

فيزياء 2

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طريقة دراسة المادة :

- ١- متابعة للمحاضرات أول بأول وعدم المراكمة ضروريين.
- ٢- حل الاوتلاين كل نهاية تشابتر وإذا اجى الفاينال أو الميڊ ومش حالينهم ما تضيعوا وقت عليهم وحلوا فورمات كثير ضروري.
- ٣- فورمات ثم فورمات ثم فورمات حرقياً إذا درستوا فورمات هتربطوا.
- ٤- وتوكلوا على الله واعطوها حقها سهلة بس بدها تركيز وان شاء الله موفقين.

Chapter 21:

$$q = \pm ne., n=1,2,3,\dots$$

$$e = 1.6 \times 10^{-19} \text{ C.}$$

$$q_e = -1.6 \times 10^{-19} \text{ C.}$$

$$q_p = 1.6 \times 10^{-19} \text{ C.}$$

$$m_e = 9.11 \times 10^{-31} \text{ kg.}$$

Repulsive force: $F_{12} \leftarrow \oplus \text{ } q_1 \text{ --- } \oplus \text{ } q_2 \rightarrow F_{21}$
لـ قـوـى التـجـاذـب

Attractive force: $\Rightarrow$ قـوـى التـجـاذـب $q_1 \ominus \xrightarrow{F_{12}} \quad \xleftarrow{F_{21}} \oplus q_2$

Electric force: $\Rightarrow F = k \frac{q_1 q_2}{r^2}$

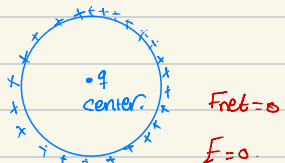
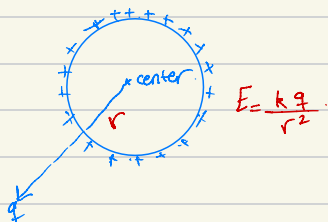
K depends on :

1- medium between q_1 & q_2 .

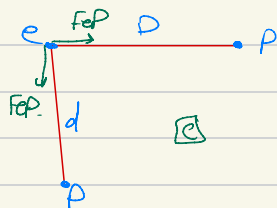
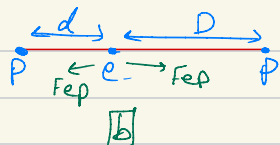
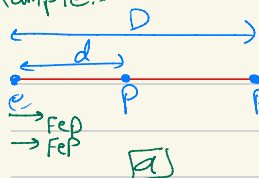
2- units in the air (vacume) $= k = 9 \times 10^9 \text{ N.m}^2/\text{C}^2$.

$$\hookrightarrow k = \frac{1}{4\pi\epsilon_0}, \quad \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N.m}^2$$

$\hookrightarrow$ permittivity constant for air (vacume).



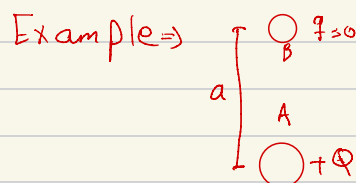
Example:-



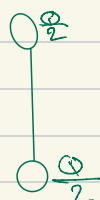
$\Rightarrow$ largest $\Rightarrow a > c > b$.

$\Rightarrow$ In the situation C, is the angle between the net force and line d less than or more than 45° ? $\Rightarrow$ less than 45°

$\hookrightarrow \phi = 0$ because $F_{ep} > F_{ep}$
d D



بقدر التماس



$$\Rightarrow \text{So } F = \frac{k q_1 q_2}{r^2} = \frac{k \frac{Q}{2} \frac{Q}{2}}{a^2} = \frac{k Q^2}{4a^2}$$

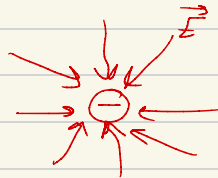
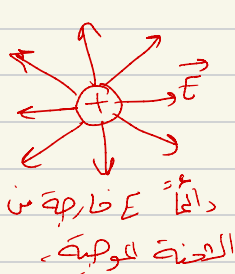
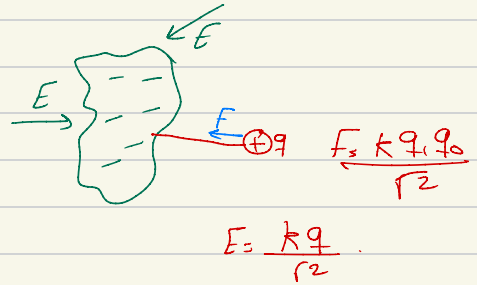
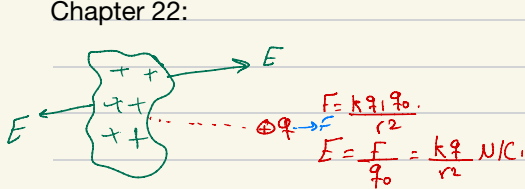
Gravitational force: $\Rightarrow F = G \frac{m_1 m_2}{r^2}$

$$6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$$

If we change proton into neutron so we will have a positron, e^+

If we change neutron into proton so we will have an electron, e^-

Chapter 22:



حالات التعداد :

- ١- عندي شحنتان متماثلتان (موجبتين أو سالبتين) : خارج الخط الواصل بينهما بعيداً عن الشحنة الأصغر غالباً.
- ٢- عندي شحنتان مختلفتين: داخل المسافة بينهما على الخط الواصل بينهما أقرب إلى الشحنة الأصغر.
- ٣- عندي شحنتان مختلفتين ومتساويتين : منتصف المسافة بينهما مباشرة.

Electric dipole:

$$P = q d$$

$$V_f = v_i + at$$

$$V_f^2 = v_i^2 + 2ad$$

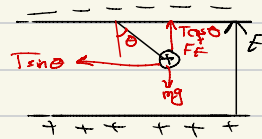
$$d = v_i t + 0.5 a t^2$$

$$W = F \cdot d = F d \cos \theta$$

$$W = q (E \cdot d)$$

$$W_{\text{net}} = K$$

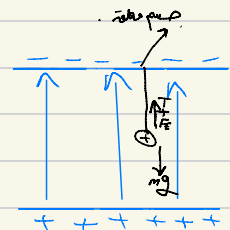
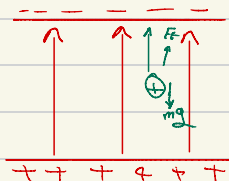
$$W = 0.5 m (V_f^2 - V_i^2)$$



$$F = m a$$

$$E q = m a$$

$$E = \frac{m a}{q}$$



Potential energy:

$$U = -P \cdot E$$

$$U = -P E \cos \theta.$$

Torque:

$$\tau = P \times E$$

$$\tau = P E \sin \theta.$$

example $\Rightarrow \vec{p} = 2\hat{i} + 3\hat{j}$.

$$\vec{E} = 2\hat{i} + \hat{j}.$$

$$\Rightarrow \tau = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 3 & 0 \\ 2 & 1 & 0 \end{vmatrix} = (2 \cdot 0) \hat{i} - (2 \cdot 0) \hat{j} + (-4) \hat{k}.$$

$$= -4\hat{k}.$$

1- linear charge density : $\lambda = \frac{q}{L}$



نسبة الشحنة لكل وحدة طول

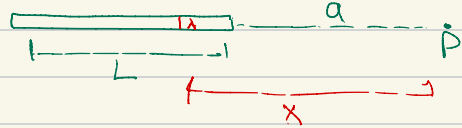
2- surface charge density : $\sigma = \frac{q}{A}$

3- volume charge density : $\rho = \frac{q}{V}$

دائماً تكون فيها موجبة

Rod :

من الشحنة في كل وحدة طول



$$dq = \lambda dx.$$

$$E = \frac{k \lambda L}{a(L+a)}.$$

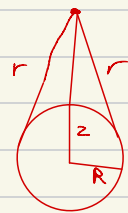
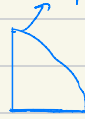
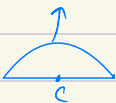
Ring :

$$E = \frac{2k \lambda}{R}$$

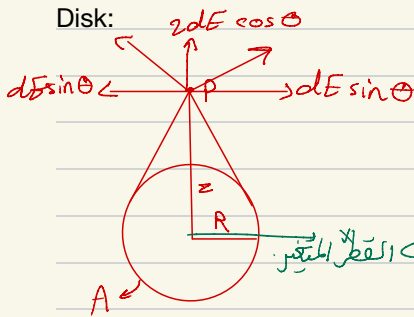
$$E = \frac{k \lambda}{R}$$



$$E = 0$$



$$E = \frac{2\pi R k \lambda z}{(R^2 + z^2)^{3/2}}$$



$$dq = \sigma dA$$

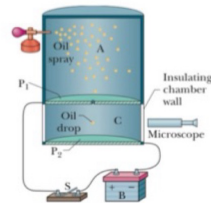
$$\cos \theta = \frac{z}{r}$$

$$\therefore E = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{z}{\sqrt{z^2 + R^2}} \right]$$

if $z \gg R \Rightarrow E = 0$

if $R \gg z \Rightarrow E = \frac{\sigma}{2\epsilon_0}$

33 In Millikan's experiment, an oil drop of radius $1.64 \mu\text{m}$ and density 0.851 g/cm^3 is suspended in chamber C (Fig. 22-16) when a downward electric field of $3.20 \times 10^5 \text{ N/C}$ is applied. (a) Find the charge on the drop, in terms of e . (b) If the drop had an additional electron, would it move upward or downward?



$r = 1.64 \times 10^{-6} \text{ m}$, $\rho = 0.851 \text{ g/cm}^3$, $E = 3.2 \times 10^5$
 $851 = \text{بليسر}$

The drop in equilibrium $\Rightarrow \Sigma F = 0$

The mass of the drop $= V\rho = \frac{4}{3}\pi R^3 \rho$

$$F_E = mg$$

$$Eq = mg$$

$$3.2 \times 10^5 q = \frac{4}{3}\pi (1.64 \times 10^{-6})^3 \times 851 \times 10$$

$$q = 4.91 \times 10^{-19}$$

$$q = ne$$

$$n = \frac{-4.91 \times 10^{-19}}{1.6 \times 10^{-19}} = -3$$

$$q = -3e$$

(b) If it had an additional e so

$$q = -4e$$

$F_E > mg$ more upward.

38 An electron enters a region of uniform electric field with an initial velocity of 30 km/s in the same direction as the electric field,

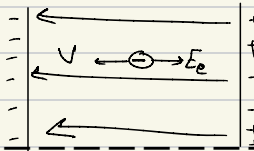
which has magnitude $E = 50 \text{ N/C}$. (a) What is the speed of the electron 1.5 ns after entering this region? (b) How far does the electron travel during the 1.5 ns interval?

$$V_i = 30 \text{ km/s} = 30000 \text{ m/s}$$

$$E = 50 \text{ N/C}$$

$$t = 1.5 \times 10^{-9} \text{ s} \quad V_f = ?? \quad \Delta x = ??$$

$$m = 9.11 \times 10^{-31}$$



11 In Fig. 22-27, two curved plastic rods, one of charge $+q$ and the other of charge $-q$, form a circle of radius $R = 4.25 \text{ cm}$ in an xy plane. The x axis passes through both of the connecting points, and the charge is distributed uniformly on both rods. If $q = 15.0 \text{ pC}$, what are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the electric field E produced at P , the center of the circle?

Figure 22-26 Problem 10.

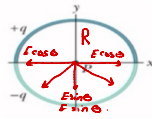


Figure 22-27 Problem 11.

$$dE_y = dE \sin \theta$$

$$\lambda = \frac{q}{s} = \frac{q}{\pi R}$$

$$dE_x = \frac{k \lambda R d\theta}{R^2} \sin \theta$$

$$= \frac{k \lambda R d\theta}{R^2} \sin \theta$$

$$E_y = \frac{k \lambda}{R} \int_0^\pi \sin \theta d\theta = \frac{k \lambda}{R} [-\cos \theta]_0^\pi$$

$$= -\frac{k \lambda}{R} - \frac{k \lambda}{R} = -\frac{2k \lambda}{R}$$

$$= -2 \times 9 \times 10^9 \times 1.12 \times 10^{-10} = -47.43 \text{ V/m}$$

$$4.25 \times 10^{-2}$$

$$\theta = 90^\circ (\downarrow)$$

$$\lambda = \frac{q}{s} = \frac{15 \times 10^{-12}}{4.25 \times 10^{-2} \times \frac{\pi}{180} \times 180}$$

$$\lambda = 1.12 \times 10^{-10}$$

14 In Fig. 22-29, a thin glass rod forms a semicircle of radius $r = 3.00 \text{ cm}$. Charge is uniformly distributed along the rod, with $+q = 4.50 \text{ pC}$ in the upper half and $-q = -4.50 \text{ pC}$ in the lower half. What are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the electric field E at P , the center of the semicircle?

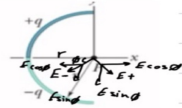


Figure 22-29 Problem 14.

$$dE_y = -dE \sin \theta$$

$$S = \pi r$$

$$= -\frac{k dq}{r^2} \sin \theta$$

$$ds = r d\theta, \quad \sigma = \frac{q}{s}$$

$$= -\frac{k \sigma r d\theta}{r^2} \sin \theta$$

$$\sigma ds = dq$$

$$= -\frac{k \sigma}{r} \int_0^\pi \sin \theta d\theta = -\frac{k \sigma}{r} [-\cos \theta]_0^\pi$$

$$\sigma r d\theta = dq$$

$$= \frac{k \sigma}{r} [\cos \frac{\pi}{2} - \cos 0] \Rightarrow E_1 = -\frac{k \sigma}{r}$$

$$E_2 = E_1$$

$$E_{\text{net}} = E_1 + E_2$$

$$= \frac{k \sigma}{r} + \frac{k \sigma}{r} = \frac{2k \sigma}{r}$$

23 A 10.0 g block with a charge of $+8.00 \times 10^{-5} \text{ C}$ is placed in an electric field $\vec{E} = (3000\hat{i} - 6000\hat{j}) \text{ N/C}$. What are the (a) magnitude

and (b) direction (relative to the positive direction of the x axis) of the electrostatic force on the block? If the block is released from rest at the origin at time $t = 0$, then at $t = 3.00 \text{ s}$ what are its (c) x and (d) y coordinates and (e) its speed?

$$m = 10 \times 10^{-3} \text{ kg}, q = 8 \times 10^{-5} \text{ C}, E = (3000\hat{i} - 6000\hat{j})$$

$$v_i = 0, t = 3$$

$$F = ??$$

$$\boxed{1} F = qE = 2.4 \times 10^{-11} \hat{i} - 4.8 \times 10^{-11} \hat{j} = 5.37 \times 10^{-11}$$

$$F_x = ma_x$$

$$2.4 \times 10^{-11} = 10 \times 10^{-3} a_x$$

$$a_x = 2.4 \times 10^{-9}$$

$$\left\{ \begin{array}{l} F_y = ma_y \\ -4.8 \times 10^{-11} = 10 \times 10^{-3} a_y \end{array} \right.$$

$$a_y = -4.8 \times 10^{-9}$$

$$\boxed{2} \Delta x = v_x t + \frac{1}{2} a_x t^2$$

$$= 0 + \frac{1}{2} (2.4 \times 10^{-9}) (9) = 1.08 \times 10^{-8}$$

$$\Delta y = v_y t + \frac{1}{2} a_y t^2$$

$$= 0 + \frac{1}{2} (9) (-4.8 \times 10^{-9}) = -2.16 \times 10^{-8}$$

$$\boxed{3} v_{fx} = v_{ix} + at$$

$$= 0 + 3 \times 2.4 \times 10^{-9} = 7.2 \times 10^{-9}$$

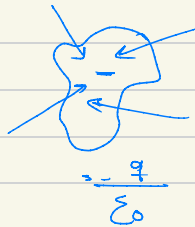
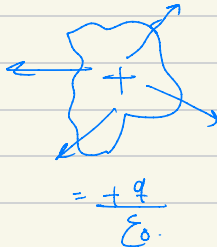
$$v_{fy} = v_{iy} + at$$

$$= 0 + (4.8 \times 10^{-9}) \times 3 = 1.44 \times 10^{-8}$$

Chapter 23:

* Electric Flux $\Rightarrow \Phi = \vec{E} \cdot \vec{A} = EA \cos \theta$. (إذا الخط 0)
 $\Phi = \int \vec{E} \cdot d\vec{A} \Rightarrow$ (إذا الخط 0)

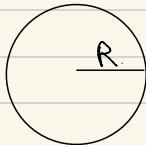
* $\Phi = \frac{q_{enc}}{\epsilon_0}$. * $\int \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$.



Applications on Gauss's law :

1- spherical symmetry:

E due to a uniformly charged conducting sphere: $\rightarrow \sigma = \frac{q}{A} = \frac{q}{4\pi R^2}$

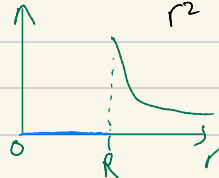


$$\rho = \frac{q}{V} = \frac{q}{\frac{4}{3}\pi R^3}$$

E at $r > R = \frac{kq}{r^2}$

E at $r < R = 0$

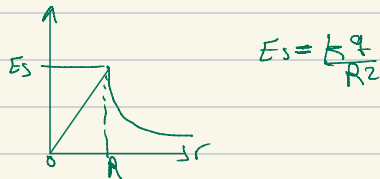
E at $r = R = \frac{kq}{r^2}$



E due to a uniformly charged nonconducting solid sphere: $\rightarrow \rho = \frac{q}{V} = \frac{q}{\frac{4}{3}\pi R^3}$

For $r > R \Rightarrow \int E \cdot dA = \frac{q}{\epsilon_0} = \frac{kq}{r^2}$

For $r < R \Rightarrow E_s = \frac{\rho r}{3\epsilon_0}$
 $\int E \cdot dA = \frac{q}{\epsilon_0}$ Volume



2- cylindrical symmetry :

E due to a uniformly charged infinite rod .

$\int E \cdot dA = \frac{q_{enc}}{\epsilon_0} \rightarrow \lambda h$
الحل

$E = \frac{\lambda}{2\pi r \epsilon_0} ; r \ll L$

3- planer symmetry :

E due to a uniformly charged thin infinite nonconducting surface:

$\int E \cdot dA = \frac{q_{enc}}{\epsilon_0} \rightarrow \sigma A$
 $EA + EA$ } $\Rightarrow E = \frac{\sigma}{2\epsilon_0}$

4- a charged isolated conductor :

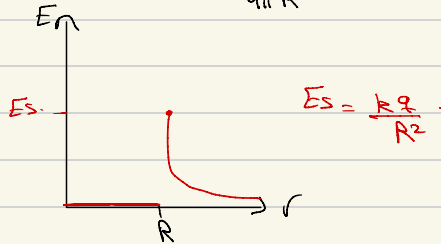


$\Rightarrow E_{inside} = 0$
 $q_{inside} = 0$
 $E_{outside} = \frac{\sigma}{\epsilon_0}$

5- E due to a uniformly charged conducting sphere: $\rightarrow \sigma = \frac{q}{4\pi R^2}$

$\rightarrow E \text{ at } r < R = 0.$

$\rightarrow E \text{ at } r \geq R = \frac{kq}{r^2}$



E due to a uniformly charged conducting sphere :

$E \text{ at } r < R = 0.$

$E \text{ at } r \geq R = \frac{kq}{r^2}$

E due to a uniformly charged nonconducting solid sphere:

$E = \frac{kq}{r^2}, r \geq R.$

$E = \frac{\rho r}{3\epsilon_0}, r \leq R.$

E due to a uniformly charged infinite rod :

$$E = \frac{\lambda}{2\pi r \epsilon_0}$$

E due to a uniformly charged thin infinite nonconducting surface:

$$E = \frac{\sigma}{2\epsilon_0}$$

A charged isolated conductor: $E = \frac{\sigma}{\epsilon_0}$

17 In Fig. 23-30, a proton is a distance $d/2$ directly above the center of a square of side d . What is the magnitude of the electric flux through the square? (Hint: Think of the square as one face of a cube with edge d .)

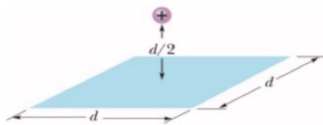


Figure 23-30 Problem 17.

$$\phi_{\text{cube}} = \frac{q_{\text{enc}}}{\epsilon_0} = \frac{1.6 \times 10^{-19}}{8.85 \times 10^{-12}} = 1.8 \times 10^{-8}$$

$$\phi_{\text{for one face}} = \frac{1.8 \times 10^{-8}}{6} = 3.0 \times 10^{-9}$$

3 An unknown charge sits on a conducting solid sphere of radius 10 cm. If the electric field 30 cm from the center of the sphere has the magnitude $3.0 \times 10^3 \text{ N/C}$ and is directed radially inward, (a) what is the net charge on the sphere? and (b) what is the charge density?

$$a) E = \frac{kq}{r^2}$$

$$-3 \times 10^3 = \frac{9 \times 10^9 q}{(0.3)^2} \Rightarrow q = -3 \times 10^{-8}$$

$$b) \sigma = \frac{q}{A} = \frac{-3 \times 10^{-8}}{4\pi (0.1)^2} = -2.38 \times 10^{-8}$$

Chapter 24:

$$F = qE \Rightarrow U = qV.$$

$$W = \int_i^f q \vec{E} \cdot d\vec{s} = -(u_f - u_i).$$

$$U_f = -q \int_{\infty}^f \vec{E} \cdot d\vec{s}.$$

$$V_f = - \int_{\infty}^f E \cdot ds = \frac{kq}{r_f}$$

$$V = \frac{1}{q} \text{ J/C (volt)}.$$

$$V_f - V_i = - \int E \cdot d\vec{s}.$$

$$E = \frac{kq}{r^2}.$$

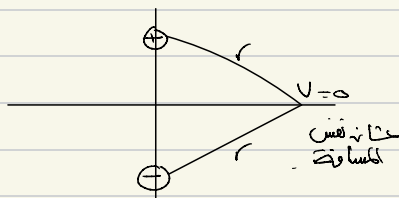
$$V = \frac{kq}{r}.$$

V due to an electric dipole :

$$V = \frac{kp}{z^2 - a^2}, \quad p = qd, \quad d = 2a.$$

الحالة البعيدة عن القطب (z > a)

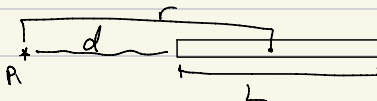
for $z \gg a \Rightarrow V = \frac{kp}{z^2}.$



Potential due to a continues distribution:

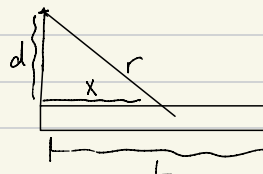
1- v due to a uniformly charged rod (line of charge):

$$V = k \lambda \ln \left(\frac{d+L}{d} \right).$$



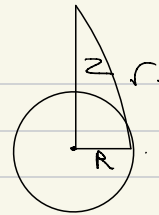
$$V = kC \left[\sqrt{d^2 + x^2} - d \right]$$

$$\lambda = Cx$$



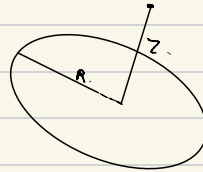
2- v due to a uniformly charged ring :

$$\lambda = \frac{q}{2\pi R} \Rightarrow V = \frac{kq}{\sqrt{z^2 + R^2}}$$



3- v due to a uniformly charged disk :

$$V = \frac{\sigma}{2\epsilon_0} \left[\sqrt{R^2 + z^2} - z \right]$$



$$E_x = -\frac{dV}{dx}, \quad E_y = -\frac{dV}{dy}, \quad E_z = -\frac{dV}{dz}$$

$$U_{12} = \frac{kq_1 q_2}{r_{12}} \rightarrow \text{جهد التفاعل}$$

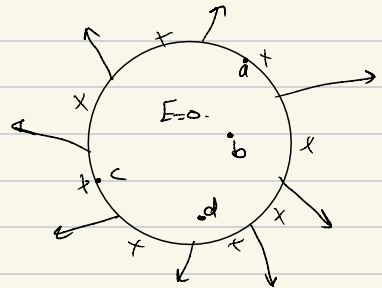
Potential of charged isolated conductor:

1- the charge inside the conductor = 0.

2- E inside the conductor = 0.

3- E near the outer surface = $\frac{\sigma}{\epsilon_0}$

4- all points have the same potential. $\phi_a = \phi_c = \phi_b = \phi_d$.



charged isolated conducting sphere :

$$\sigma = \frac{q}{4\pi R^2}, \quad \rho = 0$$

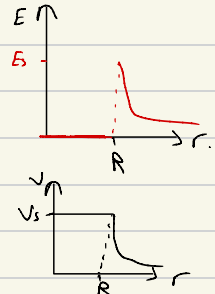
$$E_s = \frac{kq}{R^2}, \quad E_s = \frac{\sigma}{\epsilon_0}, \quad U_s = \frac{kq}{R} \quad r < R$$

$\hookrightarrow V_{\text{inside}}$

$E_{\text{inside}} = 0$

$$E_{\text{outside}} = \frac{kq}{r^2}, \quad r \geq R$$

$$U_{\text{outside}} = \frac{kq}{r}, \quad r \geq R$$



Chapter 25:

$$\Rightarrow C = \frac{q}{V} \quad \text{c/volt} = \text{farad}$$

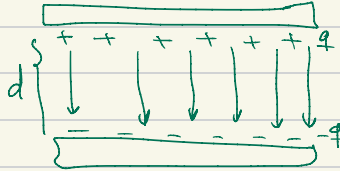
conducting sphere $\Rightarrow V = \frac{kq}{R}$, $C = kR$.

Parallel plate capacitor:

$$E = \frac{q}{\epsilon_0 A}$$

$$V = \frac{q d}{\epsilon_0 A}$$

$$C = \frac{\epsilon_0 A}{d}$$

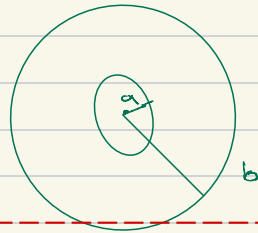


Spherical capacitor:

$$E = \frac{kq}{r^2}$$

$$V = kq \left[\frac{b-a}{ab} \right]$$

$$C = \frac{kab}{b-a}$$



Cylindrical capacitor: $\Rightarrow E = \frac{\lambda}{2\pi r \epsilon_0}$, $V = \frac{\lambda}{2\pi r \epsilon_0} \ln\left(\frac{b}{a}\right)$, $C = \frac{q}{V}$.

Energy density $\Rightarrow u = \frac{U}{\text{Volume}} = 1 - \frac{1}{2} \epsilon_0 \frac{V^2}{d^2}$
 $2 - \frac{1}{2} \epsilon_0 \left(\frac{V}{d}\right)^2$
 $3 - \frac{1}{2} \epsilon_0 E^2$

$U = \text{Area} \cdot u$ / q vs V curve.

$$1 - \frac{1}{2} qV$$

$$2 - \frac{1}{2} CV^2$$

$$3 - \frac{1}{2} \frac{q^2}{C}$$

Capacitor with dielectric $\Rightarrow K = \frac{\epsilon}{\epsilon_0} > 1 \Rightarrow C = KC_0$
 $= K \left(\frac{\epsilon_0 A}{d} \right)$

Capacitor in parallel $\Rightarrow q_{\text{total}} = q_1 + q_2 + q_3 = C_1 V_1 + C_2 V_2 + C_3 V_3$

$$V_{\text{total}} = V_1 = V_2 = V_3$$

$$C_{\text{eq}} = C_1 + C_2 + C_3 \Rightarrow C = \frac{\epsilon_0 A}{d}$$

Capacitor in series $\Rightarrow q_1 = q_2 = q_3 = q_{\text{total}}$.

$$V = V_1 + V_2 + V_3 \Rightarrow V = \frac{q_1}{C_1} + \frac{q_2}{C_2} + \frac{q_3}{C_3}$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

2 In Fig. 25-18, a potential difference $V = 75.0 \text{ V}$ is applied across a capacitor arrangement with capacitances $C_1 = 10.0 \mu\text{F}$, $C_2 = 5.00 \mu\text{F}$, and $C_3 = 15.0 \mu\text{F}$. What are (a) charge q_3 , (b) potential difference V_3 , and (c) stored energy U_3 for capacitor 3, (d) q_1 , (e) V_1 , and (f) U_1 for capacitor 1, and (g) q_2 , (h) V_2 , and (i) U_2 for capacitor 2?

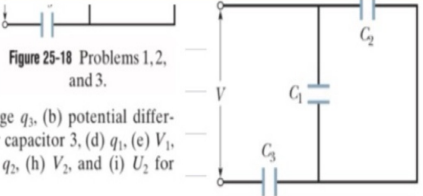


Figure 25-18 Problems 1, 2, and 3.

Figure 25-18 Problems 1, 2,

$$V = 75.$$

$$C_1 = 10 \mu\text{F}.$$

$$C_2 = 5 \mu\text{F}.$$

$$C_3 = 15 \mu\text{F}.$$

$$C_{12} = C_1 + C_2 = 15 \mu\text{F} \Rightarrow \frac{1}{C_{eq}} = \frac{1}{15 \mu\text{F}} + \frac{1}{15 \mu\text{F}} = \frac{2}{15 \mu\text{F}}$$

$$C_{eq} = 7.5 \mu\text{F}.$$

$$q_{eq} = \frac{q_{eq}}{V} \Rightarrow q_{eq} = 75 \times 7.5 = 562.5 \mu\text{C}.$$

a) $q_3 = 562.5 \mu\text{C}.$

b) $U_3 = \frac{q_3}{C_3} = \frac{562.5 \mu\text{C}}{15 \mu\text{F}} = 37.5.$

c) $U_1 = U_2 = 75 - 37.5 = 37.5.$

d) $q_1 = C_1 U_1 = 37.5 \times 10 \mu = 375 \mu.$

e) $q_2 = U_2 C_2 = 37.5 \times 5 \mu = 187.5 \mu.$

f) $U_3 = \frac{1}{2} C_3 U_3^2 = \frac{1}{2} (15 \mu) (37.5)^2 = 10546.875 \text{ MJ}.$

g) $U_1 = \frac{1}{2} C_1 U_1^2 = \frac{1}{2} (10 \mu) (37.5)^2 = 7031.25 \text{ MJ}.$

h) $U_2 = \frac{1}{2} C_2 U_2^2 = \frac{1}{2} (5 \mu) (37.5)^2 = 3515.625 \text{ MJ}.$

$\Leftarrow$ the negative (work) in pushing them ^{together} ~~apart~~
 $W = \Delta U = u_f - u_i$
 $\underbrace{u_f}_{\text{positive}} - \underbrace{u_i}_{\text{positive}}$

P53: A 100 pF capacitor is charged to a potential difference of 80.0 V and the charging battery is disconnected. The capacitor is then connected in parallel with a second (initially uncharged) capacitor. If the potential difference across the first capacitor drops to 35.0 V , what is the capacitance of this second capacitor?

Sol: $Q = CV$

q_i : before the charging battery is disconnected

$$q_i = C_1 V = 100\text{ pF} \times 80\text{ V} = 8000\text{ pC}$$

q_f : after the charging battery is disconnected and connected in parallel with C_2

$$q_f = C_2 V = 100\text{ pF} \times 35 = 3500\text{ pC}$$

q_2 : the charge on capacitor 2

$$q_2 = q_i - q_f$$

$$= 8000\text{ pC} - 3500\text{ pC}$$

$$q_2 = 4500\text{ pC}$$

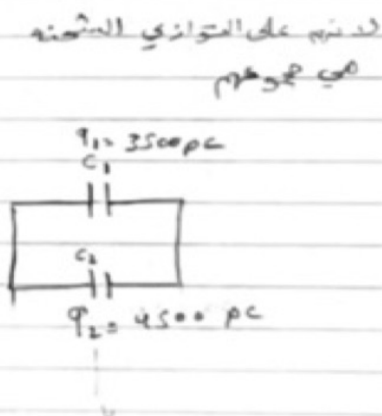
$$q_2 = C_2 V$$

$$C_2 = \frac{q_2}{V}$$

$$= \frac{4500 \times 10^{-9}}{35}$$

$$= 128.57 \times 10^{-9}$$

$$\approx 129\text{ pF}$$



31 Figure 25-30 shows a parallel-plate capacitor with a plate area $A = 7.89 \text{ cm}^2$ and plate separation $d = 4.62 \text{ mm}$. The top half of the gap is filled with material of dielectric constant $\kappa_1 = 11.0$; the bottom half is filled with material of dielectric constant $\kappa_2 = 4.0$. What is the capacitance?

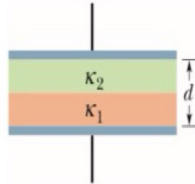


Figure 25-30

$$A = 7.89 \times 10^{-4}$$

$$d = 4.62 \times 10^{-3}$$

$$C_1 = \frac{\kappa \epsilon_0 A}{d}$$

$$= \frac{11 \times 8.85 \times 10^{-12} \left(\frac{7.89 \times 10^{-4}}{2} \right)}{\left(\frac{4.62 \times 10^{-3}}{2} \right)}$$

$$= 1.66 \times 10^{-11}$$

$$C_2 = \frac{\kappa \epsilon_0 A}{d} = 6.05 \times 10^{-12}$$

$$C_{eq} = \frac{1}{\frac{1}{1.66 \times 10^{-11}} + \frac{1}{6.05 \times 10^{-12}}} \Rightarrow C_{eq} = 2.26 \times 10^{-11} \text{ C}$$

$$\star F = \frac{q^2}{2\epsilon_0 A} = \frac{qE}{2}, U = \frac{q^2}{2C} = \frac{q^2 d}{2\epsilon_0 A}$$

Chapter 26:

$$* I = \frac{dq}{dt} = \int \vec{J} \cdot d\vec{A} = J A = \frac{\Delta q}{\Delta t} = \frac{en A L}{\Delta t} = en A v_d \text{ Vol.}$$

السرعة الانزياحية = drift speed.

number of electrons in the wire = $n A L$.

$$q = en A L.$$

$$* J = \frac{I}{A} = en A v_d.$$

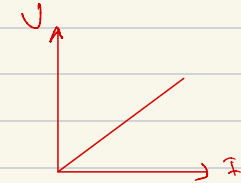
$$* V = E L.$$

$$* E = \rho J.$$

$$* R = \frac{\rho L}{A}.$$

$$* \sigma = \frac{1}{\rho}.$$

$$* V = I R.$$



$$* P - P_0 = P_0 \alpha (T - T_0).$$

$$* R - R_0 = R_0 \alpha (T - T_0).$$

Resistors in series $\Rightarrow V = V_1 + V_2 + V_3.$

$$V = I R_1 + I R_2 + I R_3.$$

$$R_{eq} = R_1 + R_2 + R_3.$$

$$I_{eq} = I_1 = I_2 = I_3.$$

Resistors in parallel $\Rightarrow V_{eq} = V_1 = V_2 = V_3.$

$$I = I_1 + I_2 + I_3.$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}.$$

$$* P = \frac{dU}{dt} = V I = \frac{E}{dE} \cdot I$$

$$= I^2 R$$

$$* \varepsilon = \frac{\Delta W}{\Delta q}$$

$$* t = \frac{L}{v_d} \text{ , زحلوا}$$

vd . عرسل

$$= \frac{V^2}{R}.$$

$$= \varepsilon I$$

$$= I V$$

$$* I = \frac{\varepsilon}{R} = \frac{\varepsilon}{R + r}.$$

3 An electrical cable consists of 63 strands of fine wire, each having $2.65 \mu\Omega$ resistance. The same potential difference is applied between the ends of all the strands and results in a total current of 0.750 A. (a) What is the current in each strand? (b) What is the applied potential difference? (c) What is the resistance of the cable?

$$R = 2.65 \times 10^{-6} \quad V \Rightarrow \text{سلسلة}$$

$$I = 0.75$$

$$a) I = \frac{I_{\text{total}}}{\text{number of strands}} = \frac{0.75}{63} = 0.0119 \text{ A}$$

$$b) V = IR = 0.0119 \times 2.65 \times 10^{-6} = 3.15 \times 10^{-8}$$

$$c) R = \frac{V}{I} = \frac{3.15 \times 10^{-8}}{0.75} = 4.2 \times 10^{-8}$$

Chapter 27:

$\mathcal{E}$ $\Rightarrow$ electromotive force of the power source.

$$\mathcal{E} = \frac{dw}{dq} \text{ J/C} = \text{Volt.}$$

$$P_E = \mathcal{E} I, \quad P_R = I^2 R \Rightarrow \text{consumed} : 20W \quad \text{supplied} \Rightarrow \dots$$

* Kirchhoff's $\Rightarrow \sum I_{\text{entering}} = \sum I_{\text{leaving}}.$
 $\sum V = 0.$

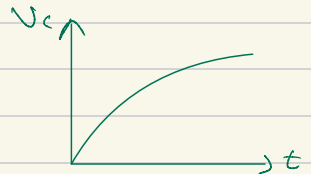
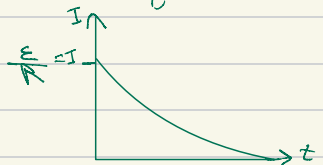
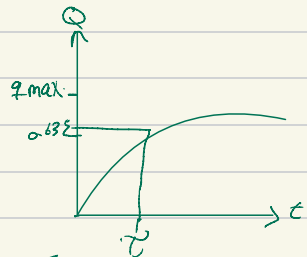
* Circuits :-

RC-circuit $\Rightarrow \mathcal{E} = RI + \frac{q}{C}$
 $q(t) = C\mathcal{E}(1 - e^{-t/RC})$
 $q(t) = C\mathcal{E}(1 - e^{-t/\tau})$

time constant $\tau = RC$

$$I = \frac{\mathcal{E}}{R} e^{-t/RC}$$

$$V_C(t) = \frac{q(t)}{C} = \mathcal{E}(1 - e^{-t/\tau})$$

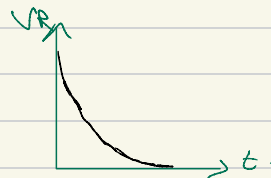


$$V_R = RI = \mathcal{E} e^{-t/\tau}$$

$$\Rightarrow Q_{\text{max}} = C\mathcal{E}$$

$$\mathcal{E} = \mathcal{E}_0 (e^{-t/\tau})$$

$$\mathcal{E} = \frac{W}{q}$$



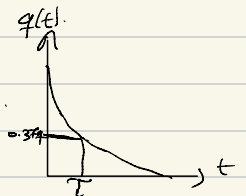
* Discharging a capacitor $\Rightarrow$

$$q(t) = q_{\text{max}} e^{-t/\tau}$$

$$I(t) = I_{\text{max}} e^{-t/\tau} = -\frac{q}{\tau} e^{-t/\tau}$$

$$E = \frac{q^2}{2C}$$

stored energy



15 What multiple of the time constant τ gives the time taken by an initially uncharged capacitor in an RC series circuit to be charged to 89.0% of its final charge?

$$Q(t) = Q_m(1 - e^{-t/\tau})$$

$$0.89 Q_m = Q_m(1 - e^{-t/\tau})$$

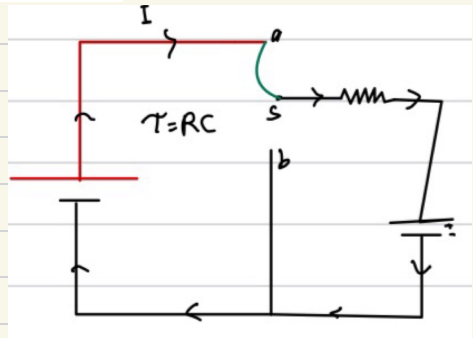
$$0.89 = 1 - e^{-t/\tau}$$

$$e^{-t/\tau} = 1 - 0.89$$

$$e^{-t/\tau} = 0.11$$

$$\frac{-t}{\tau} = \ln 0.11$$

$$t = -\tau(-2.21) \Rightarrow t = 2.21\tau$$



$$Q(t) = Q_m(1 - e^{-t/\tau})$$

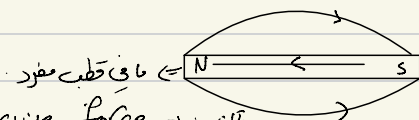
$$0.99 Q_m = Q_m(1 - e^{-t/\tau})$$

$$e^{-t/\tau} = 0.01$$

$$\frac{-t}{\tau} = \ln 0.01 \Rightarrow t = -\tau(-5)$$

$$t = 5\tau$$

Chapter 28:



$N-S \Rightarrow$ attractive force $\Rightarrow$ جذب

$N-N, S-S \Rightarrow$ repulsive force $\Rightarrow$ داف

$$\vec{F}_B = q \vec{v} \times \vec{B} = q v B \sin \theta$$

only changes the direction of v only.

it could not change K energy.

it could not change the magnitude of v .

$W_B = 0 \Rightarrow$ always.

$\vec{F}_B$ change the linear momentum ($m\vec{v}$).

$$K = \frac{1}{2} m v^2$$

Application on $q v \times B$:

q moves in a uniform circular motion:

$$r = \frac{m v}{q B}$$

$$v = \frac{q B r}{m}$$

$$T = \frac{2\pi m}{q B} = \frac{2\pi r}{v}$$

$$f = \frac{1}{T} = \frac{q B}{2\pi m}$$

Cyclotron: to accelerate charged particles:

$$K_{\max} = \frac{1}{2} m v_{\max}^2 = N Z q V = \frac{1}{2} \frac{q^2 B^2 R^2}{m}$$

$$v_{\max} = \frac{q B R}{m}$$

$$V = v_{\max} \sin \omega t = v_{\max} \sin(2\pi f t)$$

Mass spectrometer $\Rightarrow$ to measure mass of ions:-

$$q V = \frac{1}{2} m v^2, r = \frac{m v}{q B}$$

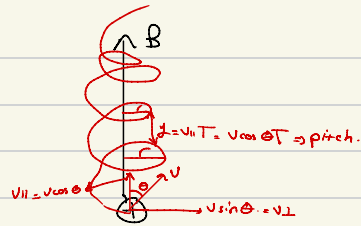
$$r^2 = \frac{2 m V}{q B^2}$$

$$M = \frac{q B^2 r^2}{2 V} = \frac{q B^2 x^2}{8 V}, r = \frac{x}{2}$$

Helical motion :

$$\frac{mv_{\perp}^2}{2} = q V_L B$$

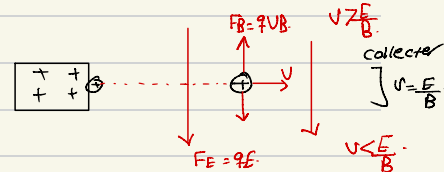
$$r = \frac{mv \sin \theta}{q B}, \quad T = \frac{2\pi r}{v_{\parallel}} = \frac{2\pi m}{q B}$$



Crossed field velocity selector :

$$F_B = F_E = 0$$

$$qVB - qE = 0 \Rightarrow v = \frac{E}{B} \text{ collected selected}$$



Hall effect (crossed fields):

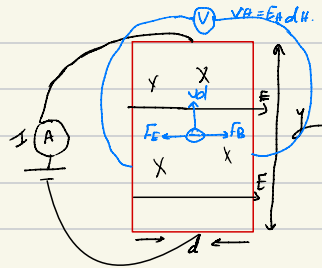
$$I = enAv_d$$

$$F = e v_d \times B$$

$$\text{at eq. equilibrium} \Rightarrow e v_d B = e E_H = \phi$$

$$v_d = \frac{E_H}{B} = \frac{V_H}{Bd}$$

$$n = \frac{IB}{e L V_H}$$



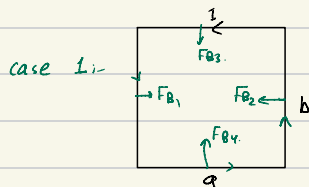
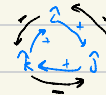
Lorentz force:

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

for (12) 2nd part

Magnetic force on a wire carrying current :

$$\vec{F} = I \vec{L} \times \vec{B} = ILB \sin \theta$$



$$\text{case 1: } \Rightarrow F_{\text{net}} = 0, \quad \tau_{\text{net}} = 0 \Rightarrow F = IL \times B$$

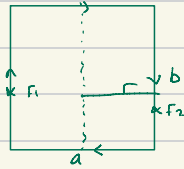
$$F_1 = I b B \uparrow$$

$$F_2 = I b B \leftarrow$$

$$F_3 = I b B \downarrow$$

$$F_4 = I b B \rightarrow$$

case 2:-



$$\Rightarrow F_{net} = 0, \tau \neq 0$$

$$\tau = r \times F = \frac{a}{2} \times (IbB) \text{ clockwise.}$$

$$\tau_{net} = I(ab)B \text{ clockwise.}$$

$$\tau_{net} = IAB.$$

$$\text{for } N \text{ Loops} \Rightarrow \tau_{net} = NIAB \text{ clockwise.}$$

case 3 $\Rightarrow$ general case $\Rightarrow$ There is an angle between $\vec{B}$ and the normal of the plane.

$$\tau = IabB \sin \theta.$$

Full Crossed Box Solution

$$\tau = NIabB \sin \theta = (NIA)B \sin \theta.$$

$$\times \text{ Magnetic dipole moment} \Rightarrow \tau = \mu B; \mu = NIA$$

$$\text{In general} \Rightarrow \tau = \mu \times B = \mu B \sin \theta.$$

$$\times \text{ Magnetic potential energy} \Rightarrow -\mu \cdot B$$

Remember $\Rightarrow$ Electric Dipole moment $= qd$.

$$\tau = P \times E, U = -P \cdot E.$$

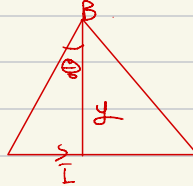
Chapter 29:

• $|dB| = \left(\frac{\mu_0}{4\pi} \right) \frac{I ds \sin \theta}{r^2}$. *المجال الناتج عن شريحة صغيرة*

$\mu_0 = 4\pi \times 10^{-7} \text{ T.m/A}$

B due to I in a long straight wire (not infinite):

$B = \frac{\mu_0 I \sin \theta}{2\pi y}$



consider the following two cases:-

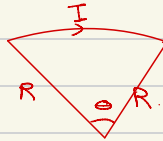
1] For infinite wire $L \gg R \Rightarrow \theta_0 = \frac{\pi}{2}$

$B = \frac{\mu_0 I}{2\pi r}$

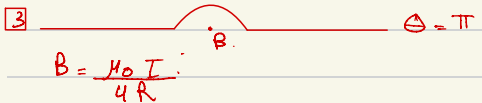
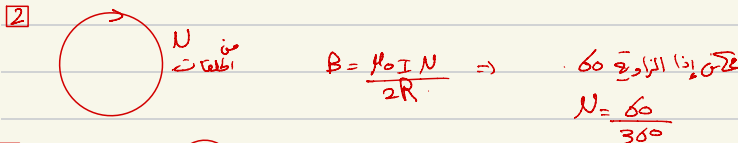
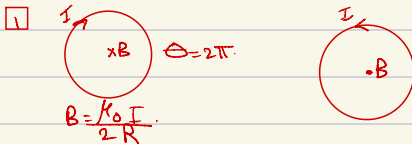
2] For semi infinite wire $\Rightarrow B = \frac{\mu_0 I}{4\pi r}$

B due to I in Arc:

$\vec{B} = \frac{\mu_0 I \theta}{4\pi R}$, θ in rad.



consider the following cases:-

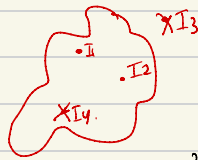


* Ampere's Law:-

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{enc.}$$

$$B \cos \theta ds$$

Exp $\Rightarrow$



$$\Rightarrow \int B \cdot ds = \mu_0 (I_1 + I_2 - I_3)$$



* B due to wire $\Rightarrow$ (not infinite) $\Rightarrow B = \frac{\mu I \sin \theta}{2\pi r}$

* B due to infinite wire $= \frac{\mu I}{2\pi r}$

* B due to semi infinite wire $\Rightarrow B = \frac{\mu I}{4\pi r}$

* B due to arc $\Rightarrow B = \frac{\mu I \theta}{4\pi R}$

Biot Savart
 $B = \frac{\mu}{4\pi} \frac{I ds \sin \theta}{R^2}$

Integration
 $\int B \cdot ds = \mu I_{enc.}$

* B = $\frac{\mu I}{2R}$ (inside solenoid)

* B = $\frac{\mu I N}{2R}$ (outside solenoid)

* B due to infinite wire $\Rightarrow$

$r > R$
 $B = \frac{\mu I}{2\pi r}$

$r < R$
 $B = \frac{\mu I r}{2\pi R^2}$

* B due to solenoid $\Rightarrow B = \mu n I$; $n = \frac{N}{L}$

* B due to Toroid $\Rightarrow B = \frac{\mu I N}{2\pi r}$

* Force between 2 wires $\Rightarrow F_a = \frac{\mu I_a I_b L}{2\pi d}$

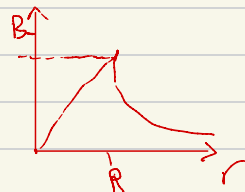
* Ampere's Law is useful in calculating B due to I in a system having high symmetry.

* B due to I outside an infinite wire: $= \int \vec{B} \cdot d\vec{A}$

Infinite wire $\Rightarrow$ very long current $= I \Rightarrow \vec{B} = \frac{\mu_0 I}{2\pi R^2}$

B outside ($r > R$) $\Rightarrow B = \frac{\mu_0 I}{2\pi r}$

B inside ($r < R$) $\Rightarrow B = \frac{\mu_0 I r}{2\pi R^2}, r \leq R$



* B due to I in an ideal solenoid $\Rightarrow$ ملف لانهي
 $\hookrightarrow$ B near the solenoid is zero.

* B inside the solenoid $\Rightarrow B = \mu_0 I n; n = \frac{N}{L}$

طول الملف وليس طول السلك
 طول السلك = طول الملف $\times$ عدد اللفات

* B due to I in Toroid:

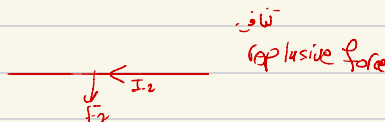
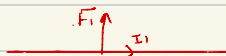
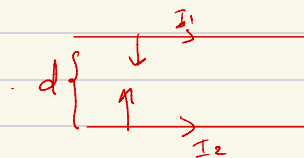
$$B = \frac{\mu N I}{2\pi r}$$

$\mu = I A \Rightarrow$ Magnetic dipole moment.

* Magnetic Force between 2 parallel wires

$$B_2 = \frac{\mu_0 I_2}{2\pi d}$$

$$F_2 = \frac{\mu_0 I_1 I_2 L}{2\pi d}$$



تأخير سريع - (أصل)
قانون أمبير في المغناطيسية $\Rightarrow$

$$\sum B \cdot dL = \sum I \mu_0$$

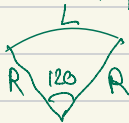
لما اطلب اوجه الدائرة للمغناطيسية $\Rightarrow$ بدعوى $\sum B \cdot dL$

$$\sum I = \boxed{0} + \text{بدعوى}$$

$$\boxed{0} - \text{بدعوى}$$

$$n = \frac{N}{L}, B_c = \mu_0 n I = B_c = \frac{\mu_0 I N}{L} \quad \text{طول الملف} \quad \text{+ الملف المزدوج} \Rightarrow$$

$\Rightarrow$ طوله 20.47 cm كما في الشكل اطلب نصف القطر للملف R



$$(القوس) L = 2R + L \quad (2 \text{ راد})$$

$$20.47 = 2R + \mu (2\pi R)$$

$$20.47 = 2R + \frac{1}{3} (2\pi R)$$

$$\boxed{R = 5 \text{ cm}}$$

$\Rightarrow$ للمغناطيسية المتحدة بالمركز في الزاوية بين المستويين $\theta = 60^\circ$ تكون الزاوية بين المجالين B_1, B_2 تساوي 60° إذا كانت عمالات الحلقة أعلى الحلقة لنفس الاتجاه.

$\Rightarrow$ إذا كانت لهما لآل أعلى الحلقة متعاكسة $\theta = 180 - 120^\circ$

$\Rightarrow$ متوازيات متعاكسة $\theta = 90^\circ$ و $B = 90^\circ$ الزاوية بين المجالين $B_2 < B_1$

$$\Rightarrow F_B = q \nabla B \sin \theta = \frac{\mu_0 I_1 I_2 L_2}{2\pi R} = I L B \sin \theta$$

$$\Rightarrow F_B = \frac{m v^2}{R} \Rightarrow R = \frac{m v}{q B}$$

$\Rightarrow$ الشحنات العاكسة تولد فقط مجال كهربائي E ، لكن الشحنات الكهربائية المتحركة تولد مجالين E, B

$$I \cdot dL = \text{شحنة موجبة} \rightarrow \text{تيار} \leftarrow$$

قانون بيوتسافاري $\Rightarrow I = \frac{\Delta \phi}{\Delta t}$, $V = \frac{\Delta L}{\Delta t}$ $\Rightarrow I = \frac{\Delta L}{\Delta t}$

$\Rightarrow I = \frac{\Delta L}{\Delta t}$

$\Delta B = \frac{\mu_0}{4\pi} \frac{I \Delta L}{R^2} \sin \theta$

$\Rightarrow B = \frac{\mu_0 I}{2\pi R} \sin \theta$, $R \sin \theta = R_1$ البعد المماس والباق مع R

نقطة التعادل:

- ١- إذا كان التياران بنفس الاتجاه تقع نقطة التعادل بينهما قرب الصغرى.
- ٢- إذا كان التياران متعاكسين بالاتجاه تقع نقطة التعادل في الخارج قرب الصغرى.
- ٣- إذا كان التياران بنفس الاتجاه ومتساويان مقداراً تقع نقطة التعادل في المنتصف.

تيار (+) قاعدة يد اليمين ، تيار (-) قاعدة يد لوف مع عكس الاتجاه الناتج

$B_c = \frac{\mu_0 I N}{2R}$, $N = \frac{\text{طول السلك}}{2\pi R}$ $\left. \begin{array}{l} \text{طول السلك} \\ \text{طول القوس} \end{array} \right\}$ عدد اللفات $\Rightarrow$ الملف المائلي $\Rightarrow$

$N = \frac{\phi}{360}$

$B_{out} = 0$ متوسط + دائري

$\Rightarrow \frac{B_f}{B_i} = \left(\frac{N_f}{N_i} \right)^2$

Chapter 30:

Magnetic Flux $\Rightarrow \Phi_B = \vec{B} \cdot \vec{A} = BA \cos \theta$.

أو النسبة المتقاطعة بين المجال المغناطيسي والمساحة المتعامدة

$$\mathcal{E}_{ind} = (-) \frac{N d \Phi_B}{dt} \Rightarrow \text{الاتجاه مع المجال يولد بقلب مع التيار} \quad \mathcal{E}_{ind} = BLV$$

$$I_{ind} = \frac{\mathcal{E}_{ind}}{R}, \quad \mathcal{E}_{net} = \mathcal{E}_{bat} + \mathcal{E}_{ind}$$

$$I_{net} = \frac{\mathcal{E}_{net}}{R}$$

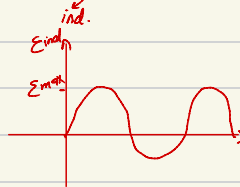
* Thermal power $\Rightarrow P_R = I^2 R = \frac{B^2 L^2 V^2}{R}$, $P_{\mathcal{E}} = I \mathcal{E}$

$$F_B = \frac{L^2 B^2 V}{R}$$

$$P = \vec{F} \cdot \vec{v} = \frac{B^2 L^2 V^2}{R}, \quad F_{ext} = F_{wire} = ILB \sin \theta$$

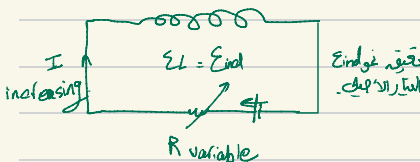
* $\mathcal{E}_{ind} = 2\pi f N B a b \sin \omega t$

↓
الطول $\times$ العرض

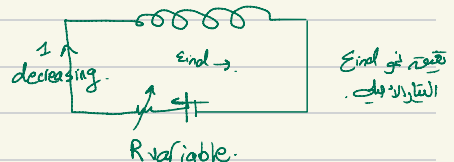


$$\mathcal{E}_{max} = 2\pi f N B a b \text{ volts}$$

* Inductor and Inductance:



مقاومة متغيرة



مقاومة متغيرة

$$\mathcal{E}_L = -L \frac{dI}{dt}, \quad \text{Inductance} = \frac{V \cdot s}{A} = H$$

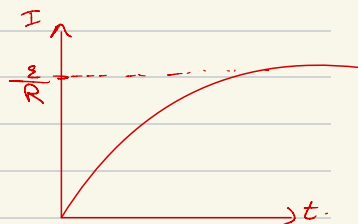
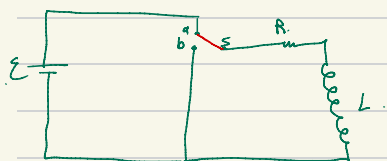
$$\mathcal{E}_L = \frac{N d \Phi_B}{dt} = -L \frac{dI}{dt}$$

$$L = \frac{N \Phi_B}{I} = \frac{T \cdot m^2}{Ampere} = H$$

$$L = \mu_0 n^2 A L$$

$$\mathcal{E}_L = \mathcal{E} e^{-t/\tau_L}$$

* RL-circuit:-



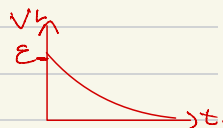
$$I(t) = \frac{\varepsilon}{R} (1 - e^{-Rt/L}) = \frac{\varepsilon}{R} (1 - e^{-t/\tau_L}), \quad \tau_L = \frac{L}{R}$$

$$I_{\infty} = \frac{\varepsilon}{R}$$

$$* V_R(t) = IR = \varepsilon (1 - e^{-t/\tau_L})$$



$$* V_L = -L \frac{dI}{dt} = \varepsilon e^{-t/\tau_L}$$



② connect s with b $\Rightarrow$ $\vec{q}$, Null is up & left

$$I(t) = I_m e^{-t/\tau_L}; \quad I_m = I \text{ at } t=0.$$

$$\tau_L = \frac{L}{R}$$

* Magnetic energy:-

$$\hookrightarrow (RL\text{-circuit}) \Rightarrow \varepsilon = RI + L \frac{dI}{dt}$$

$$\begin{array}{ccc} \varepsilon I & = & RI^2 + L I \frac{dI}{dt} \\ \downarrow & & \downarrow \\ P_{\varepsilon} & & P_R \quad \downarrow \frac{dU_B}{dt} \end{array}$$

$$U_B = \frac{1}{2} L I^2$$

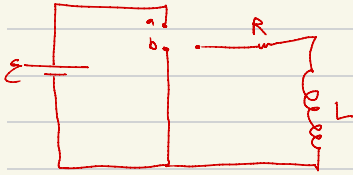
$$* \text{magnetic energy density} = \frac{U_B}{\text{volume}}$$

$$U_B = \frac{1}{2} \frac{B^2}{\mu_0} \text{ J/m}^3$$

$$U_E = \frac{1}{2} \frac{Q^2}{C}$$

$$U_E = \frac{1}{2} \varepsilon_0 E^2 \text{ J/m}^3$$

$$\Rightarrow \varepsilon_{\text{ind}} = L \frac{dI}{dt}$$



connect switch with b:-

$$\mathcal{E} = RI + L \frac{dI}{dt} = 0$$

$$I(t) = I_m e^{-t/\tau_L}, \quad I_m = I \quad \text{at } t=0.$$

$$\tau_L = \frac{L}{R}$$

connect switch a:-

$$I(t) = \frac{\mathcal{E}}{R} (1 - e^{-t/\tau_L})$$

$$I(t) = I_m (1 - e^{-t/\tau_L})$$

$$\mathcal{E}_L = \mathcal{E} e^{-t/\tau_L}$$

