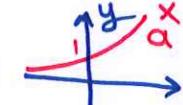
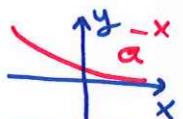


Recall that  $f(x) = a^x$ ,  $a > 1$  represents exponential growth



$f(x) = a^{-x}$ ,  $a > 1$  = decay



Exp solve the exponential equation

$$\textcircled{1} \quad \frac{4}{4} (25)^{2x} = \frac{20}{4} \Rightarrow (25)^{2x} = 5 \quad \begin{matrix} \text{or} \\ (5^2)^{2x} = 5 \end{matrix} \quad \begin{matrix} \ln(25)^{2x} = \ln 5 \\ 2x \ln 25 = \ln 5 \\ 2x \ln 5^2 = \ln 5 \end{matrix}$$

$$\begin{matrix} \frac{4x}{5} = \frac{1}{5} \\ 4x = 1 \\ x = \frac{1}{4} \end{matrix} \quad \begin{matrix} 4x = 1 \\ x = \frac{1}{4} \end{matrix}$$

$$\textcircled{2} \quad 8^{3x} = 216 \Rightarrow 8^{3x} = (8)(27) \Rightarrow \ln 8^{3x} = \ln(8)(27)$$

$$\Rightarrow 3x \ln 8 = \ln 8 + \ln 27$$

$$3x \ln 2^3 = \ln 2^3 + \ln 3^3$$

$$\frac{9x \ln 2}{9 \ln 2} = \frac{3 \ln 2 + 3 \ln 3}{9 \ln 2}$$

$$x = \frac{1}{3} + \frac{1}{3} \frac{\ln 3}{\ln 2}$$

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$$\textcircled{3} \quad 25000 = 10,000 5^{2x} \Rightarrow \frac{25000}{10000} = 5^{2x} \Rightarrow 5^{2x} = \frac{5}{2}$$

$$5^{2x} = \frac{5}{2} \Rightarrow \ln 5^{2x} = \ln \frac{5}{2} \Rightarrow \frac{2x \ln 5}{2 \ln 5} = \frac{\ln 5 - \ln 2}{2 \ln 5}$$

$$x = \frac{\ln 5}{2 \ln 5} - \frac{\ln 2}{2 \ln 5}$$

$$= \frac{1}{2} - \frac{\ln 2}{2 \ln 5}$$

(4)

$$\log_5(x+2) = 2 \Rightarrow 5^2 = x+2$$

$$25 = x+2$$

23 = x

13 100

$$(5) \ln(x+2) + \ln x = \ln(x+12) \rightarrow x^2 + x - 12 = 0$$

$$\ln x(x+2) = \ln(x+12) \quad (x+4)(x-3) = 0$$

$$x(x+2) = x+12$$

$$x^2 + 2x = x+12$$

$$x^2 + x = 12$$

Either  $x+4=0 \Rightarrow x=-4 \times$   
or  $x-3=0 \Rightarrow \boxed{x=3} \checkmark$

(6)

$$\log_4 x - \log_4(x+3) = \log_4(x-2)$$

$$\log_4 \frac{x}{x+3} = \log_4(x-2)$$

$$\frac{x}{x+3} = x-2$$

$$x = (x-2)(x+3)$$

$$x = x^2 + 3x - 2x - 6$$

$$x^2 + x - 6 = x$$

$$x^2 - 6 = 0$$

$$x^2 = 6$$

$$x = \pm \sqrt{6}$$

$$\boxed{x = \sqrt{6}} \checkmark \text{ but } x = -\sqrt{6}$$

X rejected

since  $x > 0$

(7)

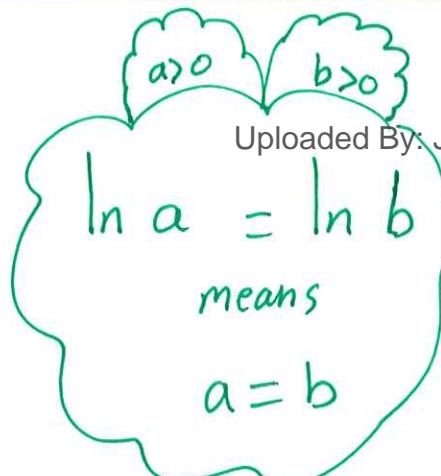
$$\ln x - \ln 2 = 3$$

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$$\ln \frac{x}{2} = \ln e^3$$

$$\frac{x}{2} = e^3$$

$x = 2e^3$



Exp Suppose the demand for commodity  $q$  is given by

14 101

$$P = 40 \cdot 2^{\frac{-q}{2}}$$
 where  $P$  is the price in dollars

(1) At what price per unit will the demand equal 4 units?

$$\text{when } q=4 \Rightarrow P = 40 \cdot 2^{\frac{-4}{2}} = 40 \cdot 2^{-2} = 40 \cdot \frac{1}{4} = \frac{40}{4}$$
$$\Rightarrow P = 10 \text{ dollars}$$

(2) How many units will be demanded if the price is \$20

$$20 = 40 \cdot 2^{\frac{-q}{2}} \Rightarrow \frac{20}{40} = 2^{\frac{-q}{2}} \Rightarrow \frac{1}{2} = 2^{\frac{-q}{2}}$$

$$\ln \frac{1}{2} = \ln 2^{\frac{-q}{2}} \Rightarrow \ln 1 - \ln 2 = -\frac{q}{2} \ln 2$$

$$0 - \ln 2 = -\frac{q}{2} \ln 2$$

$$\frac{-\ln 2}{\ln 2} = -\frac{q}{2} \Rightarrow q = 2$$

Exp Suppose the demand function for a commodity is given by

$$P = 100 e^{-\frac{x}{10}}$$
 where  $p$  is the price per unit when  $x$  units are sold

(1) Find the total revenue

$$R(x) = (P)(x) = \left(100 e^{-\frac{x}{10}}\right)x = 100x e^{-\frac{x}{10}}$$

(2) Find the total revenue if 30 units were demanded and supplied

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$$R(30) = 100 (30) e^{-\frac{30}{10}}$$

$$= 3000 e^{-3}$$

$$\approx (3000)(0.0498)$$

$$= 149.4 \text{ dollars}$$