

is, is

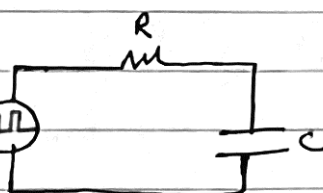
Experiment 6

Capacitors and Inductors

Ⓐ RC circuits : A circuit that contains a resistor and capacitor connected in series and powered by power supply but in our experiment by signal generator

★ Charging capacitor

During the positive half period of $E(t)$ the square wave

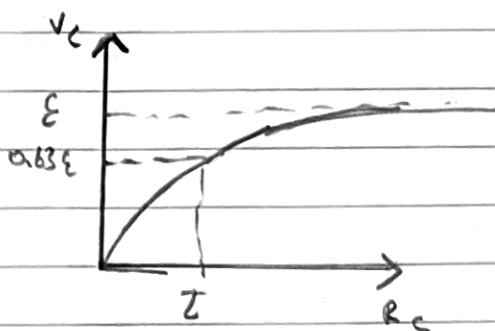


The voltage across the capacitor

$$V_c = \frac{Q}{C}$$

$$Q = \epsilon C (1 - e^{-t/RC})$$

$$\Rightarrow V_c = \epsilon (1 - e^{-t/RC})$$



- at $t=0 \rightarrow V_c = \epsilon (1 - e^0) = 0$
- at $t=\infty \rightarrow V_c = \epsilon (1 - e^{-\infty}) = \epsilon$
- at $t=T=RC \rightarrow V_c = \epsilon (1 - e^{-\frac{RC}{RC}}) = 0.63 \epsilon$

T : time constant is a measure of how fast the voltage across the capacitor rises or how fast the charging is
 or time constant: the time needed for the potential difference on capacitors to reach 0.63 of the max voltage ϵ

(2)

سلا و بیا

The voltage across the resistor

$$V_R = IR$$

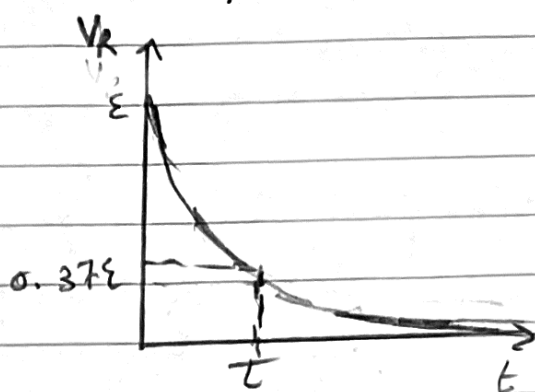
$$I = \frac{dQ}{dt}$$

$$Q = C\epsilon(1 - e^{-t/RC})$$

$$V_R = \frac{dQ}{dt} R$$

$$= \epsilon \epsilon \frac{1}{RC} e^{-t/RC} R$$

$$V_R = \epsilon e^{-t/RC}$$



- at $t=0 \rightarrow V_R = \epsilon e^0 = \epsilon$
- at $t=\infty \rightarrow V_R = \epsilon e^{-\infty} = 0$
- at $t=RC \rightarrow V_R = \epsilon e^{-1} = 0.37\epsilon$

⊛ Discharging a capacitor

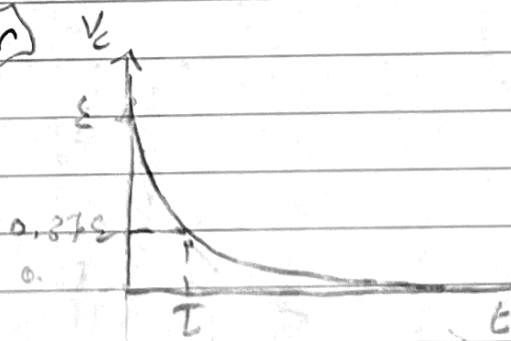
(During the negative half period of the square wave)

$$Q(t) = C\epsilon e^{-t/RC}$$

The voltage across the capacitor

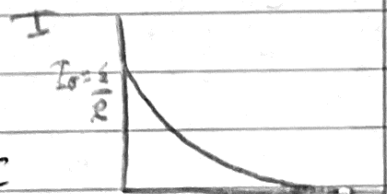
$$V_C = \frac{Q}{C} = \frac{C\epsilon e^{-t/RC}}{C}$$

$$\Rightarrow V_C = \epsilon e^{-t/RC}$$



- at $t=0 \rightarrow V_C = \epsilon e^0 = \epsilon$
- at $t=\infty \rightarrow V_C = \epsilon e^{-\infty} = 0$

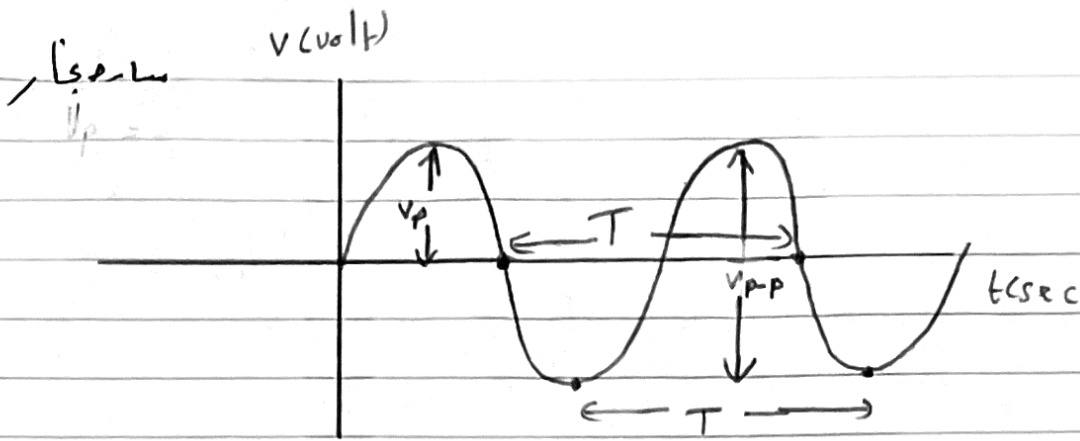
- at $t=RC=\tau \Rightarrow V_C = \epsilon e^{-1} = 0.37\epsilon$



τ : a measure of how fast the voltage across capacitor decreases

τ : the time needed for potential difference on capacitor to reach 0.63 of the max voltage

3

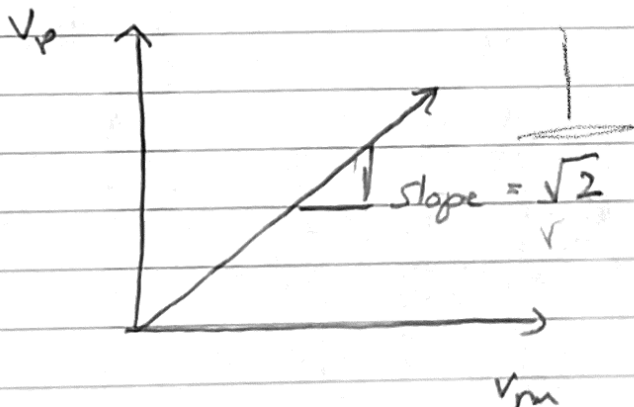
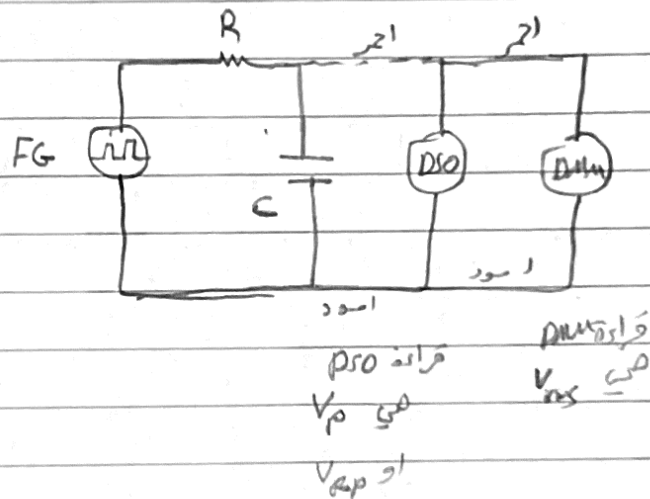


$$f = \frac{1}{T} \quad (\text{unit: Hz})$$

$$V_{p-p} = 2\sqrt{2} V_{rms}$$

$$V_{rms} = \frac{1}{2\sqrt{2}} V_{p-p}$$

$$V_{rms} = \frac{1}{\sqrt{2}} V_p$$



هي قيمة الجهد التي تكون معنا : V_{rms}
 كمية الطاقة المهدورة عندما يمر به DC voltage
 هي نفس كمية الطاقة المهدورة عندما يمر به AC voltage

(4)

سوال 4

The voltage across the Resistor

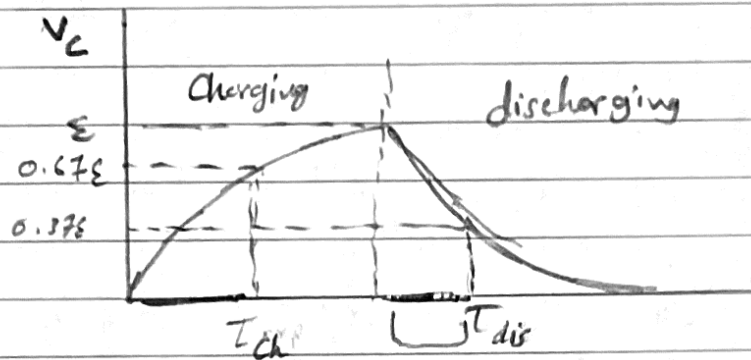
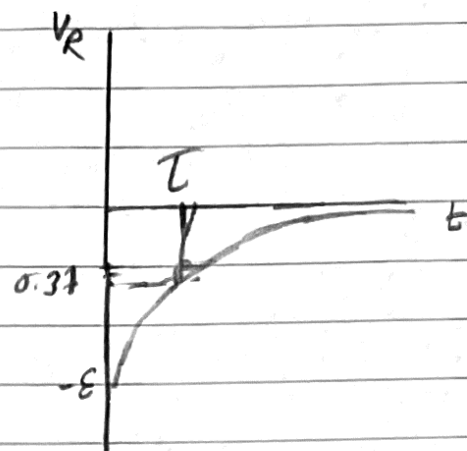
$$V_R = IR, \quad I = \frac{dQ}{dt}, \quad Q = C\epsilon e^{-t/RC} \quad \text{disg}$$

$$V_R = \frac{dQ}{dt} R$$

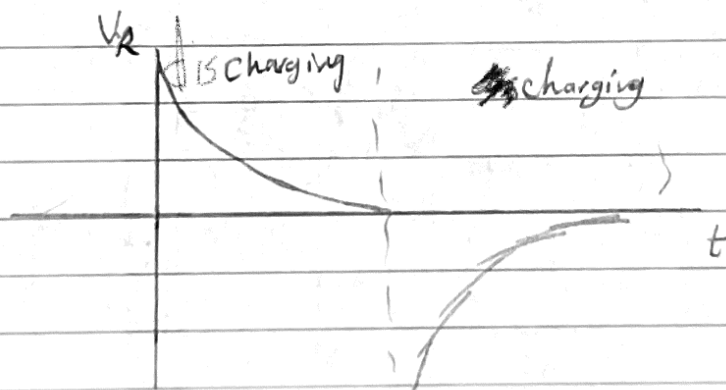
$$V_R = \frac{-1}{RC} C\epsilon e^{-t/RC} R, \quad I = \frac{dQ}{dt} = \frac{-\epsilon}{R} e^{-t/RC}$$

$$V_R = -\epsilon e^{-t/RC}$$

- at $t=0 = -\epsilon e^0 = -\epsilon$
- at $t=\infty = -\epsilon e^{-\infty} = 0$
- at $t=RC = -\epsilon e^{-1} = 0.37\epsilon$



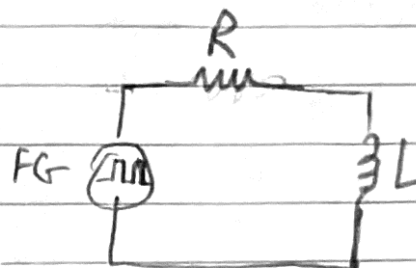
$$T_{exp} = \frac{T_{ch} + T_{dis}}{2}, \quad T_{theo} = RC$$



(5)

⑧ RL Circuit: A circuit that contains an inductor connected in series with a resistance and powered by a power supply but in our experiment by a signal generator

$$I(t) = \frac{\mathcal{E}}{R} (1 - e^{-Rt/L})$$



The voltage across the inductor L

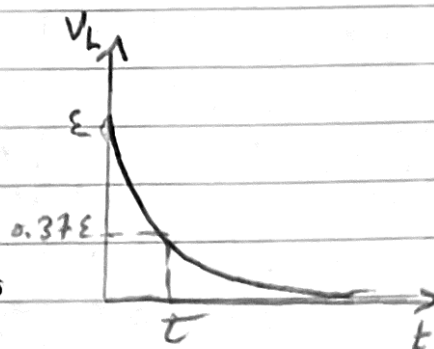
$$V_L = L \frac{dI}{dt} = L \frac{\mathcal{E}}{R} \frac{R}{L} e^{-Rt/L}$$

$$\Rightarrow V_L = \mathcal{E} e^{-Rt/L}$$

• at $t = 0 \rightarrow V_L = \mathcal{E} e^0 = \mathcal{E}$

• at $t = \infty \rightarrow V_L = \mathcal{E} e^{-\infty} = 0$

• at $t = \tau = \frac{L}{R} \rightarrow V_L = \mathcal{E} e^{-1} = 0.37 \mathcal{E}$



τ : a measure of how fast the current rises in the circuit

The voltage across the resistor R

$$V_R = IR = \frac{\mathcal{E}}{R} (1 - e^{-Rt/L}) R$$

$$V_R = \mathcal{E} (1 - e^{-Rt/L})$$

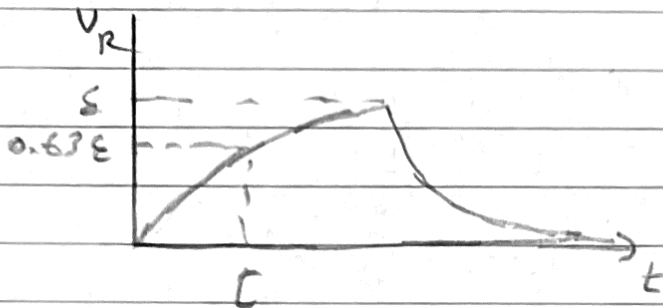
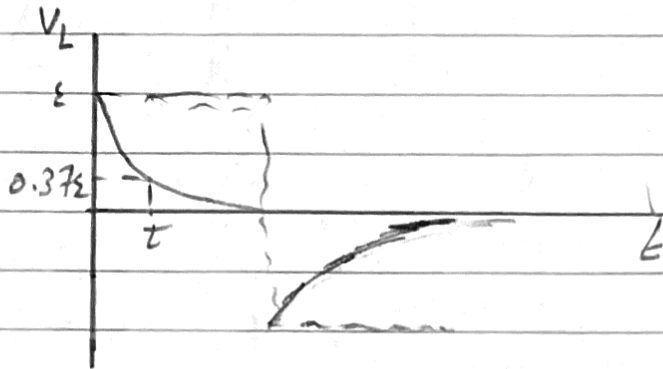
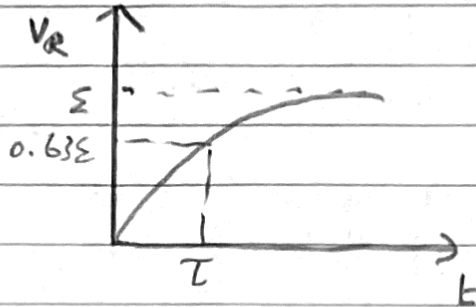
• at $t = 0 \rightarrow V_R = \mathcal{E} (1 - e^0) = 0$

6

في الـ L

• at $t = \infty \rightarrow V_R = \mathcal{E}(1 - e^{-\infty}) = \mathcal{E}$

• at $t = \frac{L}{R} \rightarrow V_R = \mathcal{E}(1 - e^{-1}) = 0.63 \mathcal{E}$



$$\tau_{exp} = \underbrace{\tau}_{\text{ch for } L} + \underbrace{\tau}_{\text{dis for } L}$$

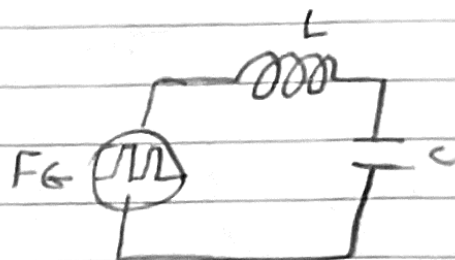
$$\tau_{theor} = L/R$$

①

سلسلہ

③ LC circuit (LC tank or LC-oscillator)

$$\varepsilon = L \frac{d^2 Q}{dt^2} + \frac{Q}{C}$$



$$\Rightarrow \phi(t) = \phi_0 \cos(\omega t + \phi)$$

$$V_C = \frac{Q}{C} = \frac{\phi_0}{C} \cos(\omega t + \phi)$$

$$\Rightarrow V_C = V_0 \cos(\omega t + \phi) \quad \text{simple harmonic oscillator}$$

$$\omega = \frac{1}{\sqrt{LC}} \quad \text{natural angular frequency}$$

$$X_L = \omega L = 2\pi f L$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

\Rightarrow at resonance

$$X_L = X_C$$

$$\omega L = \frac{1}{\omega C}$$

$$2\pi f L = \frac{1}{2\pi f C}$$

$$f^2 = \frac{1}{4\pi^2 LC}$$

$$\Rightarrow f = \frac{1}{2\pi \sqrt{LC}}$$