

ENEE2360 Analog Electronics

T9: Operational Amplifiers

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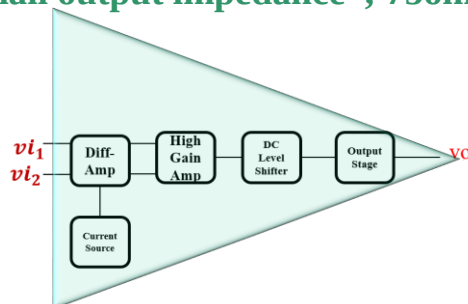
The Operational Amplifier

Designed to do mathematical operations such as addition , subtraction

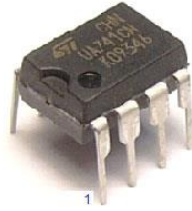
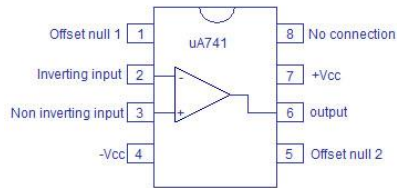
Very high voltage gain ; 200,000

Very High input impedance ; 10M ohm

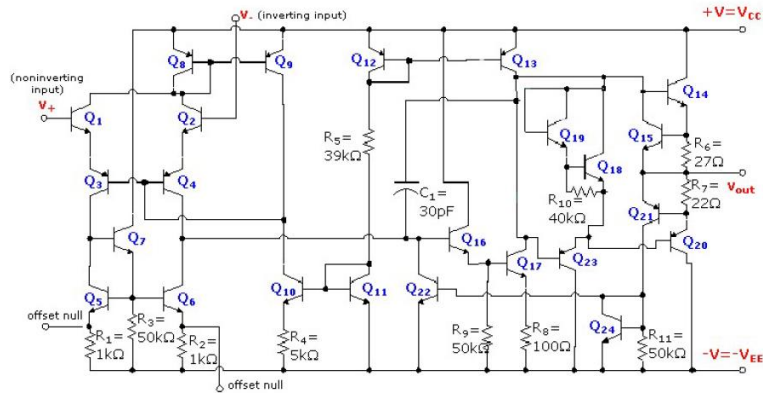
Very small output impedance ; 75ohm



Operational Amplifiers



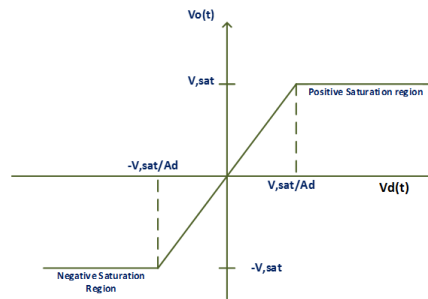
uA741 opamp Pinout and External appearance



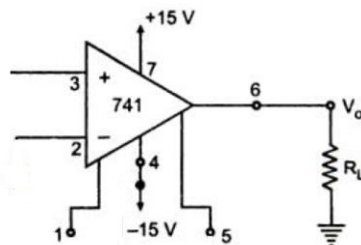
Operational Amplifier

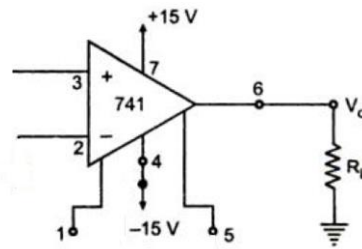
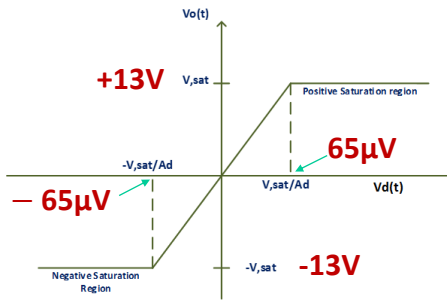
Transfer characteristic Curve:

$$V_o = \begin{cases} +V_{sat} & vd > \frac{V_{sat}}{A_d} \\ A_d vd & \frac{V_{sat}}{A_d} > vd > -\frac{V_{sat}}{A_d} \\ -V_{sat} & vd < -\frac{V_{sat}}{A_d} \end{cases}$$



$$vd = V(+) - V(-)$$





Let $\pm V_{cc} = \pm 15V ; A_d = 200,000$

$\therefore \pm V_{sat} = \pm 13V$

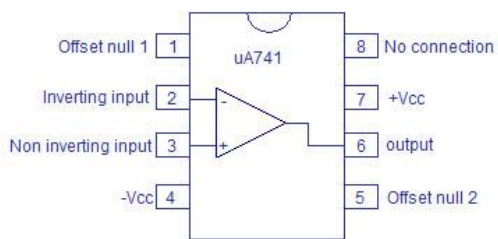
$\therefore$ If $V_d > 65\mu V ; V_o = +13V$

$\therefore$ If $V_d < -65\mu V ; V_o = -13V$

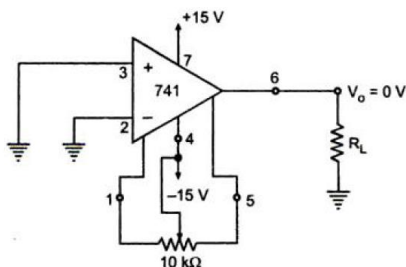
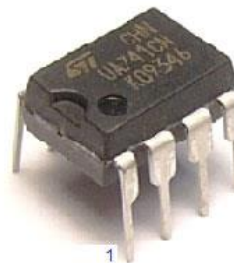
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Operational Amplifier

Pin Diagram for 741 :

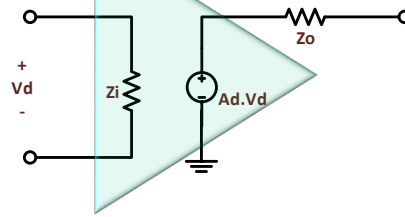


uA741 opamp Pinout and External appearance



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Op-amp Model in the Linear Region:

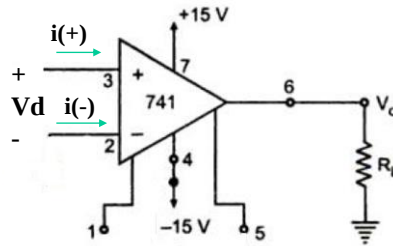


If the Op-Amp is IDEAL and in the Linear Region

Two Assumptions

1) $V_d \cong 0 \Rightarrow V(+)=V(-)$

2) $i(+)=i(-)=0$



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Op-amp Linear Applications:

1. Inverting Amplifier

a) Since $V(+)=0 ; \therefore V(-)=0$

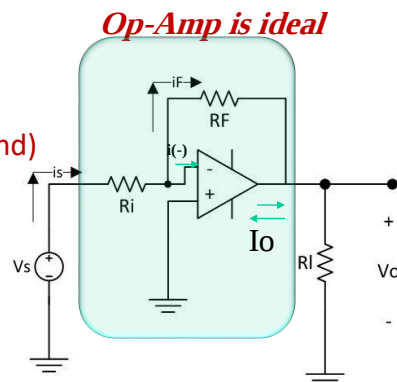
And $i_s = \frac{v_s}{R_i}$ (Virtual ground)

b) Since $i(-)=0 ; \therefore i_F = i_s$

c) $V_O = -R_F i_F$

$$V_O = -R_F i_s$$

$$V_O = -\frac{R_F}{R_i} V_s \quad \therefore A_v = -\frac{R_F}{R_i}$$



$$+V_{sat} > V_O > -V_{sat}$$

$$I_o < I_{o,max}$$

The voltage gain does not depend on RL

Op-Amp Linear Applications:

1. Inverting Amplifier

Design an inverting amplifier to provide $A_v = -200$

Solution :

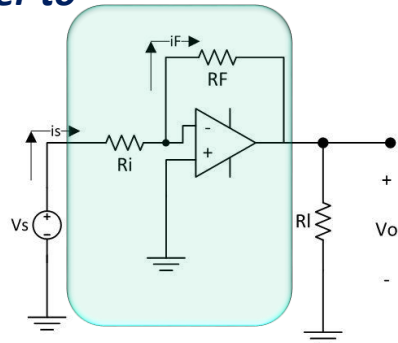
$$A_v = -\frac{R_F}{R_i} = -200$$

$$\therefore \frac{R_F}{R_i} = 200$$

Let $R_i = 20K$

$$\therefore R_F = 4000K$$

$$Z_i = R_i$$



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Op-amp Linear Applications:

2. Inverting Adder

1- Since $V(+) = 0$;

$$\therefore V(-) = 0$$

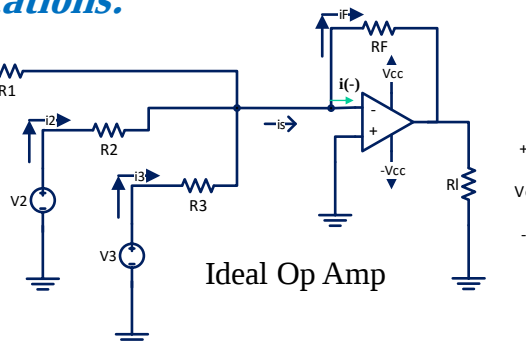
$$i_1 = \frac{v_1}{R_1} ; \quad i_2 = \frac{v_2}{R_2} ;$$

$$i_3 = \frac{v_3}{R_3}$$

$$i_s = i_1 + i_2 + i_3$$

2- Since $i(-) = 0$; $\therefore i_F = i_s$

3- $V_O = -R_F i_F$



$$V_O = -\left(\frac{R_F}{R_1} V_1 + \frac{R_F}{R_2} V_2 + \frac{R_F}{R_3} V_3\right)$$

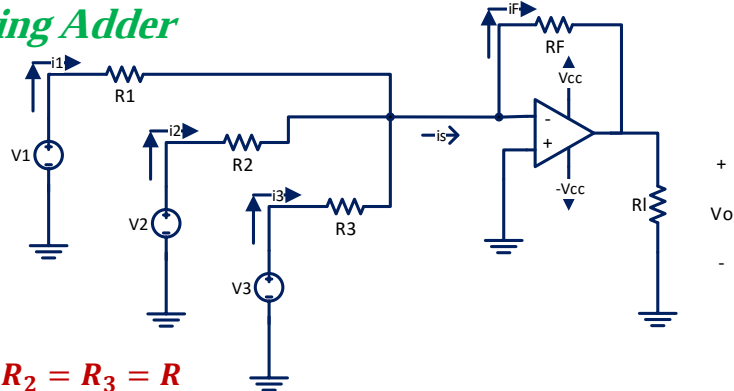
If $R_1 = R_2 = R_3 = R_F = R$

$$V_O = -(V_1 + V_2 + V_3)$$

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Op-amp Linear Applications:

2. Inverting Adder



If $R_1 = R_2 = R_3 = R$

And $R_F = \frac{R}{n} = \frac{R}{3}$

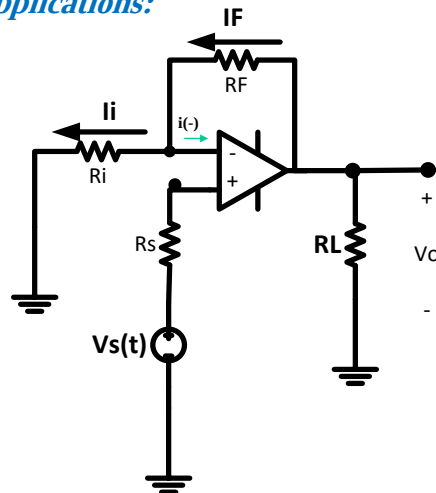


Averager

$$\therefore V_O = -\left(\frac{V_1 + V_2 + V_3}{3}\right)$$

Op-amp Linear Applications:

3. Non Inverting Amplifier



1- Since $V(+) = V_s$

$\therefore V(-) = V_s$

$$\therefore i_i = \frac{V_s}{R_i}$$

2- Since $i(-) = 0$;

$$\therefore i_F = i_i$$

$$3 - V_O = R_F i_F + R_i i_i$$

$$\Rightarrow V_O = \left(1 + \frac{R_F}{R_i}\right) V_+$$

$$Z_i = \infty$$

Op-amp Linear Applications:

Non Inverting Amplifier

Design a non inverting amplifier to provide $A_v = 100$

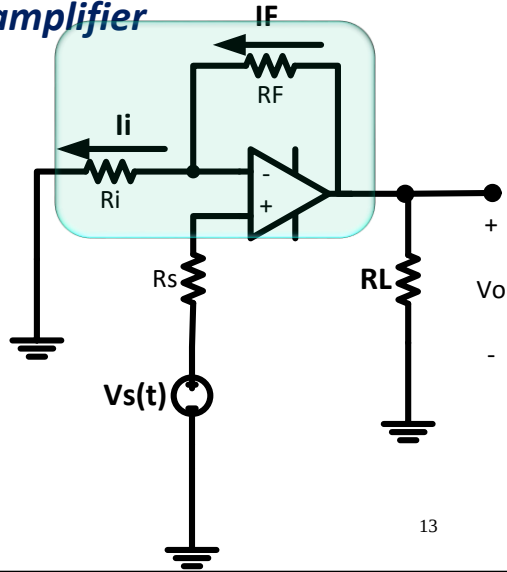
Solution :

$$A_v = 1 + \frac{R_F}{R_i} = 100$$

$$\therefore \frac{R_F}{R_i} = 99$$

Let $R_i = 10K$

$$\therefore R_F = 990K$$



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Op-amp Linear Applications:

4. Buffer, Unity Gain

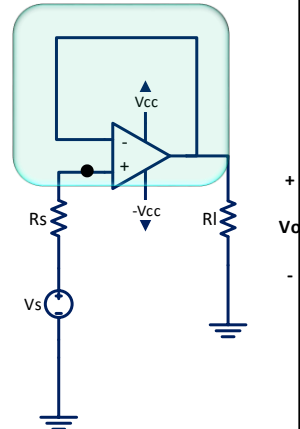
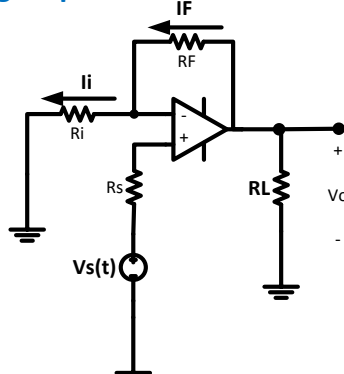
1- Since $V(+) = V_s$; $\therefore V(-) = V_s$

2- $V_o = V(-) = V_s$

Buffer is a special Case of non inverting amplifier for which:

$$R_i = \infty$$

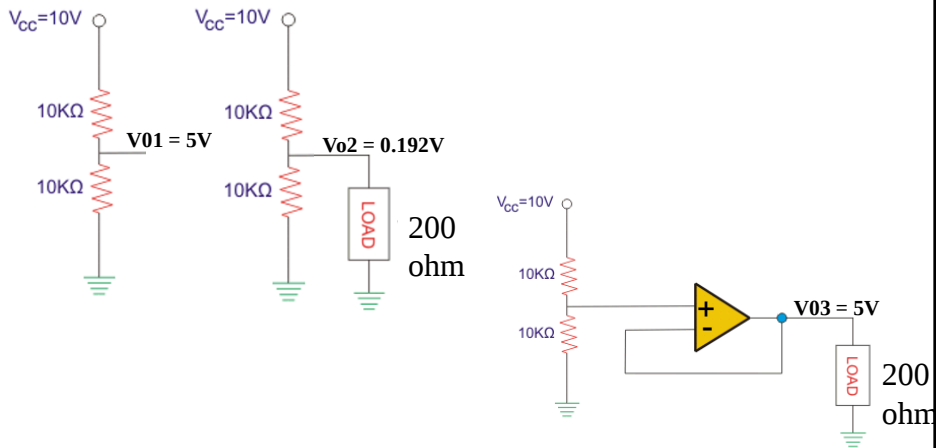
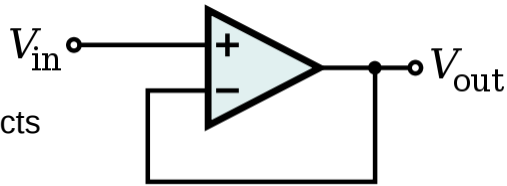
$$R_F = 0$$



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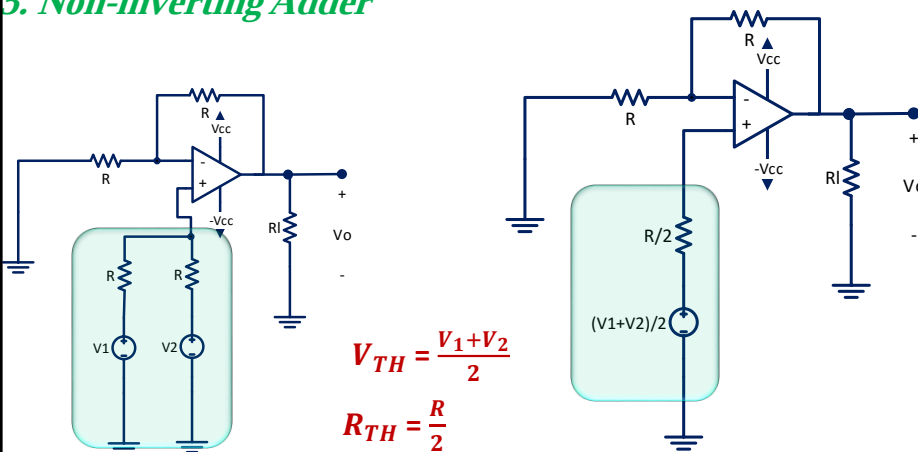
Op-Amp Buffer

$V_{out} = V_{in}$
Isolates loading effects

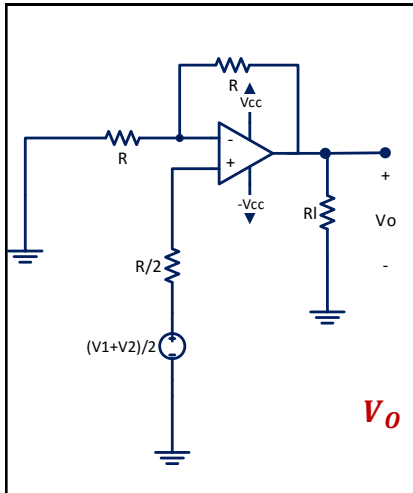


Op-amp Linear Applications:

5. Non-inverting Adder



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$$V_O = \left(1 + \frac{R}{R}\right) \left(\frac{V_1 + V_2}{2}\right) = V_1 + V_2$$

If we have n signal :

let $R_F = (n-1)R$

$$V_O = V_1 + V_2 + \dots + V_N$$

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Op-amp Linear Applications:

6. Voltage Subtraction

Using superposition

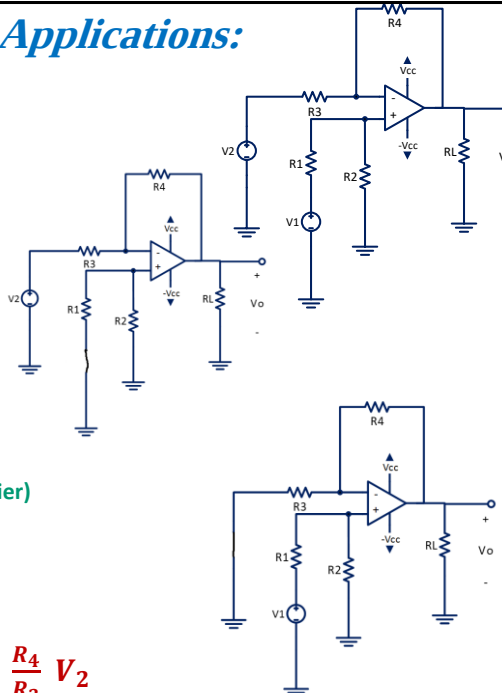
a) Let $V_1 = 0$ (Inverting amplifier)

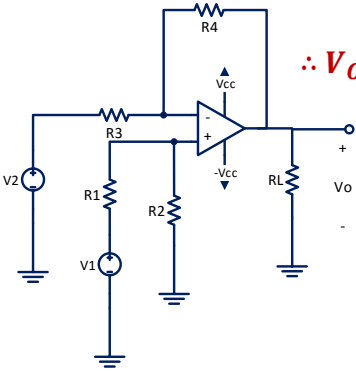
$$\therefore V_{o1} = -\frac{R_4}{R_3} V_2$$

b) Let $V_2 = 0$ (non inverting amplifier)

$$\therefore V_{o2} = \left(1 + \frac{R_4}{R_3}\right) \left(\frac{R_2}{R_1 + R_2}\right) V_1$$

c) Total $V_o = V_{o1} + V_{o2}$

$$\therefore V_O = \left(1 + \frac{R_4}{R_3}\right) \left(\frac{R_2}{R_1 + R_2}\right) V_1 - \frac{R_4}{R_3} V_2$$




$$\therefore V_O = \left(1 + \frac{R_4}{R_3}\right) \left(\frac{R_2}{R_1 + R_2}\right) V_1 - \frac{R_4}{R_3} V_2$$

$$V_O = aV_1 - bV_2$$

If $R_1 = R_3 = R$
and $R_2 = R_4 = mR$

$$V_O = m(V_1 - V_2)$$

Basic Difference Amplifier

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Op-amp Linear Applications:

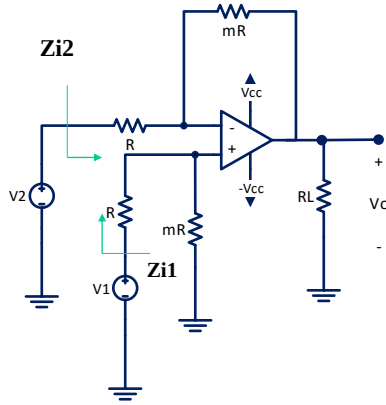
Basic Difference Amplifier

$$V_O = m(V_1 - V_2)$$

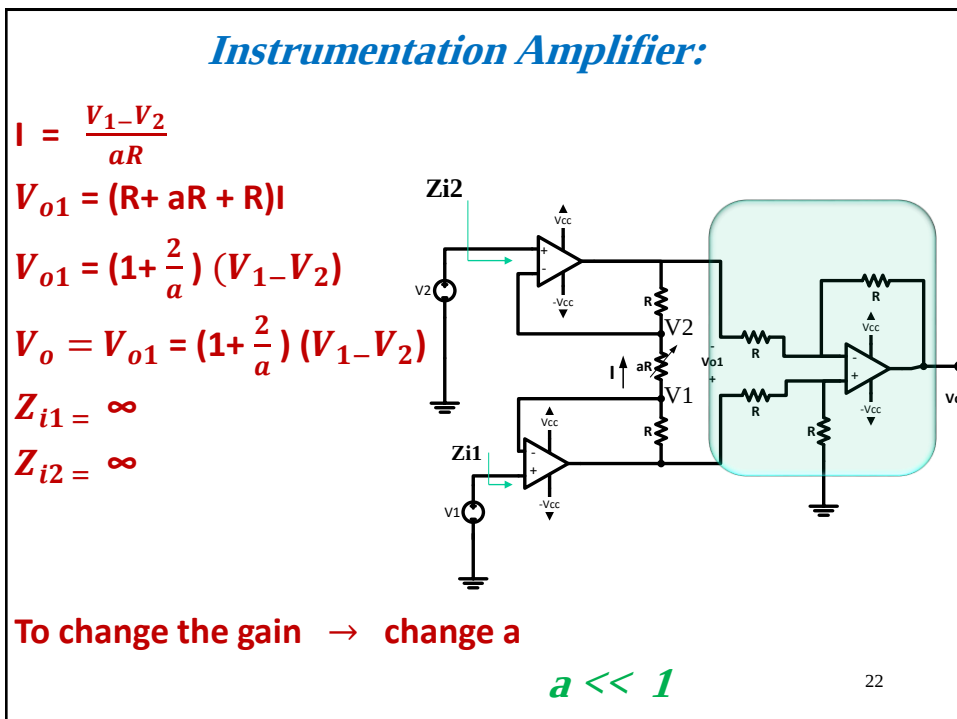
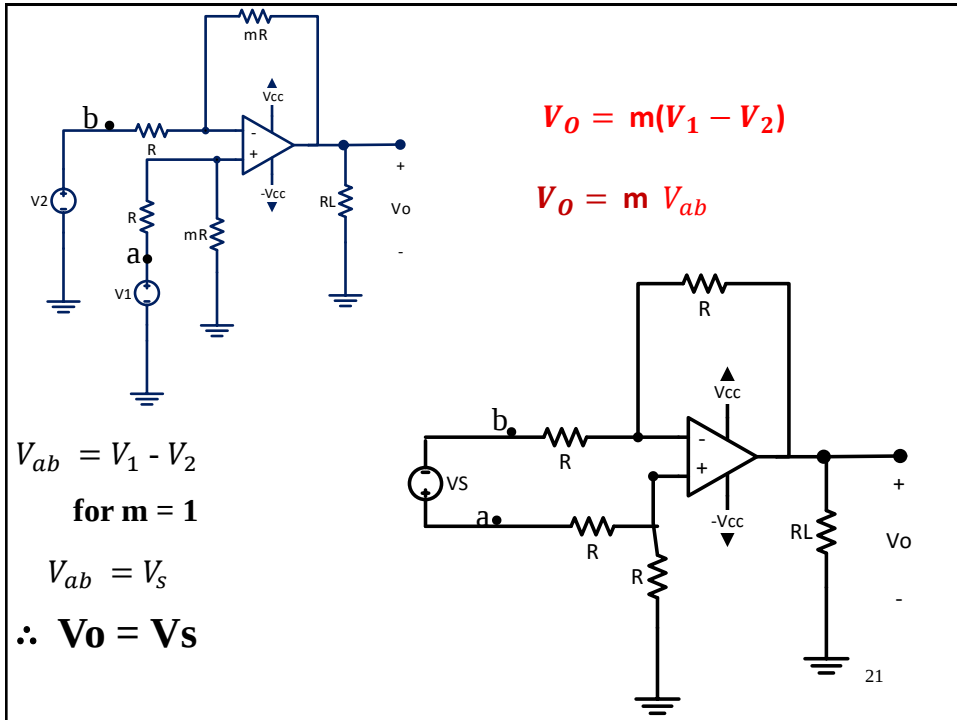
$$Z_{i1} = R + mR$$

$$Z_{i2} = R$$

***It has low input impedance**
***To Change the gain, we must change two resistors.**



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Measuring small resistance change

$$E_1 = \frac{R_1}{R_1 + R_1} E = \frac{E}{2}$$

$$E_2 = \frac{R}{R + R + \Delta R} E = \frac{R}{2R + \Delta R} E$$

$$E_1 - E_2 = \frac{E}{2} \left(\frac{\Delta R}{2R + \Delta R} \right)$$

ΔR is very small

$$E_1 - E_2 = \frac{E \Delta R}{2 \cdot 2R}$$

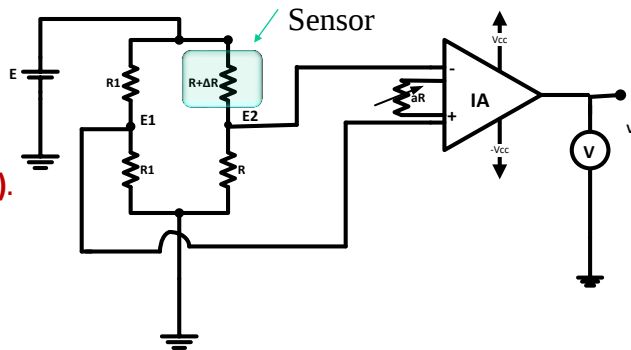
$$V_o = \left(1 + \frac{2}{a}\right) (E_1 - E_2)$$

$$\text{Let } \left(1 + \frac{2}{a}\right) = 400$$

$$V_o = (400) \left(\frac{\Delta R}{4R} \right) E$$

$$V_o = 100 E \left(\frac{\Delta R}{R} \right)$$

$$V_o = \left(1 + \frac{2}{a}\right) (E_1 - E_2)$$



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Measuring small resistance change

$$V_o = 100 E \left(\frac{\Delta R}{R} \right)$$

If $R = 10K$

$\Delta R = 0.1K$

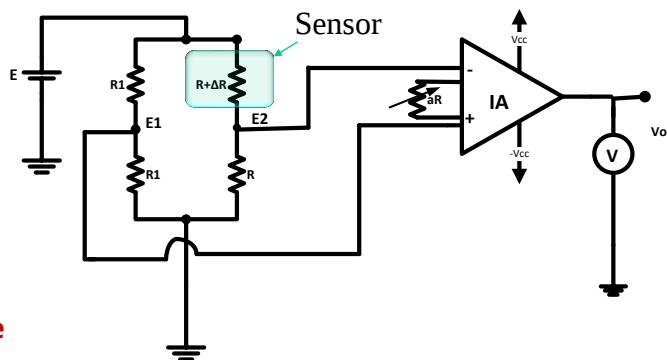
$E = 1V$

$\frac{\Delta R}{R} = 1\%$ change

$V_o = 1V$

$\therefore 1V \text{ per } 1\%$

change in resistance



If $V_o = 2V \rightarrow \Delta R = 0.2K$

If $V_o = 0.1V \rightarrow \Delta R = 0.01K$

If $V_o = 0.01V \rightarrow \Delta R = 0.001K$

If $V_o = 1mV \rightarrow \Delta R = 0.0001K$

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Voltage to current Converter

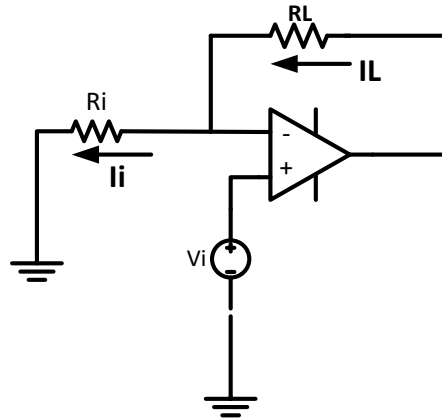
a) Floating load

Since $V(+) = V_i$

$$\therefore V(-) = V_i$$

$$I_i = \frac{V_i}{R_i}$$

$$I_L = I_i = \frac{V_i}{R_i}$$



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High-Resistance DC Voltmeter

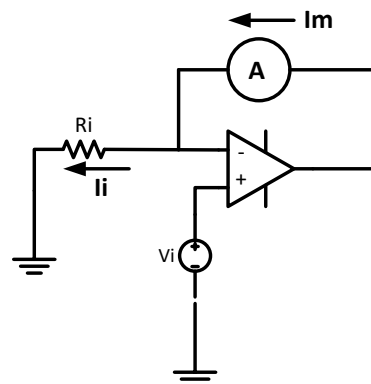
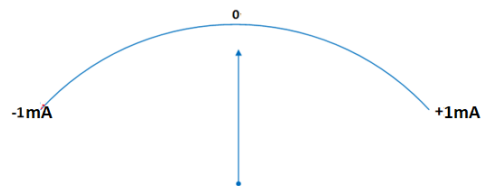
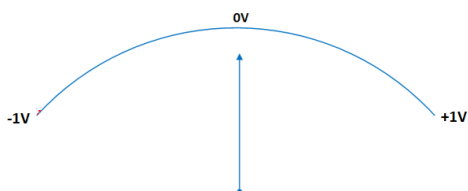
$$I_m = I_i = \frac{V_i}{R_i}$$

$$\text{If } V_i = +1 \rightarrow I_m = +1\text{mA}$$

$$R_i = 1\text{k}$$

$$\text{If } V_i = -1\text{V} \rightarrow I_m = -1\text{mA}$$

$$R_i = 1\text{k}$$



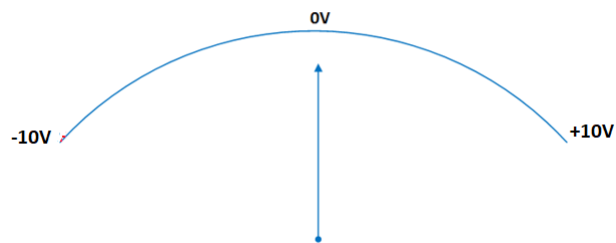
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If $V_i = +10\text{ V} \rightarrow I_m = +1\text{ mA}$

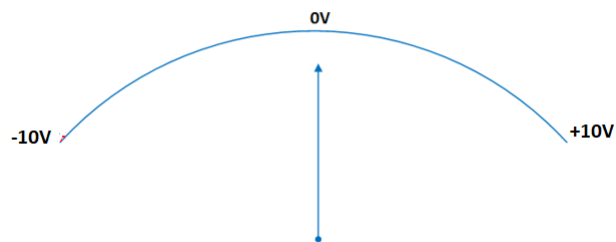
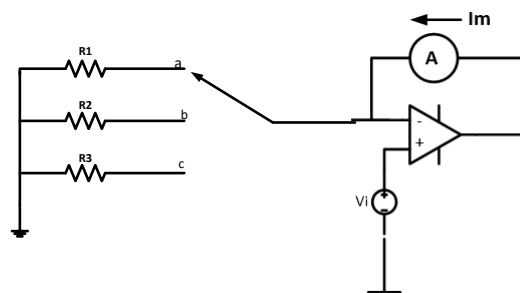
$R_i = 10\text{ k}$

If $V_i = -10\text{ V} \rightarrow I_m = -1\text{ mA}$

$R_i = 10\text{ k}$



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Voltage to current Converter

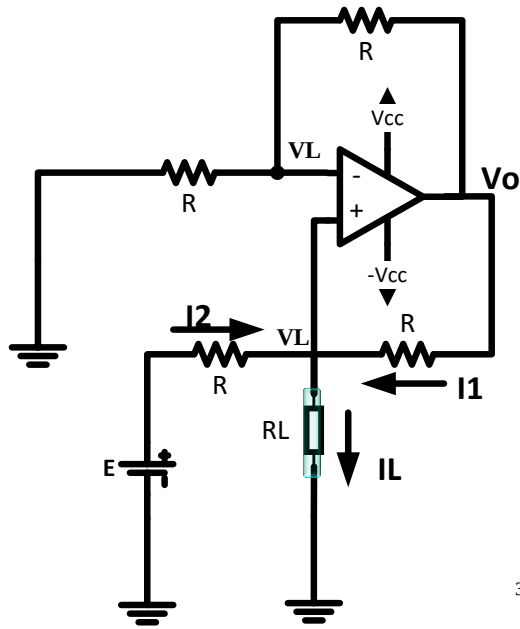
b) Grounded load

$$V_L = V(-) = \frac{1}{2} V_o$$

$$I_L = I_1 + I_2$$

$$I_L = \frac{V_o - V_L}{R} + \frac{E - V_L}{R}$$

$$\therefore I_L = \frac{E}{R}$$



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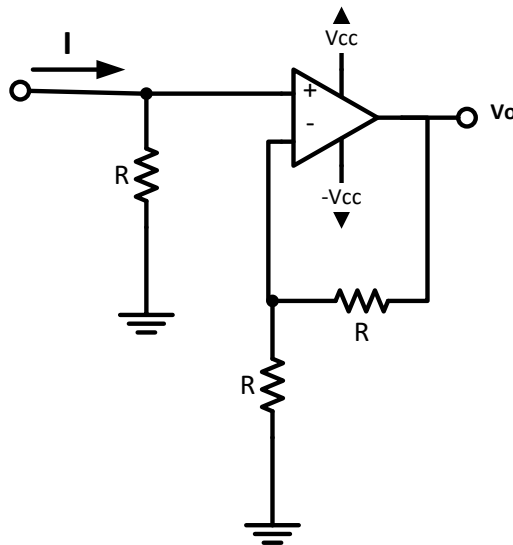
Current to Voltage Converter

$$V(+) = R I$$

$$V_o = \left(1 + \frac{R}{R}\right) V(+)$$

$$V_o = \left(1 + \frac{R}{R}\right) R I$$

$$V_o = K I$$



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Integrator

- So far, the input and feedback components have been resistors. If the feedback component used is a capacitor, the resulting connection is called an *integrator*.
- Recall that virtual ground means that we can consider the voltage at the junction of R and X_c to be ground (since $V_- = 0$ V) but that no current goes into ground at that point.

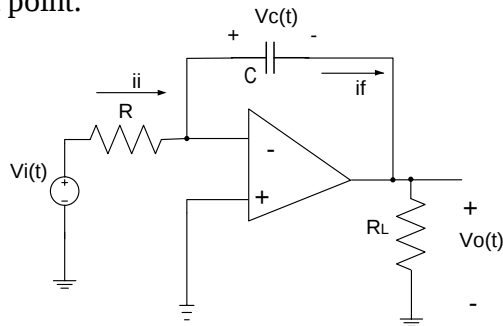
$$i_{i(t)} = i_{f(t)} = \frac{V_{i(t)}}{R}$$

$$V_c(t) = \frac{1}{C} \int_0^t i_f(t) dt$$

$$V_{o(t)} = -V_c(t)$$

$$V_{o(t)} = -\frac{1}{C} \int_0^t \frac{V_{i(t)}}{R_i} dt$$

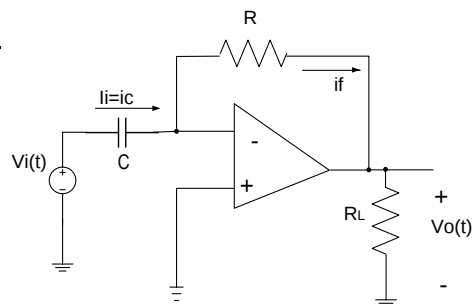
$$= -\frac{1}{RC} \int_0^t V_{i(t)} dt$$



Differentiator

A differentiator, while not as useful as the circuit forms covered above, the differentiator does provide a useful operation, the resulting relation for the circuit being

$$i_{i(t)} = i_{f(t)} = i_{C(t)} = C \frac{dV_{i(t)}}{dt}$$

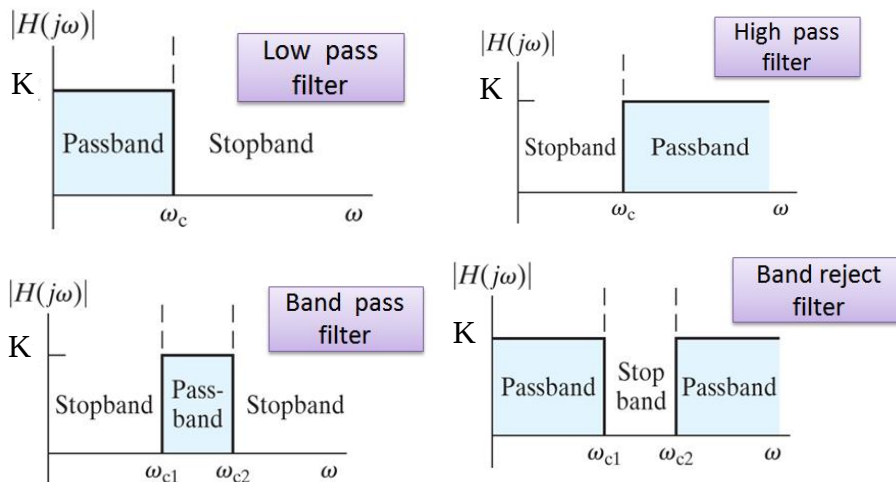


Filters are circuits pass signals of certain frequencies and block or attenuate signals of other frequencies

Active filters

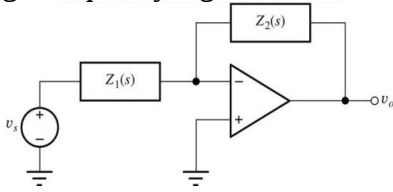
- Based on circuits with op amps, which are active devices, since they require an external power supply ($\pm V_{CC}$).
- Eliminate all of the disadvantages of passive filters:
 - Can create a pass band gain > 1 ;
 - Can add loads without changing the filter characteristics;
 - All four types of filters can be created using op amps, resistors, and capacitors – no inductors;
 - Can cascade simple (first- and second-order) filters to create higher order filters that are more nearly ideal.

Ideal Active Filter Classification



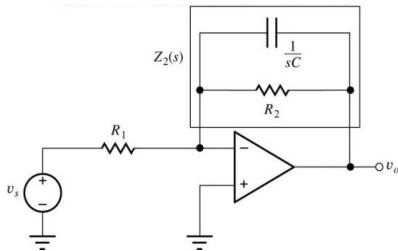
The Active Low-pass Filter

Low pass filters are used to pass low-frequency signals and attenuate high frequency signals



$$A_{v(j\omega)} = \frac{\tilde{v}_o(j\omega)}{\tilde{v}_s(j\omega)} = -\frac{Z_2(j\omega)}{Z_1(j\omega)}$$

$$Z_2(j\omega) = \frac{R_2 \frac{1}{j\omega C}}{R_2 + \frac{1}{j\omega C}} = \frac{R_2}{j\omega C R_2 + 1} \quad Z_1(j\omega) = R_1$$



$$A_{v(j\omega)} = -\frac{R_2}{R_1} \frac{1}{(1 + j\omega C R_2)}$$

$$= \frac{-K}{\left(1 + \frac{j\omega}{\omega_c}\right)}$$

$$K = \frac{R_2}{R_1}$$

& cut-off frequency: $\omega_c = 2\pi f_c = \frac{1}{R_2 C} \therefore f_c = \frac{1}{2\pi R_2 C}$

Frequency Response (Bode Plot)

Magnitude Plot (Magnitude in decibels vs log of frequency)

$$\log(AB) = \log A + \log B$$

$$\log\left(\frac{N}{D}\right) = \log N - \log D$$

$$A_{dB} = 20 \log |H(j\omega)|$$

$$|H(j\omega)| = |A_v(j\omega)|$$

$$|A_v(j\omega)| = \frac{K}{\sqrt{1 + \left(\frac{\omega}{\omega_c}\right)^2}}$$

at $\omega = 0.1\omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{0.1\omega_c}{\omega_c}\right)^2}}$$

$$= 20 \log \frac{1}{\sqrt{1 + 0.01}}$$

$$\cong 20 \log 1 = 0dB$$

at $\omega = \omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{\omega_c}\right)^2}}$$

$$= 20 \log \frac{1}{\sqrt{1 + 1}}$$

$$= 20 \log |0.707| = -3dB$$

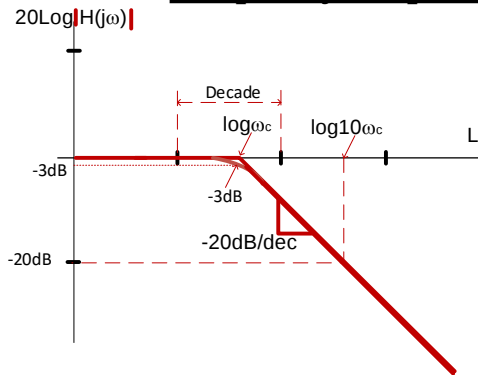
at $\omega = 10\omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{10\omega_c}{\omega_c}\right)^2}}$$

$$= 20 \log \frac{1}{\sqrt{1 + 100}}$$

$$= 20 \log |0.1| = -20dB$$

Frequency Response (Bode Plot)



Summary

at $\omega = 0.1\omega_c$
 $\text{Log } \omega = 20\log 1 = 0\text{dB}$
 at $\omega = \omega_c$
 $= 20\log 0.707 = -3\text{dB}$
 at $\omega = 10\omega_c$
 $= 20\log 0.1 = -20\text{dB}$
 at $\omega = 100\omega_c$
 $= 20\log 0.01 = -40\text{dB}$

- At frequencies below ω_c , the amplifier is an inverting amplifier with gain set by the ratio of resistors R_2 and R_1 .
- At frequencies above ω_c the amplifier response “rolls off” at -20dB/decade.
- Notice that cutoff frequency and gain can be independently set.

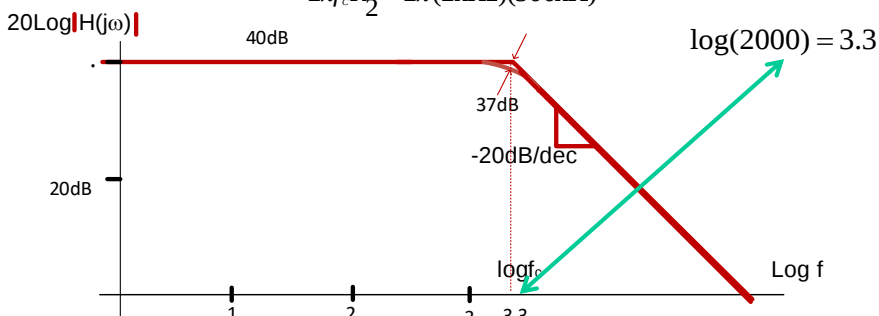
Active Low-pass Filter: Example

- **Problem:** Design an active low-pass filter
- **Given Data:** $A_v = 40\text{ dB}$, $R_{in} = 5\text{ k}\Omega$, $f_c = 2\text{ kHz}$
- **Assumptions:** Ideal op amp, specified gain represents the desired low-frequency gain.
- **Analysis:** $|A_v| = 10^{40\text{dB}/20\text{dB}} = 100$

Input resistance is controlled by R_1 and voltage gain is set by R_2 / R_1 .
 The cutoff frequency is then set by C.

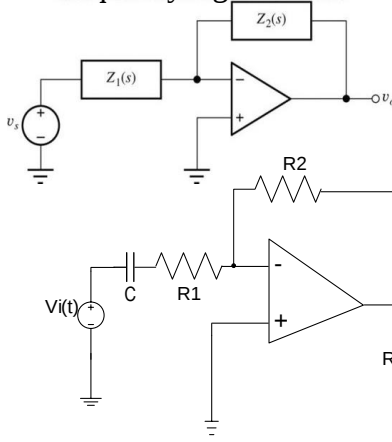
$$R_1 = R_{in} = 5\text{ k}\Omega \quad \text{and} \quad |A_v| = \frac{R_2}{R_1} \Rightarrow R_2 = 100R_1 = 500\text{ k}\Omega$$

$$C = \frac{1}{2\pi f_c R_2} = \frac{1}{2\pi (2\text{ kHz})(500\text{ k}\Omega)} = 159\text{ pF}$$



The Active High-pass Filter

High pass filters are used to pass high-frequency signals and attenuate low frequency signals



$$A_{v(j\omega)} = \frac{\tilde{v}_o(j\omega)}{\tilde{v}_s(j\omega)} = -\frac{Z_2(j\omega)}{Z_1(j\omega)}$$

$$Z_1(j\omega) = R_1 + \frac{1}{j\omega C} \quad Z_2(j\omega) = R_2$$

$$A_{v(j\omega)} = -\frac{R_2}{(R_1 + \frac{1}{j\omega C})}$$

$$A_{v(j\omega)} = -\frac{R_2/R_1}{(1 + \frac{1}{j\omega R_1 C})}$$

$$= \frac{-K}{(1 + \frac{\omega_c}{j\omega})}$$

$$K = \frac{R_2}{R_1} \text{ high frequency gain}$$

$$\omega_c = 2\pi f_c = \frac{1}{R_1 C} \quad \therefore f_c = \frac{1}{2\pi R_1 C}$$

Frequency Response (Bode Plot)

Magnitude Plot
(Magnitude in decibels
vs log of frequency)

$$A_{dB} = 20 \log |H(j\omega)|$$

$$|H(j\omega)| = \frac{|A_v(j\omega)|}{K}$$

$$= \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{\omega}\right)^2}}$$

at $\omega = \omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{\omega_c}\right)^2}}$$

$$= 20 \log \frac{1}{\sqrt{1 + 1}}$$

$$= 20 \log |0.707| = -3dB$$

at $\omega = 0.1\omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{0.1\omega_c}\right)^2}} = 20 \log \frac{1}{\sqrt{1 + 100}}$$

$$\cong 20 \log 0.1 = -20dB$$

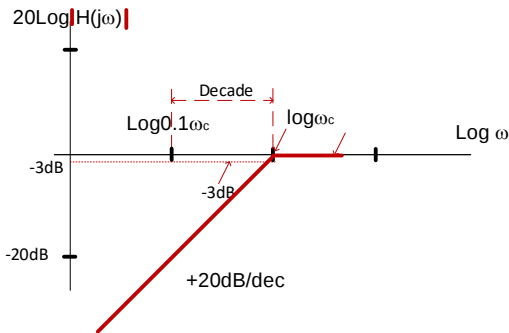
at $\omega = 0.01\omega_c$

$$20 \log \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{0.01\omega_c}\right)^2}}$$

$$= 20 \log \frac{1}{\sqrt{1 + 10000}}$$

$$= 20 \log 0.01 = -40dB$$

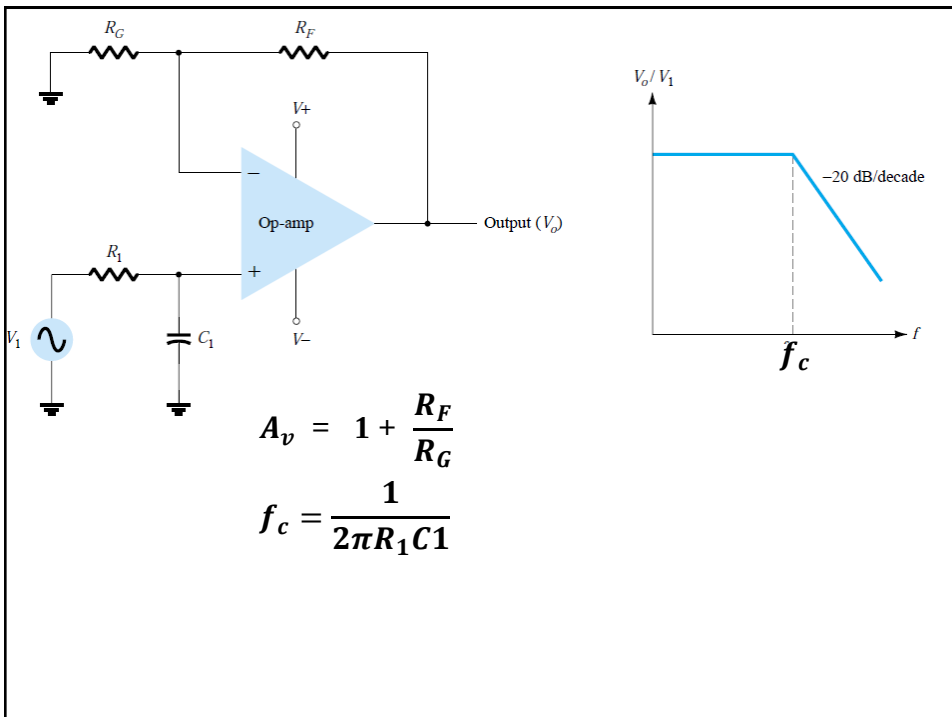
Frequency Response (Bode Plot)



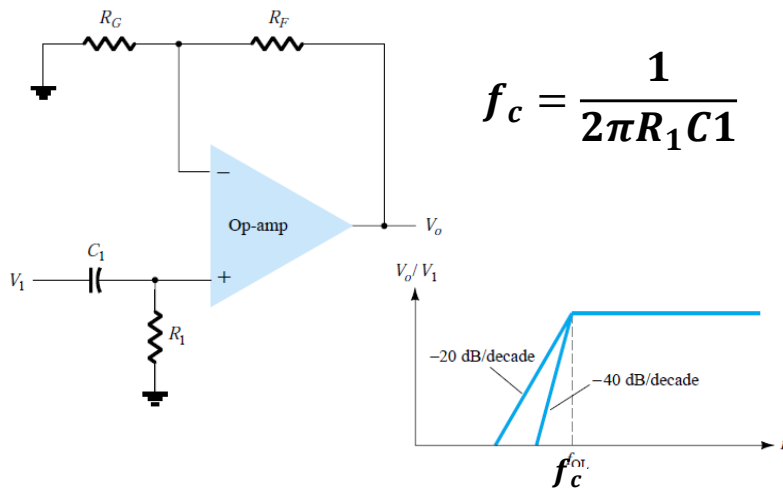
Summary

at $\omega = 0.1\omega_c$
 $= 20 \log 0.1 = -20dB$
 at $\omega = \omega_c$
 $= 20 \log 0.707 = -3dB$
 at $\omega = 0.01\omega_c$
 $= 20 \log 0.01 = -40dB$
 at $\omega = 0$
 $= 20 \log 1 = 0dB$

- At frequencies above ω_c , the amplifier is an inverting amplifier with gain set by the ratio of resistors R_2 and R_1 .
- At frequencies below ω_c the amplifier response “rolls off” at -20dB/decade.
- Notice that cutoff frequency and gain



High-Pass Active Filter



Comparator : Zero -Level detector

Exact analysis:

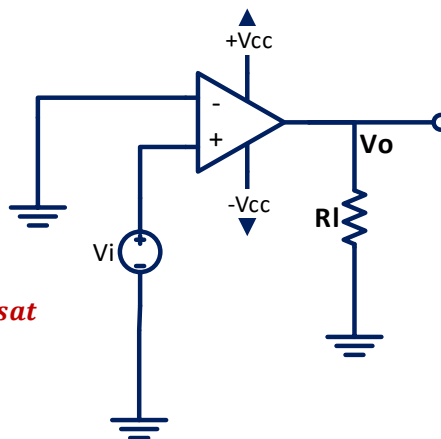
When $v_d > 65\mu V$; $V_O = +V_{sat}$

When $v_d < -65\mu V$; $V_O = -V_{sat}$

Approximate analysis

When $v_d > 0V$; $V_O = +V_{sat}$

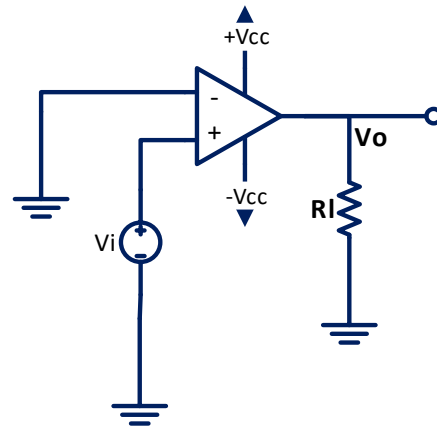
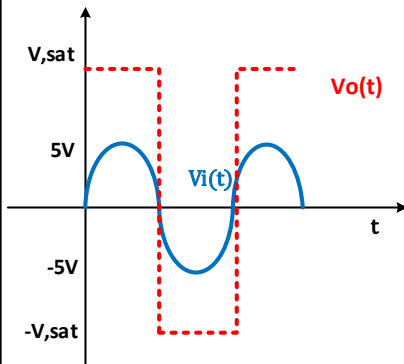
When $v_d < 0V$; $V_O = -V_{sat}$



Comparator : Zero –Level detector

$$V_i(t) = 5\sin \omega t \text{ v}$$

$$\pm V_{sat} = \pm 13 \text{ v}$$



When $v_d > 0\text{V}$; $V_o = +V_{sat}$

When $v_d < 0\text{V}$; $V_o = -V_{sat}$

$\therefore$ When $V_i > 0\text{V}$; $V_o = +V_{sat}$

$\therefore$ When $V_i < 0\text{V}$; $V_o = -V_{sat}$

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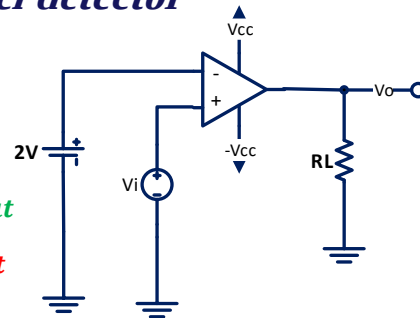
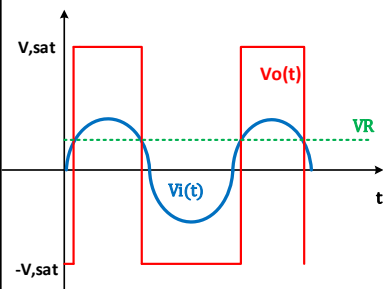
Non Zero –Level detector

$$V_i(t) = 5\sin \omega t \text{ v}$$

$$\pm V_{sat} = \pm 13 \text{ v}$$

When $V_i > 2\text{V}$; $V_o = +V_{sat}$

When $V_i < 2\text{V}$; $V_o = -V_{sat}$



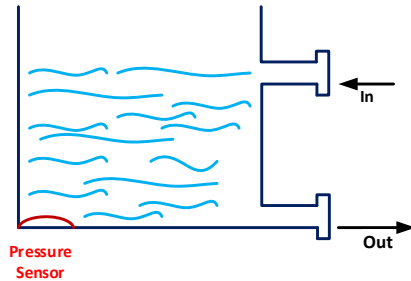
When $v_d > 0\text{V}$; $V_o = +V_{sat}$

When $v_d < 0\text{V}$; $V_o = -V_{sat}$

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Practical Non Zero –Level detector

Application



The pressure sensor generates a voltage proportional to the water level in the tank

When water level reaches the maximum allowable lever

$V_i = 2V$

$V(-) = 2V$

When $V_i > 2V$; $V_O = +V_{sat}$

When $V_i < 2V$; $V_O = -V_{sat}$

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Voltage–Level detector with LEDs:

When $V_i > 2V$; $V_O = +V_{sat}$

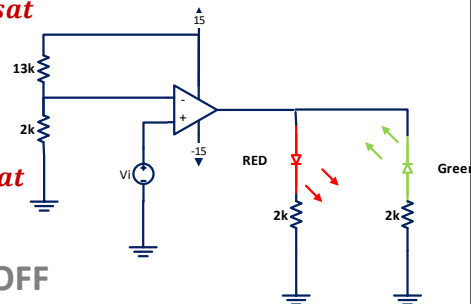
$\therefore$ Red LED is ON

$\therefore$ green LED is OFF

When $V_i < 2V$; $V_O = -V_{sat}$

$\therefore$ green LED is ON

$\therefore$ Red LED is OFF



When $V_i = 2V$; $V_O = 0$

$\therefore$ green LED and the Red LED are OFF

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Over Temperature sensing Circuit

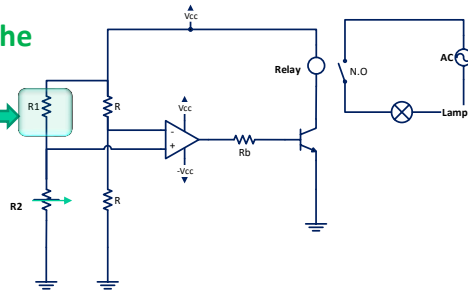
$R_1 \uparrow$ as $T \downarrow$

R_1 = Resistance of the thermistor.

R_2 is set equal to the resistance of the thermistor at the critical temp.

$R = 100k$

This is the thermistor



1) At Normal temperature ($T < T_c$)

$$R_1 > R_2$$

$$V(+)=\frac{R_2}{R_1+R_2} V_{CC} < \frac{1}{2} V_{CC}$$

$$V(-)=\frac{1}{2} V_{CC}$$

$$\therefore V(-) > V(+), \therefore V_{op} = -V_{sat}$$

$$\therefore \text{transistor is cut off ; } I_C = 0$$

$\therefore$ Relay is denergized

$\therefore$ switch is open

$\therefore$ Lamp is OFF

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Over Temperature sensing Circuit

2) When $T = T_c$

$$R_1 = R_2$$

$$V(+)=V(-)=\frac{1}{2} V_{cc}$$

$$\therefore V_{op} = 0$$

$$\therefore \text{transistor is in cut off ;}$$

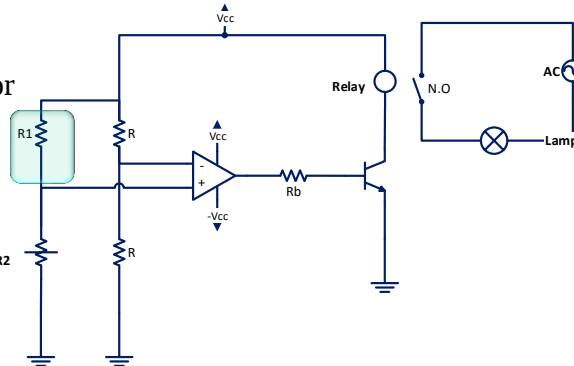
$$I_C = 0$$

$\therefore$ Relay is denergized

$\therefore$ switch is open

$\therefore$ Lamp is OFF

Sensor



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Over Temperature sensing Circuit

3- When $T > T_c$

$$R_1 < R_2$$

$$V(+)=\frac{R_2}{R_1+R_2} V_{cc} > \frac{1}{2} V_{cc}$$

$$V(-)=\frac{1}{2} V_{cc}$$

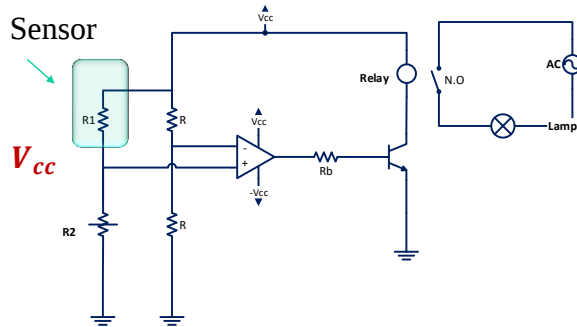
$$\therefore V(+)>V(-)$$

$$\therefore V_{op}=+V_{sat}$$

$\therefore$ transistor is conducting

$\therefore$ Relay is energized

$\therefore$ Lamp is on



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Schmitt Trigger Comparator

1. Assume $V_O = +V_{sat}$

$$V(-)=V_i$$

$$V(+)=\frac{R_2}{R_1+R_2} (+V_{sat}) = V_{UT}$$

$$V_d > 0$$

$$\frac{R_2}{R_1+R_2} (+V_{sat}) - V_i > 0$$

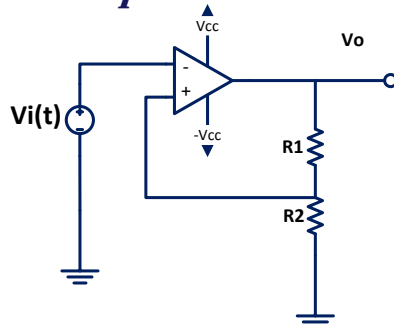
$$\therefore V_i < \frac{R_2}{R_1+R_2} (+V_{sat})$$

$$\therefore \text{as long as } V_i < \frac{R_2}{R_1+R_2} (+V_{sat})$$

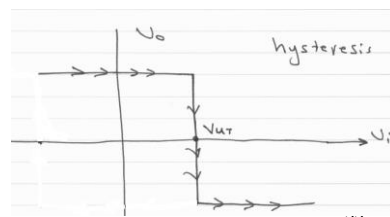
$$V_O = +V_{sat}$$

$$\text{But when } V_i > \frac{R_2}{R_1+R_2} (+V_{sat})$$

$$V_O \text{ switch to } (-V_{sat})$$



Inverting Schmitt trigger comparator



Schmitt Trigger Comparator

2. Assume $V_O = -V_{sat}$

$$V(-) = V_i$$

$$V(+) = \frac{R_2}{R_1 + R_2} (-V_{sat}) = V_{LT}$$

$$v_d < 0$$

$$\frac{R_2}{R_1 + R_2} (-V_{sat}) - V_i < 0$$

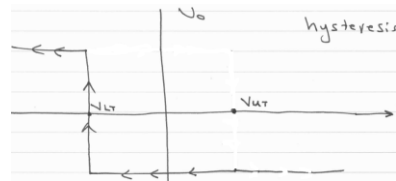
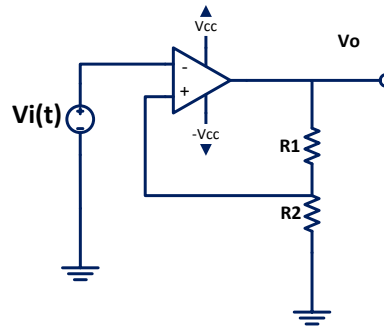
$$\therefore V_i > \frac{R_2}{R_1 + R_2} (-V_{sat})$$

$$\therefore \text{as long as } V_i > \frac{R_2}{R_1 + R_2} (-V_{sat})$$

$$V_O = -V_{sat}$$

$$\text{But when } V_i < \frac{R_2}{R_1 + R_2} (-V_{sat})$$

$$V_O \text{ switch to } (+V_{sat})$$



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Schmitt Trigger Comparator

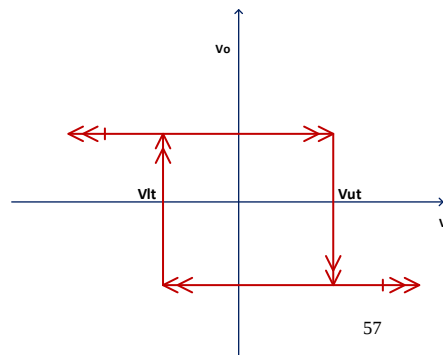
Hysteresis voltage $\equiv V_H = V_{UT} - V_{LT}$

$V_{UT} \equiv$ Upper Threshold voltage

$$V_{UT} = \frac{R_2}{R_1 + R_2} (+V_{sat})$$

$V_{LT} \equiv$ Lower Threshold voltage

$$V_{LT} = \frac{R_2}{R_1 + R_2} (-V_{sat})$$



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Schmitt Trigger Comparator

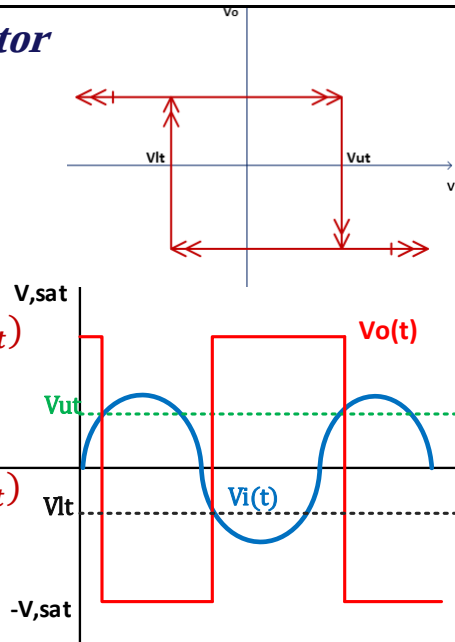
Signal Wave form

when $V_i < \frac{R_2}{R_1 + R_2} (-V_{sat})$

V_o switch to $(+V_{sat})$

when $V_i > \frac{R_2}{R_1 + R_2} (+V_{sat})$

V_o switch to $(-V_{sat})$



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Room Thermostat

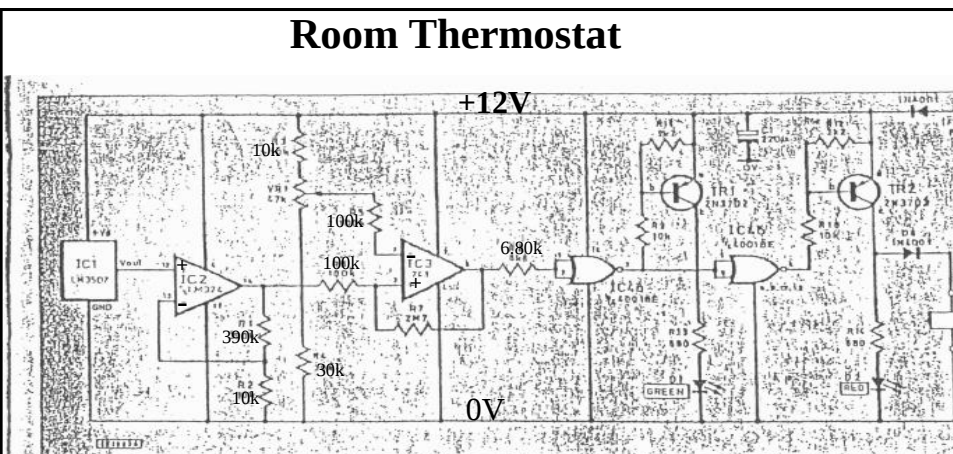


Fig. 2. Complete circuit diagram for the Room Thermostat. The connections to the "relay" are for the low voltage only.

IC1 = LM3502

IC2 = LM324

IC3 = MA741

IC4 = 4001B

TR1 = 2N3702

TR2 = 2N3702

R1 = 390K

R2 = 10K

R3 = 10K

VR1 = 47K

R4 = 30K

R5 = 100K

R6 = 100K

R7 = 2.7MΩ

R8 = 6.8K

R9 = 10K

R10 = 10K

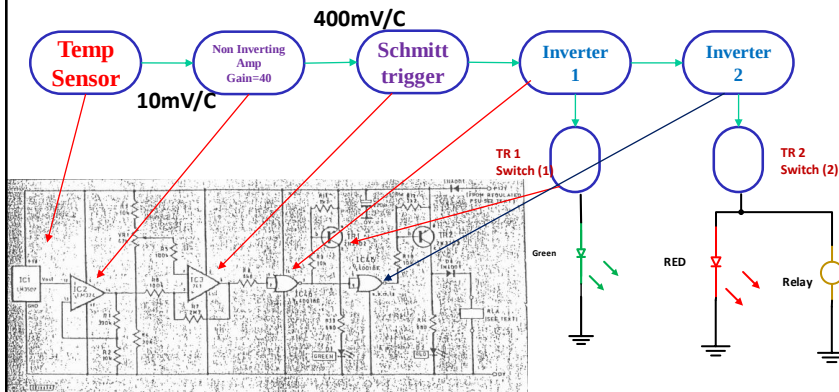
R11 = 2.2K

R12 = 2.2K

R13 = 0.68K

Schmitt Trigger Comparator

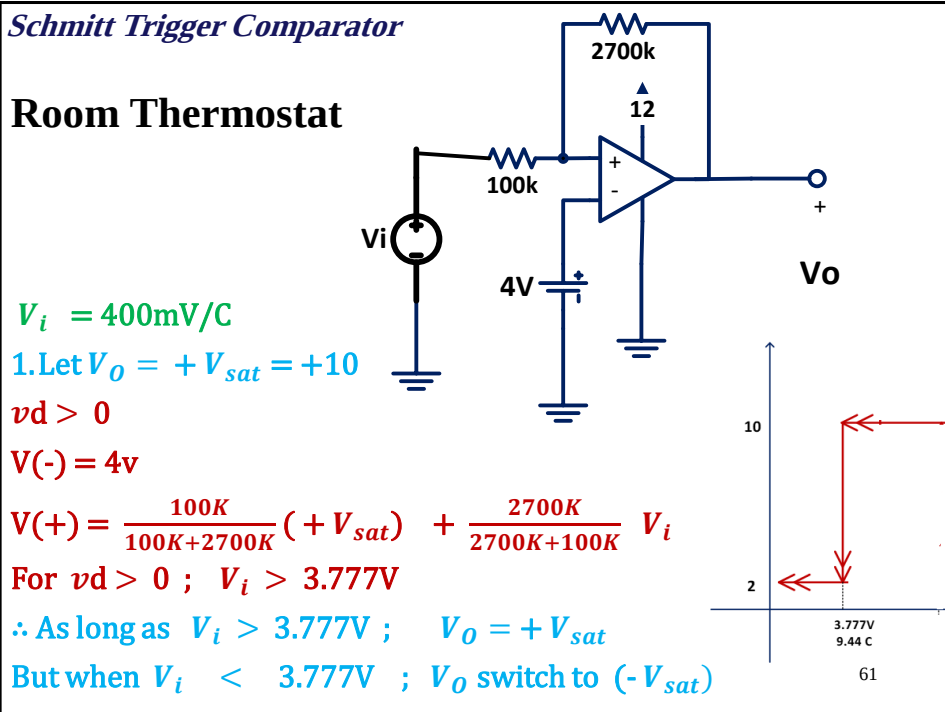
Room Thermostat



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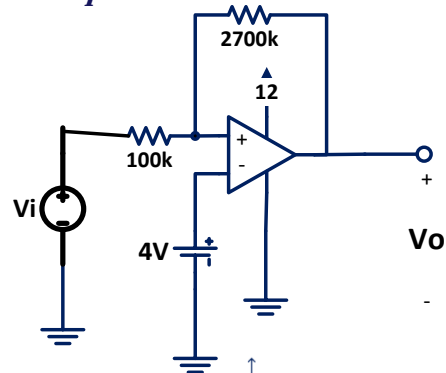
Schmitt Trigger Comparator

Room Thermostat



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Schmitt Trigger Comparator



2. Let $V_O = -V_{sat} = +2$

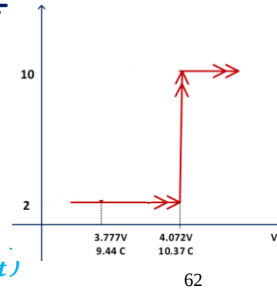
$v_d < 0$

$V(-) = 4V$

$$V(+)=\frac{100K}{100K+2700K}(-V_{sat})+\frac{2700K}{2700K+100K}V_i$$

For $v_d < 0$; $V_i < 4.072V$

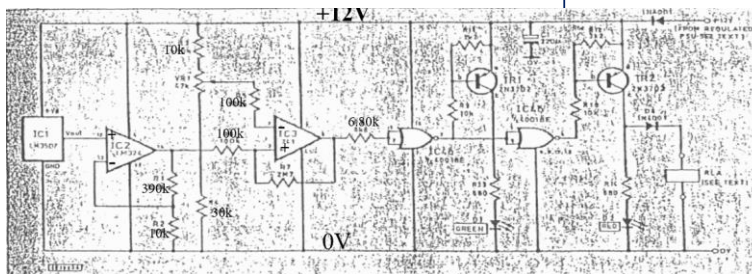
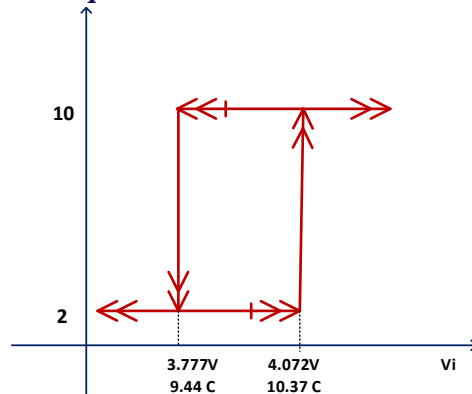
∴ As long as $V_i < 4.072V$; $V_O = -V_{sat}$
But when $V_i > 4.072V$; V_O switch to $(+V_{sat})$



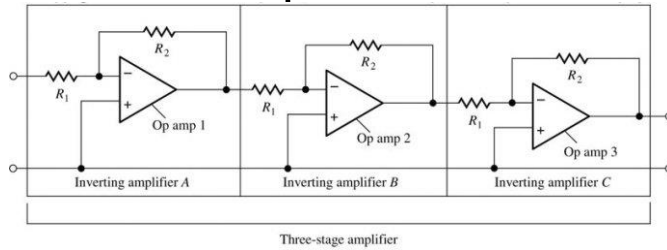
Schmitt Trigger Comparator

1) When $T > 10.37^\circ\text{C}$, $V_o = +V_{sat}$
Transistor (2) is Off, Relay is
denergized and Heater is Off.

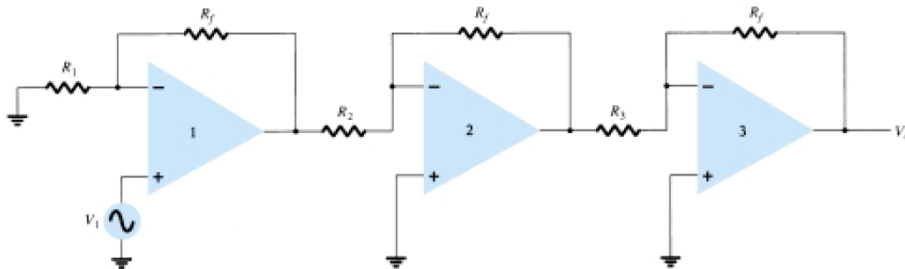
2) Then $T < 9.44^\circ\text{C}$, $V_o = -V_{sat}$
Transistor (2) is On, Relay is
energized and Heater is on.



Cascaded Amplifiers



- Connecting several amplifiers in cascade (output of one stage connected to the input of the next) can meet design specifications not met by a single amplifier.
- Each Amplifier stage is built using an op amp with parameters A , R_{id} , R_o , called open loop parameters, that describe the op amp with no external elements.
- A_v , R_{in} , R_{out} are closed loop parameters that can be used to describe each closed-loop op amp stage with its feedback network, as well as the overall composite (cascaded) amplifier.
- The gain of each stage can be calculated separately, then the total gain is found by multiplying the resulting gains



$$A = A_1 A_2 A_3$$

where $A_1 = 1 + R_f/R_1$, $A_2 = -R_f/R_2$, and $A_3 = -R_f/R_3$.