UPLOADED BY AHMAD JUNDI Written by Alaa Etaiwi Chap 4: Increasing and decreasing functions Basic Def: - f is a fonction defind on interval I:-->if wherever X2>X1 we have $f(X_2) > f(X_1) \forall x \in I$ then f is increasing on I \rightarrow if wherever $X_2 > X_1$, we have $f(X_2) < f(X_1) \forall x \in I$ then b is decreasing on I Sif f'(x) >0 > f is in crasing V x E (a,b)) [on [a,b] The (that we use):- f is cont on [a,b] Thon, Scliff on (a,b) ×if b(x)<0 → fis de oceaning v x (ab) on [ab] Extreme values Absolute local . Mis an Abs. Max at CEI • M is a local Max on I If H=f(C) ≥f(X) ¥ X € I $if \mathcal{M} = f(c) \ge f(x)$ and its a local Max on small interval around c •m is a local min on I if M=f(c) \$f(x) \$\to x\$ E I · Mis an Abs Min m at c if m=f(c)=f(x) and its a local min on small interval around c

UPLOADED BY AHMAD JUNDI Written by Alaa Etaiwi Sketc - Inelysing -M · a, b End points - y= f(x) C2 Interiore points fis 603 cutical points:-(CI, FCG) (C2, F(C2)) m (C3. f(C3)) (CA, FICA)) ac Co C4 · & has Absillax of M at C4 -> + also local Max · f has Abs. Min of m at Ci - + also local Min · f has local Max of f(Ca) at Ca (R! : Abs => lo (RI : As => local . I has local Min of & CC3) at C3 RI if f= X Then Then & has Abs Mar Theory il fis on [a,b] then & Abs Min at all 15 I has Abs. Max & Abs Min VIN the extreme values May occure for y=f(x) at Intocion Points E P end points f(x)=0 f is not

<u>LIPLO</u>ADED BY AHMAD JUNDI Written by Alaa Etaiwi creitical points Interior S.t: f(0)= 0 or fis unat these points The is differ on I and has extreme values at X=C GI Then f'Cc)=0 But f'(Z)=0 Then f may not have extreme values at j? X-Z to classify the critical points we use either The SDI second derivative Test-The FDT First Derivative Test-· suppose f"(c)= 0 and fis · Suppose that & has critical point at X = C and &' Cont on an open I containing C. Then :-Il if f"cc)>0 thenfcc) exists on open I containing C is local min 12 16 f"Co><0 then fcc) " 1] if f' changes sign from + to-at X=C then fccs is local Max 12 if f changes sign from - to + at x=C then fccs is local Un is local Max 13) if fices = 0 Then the 13 if f' claes not change esign at X=C then f claes not have extreme values at X=C test fails

Remarkt :_ free So > Con Cave up inflection point : & has an inflection point at X=C 16: IT & has tangent at X=C and to bind it we use: 26 Changes Concavity 6"CX)=0 Remarches for Solving Questions:-when we find the critical points and we want to check when is & inoceasing on decressing we use points of X-that lies in the I and we calculate f' at these points f' x cy x c2 x and when f'>0 Then increase and when f'<0 Then decreasing EXP

UPLOADED BY AHMAD JUNDI Written by Alaa Etaiwi SKOTCHING UN METENA · steps :-I find the Domain D(f) = How to final them ? I find the Asymptotes 3 finel the ocitical points Go back to Chap: 2 [4] find the decreasing & inoceasing How to Know a point is Intervals of f(x) Go back to Chap: 4 Efinal the Intervals of Concavity for f(X) How to Know a point's an inflection points ove 20+? Blfine inflection points Fline local Max and Min Go back to chep , 4 Dointo The (Roll's Th) if few is tout on [a,b] and deff on (a,b) @ feas = feb Them - Jat least one point CG (a,b) s.t fr'(c)=0 In Alean This if f(X) is & cont on bask & deft on (a,b) then I dean This if f(X) is & cont on bask & deft on (a,b) then I one point c E (a,b) s.t f(c)=f(b)-f(a)