

Reinforced Concrete Design I

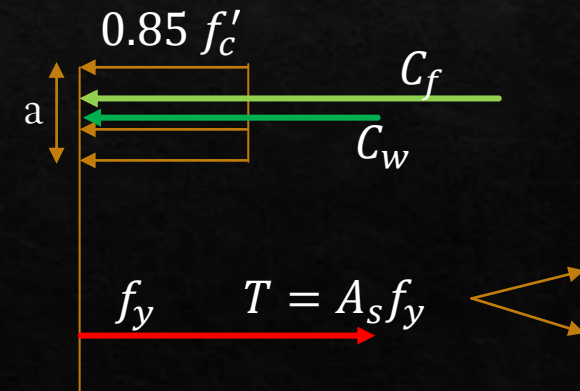
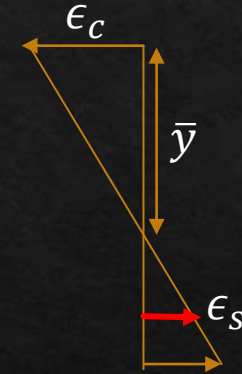
ENCE 335

Shear Design

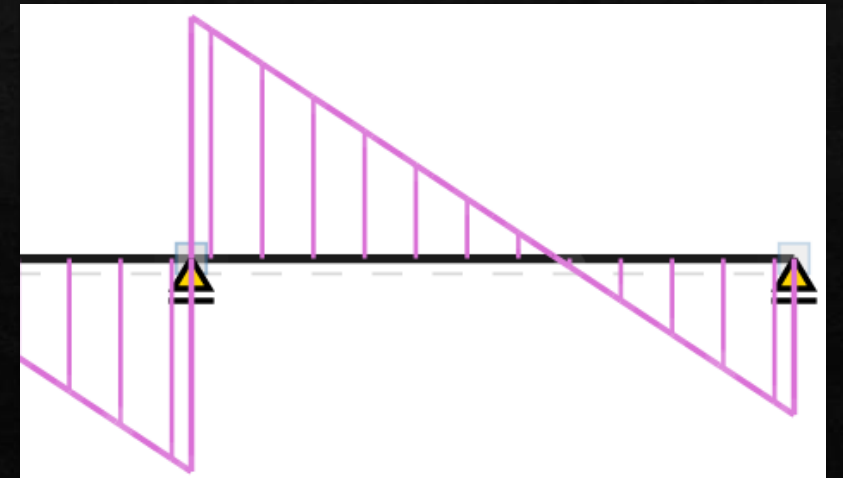
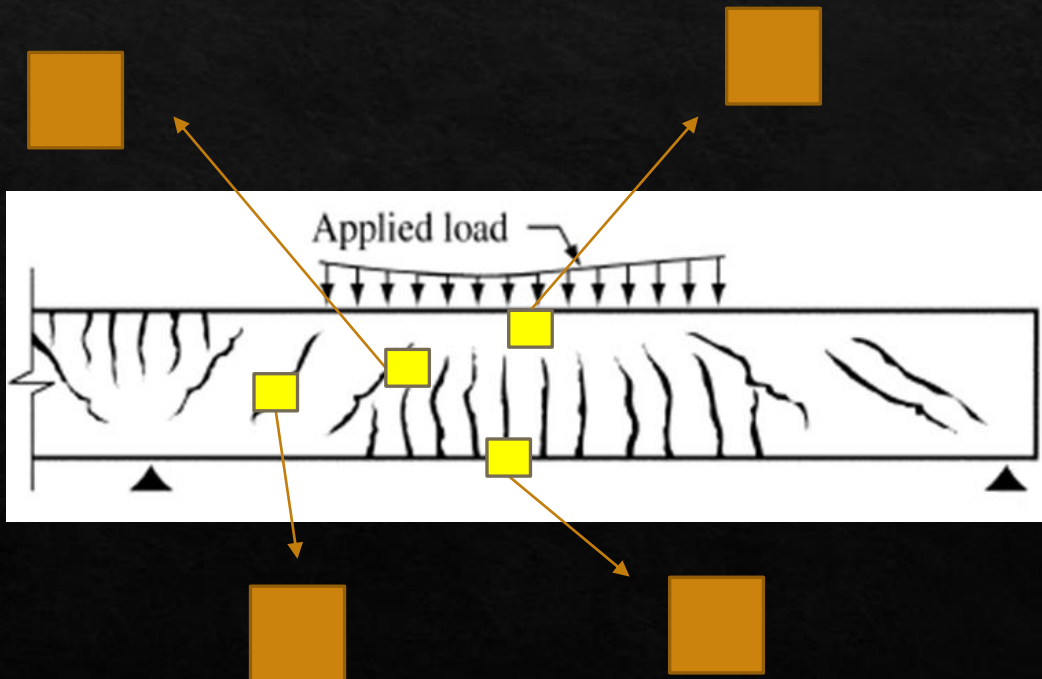
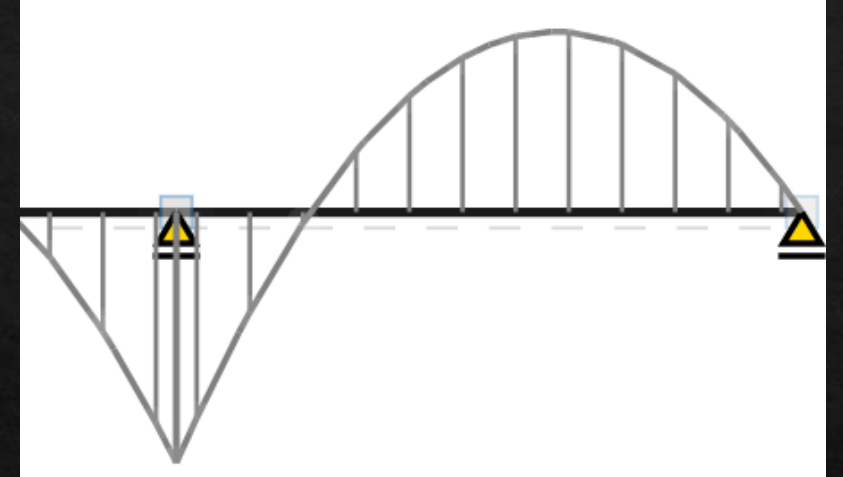
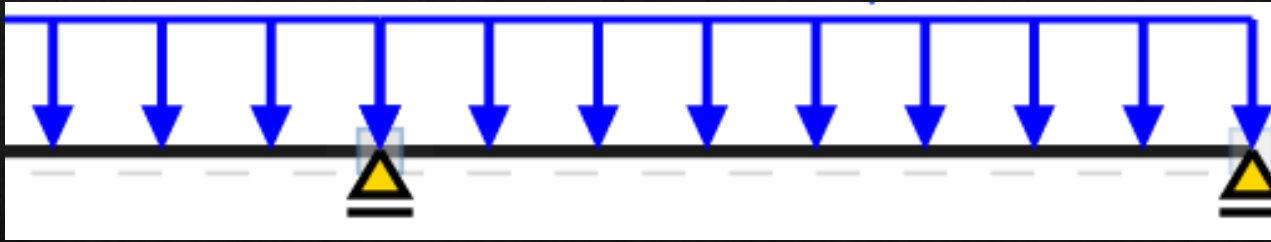
Dr. Khalil M. Qatu

Previously on Design I

- ◆ We only designed for the internal Bending moment
 - ◆ Rectangular sections (Single, Double) reinforced.
 - ◆ T-sections
 - ◆ Arbitrary sections
 - ◆ In all cases we relied on stress and strain distributions
 - ◆ We need to comply with ACI code requirements for
 - ◆ Minimum spacing between bars (Width)
 - ◆ Minimum and maximum reinforcement ratios (maintain a min 0.004 tension strain)
 - ◆ Minimum depth



Cracks in Reinforced beams



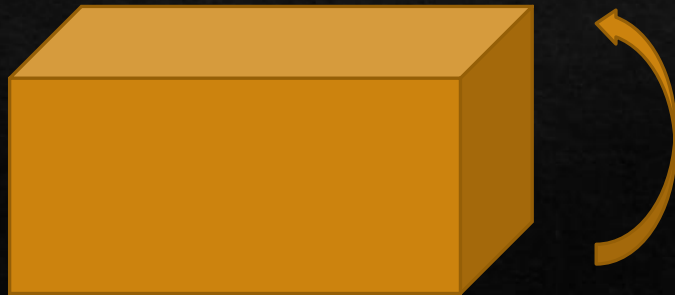
Cracks in Reinforced beams

◇ Shear Cracks

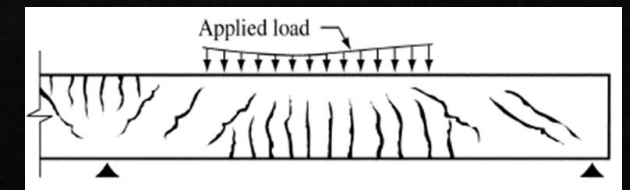
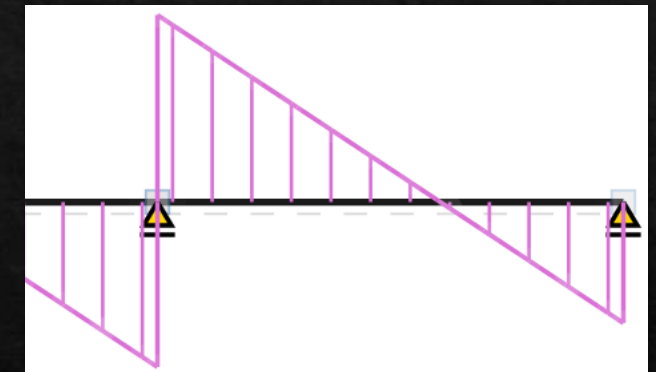
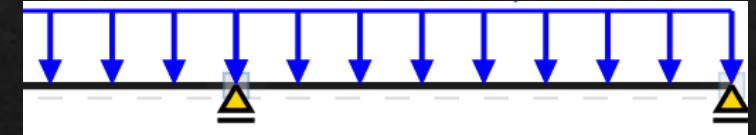
◇ Shear forces are typically maximum near supports

◇ This not always the case, depends on the loading pattern

◇ Shear stress distribution in the cross-section ?? (Mechanics)



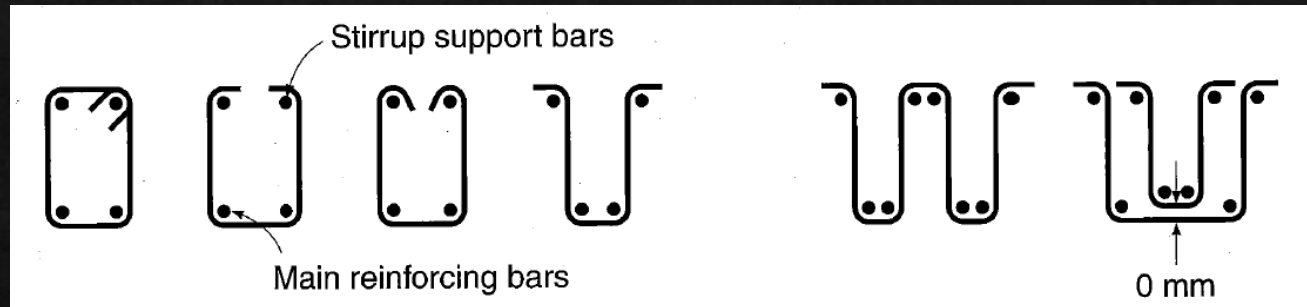
◇ Where is the critical section in concrete ?? (Mohr Circle)



Shear reinforcement

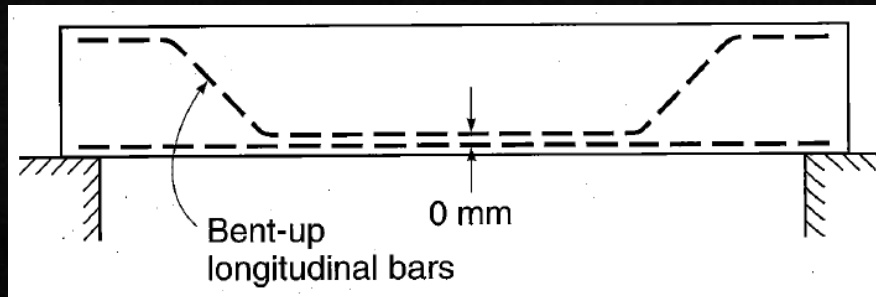
◆ We need to put the steel in a way to bridge these shear cracks

◆ Stirrups

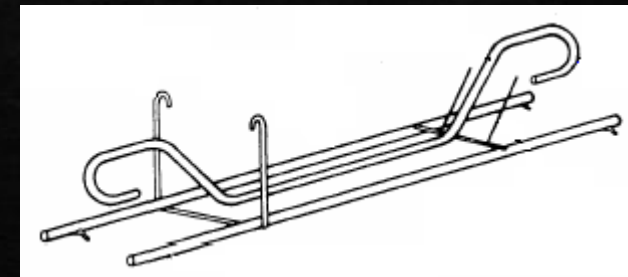
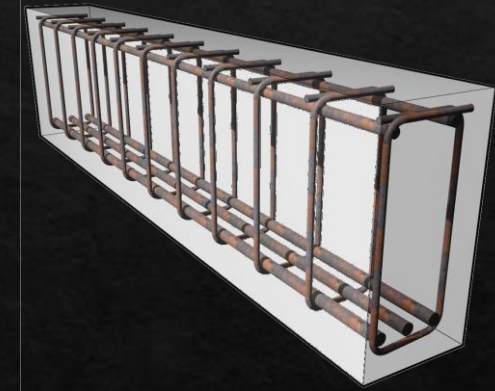


Which one is more efficient ??

◆ Bent Bars



What steel area resist shear stress ???



Shear resistance components

◆ Concrete resistance for shear

$$V_c = 0.17 \sqrt{f'_c} b_w d$$

◆ Shear reinforcement (steel stirrups)

$$V_s = \frac{A_v f_y d}{s} \dots\dots\dots V_s = \frac{A_v f_y d (\sin \alpha + \cos \alpha)}{s}$$

Where : A_v : steel area resisting shear stress

f_y : yield stress of steel

d : effective depth

s : Spacing between reinforcement

α : angle of bent bars

ACI Code requirements

◇ When do we need shear reinforcement ??

◇ If $V_u \leq \frac{\phi V_c}{2} \rightarrow$ No reinforcement is needed

◇ If $\phi V_c > V_u \geq \frac{\phi V_c}{2} \rightarrow$ Minimum reinforcement is needed (Except ??)

◇ In general, we choose the stirrups diameter and control the spacing between them

◇ This means, Minimum shear reinforcement \rightarrow max spacing

$$S_{max} = \max \left\{ \begin{array}{l} \frac{A_v f_y}{0.062 \sqrt{f'_c} b_w} \leq \frac{A_v f_y}{0.35 b_w} \\ \frac{d}{2} \dots \dots \left(\frac{3}{4} d \text{ for bent bars } \right) \\ 600 \text{ mm} \end{array} \right.$$

◇ If $\phi V_c > V_u \rightarrow$ We Need to Calculate the required spacing for reinforcement (from previous slide) and compare it with max spacing

◇ If $V_s > 2V_c = 0.33 \sqrt{f'_c} b_w d \rightarrow$ The max spacing is divided by 2

Table 9.6.3.1—Cases where $A_{v,min}$ is not required if $V_u \leq \phi V_c$

Beam type	Conditions
Shallow depth	$h \leq 250 \text{ mm}$
Integral with slab	$h \leq \text{greater of } 2.5t_f \text{ or } 0.5b_w$ and $h \leq 600 \text{ mm}$
Constructed with steel fiber-reinforced normalweight concrete conforming to 26.4.1.5.1(a), 26.4.2.2(i), and 26.12.7.1(a) and with $f'_c \leq 40 \text{ MPa}$	$h \leq 600 \text{ mm}$ and $V_u \leq 0.17 \phi \sqrt{f'_c} b_w d$
One-way joist system	In accordance with 9.8

ACI Code requirements

◇ Minimum spacing between stirrups: recommended not less than 100mm

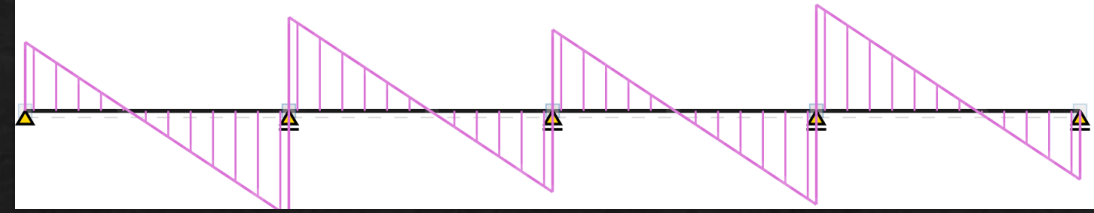
◇ Strength reduction Factor: $\phi = 0.75$

◇ V_u : shear at distance d from the face of support $V_{u@ d}$

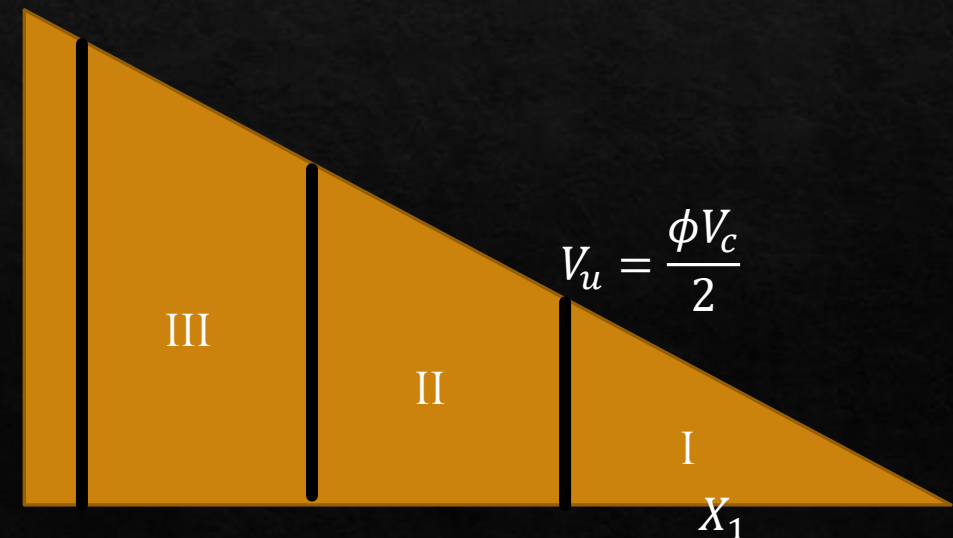
◇ If $V_s > 4V_c = 0.66\sqrt{f'_c}b_wd \rightarrow$ Section geometry must be increased

Action or structural element	ϕ	Exceptions
(a) Moment, axial force, or combined moment and axial force	0.65 to 0.90 in accordance with 21.2.2	Near ends of pretensioned members where strands are not fully developed, ϕ shall be in accordance with 21.2.3.
(b) Shear	0.75	Additional requirements are given in 21.2.4 for structures designed to resist earthquake effects.
(c) Torsion	0.75	—
(d) Bearing	0.65	—
(e) Post-tensioned anchorage zones	0.85	—
(f) Brackets and corbels	0.75	—
(g) Struts, ties, nodal zones, and bearing areas designed in accordance with strut-and-tie method in Chapter 23	0.75	—
(h) Components of connections of precast members controlled by yielding of steel elements in tension	0.90	—
(i) Plain concrete elements	0.60	—
(j) Anchors in concrete elements	0.45 to 0.75 in accordance with Chapter 17	—

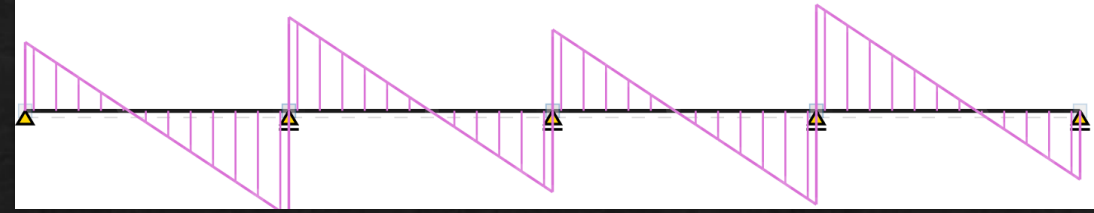
Summary



- ◆ Draw shear diagram → and get a triangle (if it is a triangular shape)
 - ◆ Since shear is changing, we need to change the spacing accordingly
 - ◆ We divide the shear diagram into three regions
 - ◆ Region I: No shear reinforcement is needed
 - ◆ We need to find where on the shear diagram $V_u = \frac{\phi V_c}{2}$



Summary



- ◇ Draw shear diagram → and get a triangle (if it is a triangular shape)
- ◇ We divide the shear diagram into three regions
 - ◇ Region II: Max spacing is needed

- ◇ For this we need to calculate the shear force to be carried by steel

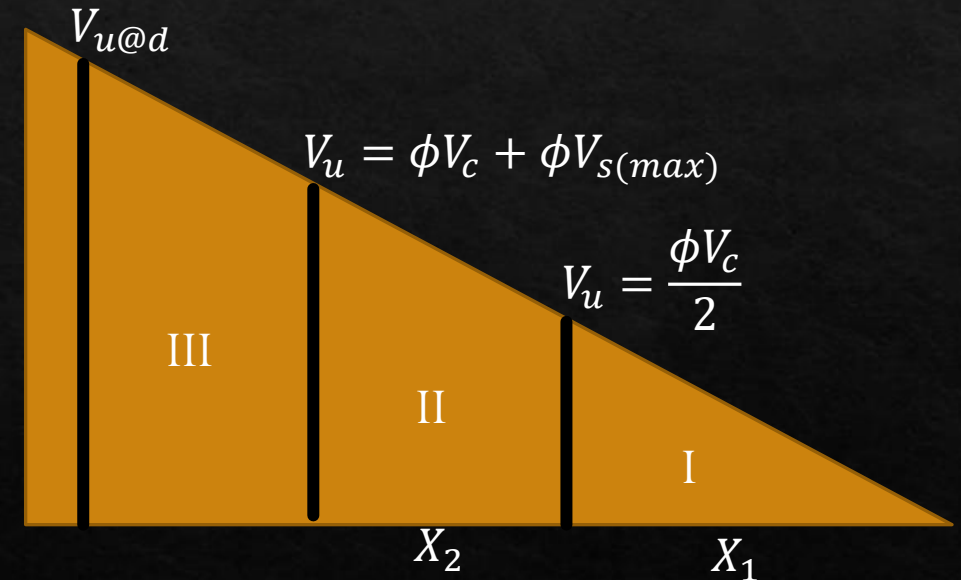
$$V_s = \frac{V_{u@d} - \phi V_c}{\phi}$$

- ◇ Compare V_s with $2V_c = 0.33\sqrt{f'_c}b_wd$
 - ◇ $V_s \leq 2V_c = 0.33\sqrt{f'_c}b_wd \rightarrow$ The max spacing remains the same
 - ◇ $V_s > 2V_c = 0.33\sqrt{f'_c}b_wd \rightarrow$ The max spacing is divided by 2
 - ◇ $V_s > 4V_c = 0.66\sqrt{f'_c}b_wd \rightarrow$ Change Section geometry
- ◇ Calculate the shear force stirrups can support with max spacing

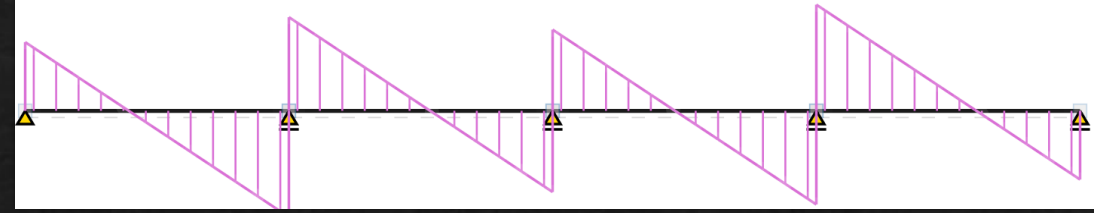
$$\phi V_{s(max)} = \frac{\phi A_v f_y d}{S_{max}}$$

- ◇ Calculate the shear force the section can support with max spacing and locate it on the shear diagram

$$V_u = \phi V_c + \phi V_s$$



Summary



◆ Draw shear diagram → and get a triangle (if it is a triangular shape)

◆ We divide the shear diagram into three regions

◆ Region III: Specially designed

◆ For this we need to calculate the shear force to be carried by steel

$$V_s = \frac{V_{u@d} - \phi V_c}{\phi}$$

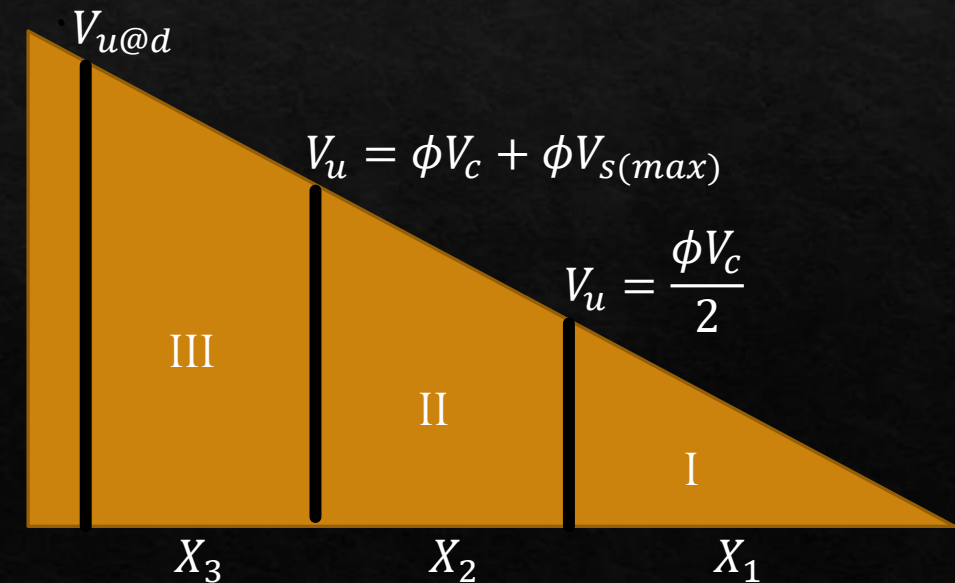
◆ Calculate the spacing required to support the shear force

$$S = \frac{\phi A_v f_y d}{V_s}$$

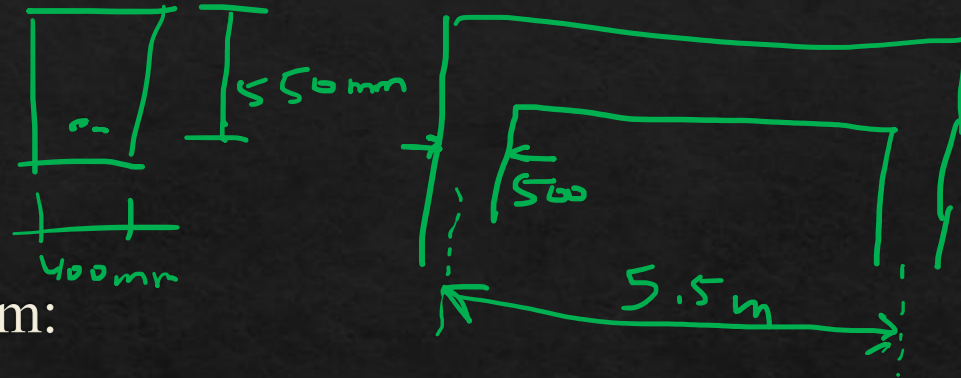
◆ Calculate the total # of stirrups needed

$$\#stirrups = \frac{X_3}{S} + \frac{X_2}{S_{max}} + 1$$

Total # of stirrups for the beam ????



Example



Design the following beam:

Simply supported beam with 5.5m span (center to center)

B=400 mm ... d=550 mm

Column width 500 mm

$$w_D = 60 \frac{kN}{m} \dots w_L = 60 \frac{kN}{m}$$

$$f'_c = 28 MPa \dots f_y = 420 MPa$$

Analysis

$$w_u = 1.2(60) + 1.6(60) = 168 kN/m$$

