

chapter 4: distributions of functions of Random variables

4.1: sampling Theory

Def 1: a function of one or more Random variables that does not depend up on any unknown parameter is called a statistic.

Def 2: let $x_1, x_2, \dots, x_n$ be n indep. random variables each of which has the same but possibly unknown p.d.f that is, the p.d.f's of $x_1, \dots, x_n$ are respectively $f_1(x_1) = f(x_1), f_2(x_2) = f(x_2), \dots, f_n(x_n) = f(x_n)$ so that the joint p.d.f of $x_1, \dots, x_n$ is $f_1(x_1) \dots f_n(x_n) = f(x_1) \dots f(x_n)$.

The Random variables $x_1, \dots, x_n$ are said to constitute a Random sample from dist. that has p.d.f $f(x)$, that is the observations of a Random sample are independent and identically distributed (often abbreviated as i.i.d).

Def 3: $x_1, \dots, x_n$ Random sample of size n

$$\bullet \bar{X} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i \quad \text{"statistic called sample mean"}$$

$$\bullet S^2 = \frac{\sum (x_i - \bar{x})^2}{n} \quad \text{"statistic called sample variance"}$$

$$\text{RMK: } S_{n-1}^2 = \frac{\sum (x_i - \bar{x})^2}{n-1} \quad \text{"statistic called sample variance"}$$

ex 1 x