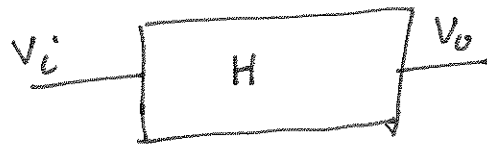


Experiment 5 Filters

(11)

- o A filter is a frequency selective device. It allows certain frequencies to pass almost unattenuated within the passband and rejects (suppresses) other frequencies within the rejection band.

- o The decibel concept
The attenuation or (gain) of a network is



$$G = \frac{V_o}{V_i}$$

in logarithmic, called the decibel, terms, the gain (attenuation) is defined as

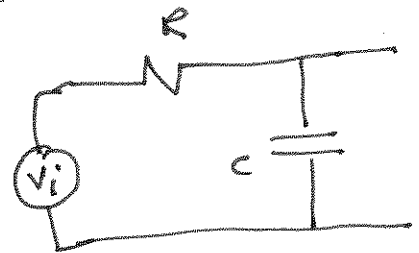
$$G_{dB} = 20 \log_{10} \frac{V_o}{V_i}$$

- o The First order low pass Filter

Let $v_i(t) = \sqrt{2} V_i \cos 2\pi f t$

In phasor term, it is expressed

as $V_i \angle 0$



The transfer function of the network is

$$H(f) = \frac{1/j\omega C}{R + 1/j\omega C} = \frac{1}{1 + j\omega R C} = \frac{1}{\sqrt{1 + (\omega R C)^2}} \angle -\tan^{-1} \omega R C$$

• The magnitude of $H(f)$ is

(2)

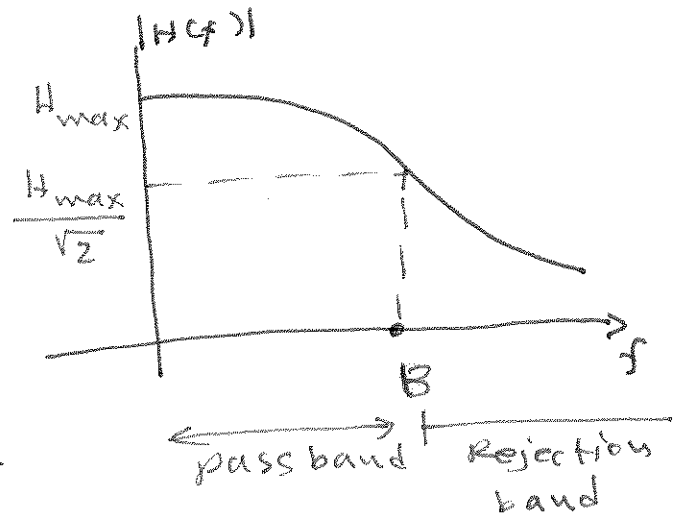
$$|H(f)| = \frac{1}{\sqrt{(2\pi fRC)^2 + 1}}$$

$$H(0) = 1$$

$$H\left(f_c = \frac{1}{2\pi RC}\right) = \frac{1}{\sqrt{2}}$$

$f_c = \frac{1}{2\pi RC}$ is called the
3-dB bandwidth

and is plotted below



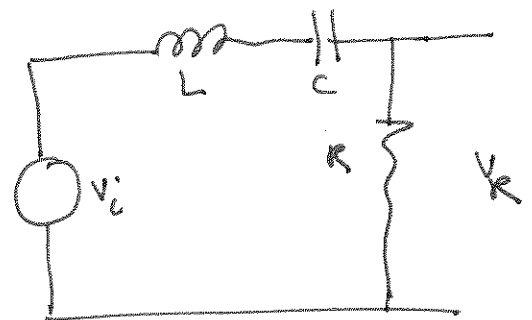
Note that $20 \log \frac{H(f_c)}{H_{max}} = 20 \log \frac{1/\sqrt{2}}{1} = -20 \log \sqrt{2} = -3 \text{ dB}$

Second order Filter

The filter transfer function

$$H(f) = \frac{V_R}{V_i} = \frac{R}{R + j\omega L + 1/j\omega C}$$

$$H(f) = \frac{\omega RC}{\omega RC + j(\omega^2 LC - 1)}$$



$$|H(f)| = \frac{\omega RC}{\sqrt{(\omega RC)^2 + [\omega^2 LC - 1]^2}}$$

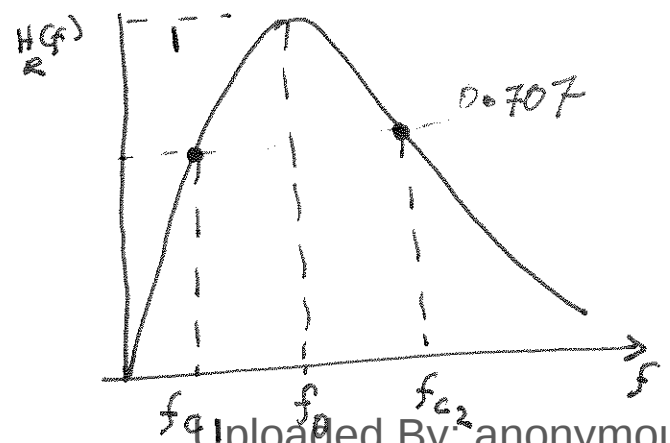
critical points when $\boxed{(\omega RC) = [\omega^2 LC - 1]}$

solve for f_{c1} and f_{c2}

f_0 : Resonance frequency

$$\omega_0^2 LC = 1 \text{ or } f_0 = \frac{1}{2\pi \sqrt{LC}}$$

$$\text{Filter bandwidth} = f_{c2} - f_{c1}$$



Active Filter

The transfer function of the inverting OP-AMP is

$$H(f) = \frac{V_o}{V_i} = -\frac{1}{R_1} Z_2$$

$$Z_2 = R_2 \parallel (1/j\omega C)$$

$$= \frac{R_2 \cdot \frac{1}{j\omega C}}{R_2 + \frac{1}{j\omega C}}$$

$$= \frac{R_2}{1 + j\omega R_2 C}$$

$$H(f) = \frac{R_2}{R_1} \cdot \frac{1}{1 + j\omega R_2 C}$$

$$|H(f)| = \frac{R_2}{R_1} \cdot \frac{1}{\sqrt{1 + (\omega R_2 C)^2}}$$

3-dB point when $\omega_c R_2 C = 1 \Rightarrow f_c = \frac{1}{2\pi R_2 C}$

Note that $|H(f=0)| = \frac{R_2}{R_1}$

