

❖ After trying several pressure angles ~~✓~~ the one that fixed with the values given was 22.5 degree. ✓

Data Given: External Gear, $V_R = 3.7$, $C \leq 100$ mm.

From Interference theory and equation the teeth numbers will be found

$$(N_P)_{\min} = \frac{2K}{(1+2V_R)\sin^2\phi} [VR + \sqrt{VR^2 + (2VR + 1)\sin^2\phi}] \dots\dots\dots (1)$$

Consider $K=1$, Full depth teeth.

$$(N_P)_{\min} = \frac{2}{(1+2*3.7)\sin^2 22.5} [3.7 + \sqrt{3.7^2 + (2 * 3.7 + 1)\sin^2 22.5}].$$

$$(N_P) \geq 12.3.$$

Take $N_P = 13$ teeth.

$$(N_g)_{\max} = \frac{NP^2 \sin^2\phi - 4K^2}{4K - 2*NP \sin^2\phi} \dots\dots\dots (2)$$

$$(N_g) \leq 107.852.$$

Take $N_g = 48$ teeth.

$$V_R = \frac{N_g}{N_P} = \frac{48}{13} = 3.7 \text{ as given.}$$

$$C = \frac{N_P + N_g}{2} * m, \quad m: \text{ is the module } \dots\dots\dots (3).$$

Assume $C = 90$ mm,

From the previous equation

$$m = 2.95.$$

Take $m = 3$ for standard value then by substituting m in the previous equation we have $C = 91.5$ mm. ✓

❖ For Pinion :

$$m = \frac{dp}{Np} \dots\dots\dots (4)$$

$$d_p = N_p * m = 13 * 3 = \mathbf{39 \text{ mm}}$$

$$d_{bp} = d_p * \cos \Phi \dots\dots\dots (5)$$

$$d_{bp} = 39 * \cos 22.5 = \mathbf{36.03 \text{ mm}}$$

$$\text{Addendum radius } r_{ap} = r_p + m \dots\dots\dots (6)$$

$$r_{ap} = 19.5 + 3 = \mathbf{22.5 \text{ mm}}$$

$$\text{Dedendum radius } r_{dp} = r_p - 1.25m \dots\dots\dots (7)$$

$$r_{dp} = 19.5 - 3.75 = \mathbf{15.75 \text{ mm}}$$

❖ For Gear :

From equation (4)

$$d_g = 48 * 3 = \mathbf{144 \text{ mm}}$$

From equation (5)

$$d_{bg} = 144 * \cos 22.5 = \mathbf{133.04 \text{ mm}}$$

From equation (6)

$$r_{ag} = 72 + 3 = \mathbf{75 \text{ mm}}$$

From equation (7)

$$R_{dg} = 72 - 3.75 = \mathbf{68.25 \text{ mm}}$$

❖ Contact Ratio Check

$$C.R = \frac{Lab}{Pb} \dots\dots\dots (8)$$

$$L_{ab} = \sqrt{rap^2 - rbp^2} + \sqrt{rag^2 - rgb^2} - C * \sin \phi \dots\dots\dots (9)$$

$$L_{ab} = \sqrt{22.5^2 - 18.015^2} + \sqrt{75^2 - 66.52^2} - 91.5 \sin 22.5$$

$$L_{ab} = \mathbf{13.10675}.$$

$$P_b = P_c \cos \Phi \dots\dots (10)$$

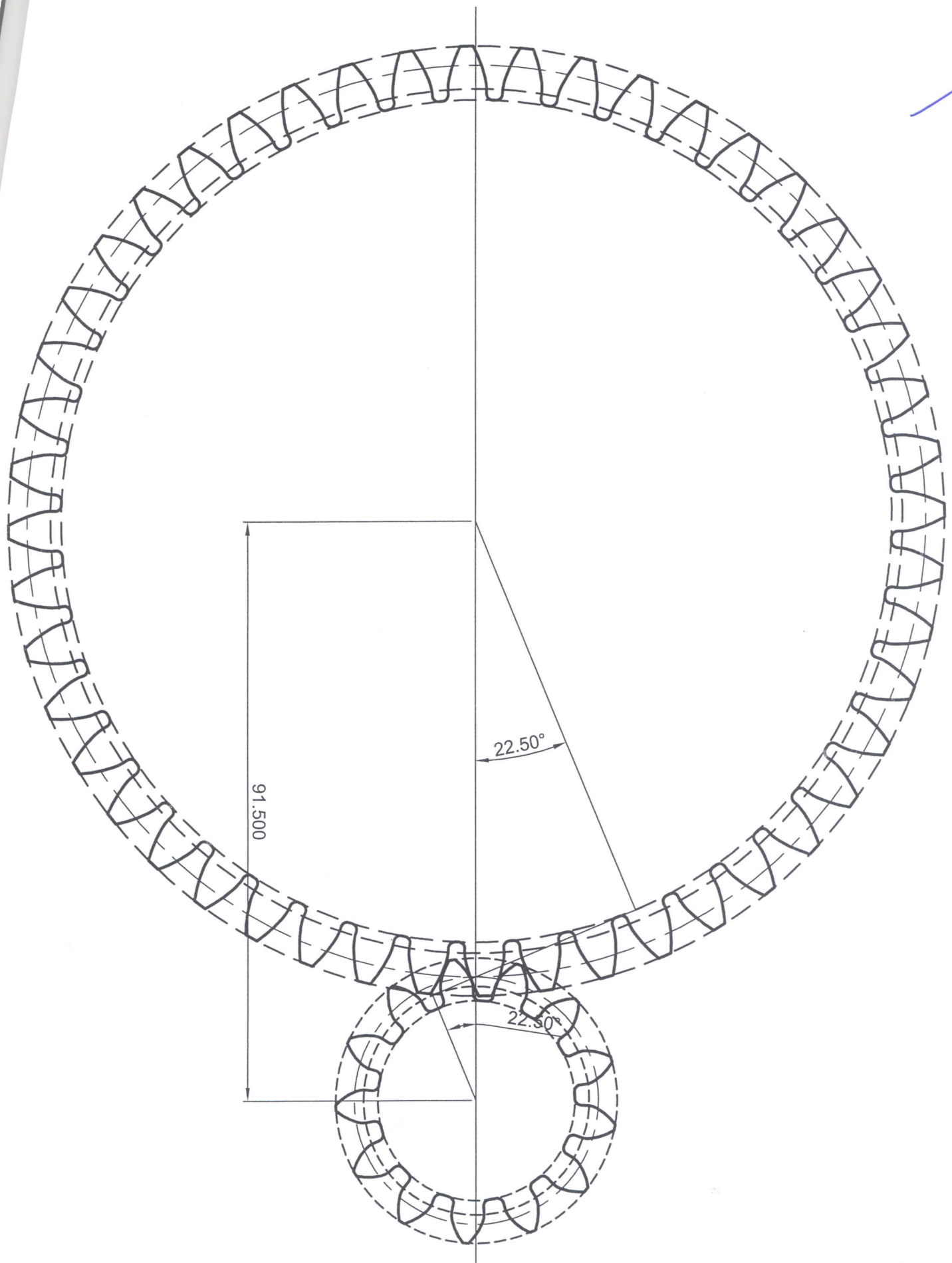
$$\text{But } P_c = \pi m \dots\dots (11)$$

$$P_c = \mathbf{3\pi}$$

$$P_b = 3\pi \cos 22.5$$

$$P_b = \mathbf{8.707}$$

$$C.R = \frac{13.10675}{8.707} = \mathbf{\underline{1.50525}} > 1$$



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22.50°