

Example

Find d of cold-drawn steel of shaft under fluctuating load

$$F = 0 - 72 \text{ kN}$$

$$S_y = 510 \text{ MPa}, S_{ut} = 650 \text{ MPa}, n = 2.0$$

$$K_t = 2.02$$

Solution:

$$S_e' = 0.5 S_{ut} = 325 \text{ MPa}$$

$$K_a = a S_{ut}^b = 4.51 (650)^{-0.265} = 0.81$$

Cold-drawn $\rightarrow$ Table [7-4]

$$K_b = 1.0 \rightarrow \text{axial load}$$

$$K_c = 0.85 \rightarrow \text{axial load}$$

$$q = 0.87 \rightarrow \text{Fig. [7-20]} \quad r = 5 \text{ mm}$$

$$K_f = 1 + q(K_t - 1) = 1.59$$

$$K_e = \frac{1}{K_f} = 0.529$$

$$S_e = K_a K_b K_c K_d K_e S_e'$$

$$= 0.81 \times 1 \times 0.85 \times 0.529 \times 325 = 118.44 \text{ MPa}$$

$$F_a = F_m = \frac{72}{2} = 36 \text{ kN}$$

$$S_e = 228.76 \text{ MPa}$$

$$\sigma_a = \sigma_m = \frac{4 F_a}{\pi d^2} = \frac{4 F_m}{\pi d^2} = \frac{45.84 \times 10^3}{d^2} \text{ MPa} \times K_f$$

Goodman line.

against yielding.

$$\frac{\sigma_a}{S_e} + \frac{\sigma_m}{S_{ut}} = \frac{1}{n}$$

$$\sigma_a + \sigma_m = \frac{S_y}{n}$$

$$K_f \frac{45.84 \times 10^3}{d^2} \left(\frac{1}{S_e} + \frac{1}{S_{ut}} \right) = \frac{1}{2}$$

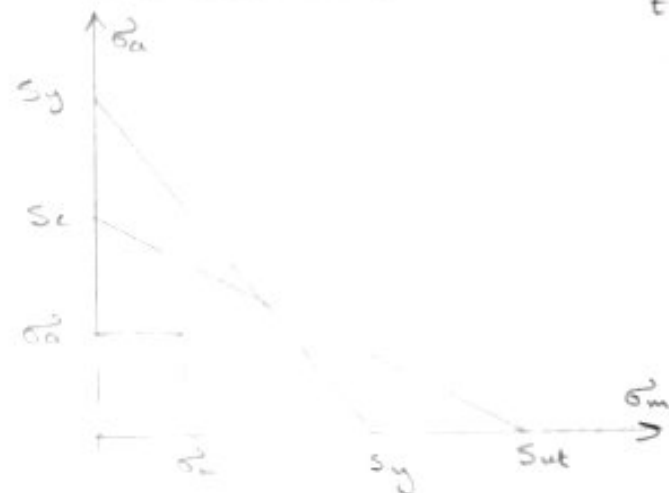
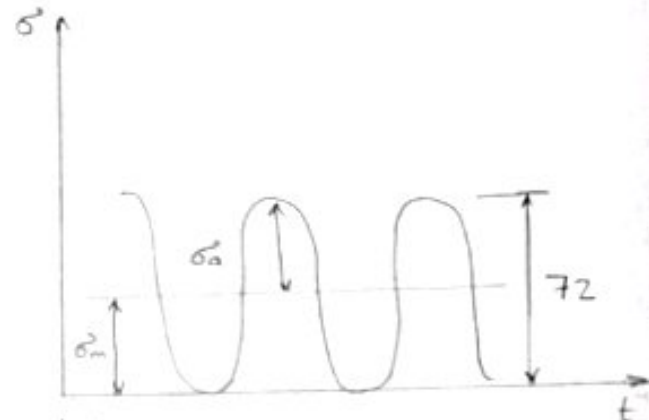
$$K_f \frac{45.84 \times 10^3}{d^2} \times 2 = \frac{510}{2}$$

$$\rightarrow d = 26 \text{ mm}$$

$$d = 32.15 \text{ mm}$$

$\rightarrow$

$$\boxed{d = 33} \text{ mm}$$



$$\sqrt{a} = \frac{139}{S_{ut}} \sqrt{\sigma_m}$$

Table [7-8]

Find (d) of cold-drawn steel shaft

$$S_y = 510 \text{ MPa}, S_{ut} = 650 \text{ MPa}$$

Tensile preload, $F_s = 36 \text{ kN}$

Fluctuating load, $F = 0 - 72 \text{ kN}$

For $n = 2.0$, $K_t = 2.02$, $r = 5 \text{ mm}$



Solution:

$$S_e' = 0.5 S_{ut} = 325 \text{ MPa}$$

$$K_a = a S_{ut}^b = 4.51 (650)^{-0.265} = 0.81 \rightarrow \text{cold-drawn steel}$$

$$K_b = 1.0 \text{ axial loading}, K_c = 0.923 \rightarrow \text{axial loading } S_{ut} < 1520 \text{ MPa}$$

$$K_f = 1 + q(K_t - 1), q = 0.87, K_f = 1.89, K_e = \frac{1}{K_f} = 0.529$$

$$S_e = K_a K_b K_c K_d K_e S_e' = 0.81 \times 1 \times 0.923 \times 0.529 \times 325 = 128.53 \text{ MPa}$$

$$S_e [K_e = 1] = 118.44$$

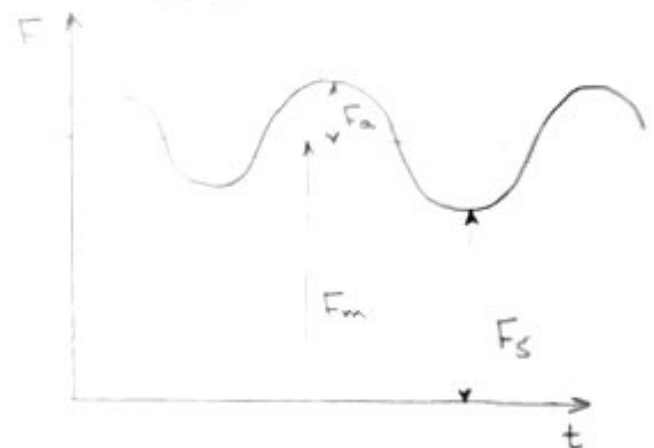
$$F_a = \frac{72}{2} = 36 \text{ kN}$$

$$F_m = F_s + F_a = 72 \text{ kN}$$

$$\sigma_m = \frac{4 F_m}{\pi d^2} = \frac{91.67 \times 10^3}{d^2} \text{ Pa}$$

$$\sigma_a = \frac{4 F_a}{\pi d^2} = \frac{45.84 \times 10^3}{d^2} \text{ Pa}$$

$$\sigma_s = \frac{4 F_s}{\pi d^2} = \frac{45.84 \times 10^3}{d^2} \text{ Pa}$$



Goodman line:

$$\frac{\sigma_m}{S_{ut}} + \frac{\sigma_a}{S_e} = \frac{1}{n}$$

$$\frac{\sigma_a}{\sigma_m} = 0.5$$

$$S_m = \frac{S_{ut} S_e}{S_e + \left(\frac{\sigma_a}{\sigma_m}\right) S_{ut}} = 184.215 \text{ MPa} \Rightarrow n = \frac{S_m}{\sigma_m} = 2.0$$

$$\Rightarrow d = 31.55 \text{ mm}$$

For axial loading: $K_b = 1.0$

Yielding line:

$$\sigma_m + \sigma_a = S_y \Rightarrow n = \frac{S_y}{\sigma_m + \sigma_a} \Rightarrow d = 23 \text{ mm}$$



$$n = \frac{S_a}{\sigma_a}$$

$$S_a = \frac{S_{ut} - \sigma_s}{\frac{1}{m} + \frac{S_{ut}}{S_c}}$$

$$m = \frac{K_f \sigma_a}{K_f \sigma_m - \sigma_s} = 1.0$$

ملاحظة

$$= 0.254 [S_{ut} - \sigma_s]$$

$$n = \frac{S_a}{\sigma_a} = 2 \rightarrow 2 = \frac{0.254 [S_{ut} - \sigma_s]}{\sigma_a} = 7.81 \sigma_a = S_{ut} - \sigma_s$$

$$\sigma_a = \sigma_s \Rightarrow 8.8 \sigma_a = S_{ut} \rightarrow 8.8 \cdot K_f \frac{45 \times 10^3}{d^2} = S_{ut} \rightarrow d = 34.2 \text{ mm.}$$

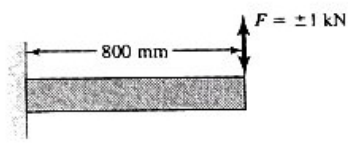
yielding

$$S_a = \frac{S_y - \sigma_s}{\frac{1}{m} + \frac{S_y}{S_y}} = \frac{S_y - \sigma_s}{2}$$

$$n = \frac{S_a}{\sigma_a} = 2$$

$$2 = \frac{S_y - \sigma_s}{2 \sigma_a} \rightarrow 5 \sigma_a = S_y$$

$$d = 21.2 \text{ mm}$$



$$f = 0.9$$

$$n = 1.5$$

$$N = 10^4 \text{ cycles}$$

Hot Rolled
HR

For AISI 1045 HR steel, $S_{ut} = 570 \text{ MPa}$ and $S_y = 310 \text{ MPa}$

$$S'_e = 0.504(570 \text{ MPa}) = 287.3 \text{ MPa}$$

Find an initial guess based on yielding:

$$\sigma_a = \sigma_{\max} = \frac{Mc}{I} = \frac{M(b/2)}{b(b^3)/12} = \frac{6M}{b^3}$$

$$M_{\max} = (1 \text{ kN})(800 \text{ mm}) = 800 \text{ N} \cdot \text{m}$$

$$\sigma_{\max} = \frac{S_y}{n} \Rightarrow \frac{6(800 \times 10^3 \text{ N} \cdot \text{mm})}{b^3} = \frac{310 \text{ N/mm}^2}{1.5}$$

$$b = 28.5 \text{ mm}$$

Eq. (7-24): $d_e = 0.808b$

Eq. (7-19): $k_b = \left(\frac{0.808b}{7.62} \right)^{-0.107} = 1.2714b^{-0.107}$

$$k_b = 0.888$$

$$\sigma = \frac{6M}{b^3} = \frac{6 \times 800}{b^3}$$

$$K_a = 0.606$$

$$K_b = 1.0 \text{ --- assumed}$$

$$K_c = 1.0$$

$$S_e = 0.606 \times 287.3 = 174 \text{ MPa}$$

$$S_f = 343.9 \text{ MPa}$$

$$n = \frac{S_f}{S_e} = 1.5$$

$$\frac{343.9}{1.5} = \frac{4800}{b^3}$$

$$b = 27.6 \text{ mm}$$

$$d_e = 0.308 b = 22.27 \text{ mm}$$

$$K_b = \left(\frac{d}{7.62} \right)^{0.107} = 0.89$$

$$S_e = 0.606 \times 0.89 \times 287.3 = 155.13 \text{ MPa}$$

$$b = \frac{1}{3} \log \frac{0.9 K_{Sut}}{S_e} = -0.173$$

$$c = \log \frac{0.9 (S_{ut})^2}{S_e} = 3.23$$

$$S_f = 345.14 \text{ MPa}$$

$$n = \frac{S_f}{S_e} \rightarrow b = \left(\frac{1.5 \times 4800}{231.74} \right)^{1/3} = 31.4$$

$$n = \frac{S_f b^3}{6M}$$

$$b = \left(\frac{n 6M}{S_f} \right)^{1/3} = 27.5 \text{ mm}$$

Combined loading

(25)

General case of stress:

Bending stress: σ_a, σ_m

Torsional stress: τ_a, τ_m

Axial stress: $(\sigma_a)_{axial}, (\sigma_m)_{axial}$

Design procedure:

- 1- Find endurance limit (S_e), assume ($K_e = 1$)
- 2- Multiply the alternating component by the corresponding stress concentration factor

$$K_f \sigma_a, K_{fs} \tau_a, (K_f)_{axial} (\sigma_a)_{axial}$$

- 3- For axial loading, multiply the alternating component by $\frac{1}{(K_c)_{axial}}$
 $\Rightarrow \frac{1}{(K_c)_{axial}} (\sigma_a)_{axial}$

- 4- Find the principal stress for alternating and mean component

$$(\sigma_{1a}, \sigma_{2a}) \text{ and } (\sigma_{1m}, \sigma_{2m})$$

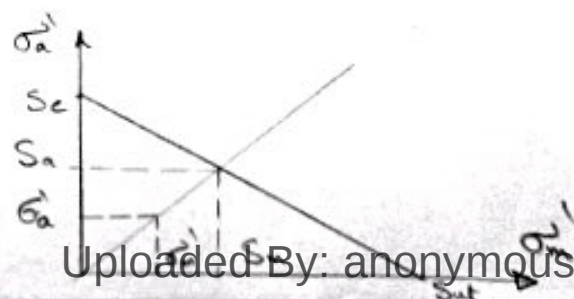
- 5- Find the von-mises stresses, the critical stresses according to DET

$$\sigma'_m = \sqrt{\sigma_{1m}^2 - \sigma_{1m} \sigma_{2m} + \sigma_{2m}^2}$$

$$\sigma'_a = \sqrt{\sigma_{1a}^2 - \sigma_{1a} \sigma_{2a} + \sigma_{2a}^2}$$

- 6- Draw $(\sigma'_m - \sigma'_a)$ diagram using Goodman line.

$$\frac{\sigma'_a}{S_e} + \frac{\sigma'_m}{S_{ut}} = \frac{1}{n} \Rightarrow n = \frac{S_{ut}}{\sigma'_m + \left(\frac{S_{ut}}{S_e}\right) \sigma'_a}$$



For pure shear [Torsion]:

(26)

$$\sigma_x = \sigma_y = 0$$

Torsional stresses; τ_a, τ_m

For yielding: $n = \frac{S_{sy}}{\tau_{max}} = \frac{S_{sy}}{\tau_m + \tau_a}$

For Fatigue: $\frac{\tau_a}{S_{se}} + \frac{\tau_m}{S_{su}} = \frac{1}{n}$

For a state of stress of single axial and Torsional stress (σ_x, τ_{xy})

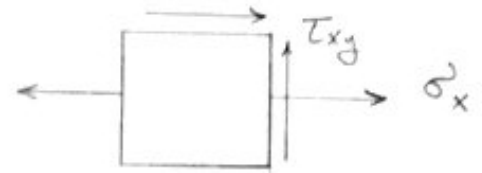
$$\sigma_x = \sigma_a, \sigma_m$$

$$\tau_{xy} = \tau_a, \tau_m$$

DET

$$\sigma'_m = \sqrt{\sigma_m^2 + 3\tau_m^2}$$

$$\sigma'_a = \sqrt{\sigma_a^2 + 3\tau_a^2}$$

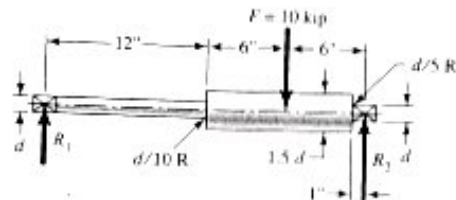


For combined loading the factor of safety against yielding:

$$n = \frac{S_y}{\sigma'_{max}} = \frac{S_y}{\sigma'_a + \sigma'_m}$$

- 7-11** Bearing reactions R_1 and R_2 are exerted on the shaft shown in the figure, which rotates at 1150 rev/min and supports a 10-kip bending force. Use a 1095 steel. Specify a diameter d using a design factor of $n_d = 1.6$ for a life of 3 min. The surfaces are machined.

Problem 7-11



7-11 A priori design decisions:

The design decision will be: d

Material and condition: 1095 HR and from Table A-20 $S_{ut} = 120$, $S_y = 66$ kpsi.

Design factor: $n_f = 1.6$ per problem statement.

Life: $(1150)(3) = 3450$ cycles

Function: carry 10 000 lbf load

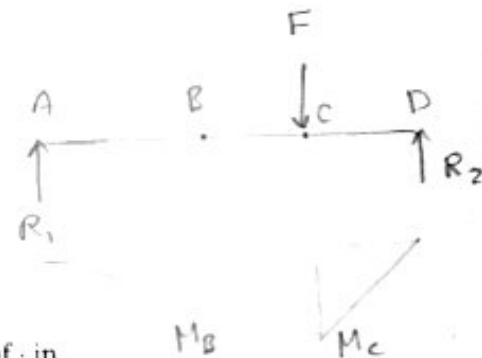
Preliminaries to iterative solution:

$$S'_e = 0.504(120) = 60.5 \text{ kpsi}$$

$$k_a = 2.70(120)^{-0.265} = 0.759$$

$$\frac{I}{c} = \frac{\pi d^3}{32} = 0.09817d^3$$

$$M(\text{crit.}) = \left(\frac{6}{24}\right)(10\,000)(12) = 30\,000 \text{ lbf} \cdot \text{in}$$



The critical location is in the middle of the shaft at the shoulder. From Fig. A-15-9: $D/d = 1.5$, $r/d = 0.10$, and $K_t = 1.68$. With no direct information concerning f , use $f = 0.9$.

For an initial trial, set $d = 2.00$ in

$$k_b = \left(\frac{2.00}{0.30}\right)^{-0.107} = 0.816$$

$$S_e = 0.759(0.816)(60.5) = 37.5 \text{ kpsi}$$

$$a = \frac{[0.9(120)]^2}{37.5} = 311.0$$

$$b = -\frac{1}{3} \log \frac{0.9(120)}{37.5} = -0.1531$$

$$S_f = 311.0(3450)^{-0.1531} = 89.3$$

$$c = \log \frac{(0.9 S_{ut})^2}{S_e} = 2.49$$

$$S_f = N^b 10^c$$

$$M_c = 45 \text{ kip} \cdot \text{in}$$

$$M_B = 30 \text{ kip} \cdot \text{in}$$

$$\sigma = \frac{32 M}{\pi d^3}$$

$$\sigma_B = \frac{135.8}{d^3}$$

$$\sigma_B = \frac{305.57}{d^3}$$

$$\sigma_B > \sigma_c$$

$$\sigma_0 = \frac{M}{I/c} = \frac{30}{0.09817d^3} = \frac{305.6}{d^3}$$

$$= \frac{305.6}{2^3} = 38.2 \text{ kpsi}$$

$$r = \frac{d}{10} = \frac{2}{10} = 0.2$$

$$K_f = \frac{1.68}{1 + (2/\sqrt{0.2}) [(1.68 - 1)/1.68](4/120)} = 1.584$$

Eq. (7-37):

$$(K_f)_{10^3} = 1 - (1.584 - 1)[0.18 - 0.43(10^{-2})120 + 0.45(10^{-5})120^2]$$

$$= 1.158$$

Eq. (7-38):

$$(K_f)_N = K_{3450} = \frac{1.158^2}{1.584} (3450)^{-(1/3) \log(1.158/1.584)}$$

$$= 1.225$$

$$\sigma_0 = \frac{305.6}{2^3} = 38.2 \text{ kpsi}$$

$$\sigma_a = (K_f)_N \sigma_0 = 1.225(38.2) = 46.8 \text{ kpsi}$$

$$n_f = \frac{(S_f)_{3450}}{\sigma_a} = \frac{89.3}{46.8} = 1.91$$

The design is satisfactory. Reducing the diameter will reduce n , but the resulting preferred size will be $d = 2.00$ in.

7-12

$$\sigma'_a = 172 \text{ MPa}, \quad \sigma'_m = \sqrt{3}\tau_m = \sqrt{3}(103) = 178.4 \text{ MPa}$$

Yield: $172 + 178.4 = \frac{S_y}{n_y} = \frac{413}{n_y} \Rightarrow n_y = 1.18 \text{ Ans.}$

(a) Modified Goodman, Table 7-9

$$n_f = \frac{1}{(172/276) + (178.4/551)} = 1.06 \text{ Ans.}$$

(b) Gerber, Table 7-10

$$n_f = \frac{1}{2} \left(\frac{551}{178.4} \right)^2 \left(\frac{172}{276} \right) \left\{ -1 + \sqrt{1 + \left[\frac{2(178.4)(276)}{551(172)} \right]^2} \right\} = 1.31 \text{ Ans.}$$

(c) ASME-Elliptic, Table 7-11

$$a = \frac{1}{K_f} =$$

$$b = -\frac{1}{3} \log \frac{1}{K_f}$$

$$K_f' = a N^b$$

$$= \frac{1}{1.584} (3450)^{0.066}$$

$$=$$

$$a = \frac{1}{K_f} =$$

$$b = -\frac{1}{3} \log \frac{1}{K_f}$$

$$b = -0.063$$

$$a =$$

Example: Disk sander.

The shaft is made of steel $S_{ut} = 900 \text{ MPa}$
machine finished. $S_y = 750 \text{ MPa}$

The friction torque developed by force F_t
at (100 mm radius), $T = 12 \text{ N.m}$

$\mu = 0.6$ between the object and the disk.

Find factor of safety (n) against fatigue
failure.

Solution:

$$1 - T = F_t R = F_t (0.1)$$

$$\Rightarrow F_t = 120 \text{ N}$$

$$F_t = \mu F_n \Rightarrow F_n = \frac{F_t}{\mu} = \frac{120}{0.6} = 200 \text{ N}$$

Torque $T = 12 \text{ N.m}$

axial force: $P = 200 \text{ N}$ axial force.

Bending: Horizontal plane, $M_h = 120 \text{ N} \times 50 \text{ mm}$

Vertical plane $\rightarrow M_v = 200 \times 100 \text{ mm}$

$$\begin{aligned} M &= \sqrt{M_h^2 + M_v^2} \\ M &= 20,900 \text{ N.m} \end{aligned}$$

2 - Stress concentration:

$$K_t = 1.28, K_{ts} = 1.1, (K_t)_a = 1.28$$

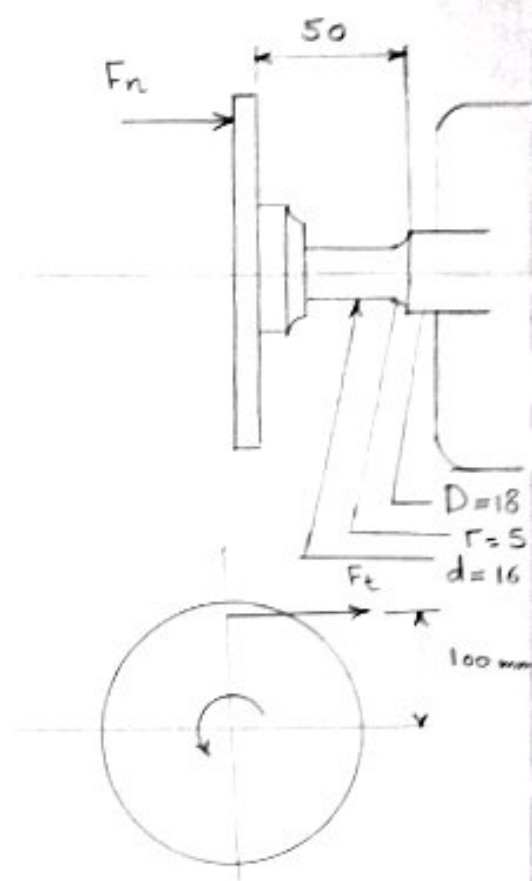
$$\text{For } r = 5 \text{ mm}, S_{ut} = 900 \text{ MPa.} \Rightarrow q = 0.91 \text{ (axial and bending)}$$

$$q_s = 0.93 \text{ (Torsion).}$$

$$\Rightarrow K_{fs} = 1.09$$

$$K_f = 1.25$$

$$(K_f)_a = 1.25$$



3 - Stresses at fillet:

$$\tau_m = \frac{16 T_m}{\pi d^3} K_{fs}, \quad \tau_a = \frac{16 T_m}{\pi d^3} = 0$$

$$(\sigma_m)_{\text{axial}} = \frac{P}{A} = \frac{4P}{\pi d^2} K_{f_{\text{axial}}}, \quad (\sigma_a)_b = \frac{32 M}{\pi d^3}, \quad (\sigma_m)_b = 0$$

$$\sigma_m = (\sigma_m)_{\text{axial}}, \quad (\sigma_a)_{\text{axial}} = 0$$

4 - Mises stress

$$\sigma_m' = \sqrt{\sigma_m^2 + 3\tau_m^2}$$

$$\sigma_m = (\sigma_m)_{\text{axial}} = \frac{4P}{\pi d^2} = \frac{4(200)}{\pi (16)^2} \times 1.25 = 1.25 \text{ MPa}$$

$$\tau_m = \frac{16T}{\pi d^3} K_f = 16.35 \text{ MPa}$$

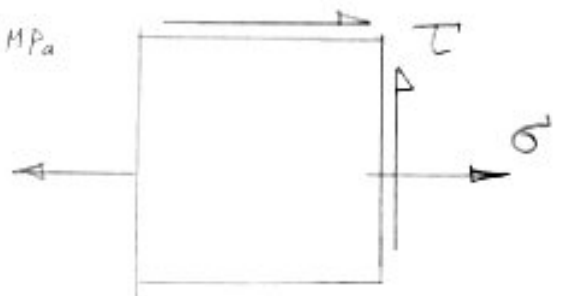
$$\sigma_m' = \sqrt{\sigma_m^2 + 3\tau_m^2} = 28.34 \text{ MPa}$$

$$\sigma_a' = \sqrt{\sigma_a^2 + 3\tau_a^2}$$

$$\sigma_a = \sigma_b = K_f \frac{32 M}{\pi d^3} = 1.25 \frac{32(20.900)}{\pi (16)^3} = 65 \text{ MPa}$$

$$\tau_a = 0$$

$$\sigma_a' = 65 \text{ MPa}$$



$$5 - S_e = 0.5 S_{ut} = 450 \text{ MPa}$$

$$K_a = a S_{ut}^b = 445 (900)^{-0.265} = 0.73$$

$$K_b = \left(\frac{d}{7.62} \right)^{-0.107} = 0.923$$

$$K_c = 1.0$$

$$K_e = 1.0, \quad K_d = 1.0$$

$$S_e = 0.73 \times 0.923 \times 450 = 303.43 \text{ MPa}$$

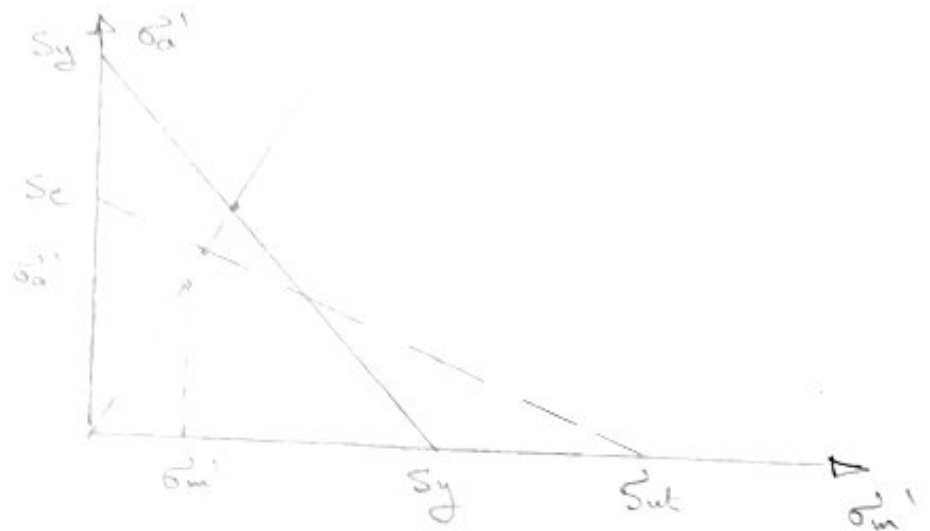
6- Goodman line.

$$\frac{\sigma_m'}{S_{ut}} + \frac{\sigma_a'}{S_e} = \frac{1}{n} \Rightarrow n = \frac{S_{ut}}{\sigma_m' + \left(\frac{S_{ut}}{S_e}\right) \sigma_a'}$$

$$n = 4.16$$

7- Factor of safety against yielding.

$$n = \frac{S_y}{\sigma_a' + \sigma_m'} = \frac{750}{65 + 28.34} = 8.03$$



$$\frac{\sigma_a}{\sigma_m} = 0.5$$

$$S_m = \frac{S_e S_{ut}}{S_e + \left(\frac{\sigma_a}{\sigma_m}\right) S_{ut}} = 184 \text{ MPa.}$$

$$n = \frac{S_m}{\sigma_m} = \frac{184}{\frac{91.67 \times 10^{-3}}{d^2}} = 2.0 \Rightarrow d = 31.5 \text{ mm}$$

$$\frac{\sigma_a}{S_e} + \frac{\sigma_m}{S_{ut}} = \frac{1}{n} \Rightarrow \frac{45.84 \times 10^{-3}}{(128.5) d^2} + \frac{91.67 \times 10^{-3}}{650 d^2} = \frac{1}{2}$$

$$d = 31.55 \text{ mm.}$$

$$\text{use } d = 32.0 \text{ mm.}$$

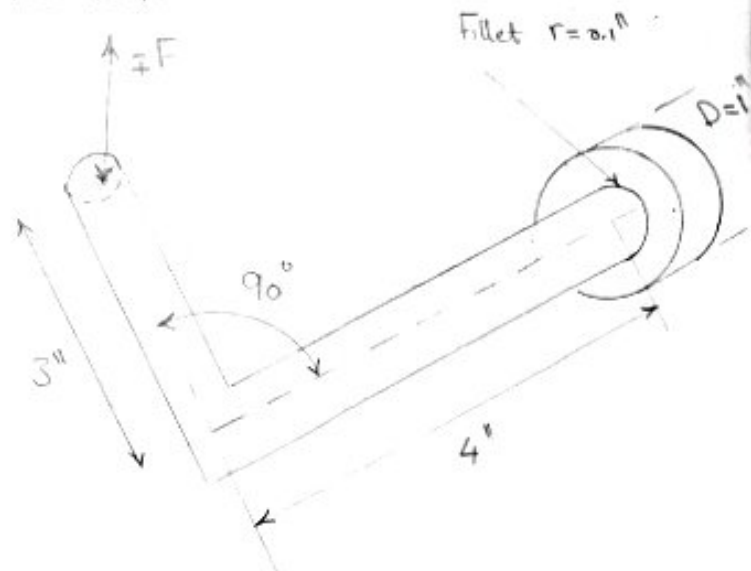
Yielding:

$$\sigma_m + \sigma_a = \frac{S_y}{n} \\ \frac{(45.84 + 91.67) \times 10^{-3}}{d^2} = \frac{510}{2}$$

$$\Rightarrow d = 23 \text{ mm}$$

Example

- a) The shown steel bar, $d = \frac{1}{2}$ in, is machine finished having, $S_{ut} = 90 \text{ kpsi}$, $S_y = 55 \text{ kpsi}$. Find the value of alternating force F which would just sufficient to cause fatigue failure of the bar.
- b) If the previous bar is subjected to constant load $F = 50 \text{ lb}$. Find the alternating superimposed F_a just sufficient to cause failure.



Solution:

1- $S_e' = 0.5 S_{ut} = 45 \text{ kpsi}$

$$K_a = a S_{ut}^b = 2.7 (90)^{-0.265} = 0.819$$

$$K_b = \left(\frac{d}{0.3} \right)^{-0.1133}$$

non-rotating shaft:

$$d_e = 0.37 d = 0.185'' \Rightarrow K_b = \left(\frac{0.185}{0.3} \right)^{-0.1133} = 1.056$$

$$K_c = 1.0 \text{ combined loading}$$

$$K_e = 1.0$$

$$K_d = 1.0$$

$$\Rightarrow S_e = 0.819 \times 1.056 \times 1 \times 1 \times 45 = 40 \text{ kpsi}$$

2- Stress concentration at (A):

Bending:

$$K_t = 1.43, q = 0.82$$

$$K_f = 1 + q(K_t - 1) = 1.35$$

Torsion:

$$K_{ts} = 1.28, q_s = 0.85$$

$$K_{fs} = 1 + q_s(K_{ts} - 1) = 1.238$$

3- Completely reversed stress:

$$\text{Bending: } \sigma_a = K_f \frac{32M}{\pi d^3} = 1.35 \frac{(4F)}{\pi (0.5)^3} = 440 F$$

$$\text{Torsion: } \tau_a = K_{fs} \frac{16T}{\pi d^3} = \frac{16(3F)}{\pi (0.5)^3} (1.24) = 151 F$$

$$4- \sigma_a' = \sqrt{\sigma_a^2 + 3\tau_a^2} = 512 F$$

5- completely reversed bending: $n = \frac{S_e}{\sigma_a'} = 1.0 \Rightarrow 512 F = 39 \times 10^3$

$$F_m = 50 \text{ lb} \quad F_a = F$$

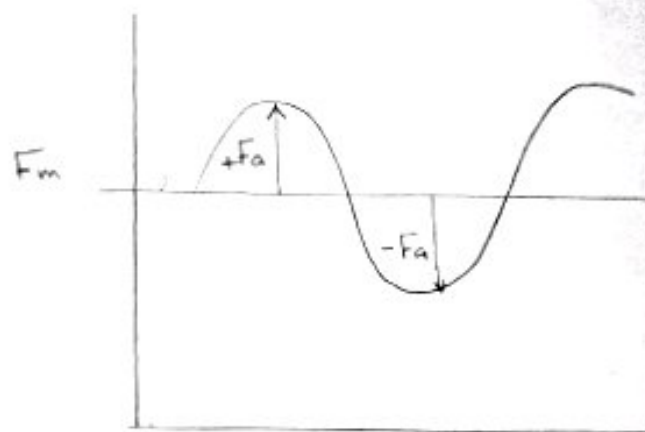
$$F_{\max} = F_s + F_a$$

$$F_{\min} = F_s - F_a$$

$$F = F_s \mp F_a$$

$$M_a = 4F \quad M_m = 4 \times 50$$

$$T_a = 3F \quad T_m = 3 \times 50$$



Stresses

$$\sigma_a = K_f \frac{32(4F)}{\pi d^3} = 440F$$

$$\sigma_m = K_f \frac{(32)(200)}{\pi d^3} = 22 \text{ kpsi}$$

$$\tau_a = K_{fs} \frac{16(3F)}{\pi d^3} = 151F$$

$$\tau_m = K_{fs} \frac{16(150)}{\pi d^3} = 7.55 \text{ kpsi}$$

Von-mises Stress

$$\sigma_a' = \sqrt{\sigma_a^2 + 3\tau_a^2} = 512F$$

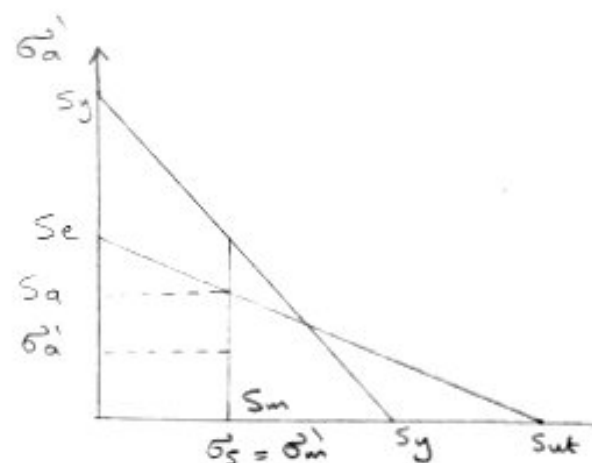
$$\sigma_m' = \sqrt{\sigma_m^2 + 3\tau_m^2} = 25.6 \text{ kpsi}$$

goodman line:

$$\frac{\sigma_a'}{S_e} + \frac{\sigma_m'}{S_{ut}} = \frac{1}{n}$$

$$S_m = \sigma_m' \rightarrow \frac{S_a}{S_e} + \frac{\sigma_m'}{S_{ut}} = 1 \rightarrow S_a = S_e \left(1 - \frac{\sigma_m'}{S_{ut}}\right) = 28.6 \text{ kpsi}$$

$$n = \frac{S_a}{\sigma_a'} = 1.0 \rightarrow S_a = \sigma_a' = 512F \Rightarrow F = 55.9 \text{ lb.}$$



Yielding line:

$$S_a + S_m = S_y \Rightarrow S_a = S_y - S_m = S_y - \sigma_m' = 55 - 25.6 = 29.4$$

$$\sigma_a' = 512F \Rightarrow F = 57.4 \text{ lb.}$$