ENCS3340 - Artificial Intelligence

Uninformed Search

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Uninformed Search Strategies

- Uninformed search strategies use only the information available in the problem definition
- Examples:
 - Breadth-first search
 - Depth-first search
 - Iterative deepening search
 - Uniform-cost search

Breadth-First Search

- all the nodes reachable from the current node are explored first
 - Expand shallowest unexpanded node
 - achieved by the TREE-SEARCH method by appending newly generated nodes at the end of the search queue



• Implementation: fringe is a FIFO queue, i.e., new successors go at end

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Fringe: [7,8,9,10,11] + [12,13]

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Fringe: [8,9.10,11,12,13] + [14,15]

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Fringe: [9,10,11,12,13,14,15] + [16,17]

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Fringe: [10,11,12,13,14,15,16,17] + [18,19]

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Fringe: [11,12,13,14,15,16,17,18,19] + [20,21]

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Fringe: [12, 13, 14, 15, 16, 17, 18, 19, 20, 21] + [22,23]

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Fringe: [13,14,15,16,17,18,19,20,21, 22, 23] + [24,25]

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Fringe: [14,15,16,17,18,19,20,21,22,23,24,25] + [26,27] STUDENTS-HUB.com



Fringe: [15,16,17,18,19,20,21,22,23,24,25,26,27] + [28,29] STUDENTS-HUB.com



Fringe: [16,17,18,19,20,21,22,23,24,25,26,27,28,29] + [30,31] STUDENTS-HUB.com



Fringe: [17,18,19,20,21,22,23,24,25,26,27,28,29,30,31]

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Fringe: [18,19,20,21,22,23,24,25,26,27,28,29,30,31]

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Fringe: [19,20,21,22,23,24,25,26,27,28,29,30,31]

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Fringe: [20,21,22,23,24,25,26,27,28,29,30,31]

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Fringe: [21,22,23,24,25,26,27,28,29,30,31]

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Fringe: [22,23,24,25,26,27,28,29,30,31]

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Fringe: [23,24,25,26,27,28,29,30,31]

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Fringe: [24,25,26,27,28,29,30,31]

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Fringe: [25,26,27,28,29,30,31]

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Time Complexity	O(b ^{d+1})
Space Complexity	O(b ^{d+1})
Completeness	yes (for finite b)
Optimality	yes (for non-negative path costs)

- b branching factor
- d depth of the optimal solution

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- Keep a set of explored (visited) nodes.
- When a node is expanded, add the generated nodes to frontier only if not in the frontier or explored set

Example: BFS for Graphs

• For the following state space, list all the visited nodes and draw the search tree to go from S to G using BFS. What is the returned solution?



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Example: BFS for Graphs (Cont.)

- Visited Nodes: S, A, B, C, H, G
- Solution (Path to goal): S, B, G





- the nodes with the lowest cost are explored first
 - similar to BREADTH-FIRST, but with an evaluation of the cost for each reachable node
 - g(n) = path cost(n) = sum of individual edge costs to reach the current node
- Implementation: fringe is a queue ordered by path cost (priority queue)
- Equivalent to breadth-first if step costs all equal

function UNIFORM-COST-SEARCH(problem) returns solution
return TREE-SEARCH(problem, COST-FN, FIFO-QUEUE())

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Uniform-Cost Snapshot



Fringe: [27(10), 4(11), 25(12), 26(12), 14(13), 24(13), 20(14), 15(16), 21(18)] 3^{3^2} UDENTS-HUB.com+ [22(16), 23(15)]Uploaded By: Malak Dar Obaid

Uniform Cost Fringe Trace

- 1. [1(0)]
- 2. [**3(3)**, 2(4)]
- 3. [**2(4)**, 6(5), 7(7)]
- 4. **[6(5)**, 5(6), 7(7), 4(11)]
- 5. [5(6), 7(7), 13(8), 12(9), 4(11)]
- 6. **[7(7)**, 13(8), 12(9), 10(10), 11(10), 4(11)]
- 7. [13(8), 12(9), 10(10), 11(10), 4(11), 14(13), 15(16)]
- 8. **[12(9)**, 10(10), 11(10), 27(10), 4(11), 26(12), 14(13), 15(16)]
- 9. [10(10), 11(10), 27(10), 4(11), 26(12), 25(12), 14(13), 24(13), 15(16)]
- 10. **[11(10)**, 27(10), 4(11), 25(12), 26(12), 14(13), 24(13), 20(14), 15(16), 21(18)]
- 11. [27(10), 4(11), 25(12), 26(12), 14(13), 24(13), 20(14), 23(15), 15(16), 22(16), 21(18)]
- 12. [4(11), 25(12), 26(12), 14(13), 24(13), 20(14), 23(15), 15(16), 23(16), 21(18)]
- 13. [25(12), 26(12), 14(13), 24(13), 8(13), 20(14), 23(15), 15(16), 23(16), 9(16), 21(18)]
- 14. [**26(12)**, 14(13), 24(13), 8(13), 20(14), 23(15), 15(16), 23(16), 9(16), 21(18)]
- 15. **[14(13)**, 24(13), 8(13), 20(14), 23(15), 15(16), 23(16), 9(16), 21(18)]
- 16. [24(13),8(13), 20(14), 23(15), 15(16), 23(16), 9(16), 29(16),21(18), 28(21)] Goal reached!

Notation: [Bold+Yellow: Current Node; White: Old Fringe Node; *Green+Italics: New Fringe Node*]. *Assumption:* New nodes with the same cost as existing nodes are added after the existing node.

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Time Complexity	O(b ^{C*/e})
Space Complexity	O(b ^{C*/e})
Completeness	yes (finite b, step costs >= e)
Optimality	yes

- b branching factor
- C* cost of the optimal solution
- e minimum cost per action

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- Keep a set of explored (visited) nodes.
- When a node is expanded, add the generated nodes to frontier only if not in the frontier or explored set
 - If the state of the generated node is in the frontier but with higher cost, replace that frontier node with newly generated node

Breadth-First vs. Uniform-Cost

- breadth-first always expands the shallowest node
 - only optimal if all step costs are equal
- uniform-cost considers the overall path cost
 - optimal for any (reasonable) cost function
 - non-zero, positive
 - gets bogged down in trees with many fruitless, short branches
 - low path cost, but no goal node
- both are complete for non-extreme problems
 - finite number of branches
 - strictly positive search function

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- continues exploring newly generated nodes
 - achieved by the TREE-SEARCH method by appending newly generated nodes at the beginning of the search queue
- Implementation: fringe = LIFO queue, i.e., put successors at front

function DEPTH-FIRST-SEARCH(problem) returns solution

return TREE-SEARCH(problem, LIFO-QUEUE())

Time Complexity	O(b ^m)	
Space Complexity	O(b*m)	b branching factor
Completeness	no (for infinite branch length)	m maximum path length
Optimality	no	
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• Given the following state space (tree search), give the sequence of visited nodes when using DFS (assume that the node O is the goal state):



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• A,



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• A, B,



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• A, B, F,



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- A, B, F,
- G,



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- A, B, F,
- G, K,



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- A, B, F,
- G, K,



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• The returned solution is the sequence of operators in the path: A, B, G, L, O



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Example: DFS for Graphs

• For the following state space, list all the visited nodes and draw the search tree to go from S to G using DFS. What is the returned solution?



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Example: DFS for Graphs (Cont.)

- Visited Nodes: S, A, C, G
- Solution (Path to goal): S, A, C, G





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Depth-First vs. Breadth-First

- depth-first goes off into one branch until it reaches a leaf node
 - not good if the goal is on another branch
 - neither complete nor optimal
 - uses much less space than breadth-first

- breadth-first is more careful by checking all alternatives
 - complete and optimal
 - very memory-intensive

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Depth-Limited Search

- similar to depth-first, but with a limit
 - overcomes problems with infinite paths
 - sometimes a depth limit can be inferred or estimated from the problem description
 - based on the TREE-SEARCH method
 - must keep track of the depth

function DEPTH-LIMITED-SEARCH(problem, depth-limit) returns solution

return TREE-SEARCH(problem, depth-limit, LIFO-QUEUE())

Time Complexity	O(b ^I)		
Space Complexity	O(b*l)	b	branching factor
Completeness	no (goal beyond I, or infinite branch length)		depth limit
Optimality	no		

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Iterative Deepening

- applies LIMITED-DEPTH with increasing depth limits
- combines advantages of BREADTH-FIRST and DEPTH-FIRST methods
- many states are expanded multiple times
 - doesn't really matter because the number of those nodes is small
- in practice, one of the best uninformed search methods
 - for large search spaces, unknown depth

```
function ITERATIVE-DEEPENING-SEARCH(problem) returns solution
for depth := 0 to unlimited do
    result := DEPTH-LIMITED-SEARCH(problem, depth-limit)
    if result != cutoff then return result
```

Time Complexity	O(b ^d)	
Space Complexity	O(b*d)	b branching factor
Completeness	yes (finite b)	d depth of optimal solution
Optimality STUDENTS-HUB.com	yes (all step costs identical)	Uploaded By: Malak Dar Obaid





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Iterative deepening search



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Iterative deepening search



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Iterative deepening search



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Example IDS



Stages in Iterative-Deepening Search

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Bi-directional Search

- search simultaneously from two directions
 - forward from the initial and backward from the goal state
- may lead to substantial savings if it is applicable
- has severe limitations
 - predecessors must be generated, which is not always possible
 - search must be coordinated between the two searches
 - one search must keep all nodes in memory

Time Complexity	O(b ^{d/2})	
Space Complexity	O(b ^{d/2})	h branching factor
Completeness	yes (b finite, breadth-first for both directions)	d depth of optimal solution
Optimality	yes (all step costs identical, breadth-first for both directions)	oaded By: Malak Dar Obaid

Improving Search Methods

- assumption for improvements
 - remember information about the search so far
 - all nodes visited so far
 - path to the current node
- make algorithms more efficient
 - avoiding repeated states
 - utilizing memory efficiently
- use additional knowledge about the problem => informed search
 - properties ("shape") of the search space
 - more interesting areas are investigated first
 - pruning of irrelevant areas
 - areas that are guaranteed not to contain a solution can be discarded

Criterion	Breadth- First	Uniform- Cost	Depth- First	Depth- Limited	Iterative Deepening	Bidirectional (if applicable)
Complete? Time Space	Yes ^a $O(b^d)$ $O(b^d)$	$ ext{Yes}^{a,b} O(b^{1+\lfloor C^*/\epsilon floor}) O(b^{1+\lfloor C^*/\epsilon floor})$	No $O(b^m)$ O(bm)	No $O(b^{\ell})$ $O(b^{\ell})$	Yes ^a $O(b^d)$ O(bd)	Yes ^{a,d} $O(b^{d/2})$ $O(b^{d/2})$
Optimal?	Yes^{c}	Yes	No	No	Yes^{c}	$\operatorname{Yes}^{c,d}$

Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.