

Circuit Analysis

By

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Chapters 1-3

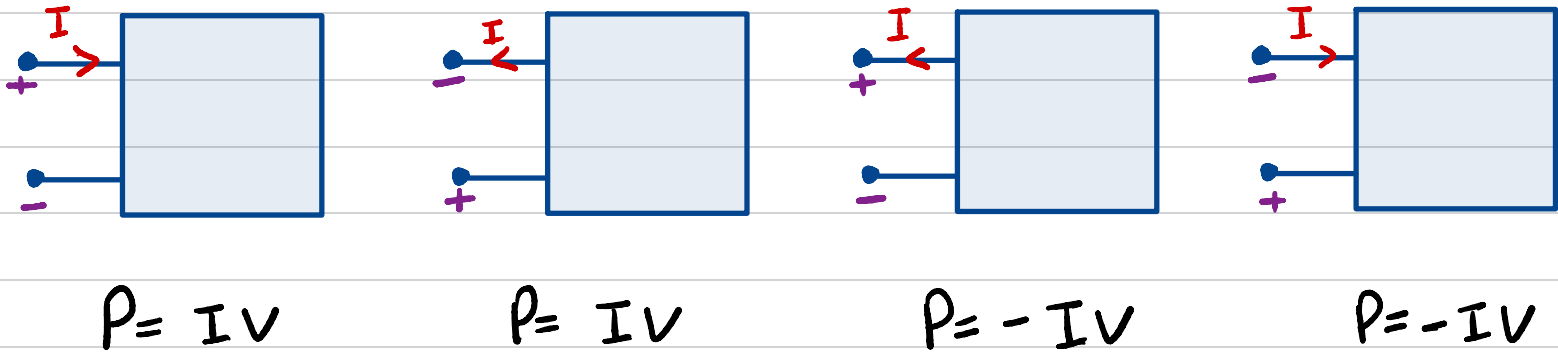
Birzeit University

2025

Chapter 1 - introduction

Passive sign convention

When to put $P = IV$ and when to put $P = -IV$?



السبب:
صوبط الجهد يكون من الموجب (+) إلى السالب (-)
إذا كان التيار مع اتجاه صوبط الجهد $\Rightarrow$ موجب
إذا كان التيار على اتجاه صوبط الجهد $\Rightarrow$ سالب

باختصار:
التيار داخل من الموجب $\Rightarrow$ موجب P
التيار داخل من السالب $\Rightarrow$ سالب P

Note :-

if $P > 0 \Rightarrow$ absorbing (تتملك طاقة)

if $P < 0 \Rightarrow$ supplying (تنتج طاقة)

Chapter 2 - Circuit Elements

Ideal circuit elements

are two terminal devices can be Simplified into Passive and active devices.

Passive elements

elements that Consume energy



R



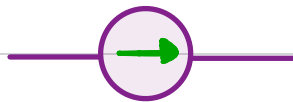
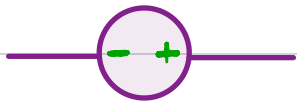
L



C

Active elements

elements that Produce energy (like Battery)



Active elements

independent
Sources

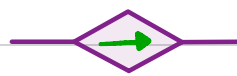
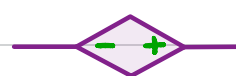
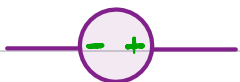
dependant
Sources

Voltage
Source

Current
Source

Voltage
Source

Current
Source



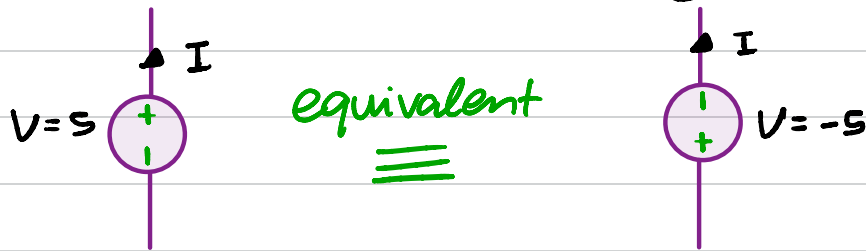
1 - Independent sources:

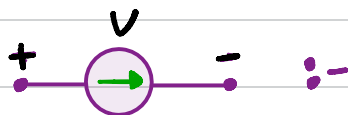
1- Voltage Source  :-

V : Constant

I : depends on the Circuit Connections " I Changes "

ideal independent voltage source : a Voltage source that maintains a specific Voltage in it.



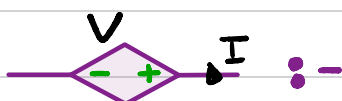
2- Current source  :-

I : Constant

V : depends on the Circuit Connections " V Changes "

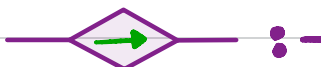
ideal independent Current source : a Current source that maintains a specific Current in it.

2 - Dependent sources:

1- Voltage Source  :-

Case 1 : $V = \text{Constant} \times V_x \Rightarrow$ Voltage controlled

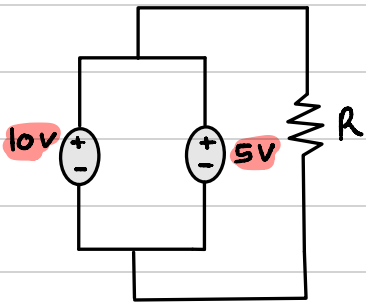
Case 2 : $V = \text{Constant} \times i_x \Rightarrow$ Current controlled

2- Current source  :-

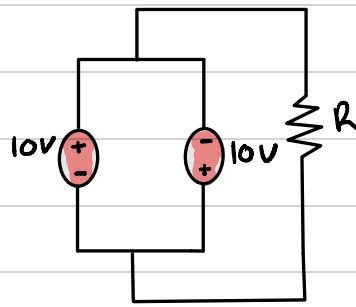
Case 1 : $i = \text{Constant} \times V_x \Rightarrow$ Voltage controlled

Case 2 : $i = \text{Constant} \times i_x \Rightarrow$ Current controlled

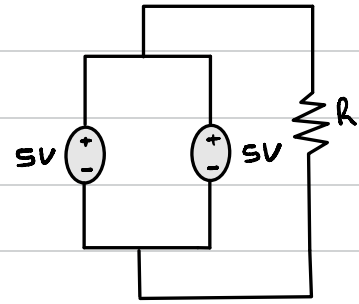
Validity of the circuits



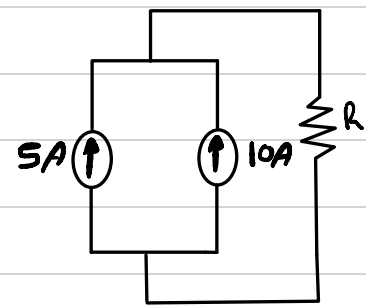
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لديجب ان تكون
القيم مختلفة



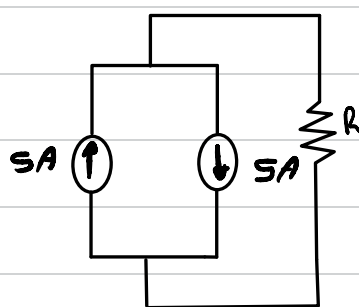
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الشارة مختلفة



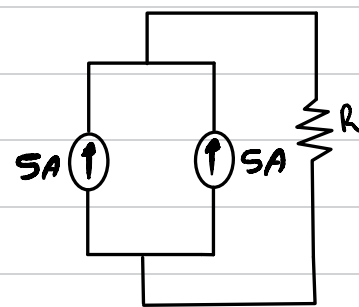
Valid ✓
نفس القيم ✓
نفس الاتجاه ✓



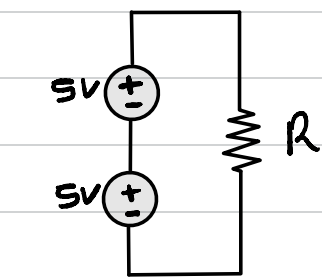
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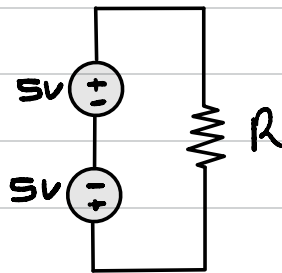
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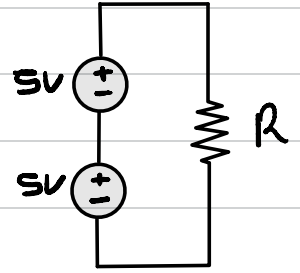
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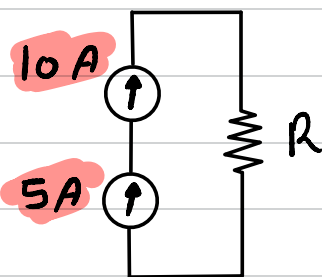
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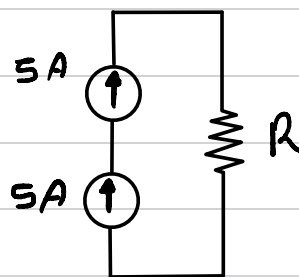
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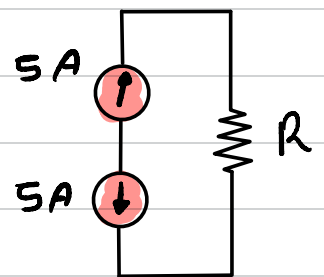
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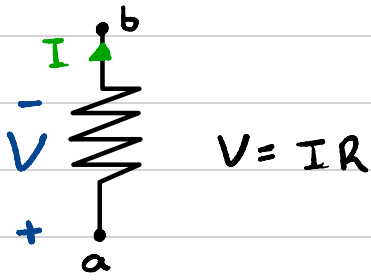


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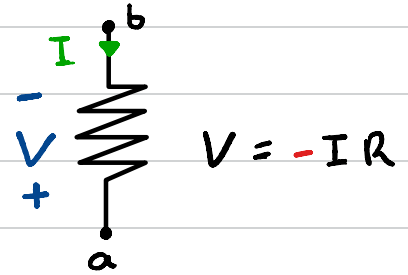


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لديجب ان تكون
الشارة مختلفة

Ohm's law



التيار داخل من الموجب
القانون موجب $\Rightarrow$

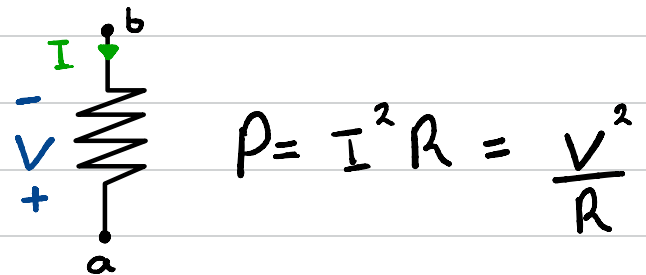
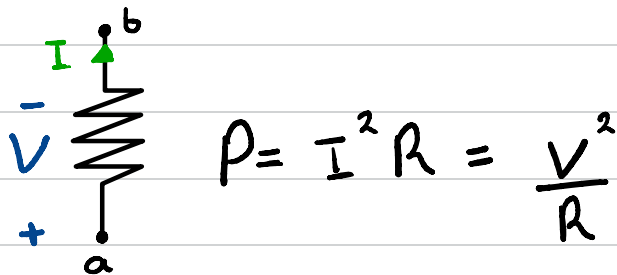


التيار داخل من السالب
القانون سالب $\Rightarrow$

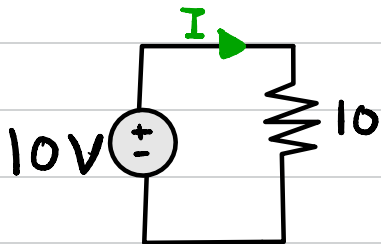
Conductance (G)

$$G = \frac{1}{R} \text{ على المقارمة}$$

Power (P)



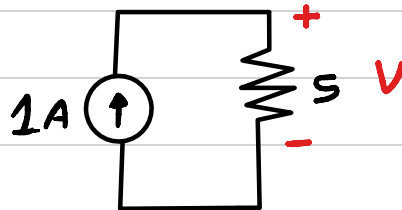
Example - find V and I ?



$$V = 10$$

$$I = \frac{V}{R} = \frac{10}{10}$$

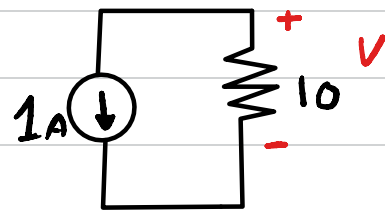
$$I = 1$$



$$I = 1$$

$$V = IR = 1 \times 5$$

$$V = 5$$



$$I = 1$$

$$V = -IR = -1 \times 10$$

$$V = -10$$

Kirchhoff Laws

① Kirchhoff current law (KCL)

The algebraic sum of the currents at any node equals Zero $\Rightarrow \sum I_{in} = \sum I_{out}$

Node

It's a point that connects **2** or more circuit elements

Essential Node

It's a point that connects **3** or more circuit elements

How to solve ?

1- امسح جميع التيارات الزائدة
او اختار من النقطة

2- أساوينا بالصفر أو
 $\sum I_{in} = \sum I_{out}$

node a :

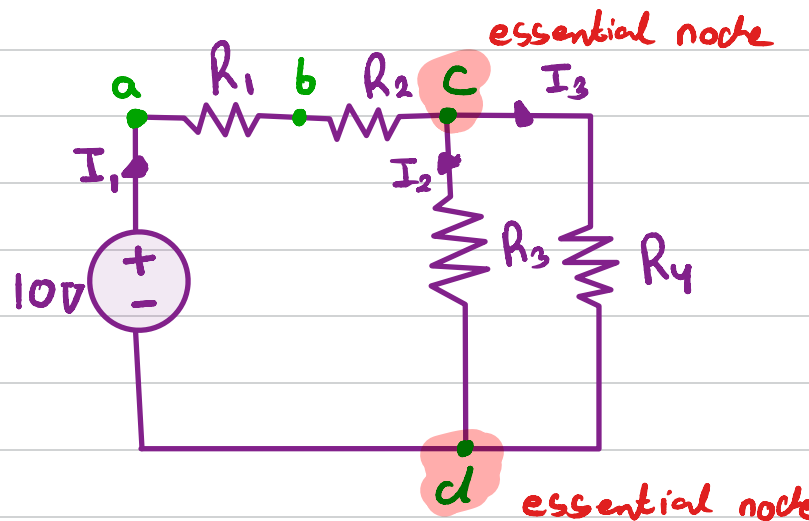
$$I_1 = I_1$$

node c :

$$-I_1 + I_2 + I_3 = 0$$

node d :

$$I_1 - I_2 - I_3 = 0$$



* Note

im just interested on essential nodes

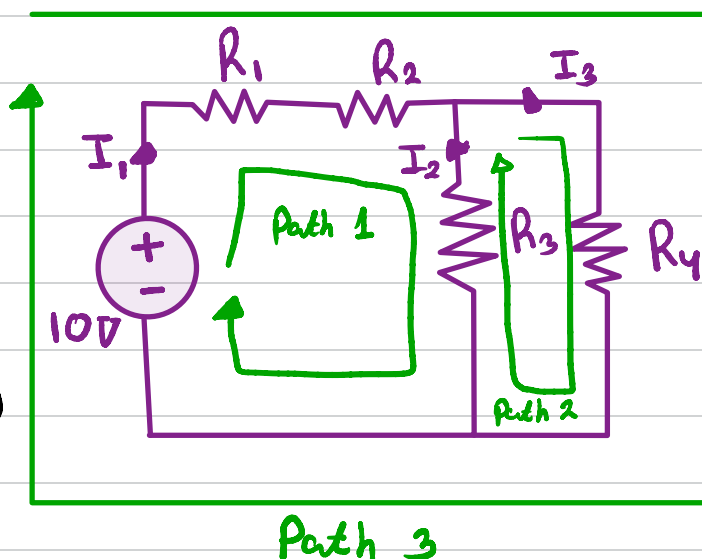
② Kirchhoff voltage law (KVL)

$\sum V$ around any closed path is equal to zero

How to Solve ?

1- draw the path in any direction
(it's better to be with I direction)

2- move with the path and don't forget to look at the signs (+-)



Path 1

$$I_1 R_1 + I_1 R_2 + I_2 R_3 - 10 = 0$$

Path 2

$$I_3 R_4 - I_2 R_3 = 0$$

Path 3

$$I_1 R_1 + I_1 R_2 + I_3 R_4 - 10 = 0$$

Example

write the KVL equation

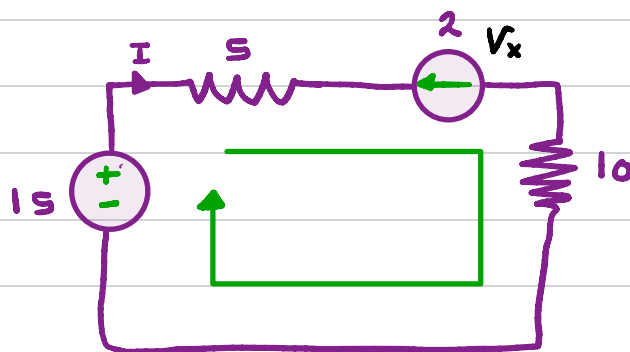
$$I \times 5 - V_x + I \times 10 - 15 = 0$$

$$15I - 15 - V_x = 0$$

* Since the current source = 2

then $I = 2$ (Rule)

$$\Rightarrow 15 \times 2 - 15 - V_x \Rightarrow V_x = 15$$



Why V_x ?

Because the current source has a voltage drop V_x

Example

Find I_1 , P on all Points

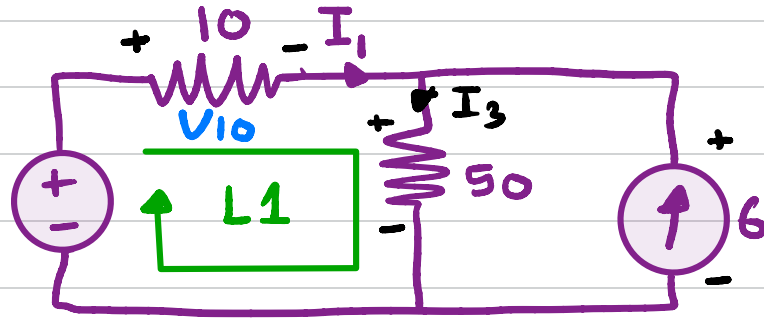
Loop 1 :

$$I_1 \times 10 + (I_1 + 6) \times 50 - 120 = 0$$

$$10 I_1 + 50 I_1 + 300 - 120 = 0$$

$$60 I_1 = -180$$

$$I_1 = -3A$$



$$P_{120} = -(-I V) \Rightarrow P_{120} = -(-3 \times 120) \Rightarrow P_{120} = 360W$$

$$P_{10} = I_1^2 R \Rightarrow P_{10} = (-3)^2 \times 10 \Rightarrow P_{10} = 90W$$

$$P_{50} = I_3^2 R \Rightarrow P_{50} = (-3 + 6)^2 \times 50 \Rightarrow P_{50} = 450W$$

$$P_6 = I V$$

$$V_{10} = I R \Rightarrow V_{10} = -3 \times 10 \Rightarrow V_{10} = -30$$

$\Rightarrow$ then the voltage of R_{50} and current source is equal to $120 - (-30) \Rightarrow V = 150$

$$P_6 = -V I \Rightarrow P_6 = -150 \times 6 \Rightarrow P_6 = -900W$$

Why $V = -150$?

Because of the voltage drop from - to +

what if we reverse the voltage drop

then V should equal 150 BUT I will

be -6 because we will move backwards

OR

$$\sum P = 0$$

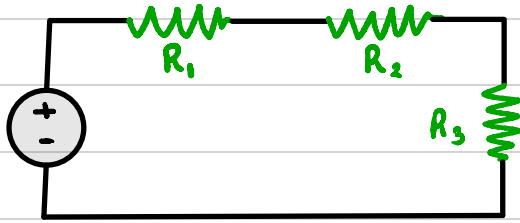
$$360 + 90 + 450 + P_6 = 0$$

$$\Rightarrow P_6 = -900W$$

Chapter 3 - Simple Resistive Circuits

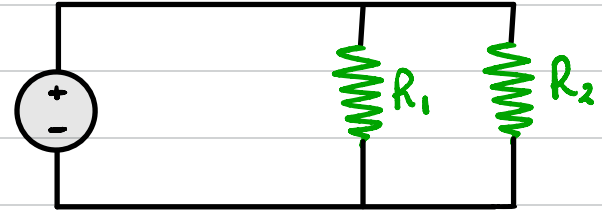
Solving for Resistors in series and resistors in parallel (R_{eq})

R_{eq} in series



$$R_{eq} = R_1 + R_2 + R_3$$

R_{eq} in parallel



$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} \quad (2 \text{ or more})$$

$$\text{or } R_{eq} = \frac{R_1 R_2}{R_1 + R_2} \quad (\text{just } 2)$$

Example 1

find i_s , i_1 , i_2

$$3 \text{ with } 6 : 3 + 6 = 9$$

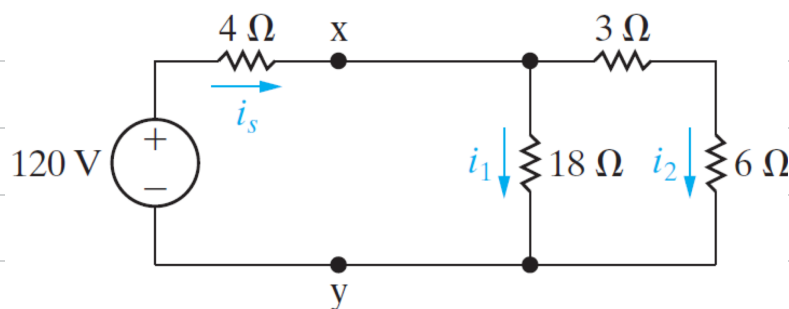
$$9 // 18 : \frac{9 \times 18}{9 + 18} = 6$$

$$6 \text{ with } 4 : 6 + 4 = 10 \Rightarrow R_{eq} = 10 \Omega$$

$$i_s = \frac{V}{R_{eq}} \Rightarrow i_s = \frac{120}{10} \Rightarrow i_s = 12 \text{ A}$$

$$V_{xy} = 120 - V_4 \Rightarrow V_{xy} = 120 - (4 \times 12) \Rightarrow V_{xy} = 72$$

$$i_1 = \frac{V_{xy}}{R_{18}} \Rightarrow i_1 = 4 \text{ A}, \text{ then } i_2 = 12 - 4 \Rightarrow i_2 = 8 \text{ A}$$



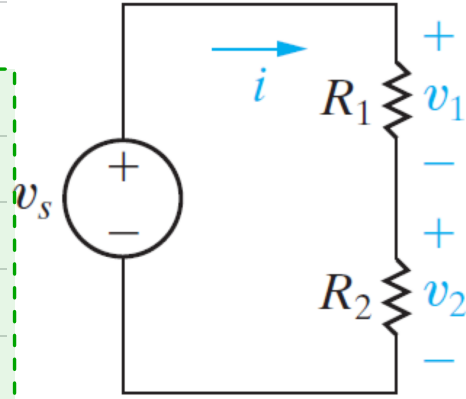
Voltage divider rule (VDR)

- we use it when we want to find the voltage on a resistors that are in **Series**.
- it's faster to find the voltages using this method.

The Rule :-

$$\text{النسبة} \times \text{مصدر الجهد المتوزع بينهما} = \frac{\text{النسبة}}{\text{النسبة} + \text{النسبة}}$$

$$V_1 = \frac{R_1}{R_1 + R_2} * V_S, \quad V_2 = \frac{R_2}{R_2 + R_1} * V_S$$



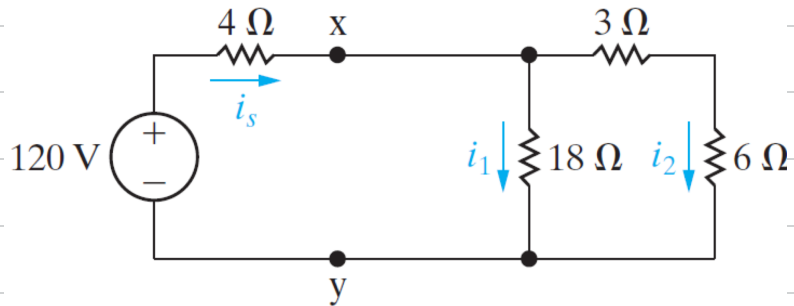
Example 2

find V_x using VDR

$$3 \text{ with } 6 : 3 + 6 = 9$$

$$9 \parallel 18 : \frac{9 * 18}{9 + 18} = 6$$

$$V_x = \frac{6}{6 + 4} * 120 \Rightarrow V_x = 72 \text{ Volt}$$



Note

- When i see Voltage Sources in Series
 $V_{eq} = V_1 + V_2 + \dots + V_n$

- When i see Current Sources in Parallel
 $I_{eq} = I_1 + I_2 + \dots + I_n$

- When you see voltage s. and current s.
then you CAN'T apply VDR or CDR

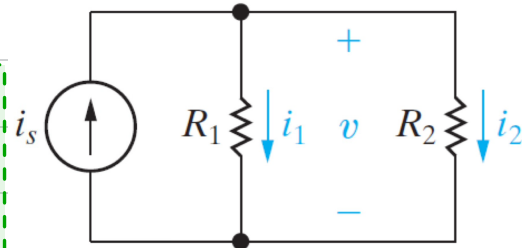
Current divider rule (CDR)

- we use it when we want to find the Current on a resistors that are in **Parallel**.
- it's faster to find the Current using this method.

The Rule :-

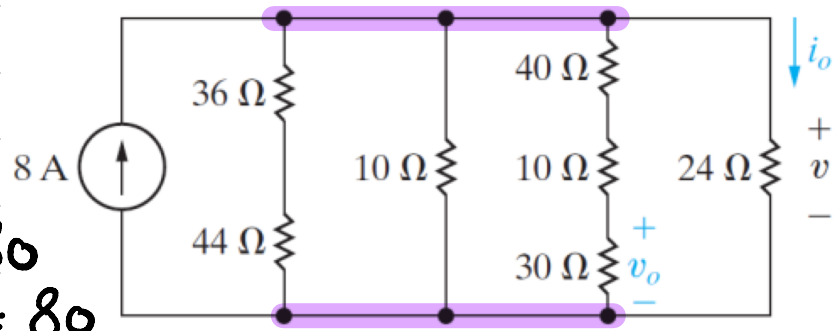
القاسم * التيار المتوزع بينهم
القاسم + القاسم

$$I_1 = \frac{R_2}{R_2 + R_1} * I_s, \quad I_2 = \frac{R_1}{R_1 + R_2} * I_s$$



Example 3

Use CDR to find i_o
Use VDR to find v_o



① $44 \text{ with } 36 : 44 + 36 = 80$
 $40, 30, 10 : 40 + 30 + 10 = 80$

Req of the highlighted :

$$\frac{1}{R_{eq}} = \frac{1}{80} + \frac{1}{80} + \frac{1}{10} \Rightarrow \frac{1}{R_{eq}} = \frac{10}{80} \Rightarrow R_{eq} = 8 \Omega$$

$$i_o = \frac{8}{8 + 24} * 8 \Rightarrow i_o = 2 A$$

② $R_{eq} = \frac{24 * 8}{24 + 8} \Rightarrow R_{eq} = 6 \Omega$

$$V = IR \Rightarrow V = 8 * 6 \Rightarrow V = 48 \text{ volt}$$

$$V_o = \frac{30}{30 + 50} * 48 \Rightarrow V_o = 18 \text{ volt}$$

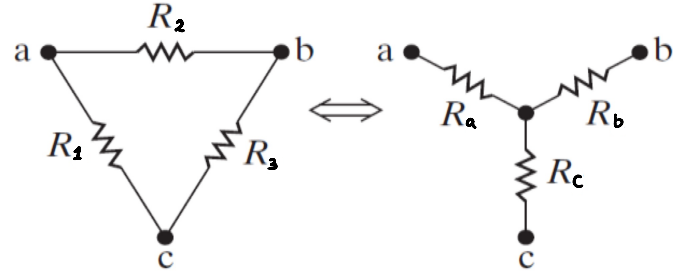
Delta to wye transformation ($\Delta \rightarrow Y$)

important note to remember

- المقام دائماً ثابت

- قبل القويل $\Leftarrow$ قبل R_1 قبل a , قبل R_2 قبل b

- بعد القويل $\Leftarrow$ بعد R_a بعد a , بعد R_b بعد b



The Rule :-

$$R_a = \frac{R_1 R_2}{R_1 + R_2 + R_3} \quad \left| \quad R_b = \frac{R_2 R_3}{R_1 + R_2 + R_3} \quad \left| \quad R_c = \frac{R_3 R_1}{R_1 + R_2 + R_3} \right.$$

Notice that

$$R_x = \frac{\text{The resistors that are connected with } R_x}{R_1 + R_2 + R_3}$$

Wye to Delta transformation ($Y \rightarrow \Delta$)

The Rule :-

$$R_1 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_b}$$

$$R_2 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_c}$$

$$R_3 = \frac{R_a R_b + R_b R_c + R_a R_c}{R_a}$$

Notice that

- البسط دائماً ثابت
وهو حاصل ضرب كل المقاومات

- المقام يكون المقاومة التي لا
تتصل مع المقاومة المراد مابها