





Periodicity * Definition: A function f(x) is periodic if there is a positive number p set f(x+p) = f(x). The smallest such value of p is the poviod of f. * Periods of trigonometric functions: Period TT examples: tan x = tan (x+TT) $\cot x = \cot (x + \pi)$ example: sinx = sin(x+211) $\cos x = \cos(x + 2\pi)$ Sec $x = Sec(x+2\pi)$ $C_{SC} x = C_{SC} (x + 2\pi)$ Example : prow Dy = cos 2x € y= cos x Note that O Multiplying x by anomber greater than 1 speeds In the trigonometric function (increase the frequency) (pt)
Dultiplying x by admimber less than 1 slows the trigonometric fuction down and lengthens its period (PD). STUDENTS-HUB.com Uploaded By: Malak Obaid y= cos 2x Cosx has p= 2TT Cos x has p=41 y=cos X cos 2 x has P=TT 山へ 311 ZTT TI 52 311

★ Double - angle Formulas:
Make A=B=0 in equation (2), we get

$$\begin{array}{c} (23)\\$$

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The law of Cosines (24)
Consider the triangle B (brown assimply
ABC. The law of Cosines
is given by

$$C^2 = a^2 + b^2 - 2ab \cos 0$$

 $c = b A(b, 0)$
 $C^2 = a^2 + b^2 - 2ab \cos 0$
 $c = b A(b, 0)$
 $C^2 = (a \cos 6 - b)^2 + (a \sin 6)^2$
 $= a^2 \cos^2 - 2ab \cos 6 + b^2 + a^2 \sin 6^2$
 $= a^2 (\cos 6^2 + \sin 6^2) + b^2 - 2ab \cos 6$
 $= a^2 (\cos 6^2 + \sin 6^2) + b^2 - 2ab \cos 6$
 $= a^2 + b^2 - 2a + b^2$
 $= a^2 + b^2 - 2a + b^2 - 2a + b^2$
 $= a^2 + b^2 - 2a + b^2 - 2a + b^2$
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 $= a^2 + b^2 - 2a + b^2 - 2a + b^2 - 2a + b^2$
 $= a^2 + b^2 - 2a + b^2 - 2$