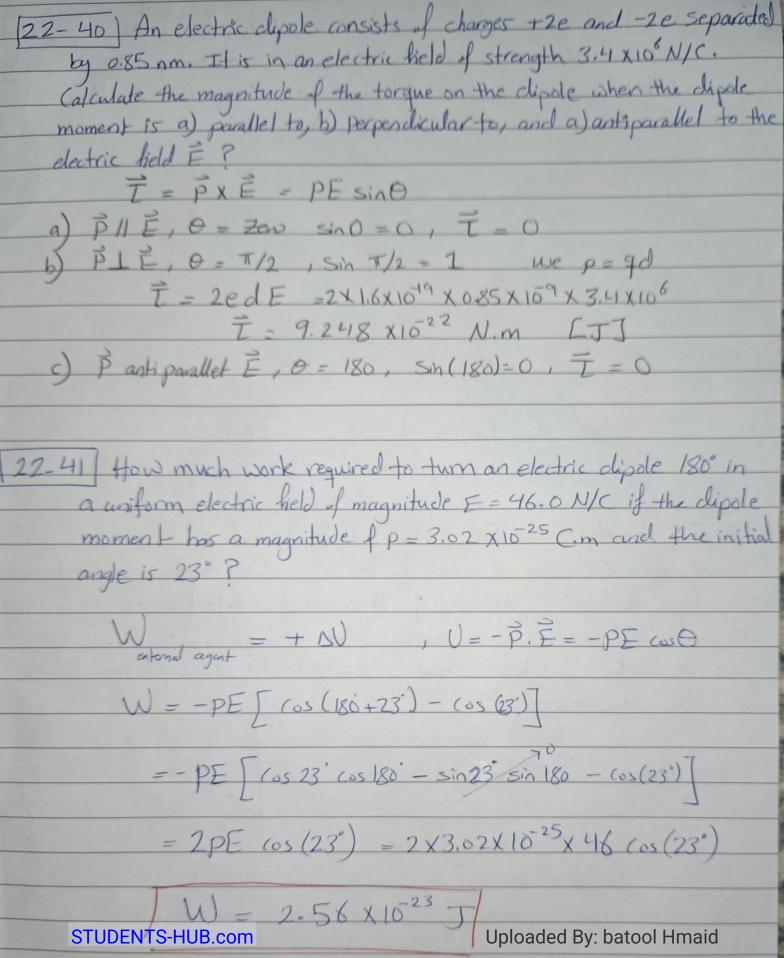
$$Zero, \ \vec{P} \ and \ \vec{E} \ perpendicular (\Theta = 772)$$

$$-PE (Least \ value), \ \vec{P} \ and \ \vec{E} \ parallel (\Theta = 0°)$$

• If the clipale orientation changes \Rightarrow The work done by the electric field \Rightarrow $W_E = -\Delta U$

if the change in the orientation is due to an external agent Wexternal agent = + DV

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Products of Vectors

Let \hat{i} , \hat{j} , and \hat{k} be unit vectors in the x, y, and z directions. Then

$$\begin{split} \hat{\mathbf{i}} \cdot \hat{\mathbf{i}} &= \hat{\mathbf{j}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{k}} = 1, \quad \hat{\mathbf{i}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{j}} \cdot \hat{\mathbf{k}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{i}} = 0, \\ \hat{\mathbf{i}} \times \hat{\mathbf{i}} &= \hat{\mathbf{j}} \times \hat{\mathbf{j}} = \hat{\mathbf{k}} \times \hat{\mathbf{k}} = 0, \\ \hat{\mathbf{i}} \times \hat{\mathbf{j}} &= \hat{\mathbf{k}}, \quad \hat{\mathbf{j}} \times \hat{\mathbf{k}} = \hat{\mathbf{i}}, \quad \hat{\mathbf{k}} \times \hat{\mathbf{i}} = \hat{\mathbf{j}} \end{split}$$

Any vector \vec{a} with components a_x , a_y , and a_z along the x, y, and z axes can be written as

$$\vec{a} = a_x \hat{\mathbf{i}} + a_y \hat{\mathbf{j}} + a_z \hat{\mathbf{k}}.$$

Let \vec{a} , \vec{b} , and \vec{c} be arbitrary vectors with magnitudes a, b, and c. Then

$$\vec{a} \times (\vec{b} + \vec{c}) = (\vec{a} \times \vec{b}) + (\vec{a} \times \vec{c})$$

 $(s\vec{a}) \times \vec{b} = \vec{a} \times (s\vec{b}) = s(\vec{a} \times \vec{b})$ (s = a scalar).

Let θ be the smaller of the two angles between \vec{a} and \vec{b} . Then

$$\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{a} = a_x b_x + a_y b_y + a_z b_z = ab \cos \theta$$

$$\vec{a} \times \vec{b} = -\vec{b} \times \vec{a} = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

$$= \hat{\mathbf{i}} \begin{vmatrix} a_y & a_z \\ b_y & b_z \end{vmatrix} - \hat{\mathbf{j}} \begin{vmatrix} a_x & a_z \\ b_x & b_z \end{vmatrix} + \hat{\mathbf{k}} \begin{vmatrix} a_x & a_y \\ b_x & b_y \end{vmatrix}$$

$$= (a_y b_z - b_y a_z) \hat{\mathbf{i}} + (a_z b_x - b_z a_x) \hat{\mathbf{j}}$$

$$+ (a_x b_y - b_x a_y) \hat{\mathbf{k}}$$

$$|\vec{a} \times \vec{b}| = ab \sin \theta$$

$$\vec{a} \cdot (\vec{b} \times \vec{c}) = \vec{b} \cdot (\vec{c} \times \vec{a}) = \vec{c} \cdot (\vec{a} \times \vec{b})$$
$$\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{c})\vec{b} - (\vec{a} \cdot \vec{b})\vec{c}$$

