

$$\begin{aligned}
 1. \quad a. \quad & AB + \bar{A}B + \bar{B}\bar{C} + \bar{B}C \\
 &= B(\underbrace{A+\bar{A}}_1) + \bar{B}(\underbrace{\bar{C}+C}_1) \\
 &= B + \bar{B} = 1 \quad (\text{a constant})
 \end{aligned}$$

$$\begin{aligned}
 b. \quad & \bar{C}D + \bar{C}B\bar{D} + BC + B\bar{C}A \\
 &= \bar{C}[D + \bar{D}B] + B[C + \bar{C}A] \\
 &= \bar{C}[(\underbrace{D+\bar{D}}_1)(D+B)] + B[(\underbrace{C+\bar{C}}_1)(C+A)] \\
 &= \bar{C}(D+B) + B(C+A) \\
 &= \bar{C}D + \bar{C}B + CB + AB \\
 &= \bar{C}D + B[\underbrace{C+\bar{C}+A}_1] \\
 &= \bar{C}D + B[1+A] = B + \bar{C}D \quad (3 \text{ literals})
 \end{aligned}$$

$$\begin{aligned}
 c. \quad & (\overline{x+z} + z)Y + X \\
 &= (\bar{x}\bar{z} + z)Y + X \\
 &= (z + \bar{z}\bar{x})Y + X = (\underbrace{z+\bar{z}}_1)(z+\bar{x})Y + X \\
 &= (z+\bar{x})Y + X \\
 &= YZ + \bar{x}Y + X \\
 &= YZ + (\underbrace{x+\bar{x}}_1) \cdot (x+Y) \\
 &= X + Y + YZ = X + Y(\underbrace{1+Z}_1) \\
 &= X + Y \quad (2 \text{ literals})
 \end{aligned}$$

$$\begin{aligned}
 d. \quad & ABC + A\bar{B}C + A\bar{B}\bar{C} \\
 &= ABC + A\bar{B}(\underbrace{C+\bar{C}}_1) \\
 &= A[\bar{B} + BC] \\
 &= A(\underbrace{\bar{B}+B}_1)(\bar{B}+C) = A[\bar{B}+C] \quad (3 \text{ literals})
 \end{aligned}$$

$$\begin{aligned} e. & \bar{x}\bar{y} + yz + \bar{x}y\bar{z} \\ &= \bar{x}\bar{y} + y[z + \bar{z}\bar{x}] \\ &= \bar{x}\bar{y} + y[\underbrace{(z + \bar{z})}_{=1}(\bar{z} + \bar{x})] \\ &= \bar{x}\bar{y} + yz + y\bar{x} \\ &= \bar{x}\bar{y} + \bar{x}y + yz \\ &= \bar{x}(\bar{y} + y) + yz = \bar{x} + yz \quad (3 \text{ literals}) \end{aligned}$$

f.  $(b' + c)(b' + c') = b' + b'c' + b'c + \underbrace{cc'}_0$   
 $= b' [1 + c' + c]$   
 $= b' \underbrace{1}_{1} \quad (1 \text{ literal})$

$$2. a. (\overline{A+B}) \cdot (\overline{\overline{A} \overline{B}}) = (\overline{A} \cdot \overline{B}) \cdot (A+B) \\ = \underbrace{\overline{A} A \overline{B}}_0 + \underbrace{\overline{A} \overline{B} B}_0 = 0$$

$$\begin{aligned} \text{b. } (x+y)(x+\bar{y}) + xy z + \bar{x} y + x y \bar{z} \\ = \cancel{x\bar{x}} + x y + x \bar{y} + \cancel{y\bar{y}} + x y z + \bar{x} y + x y \bar{z} \\ = x \underbrace{[1 + y + \bar{y}]}_1 + \bar{x} y + x y \underbrace{(z + \bar{z})}_1 \\ = x + y \underbrace{(x + \bar{x})}_1 = x + y \end{aligned}$$

$$\begin{aligned} \text{c. } & \bar{w}x\bar{z} + xw + \bar{w}x\bar{y}z + x\bar{w}yz \\ &= x[\bar{w}\bar{z} + w + \bar{w}\bar{y}z + \bar{w}yz] \\ &= x[w + \bar{w}\bar{z} + \bar{w}z(\underline{y + \bar{y}})] \\ &= x[(\underline{w + \bar{w}})(w + \bar{z}) + \bar{w}z] \\ &= x[w + \bar{w}z + \bar{z}] \\ &= x[(\underline{w + \bar{w}})(w + z) + \bar{z}] \\ &= x[w + \underline{z + \bar{z}}] \\ &= x[\underline{1 + w}] \\ &= x \end{aligned}$$

2, contd.

$$d. \quad CD + (\bar{A}\bar{B})C + (A+B)D$$

$$\text{Let } A+B=W \rightarrow \bar{A}\bar{B} = \bar{W}$$

$$\begin{aligned} CD + \bar{W}C + WD &= \bar{W}C + WD \\ &= \bar{A}\bar{B}C + (A+B)D \\ &= \bar{A}\bar{B}C + AD + BD \end{aligned}$$

$$3. \quad F = (AB' + C'D)(DE' + W)$$

(i) Using De Morgan's

$$\bar{F} = (AB' + C'D) \cdot (DE' + W)$$

$$= \overline{(AB' + C'D)} + \overline{(DE' + W)}$$

$$= \overline{AB'} \cdot \overline{C'D} + \overline{DE'} \cdot \overline{W}$$

$$= (A' + B)(C + D') + (D' + E)W'$$

$$= A'C + BC + A'D' + BD' + D'W' + EW' \quad (\text{SOP}) \quad \textcircled{1}$$

(ii) Using Duality

$$F_{\text{dual}} = [(A + B')(C' + D)] + [(D + E')(W)]$$

$$= AC' + B'C' + AD + B'D + DW + E'W$$

$$\bar{F} = F_{\text{dual}}, = A'C + BC + A'D' + BD' + D'W' + EW'$$

with literals complemented

= expression in ① above ✓

$$4. F = EW' + (AB')(C' + D)$$

$$F = \overline{\overline{F}} = \overline{EW' + AB'(C' + D)}$$

$$= \overline{EW' \cdot AB'(C' + D)}$$

a. Using AND, NOT gates:

$$C' + D = \overline{C \cdot D'}$$

OR = NOT-AND-NOT

$$F = \overline{EW' \cdot (AB') \cdot \overline{C \cdot D'}}$$

b. Using OR, NOT gates:

$$F = \overline{EW' \cdot AB'(C' + D)}$$

$$= \overline{(E' + W) \cdot [AB' + (C' + D)]}$$

$$= \overline{(E' + W) \cdot [(A' + B) + (C' + D)]}$$

$$= \overline{(E' + W) + [(A' + B) + (C' + D)]}$$

$$5. a. F = (A + \overline{B})C$$

$$\overline{F} = \overline{(A + \overline{B}) \cdot C} = \overline{(A + \overline{B})} + \overline{C}$$

$$= \overline{A}B + \overline{C}$$

b.

i.

A	B	C	$F = AC + \overline{B}C$	$\overline{F} = \overline{A}B + \overline{C}$
0	0	0		1
0	0	1	1	
0	1	0		1
0	1	1		1
1	0	0		1
1	0	1	1	
1	1	0		1
1	1	1	1	

From the truth table

$\overline{F}$  is the complement of  $F$  ✓

5 b ii.  $F\bar{F} = [(A+\bar{B})C] [\bar{A}B+\bar{C}]$   
 $= [AC + \bar{B}C] [\bar{A}B + \bar{C}]$   
 $= \underbrace{AC\bar{A}B}_0 + \underbrace{\bar{B}C\bar{A}B}_0 + \underbrace{AC\bar{C}}_0 + \underbrace{\bar{B}C\bar{C}}_0$   
 $= 0 \quad \checkmark$

$F+\bar{F} = (A+\bar{B})C + \bar{A}B + \bar{C}$   
 $= AC + \bar{B}C + \bar{A}B + \bar{C}$   
 $= \bar{C} + AC + \bar{B}C + \bar{A}B$   
 $= (\bar{C}+C)(\bar{C}+A) + \bar{B}C + \bar{A}B$   
 $= \bar{C} + \bar{B}C + A + \bar{A}B$   
 $= (\bar{C}+C)(\bar{C}+\bar{B}) + (A+\bar{A})(A+B)$   
 $= \bar{C} + \bar{B} + B + A$   
 $= 1 + A + \bar{C} = 1 \quad \checkmark$

6.  $(A\bar{C} + BA)(C + A\bar{B})$

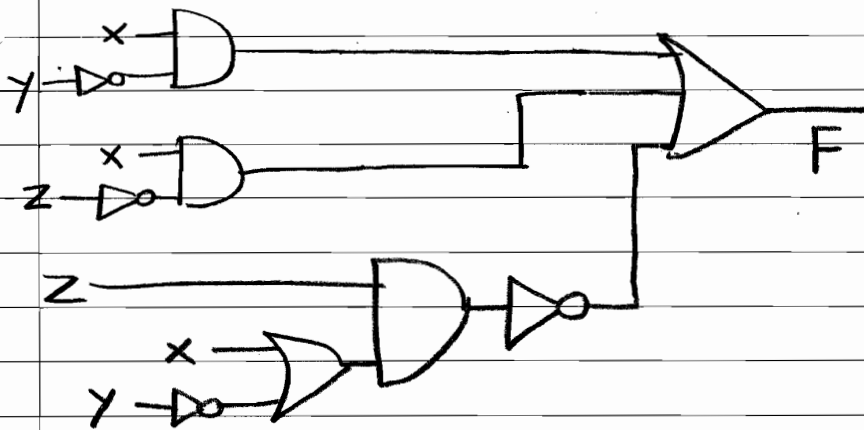
Dual:

$[(A+\bar{C}).(B+A)] + C.(A+\bar{B})$

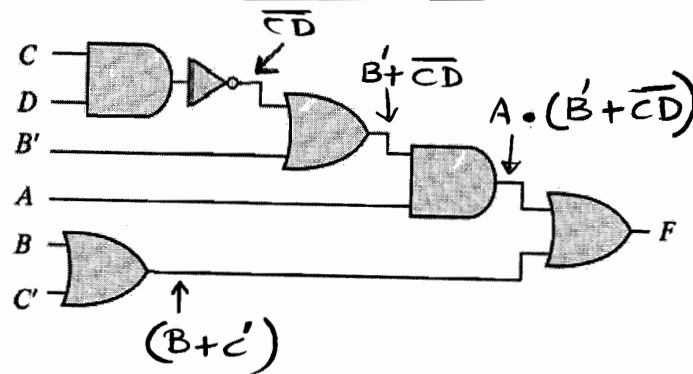
7.  $F(x,y,z) = xy' + xz' + z(x+y')$

$x$	$y$	$z$	$\downarrow$ $xy'$	$\downarrow$ $xz'$	$(x+y')$	$\downarrow$ $z(x+y)$	$\downarrow$ $\overline{z(x+y)}$	$F$
0	0	0			1		1	1
0	0	1			1	1		0
0	1	0					1	1
0	1	1					1	1
1	0	0	1	1	1		1	1
1	0	1	1		1	1		1
1	1	0		1	1		1	1
1	1	1			1	1		0

H2-8



8.



$$F = A \cdot (B' + \overline{CD}) + (B + C')$$

$$F(A, B, C, D) = B + C' + A \cdot (B' + \overline{CD})$$

$$F(1, 0, 1, 1) = 0 + 0 + 1 \cdot (1 + \overline{1 \cdot 1}) = 1 \cdot 1 = 1$$