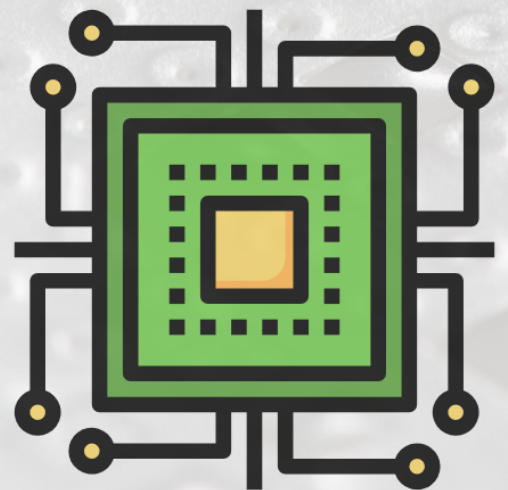


# Circuits Analysis

By Rawan Alfares

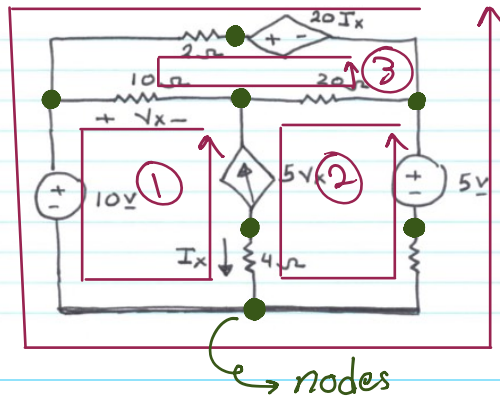


## Voltage and Current laws

**Node:** A point of Connection of two or more Circuit elements

**loop:** Any closed path through the Circuit in which no node is crossed more than once.

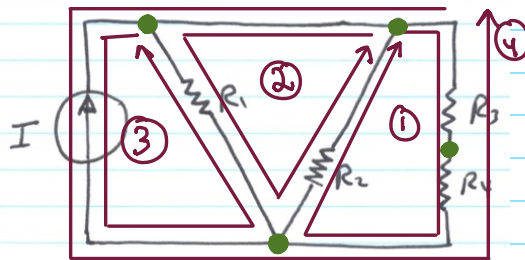
**Mesh:** Any loop that doesn't contain within it another loop. "minimum number of loops".



\* we have 4 loops

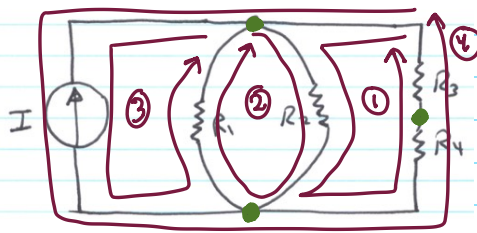
\* we have 3 Mesh (1-3)  
4 is not mesh since it has inside it 3 loops.

\* 7 nodes.



\* 4 loops

\* 4 nodes

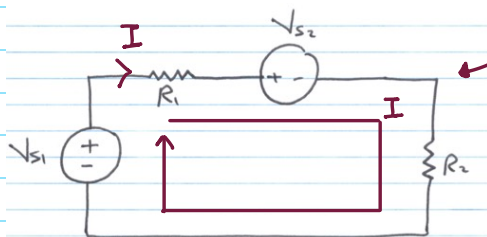


\* 4 loops , 4 mesh.

\* 3 nodes

## Series Connections

All of the elements in a Circuit that Carry the Same Current are said to be Connected in Series

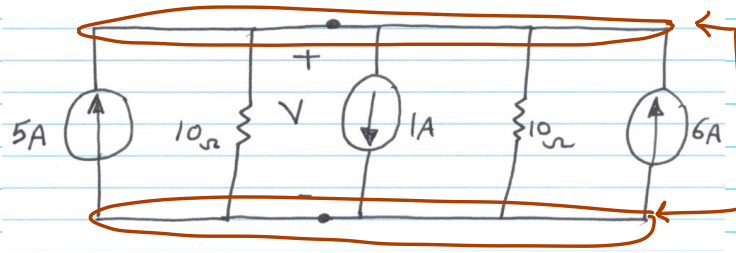


كل ال elements  
يتر فيهم نفس  
التيار

\*  $\sum V = 0$  closed path (كيرشوف).

## Parallel Connections

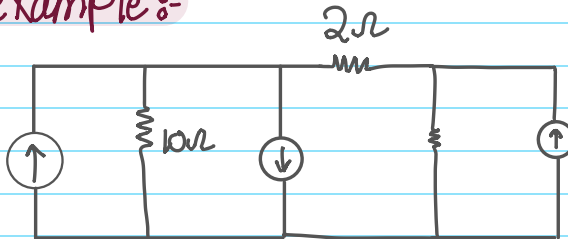
elements in a circuit having a common voltage across them are said to be connected in parallel.



بیشتر کوا مع  
بعض [nodes] \*

\* having the same voltage  
\*  $\sum I = 0$

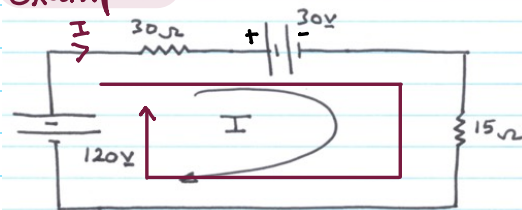
example:-



## Kirchhoff Voltage Law KVL

KVL: the algebraic sum of the voltage around any loop is zero.  
 $\sum V = 0$ , for each loop

example:



\* إذا كان اتجاه التيار بنفس اتجاه اللول  
ال Voltage.  $\pm$

1. find I

$$\sum V = 0$$

$$0 = 30I + 30 + 15I - 120$$

$$90 = 45I$$

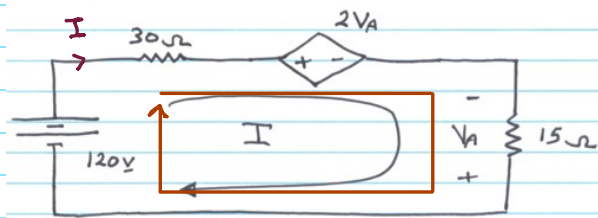
$$I = 2A$$

2. find V for each R.

$$V_{30\Omega} = IR = (2)(30) = 60V$$

$$V_{15\Omega} = IR = (2)(15) = 30V$$

example:



1. find I

method 1:

$$\sum V = 0$$

$$0 = 30I + 2V_A + 15I - 120 \rightarrow \textcircled{1}$$

$$0 = 30I - 30I + 15I - 120$$

$$\frac{120}{15} = I$$

$$I = 8A$$

$$\rightarrow V_A = -15 \times 8 = -120V$$

from the figure:

$$V_A = -15I \rightarrow \textcircled{2}$$

substitute in ①

method 2:

$$\sum V = 0$$

$$0 = 30I + 2V_A - V_A - 120$$

$$0 = 30I + V_A - 120$$

$$0 = 30I - 15I - 120$$

$$0 = 15I - 120$$

$$\frac{120}{15} = I$$

$$I = 8A$$

$$V_A = -15I$$

2. Calculate the power absorbed by each circuit elements :-

$$P_{30\Omega} = (8)^2(30) = 1920W$$

$$P_{15\Omega} = (8)^2(15) = 960W$$

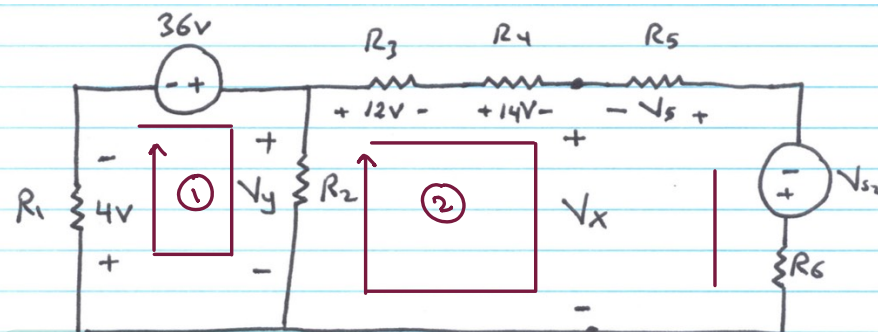
$$P = I^2 R$$

$$P_{120} = (8)(120) = -960W$$

$$P_2 = (8)(2)(-120) = -1920$$

$$P = IV$$

example:



find  $V_x$  and  $V_y$  :-

$$\sum V = -36 + V_y + 4 = 0$$

$$V_y = 32V$$

$$\sum V = 0$$

$$0 = 12 + 14 + V_x - 32$$

$$V_x = 6V$$

## Kirchhoff Current Law KCL

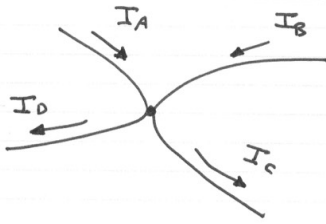
KCL: the algebraic sum of the current entering any node is zero.

-  $\sum I = 0$ , for each node

-  $\sum I_{in} = \sum I_{out}$

\* التيار الخارج من النود (+)  
التيار الداخل على النود (-)

Example:



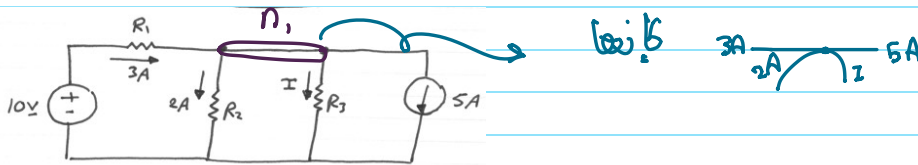
①  $\sum I = 0$

-  $I_A - I_B + I_D + I_C = 0$

②  $\sum I_{in} = \sum I_{out}$

$I_A + I_B = I_D + I_C$

Example 8-



find I:

for  $n_1$ ,  $\sum I = 0$

-  $3 + 2 + I + 5 = 0$

$I = -4A$

بذلكا مثل ده  
وبأي قانون بتعرفها بنفس الإشارة.

Example 9 find  $V_x$  :-



$V = IR$

$V = \frac{I}{G} \rightarrow I = VG$

for  $n_1$ ,  $\sum I = 0$

-  $120 + I_1 + 30 + I_2 = 0$

-  $90 + I_1 + I_2 = 0$

$I_1 + I_2 = 90$

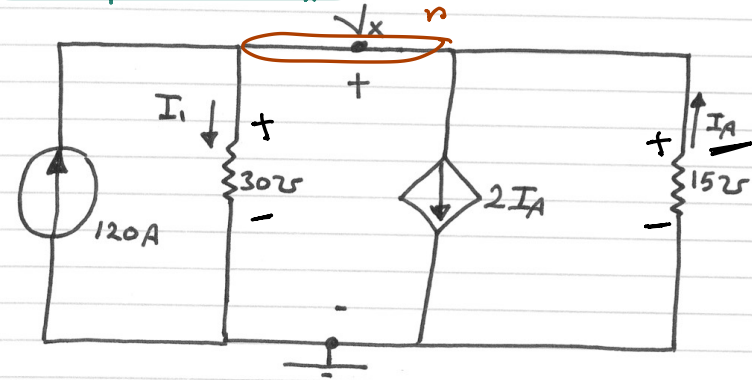
$30V_x + 15V_x = 90$

$\rightarrow 45V_x = 90 \rightarrow V_x = 2V$

$$I_1 = (30)(2) = 60 \text{ A}$$

$$I_2 = (15)(2) = 30 \text{ A}$$

Example: Find  $V_x$ :



$$V = IR$$

$$I = GV$$

$$I_1 = 30 V_x$$

$$I_A = -15 V_x$$

for  $n$ ,  $\sum I = 0$

$$-120 + I_1 + 2I_A - I_A = 0$$

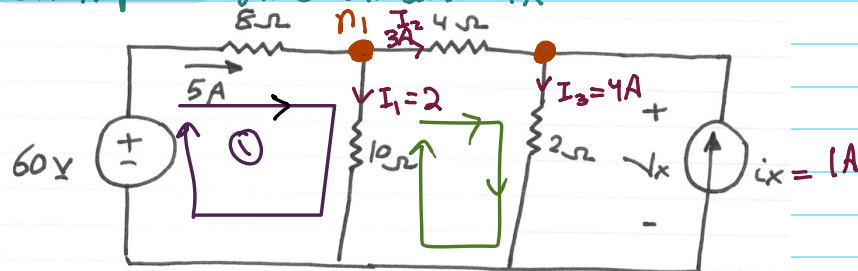
$$-120 + I_1 + I_A = 0$$

$$-120 + 30 V_x - 15 V_x = 0$$

$$-120 = -15 V_x$$

$$V_x = 8 \text{ V}$$

example: find  $V_x$  and  $i_x$



\* for  $n_1$ ,  $\sum I = 0$

$$-5 + I_1 + I_2 = 0 \rightarrow \textcircled{1}$$

\* for  $n_2$ ,  $\sum I = 0$

$$-I_2 + I_3 - i_x = 0 \rightarrow \textcircled{2}$$

\* for loop 1,  $\sum V = 0$

$$40 + 10I_1 - 60 = 0$$

$$I_1 = 2 \text{ A} \rightarrow \text{Substitute in } \textcircled{1}$$

$$-5 + 2 + I_2 = 0$$

$$I_2 = 3 \text{ A}$$

\* for loop 2,  $\sum V = 0$

$$12 + 2I_3 - 20 = 0$$

$$I_3 = 4 \text{ A} \rightarrow \text{Substitute in } \textcircled{2}$$



by eq. 2.

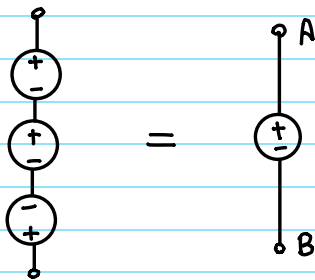
$$-3 + 4 - i_x = 0$$

$$i_x = 1 \text{ A}$$

$$V_x = I_3 R$$
$$= 4 \times 2 = 8 \text{ V}$$

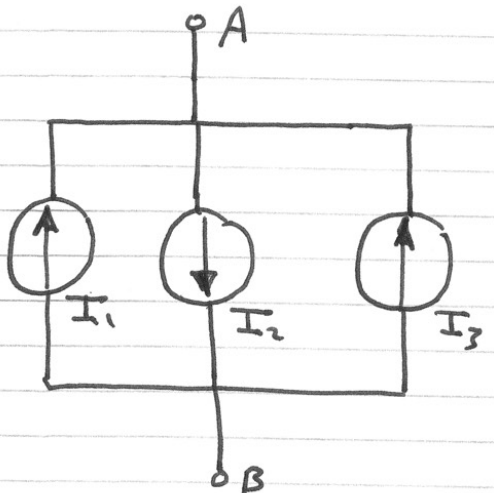
### Series And Parallel Sources

→ Voltage Sources Connected in Series Can be Combined into equivalent Source:



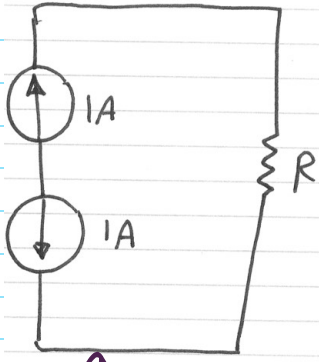
$$V_s = V_1 + V_2 - V_3$$

→ Current Sources Connected in Parallel Can be Combined into an equivalent Current Source.

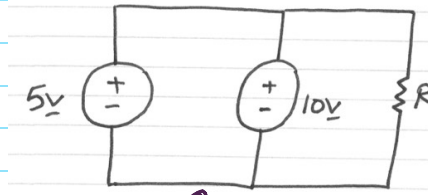


$$I_s = I_1 + I_3 - I_2$$

## Impossible Circuits



\* مستحيل يكون هسرين  
تياراة على التوالي



\* مستحيل يكون هسرين  
جهد على التوالي

ربنا تقبل منا إنك أنت السميع العليم