

Electrical Machines Fundamentals

* Motors $\Rightarrow$ electrical $\rightarrow$ Mechanical

* Generator $\Rightarrow$ Mechanical $\rightarrow$ electrical

Review's CH4, CH9 & CH10 & Complex Numbers
AC & Power calculations

1 By Amperes

2

التيار يساوي تلك يتولد كالتالي



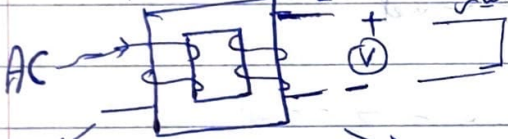
إننا نوجد المجال الناتج من التيار في دائرة مغلقة يتولد قوة حثية

Fidradly's law

$$\frac{d\phi}{dt} \left[\begin{array}{c} + \\ \text{V} \end{array} \right]$$

Transformer $\Rightarrow$ changing of voltage level.

N_1 N_2



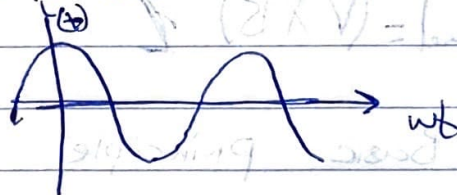
when closed circuit

مغناطيسية

core

ساحة طور التيار على Feru magnetic

$$i(t) = I \cos \omega t$$



التيار ساحة حثية كلية

فال ϕ ينتقل عبر ال core للملف الثاني ولا يتبدل تياره

يصبح هذا هو secondary

$$e_{\text{induced}} = -N \frac{d\phi}{dt}$$

← Naturally ← مغناطيسي ←
← Electrical ← كهربائي ←

[3]

لما كان مجال مغناطيسي موجود و وجبت سلك يحمل تيار

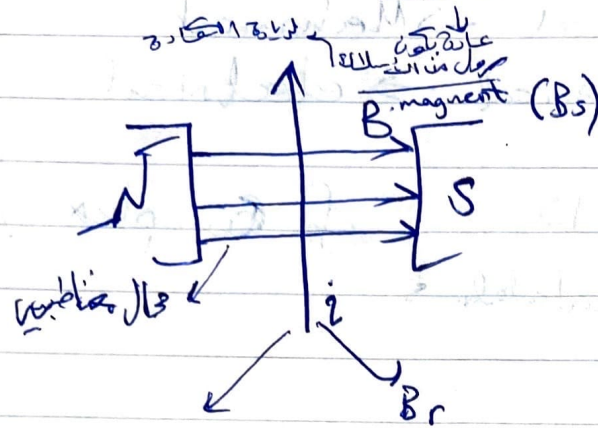
ستتلقى Force قاذرة السلك
فرك ←

الجزء المعرض للمجال المغناطيسي

$$\vec{F} = i (\vec{L} \times \vec{B})$$

تدور المجال ←

Basic principle of motor

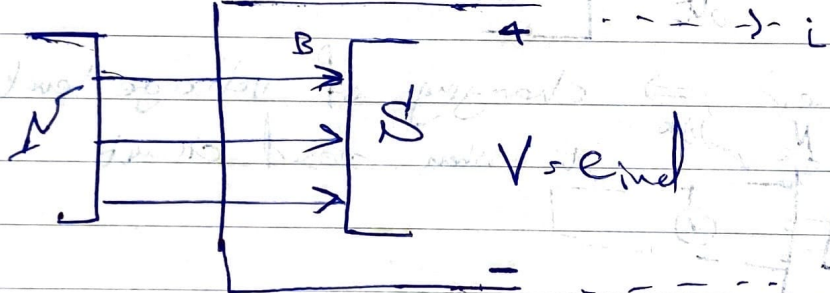


هو disturbance
B_r للتول من تيار الكهربي

[4]

بوجود مجال مغناطيسي و ولتية أقوى خطوط المجال
سيتم تدويره في اطراف السلك
بواسطة

mechanical



$$e_{ind} = (\vec{V} \times \vec{B}) \cdot \vec{l}$$

↳

Basic principle of generator

* Induction motor $\equiv$ rotational transformer

* small size

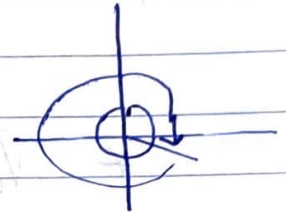
clean

مركبة
من البلاستيك
الصلب

easy to move efficiently

* linear speed / vel $= \frac{\Delta d}{\Delta t}$

* rotational ~~speed~~ angular velocity $= \frac{\Delta \theta}{\Delta t}$ angular position
rad/sec



(+) counterclockwise

(-) clockwise

* $f_m \rightarrow$ angular vel --- rev/sec

* $n_m \rightarrow$ angular vel --- rev/minute

* given rad/sec $\rightarrow$ rpm

$$157 \rightarrow 157 \times \frac{60}{2\pi}$$

larger than ω

* given rpm $\rightarrow$ rad/sec

$$1500 \text{ rpm} \rightarrow 1500 \times \frac{2\pi}{60}$$

* angular acc $= \frac{d\omega}{dt} = \frac{d\ddot{\theta}}{dt}$ rad/sec²

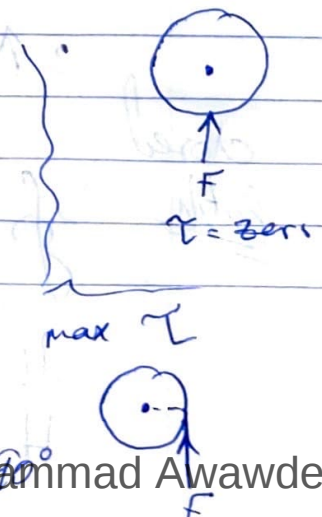
* $\tau = \text{Force} \times \text{perpendicular distance}$

$$\tau = Fr \sin \theta$$

المoment

$$\tau = J\alpha \text{ --- Nm}$$

moment of inertia
المoment of inertia



* $\int \rightarrow$ when distance varies

$$W = F \cdot d \quad \text{--- Joules}$$

$$* P = \frac{dW}{dt} = \frac{d(\tau \theta)}{dt} = \tau \frac{d\theta}{dt}$$

$$\Rightarrow \boxed{P = \tau \omega}$$

معدل التغير الزاوي للزاوية
الزوايا
ناتج القوة $\rightarrow$ J/sec

electrical power

$$* P_e = iV$$

$$i = \frac{dq}{dt}$$

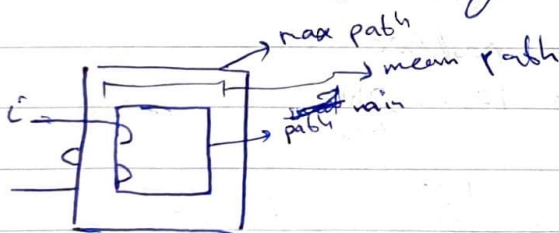
$$V = \frac{dW}{dq}$$

$$\rightarrow P = i \cdot V = \frac{dq}{dt} \times \frac{dW}{dq}$$

$$\boxed{P_e = \frac{dW}{dt}} = \tau \omega$$

* Production of Magnetic Field

→ natural magnet
→ electrical magnet



closed path

$$\oint H \cdot dl = I_{net}$$

$$= i \times N_{turns}$$

$dl \rightarrow$ mean path

$$H \cdot l_c = N i$$

$$\Rightarrow \boxed{H = \frac{N i}{l_c}}$$

A. turns

التيار الكهربائي لوجود مجال مغناطيسي

magnetic field intensity

المجال

$$\mu_0 = 4\pi \times 10^{-7}$$

$$\mu_r = 2000 - 6000$$

$$\mu = \mu_0 \mu_r$$

total

magnetic field density $\rightarrow$ كثافة المجال المغناطيسي

$$B = \mu H$$

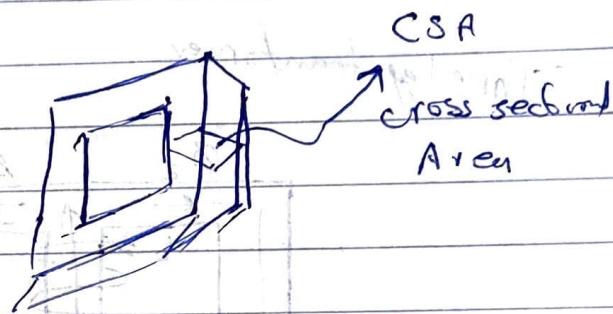
$$B = \frac{\mu N i}{l_c} \quad \text{--- Tesla.}$$

$\mu \rightarrow$ magnetic permeability
Henry / meter

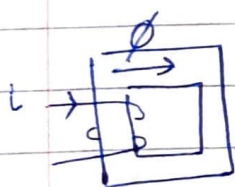
المجال المغناطيسي

$$\Phi = B A = \frac{\mu N i A}{l_c} \quad \text{--- weber}$$

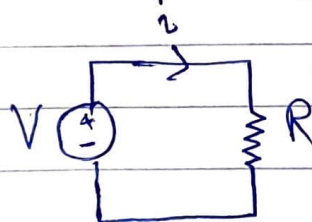
$$\Rightarrow B = \frac{d\Phi}{dA}$$



* all can't be found so we can do some jobs between electrical circuit & magnetic circuit



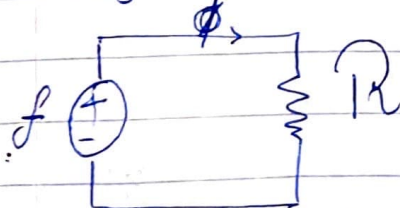
magnetic circuit



electrical circuit

$$f = N i$$

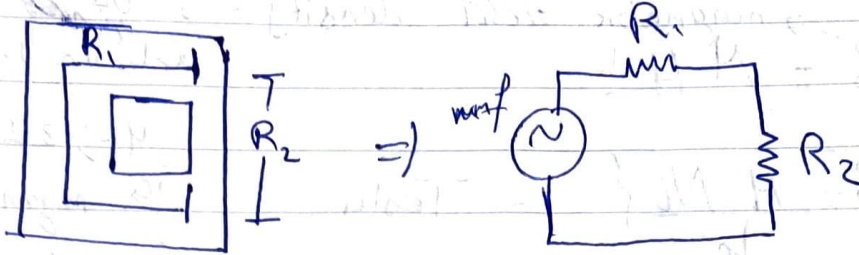
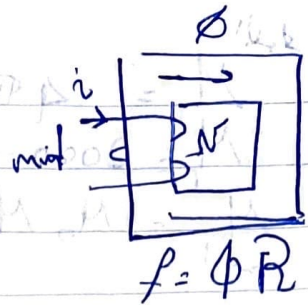
(magnet motive force)



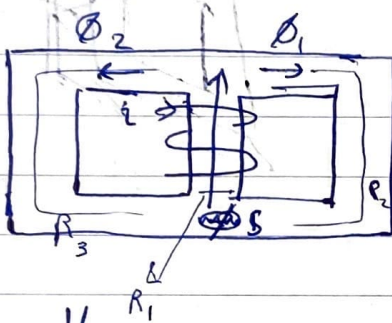
$\rightarrow$ reluctance
المقاومة للمجال المغناطيسي

$$\Rightarrow f = \Phi R$$

$R \rightarrow$ might be changeable due same system. How?

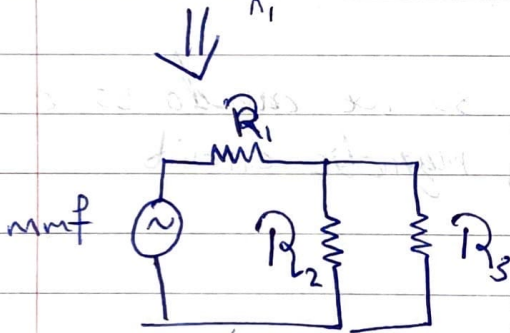


Three leg transformer



in series because same flux pass across them

application) in series or in parallel.



*In electricity

$G = \frac{1}{R}$ Siemens $\sim^{-1}$

*In magnet

permanence $P = \frac{1}{R}$
reluctance

$\Rightarrow f = \Phi R$
 $Ni = \Phi \frac{1}{P}$

$\Rightarrow P = \frac{\Phi}{Ni}$

$$R = \frac{l}{\Phi} = \frac{Nl}{\Phi} = \frac{Nl}{\frac{MNlA}{L_c}}$$

$$R = \frac{l}{MA}$$

* Possible inaccuracy $\rightarrow$ losses in flux

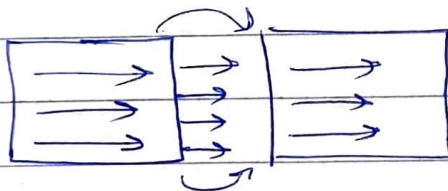
① leakage flux at edges

$\Rightarrow$ Toroidal Transformer (fillet edges)

② Mediums permeability $\rightarrow$ Ferromagnetic $\rightarrow$ high permeability
 $\rightarrow$ Air $\rightarrow$ low $\rightarrow$ leakage of flux

③ Uniform Area Cross sectional area

④ Fringing effect $\Rightarrow$ reluctance of ^{cross sectional} area differs due to the air gap

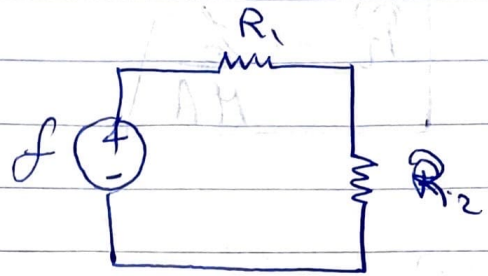


⑤ ~~Max~~ M_r & $H \Rightarrow$ non-linear relationship
 for permeability

* Example 1-1

$$\mathcal{F} = Ni$$

$$\Phi = \frac{\mathcal{F}}{R_{\text{total}}} = \frac{Ni}{R_{\text{total}}}$$



in series
cause same flux

$$R_{\text{total}} = R_1 + R_2$$

$$R_1 = \frac{l_c}{\mu A} = \frac{1.3}{(4\pi \times 10^{-7})(2500)(0.15 \times 0.1)}$$

$\swarrow$ mean path $\searrow$ width $\searrow$ depth

$$\mu = \mu_0 \mu_r$$

$$R_2 = \frac{l_c}{\mu A} = \frac{0.45}{(4\pi \times 10^{-7})(2500)(0.1 \times 0.1)}$$

$$\rightarrow R_{\text{total}}$$

$$\Phi = \frac{(200)(1\text{ A})}{R_{\text{total}}} \quad \text{Weber}$$

* Example 1-2

$$\Phi = \frac{Ni}{R_{\text{total}}}$$

$$R_{\text{core}} = \frac{l_c}{\mu A} = \frac{0.4}{(4\pi \times 10^{-7})(4000)(12 \times 10^{-4})}$$

$$R_{\text{air gap}} = \frac{0.05 \times 10^{-2}}{(4\pi \times 10^{-7})(12 \times 10^{-4} + 1.05)} =$$

N_f changes for one material

~~96.21258~~

$$\Phi = \frac{N i}{R_{\text{total}}}$$

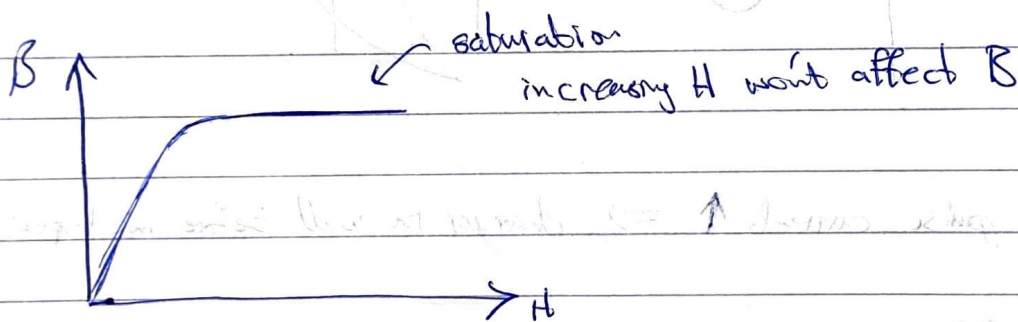
$$\Phi \cdot BA = \frac{(400)(i)}{R_{\text{total}}}$$

$$(0.5)(12 \times 10^{-4})(1.05) = \frac{(400)(i)}{R_{\text{total}}}$$

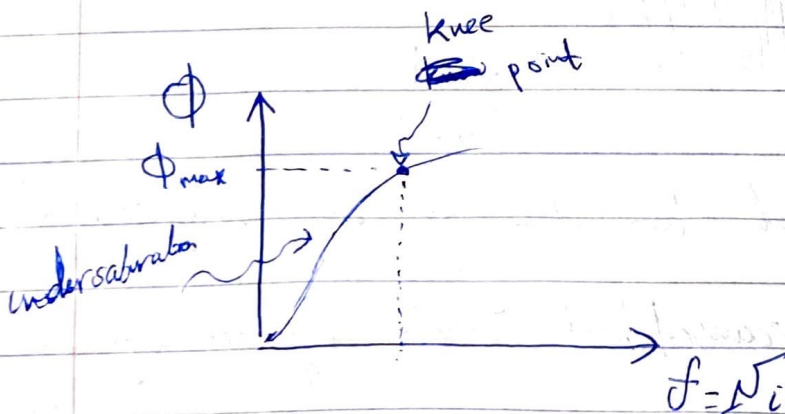
air gap area

the increase of μ because of leakage

* Magnetization curve or Saturation curve (2 plots)



* rated value for device $\Rightarrow$ value for best performance
nominal value without harming the device



a knee point $\rightarrow$ best performance with least current

$$I \uparrow \rightarrow \Phi \uparrow$$

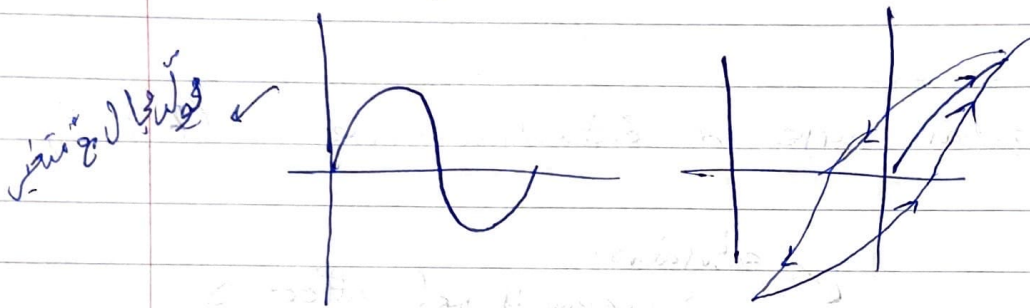
* losses in Core

- ① ☒ Hysteresis losses in one cycle

القوة الدافعة المغناطيسية $\Rightarrow$ reorientation of the magnetic domains

Ideal $\Rightarrow$ least losses when it goes & returns core at same curve.

* losses appear as heat problems

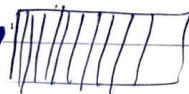


* pulse current $\uparrow \Rightarrow$ charger in wall before in laptop

- ② ☒

* to reduce eddy current & keep same performance

put slices of material



$\rightarrow$ steel lamination
How?

search How steel lamination reduce eddy current?

because of heat dissipation, reduction of eddy current will reduce heat

eddy current

current induced because of time changing in magnetic field on closed path of core it causes heat dissipation, that can be solved using steel lamination.

*
$$e_{\text{ind}} = -N \frac{d\phi}{dt}$$

because of Lenz's Law