

Ch1 - Discussion

①

① Find D and R :

a) $f(x) = \frac{1}{\sqrt{x}}$

D: $x > 0 \Rightarrow D = (0, \infty)$
 $R = (0, \infty)$

$x=1 \Rightarrow f(1) = 1 \in \mathbb{R}$

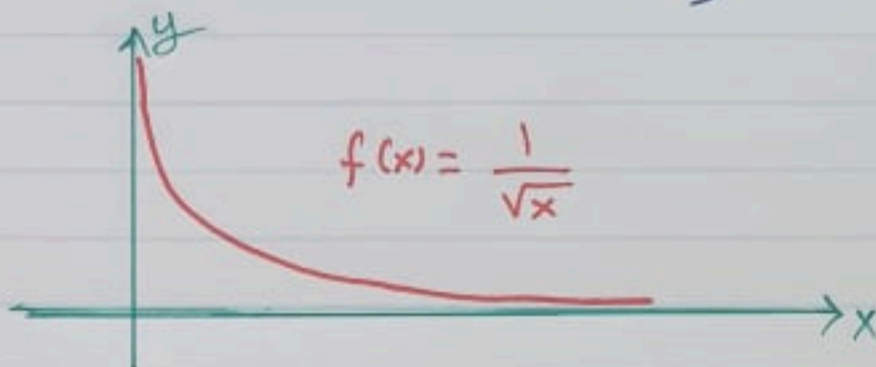
$x = \frac{1}{4} \Rightarrow f(\frac{1}{4}) = 2 \in \mathbb{R}$, $x=4 \Rightarrow f(4) = \frac{1}{2} \in \mathbb{R}$

$x = \frac{1}{16} \Rightarrow f(\frac{1}{16}) = 4 \in \mathbb{R}$, $x=16 \Rightarrow f(16) = \frac{1}{4} \in \mathbb{R}$

\vdots

\vdots

$x=25 \Rightarrow f(25) = \frac{1}{5} \in \mathbb{R}$



e) $g(x) = \frac{1}{x^2}$

D: $\mathbb{R} \setminus \{0\} = (-\infty, 0) \cup (0, \infty)$
 $x^2 \neq 0$
 $x \neq 0$

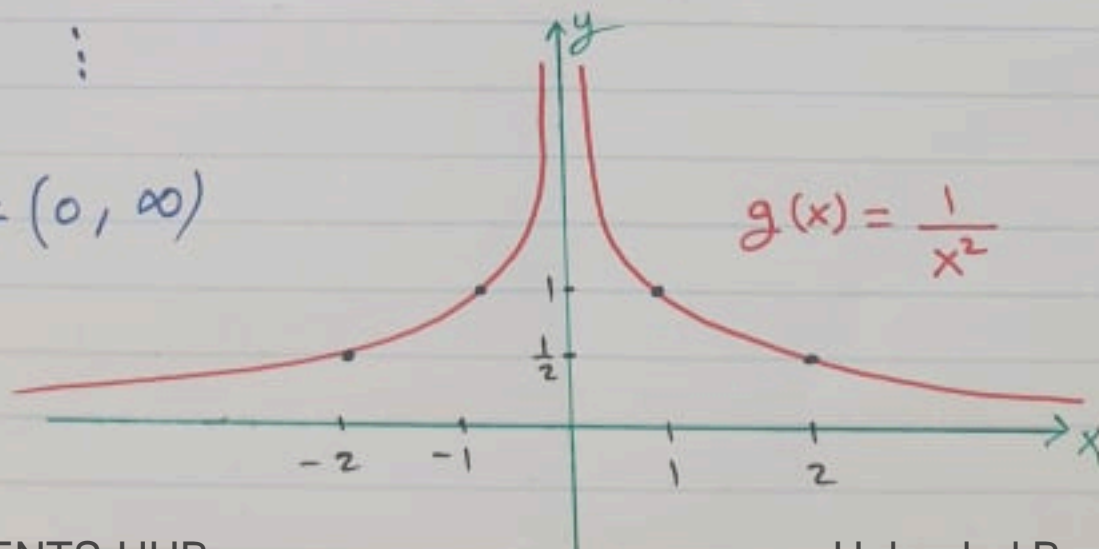
$x = \pm 2 \Rightarrow g(\pm 2) = \frac{1}{4} \in \mathbb{R}$

$x = \pm 1 \Rightarrow g(\pm 1) = 1 \in \mathbb{R}$

$x = \pm \frac{1}{2} \Rightarrow g(\pm \frac{1}{2}) = 4 \in \mathbb{R}$

\vdots

$R = (0, \infty)$



①

$$[f] \quad h(x) = \frac{1}{\sqrt{1-x^2}}$$

To find $R \Rightarrow$

$$x=0 \Rightarrow f(0)=1 \in R$$

$$x=\pm \frac{1}{2} \Rightarrow f(\pm \frac{1}{2}) = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}} \in R$$

$$x=\pm \frac{1}{4} \Rightarrow f(\pm \frac{1}{4}) = \frac{4}{\sqrt{15}} \in R$$

⋮

To find $D \Rightarrow$

$$1-x^2 > 0$$

$$1 > x^2$$

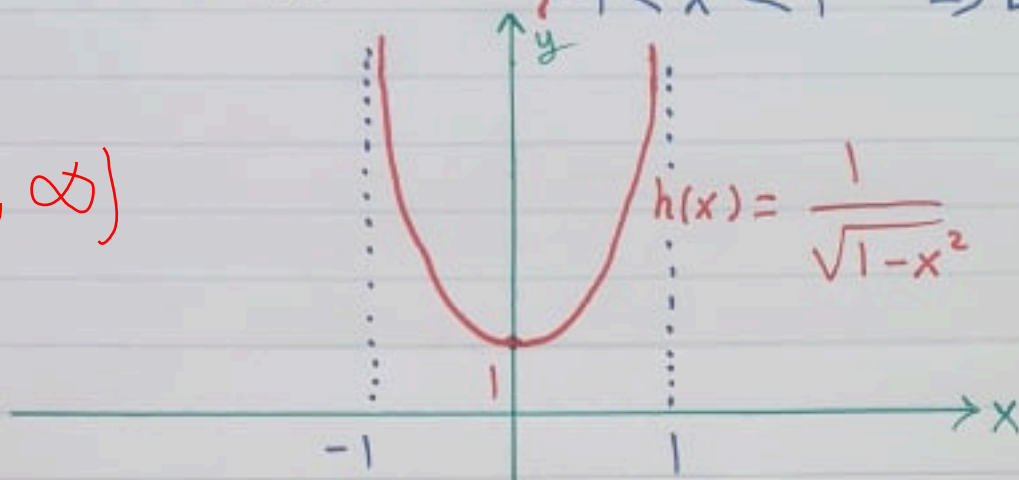
$$\sqrt{1} > \sqrt{x^2}$$

$$1 > |x|$$

$$|x| < 1$$

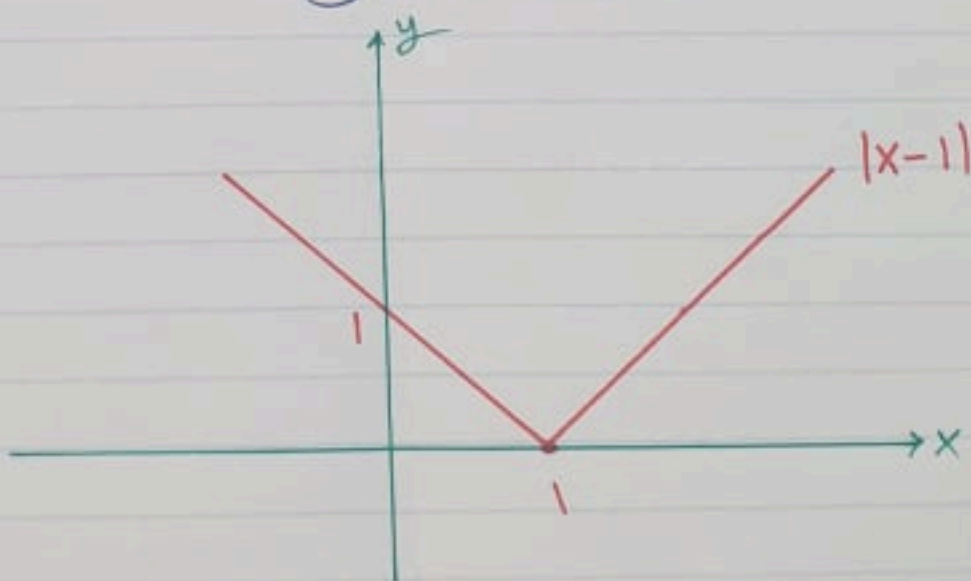
$$-1 < x < 1 \Rightarrow D = (-1, 1)$$

$$R = [1, \infty)$$



$$[2] [b] \quad y = |x-1|$$

same graph of $|x|$
but shift to the right
by one unit



②

[3] [a] $f(x) = x^2 + 1$ is even since

$$\begin{aligned} f(-x) &= (-x)^2 + 1 \\ &= x^2 + 1 \\ &= f(x) \end{aligned}$$

[b] $f(x) = x^3 + x$ is odd since

$$\begin{aligned} f(-x) &= (-x)^3 + (-x) \\ &= -x^3 - x \\ &= -(x^3 + x) \\ &= -f(x) \end{aligned}$$

[c] $g(t) = \frac{1}{t-1}$ is neither even nor odd since

$$\begin{aligned} g(-t) &= \frac{1}{(-t)-1} \\ &= \frac{1}{-t-1} = -\frac{1}{(t+1)} \end{aligned}$$

[d] $h(x) = \frac{x}{x^2-1}$ is odd since

$$h(-x) = \frac{(-x)}{(-x)^2-1}$$

$$= -\frac{x}{x^2-1}$$

$$= -h(x)$$