







EXAMPLE (4-2): 8-1-2024 Suppose that the random variable (X) can take only the values (1, 2, 3) and the random variable (Y) can take only the values (1, 2, 3, 4). The joint pdf is shown in the table. >P(x=1,y=1) 1 (x=۱٫γ*=* 2) 0.1 0 >P(x=1,y=3) 0.1 0.2 0.1 2 0.3 0 0 3 0 0.2 1- Find $f_X(x)$ and $f_Y(y)$. 2- Find $P(X \ge 2)$ 3- Are (X) and (Y) independent. 4- Find the mean and variance for both X and Y 5- Find P(X > Y)6- Find P(X = Y) 7- Find the correlation coefficient between X and Y. $PMF_{x} = P(X=x)$? in Single Random $PMF_{y} = P(y=y)$ Varible joint $\rho MF_{x,y} = \rho(X = x, Y = y)$ Probility mass function Can be described in 3 ways 8-I. using Schedual. 2. P(X = x, Y = y) = 0.1, X = 1, y = 1PMFXY ο, X=1, y=2 foint 0 X=1, y=3 X=1, y=4 3. graphs, "gonna be <u>2D</u>" 10 - 1 - 2024* the sum of probability should equals one examples 8-1. p(x=3, y=2) = 0.22. p(x=1, y < 3) = p(x=1, y=1) + p(x=1, y=2) + p(x=1, y=3) = 0.1 + 0 + 0.1 = 0.23. $p(X \leq 2, Y \leq 2) = 0.3 + 0 + 0.1 + 0 = 0.4$

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$$\begin{array}{c} 41 \ F_{xy}(2.2) = \text{jont CDF of x and y.} \\ = P(X \leq 2, y \leq 2) \\ &\text{Same as (3).} \\ &\text{S} F_{xy}(0, -\infty) = P(X \leq \infty, y \leq -\infty) \\ &= 7 \text{etb.} \\ &\text{S} F_{xy}(0, -\infty) = P(X \leq \infty, y \leq -\infty) \\ &= 7 \text{etb.} \\ &\text{S} F_{xy}(0, -\infty) = P(X \leq \infty, y \leq -\infty) \\ &= 1 \\ &\text{H} p(X = y) = 0.1 + 0.70 = 0.1 \\ &\text{S} P(X = y) = 0.1 + 0.70 = 0.1 \\ &\text{S} P(X = y) = 0.1 + 0.70 = 0.2 \\ &\text{H} p(X = y) = 0.1 + 0.70 = 0.2 \\ &\text{H} p(X = y) = 0.1 + 0.70 = 0.2 \\ &\text{H} p(X = y) = 0.1 + 0.3 + 0 = 0.4 \\ &\text{H} p(Y = y) = 0.1 + 0.3 + 0 = 0.4 \\ &\text{H} p(Y = y) = 0.1 + 0.3 + 0 = 0.4 \\ &\text{H} p(Y = y) = 0.1 + 0.3 + 0 = 0.4 \\ &\text{H} p(Y = y) = 0.1 + 0.3 + 0 = 0.4 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.6 , X = 2 \\ 0.4 , X = 3 \\ 0.4 , Y = 1 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.6 , X = 2 \\ 0.4 , X = 3 \\ 0.4 , Y = 1 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.4 , Y = 1 \\ 0.4 , Y = 1 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.4 , Y = 1 \\ 0.4 , Y = 1 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.4 , Y = 1 \\ 0.4 , Y = 1 \\ &\text{H} p(X = x) = \left(0.2 , X = 1 \\ 0.4 , Y = 1 \\ 0.4 , Y = 1 \\ &\text{H} p(X = 1) + (0.6) + (3)(0.6) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.6) + (3)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.8) \\ &\text{H} p(X = 1) + (0.6)(0.$$

$$\Re p(X=x) = \begin{cases} 0.3 , X=1 \\ 0.6 , X=2 \\ 0.3 , X=3 \\ 0.4 , X=3 \\ 0.4 , Y=3 \\ 0.4$$

$$P_{yy} = \underbrace{E(xy) - \frac{4x}{2} + \frac{4y}{2}}_{0} \quad Countines} \underbrace{\frac{9}{2} + \frac{9}{2}}_{0}$$

$$Correlation Coeff. $A \mp 1 \quad or \quad P \circ \circ \quad or \quad -1 < \frac{9}{2} + \frac{1}{2}$

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$$E[xy] = E[x] \quad E[x] = E[x] \quad end f \quad f \quad use \quad indep.$$

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$$E[xy] = Uncorrelated$$

$$exp \quad = \frac{1}{2} \quad (y \mid a) \quad (y \mid a) \quad (y \mid a) \quad (z \mid a)$$

$$end \quad end f \quad (y \mid a) \quad (z \mid a)$$

$$end \quad end \quad (z \mid a)$$

$$end \quad (z \mid a)$$

$$end$$$$$$

* let Z= X+Y find PMFZ, MZ, og Z | P(Z=Z) $\rho_{MF_{Z}} = \rho(Z=Z) = (0.1), Z=2$ 2 0.1 0.3, Z=3 0 + 0.3 3 $\begin{array}{c} 0.1 \\ 0.1 \\ 0.3 \\ .2 = 9 \\ 0.3 \\ .2 = 5 \\ 0.3 \\ .2 = 6 \\ 0 \\ 0 \\ .0 \\ .0 \\ \end{array}$ 0.1 4 5 0 +0.1 +0.2 6 0.2 $- \mathcal{M}_{z} = E[z] = (2)(0.1) + (3)(0.3) + (4)(0.1) + (5)(0.3) + (6)(0.2).$ = 4.a $M_2 = E[X+Y] = E[X] + E[Y]$ STUDENTS-HUB.com

$$E[x^{+}x^{2}] = E[x^{2}] + E[x^{2}]$$

$$f[y] @ 0 @ 0 = \sum_{i} y^{2} p(x = x_{i}) + 2 x^{2} p(x = x_{i}) + 2 e^{-x_{i}} e^{-x_{i}} + 2 e^{-x_{i}} e^{-x_{i}}$$

Examples let X be arandom variable with $\frac{1}{x} = 1$, $\Theta_{x}^{2} = 4$, Y is another Random variable with $\mu_{y} = -1$, $6y^{2} = 9$. R is another R.U S.t. R = 2X - yI MR = E[R] $= 2E[x] - E[y] = 2\mu_x - \mu_y = (2)(1) - (-1) = 3$ 3 find the Coveriance Mxy if Pxy =0.5 $\mu_{xy} = \Theta_{x} \Theta_{y} P_{xy} = (J\bar{u})(J\bar{q})(0.5) = 3$ B find o'r (var) if Pxy =0.5 $\vec{\theta}_{\mathbf{p}} = a_{\mathbf{x}}^{2}\vec{\theta}_{\mathbf{x}} + \vec{u}_{\mathbf{y}}\vec{\theta}_{\mathbf{y}} + \partial a_{\mathbf{x}}a_{\mathbf{y}}\theta_{\mathbf{x}}\theta_{\mathbf{y}}P_{\mathbf{x}\mathbf{y}}$ $=(4)(4) + (1)(9) + (2)(2)(-1)(\sqrt{4})(\sqrt{9})(-5)$ - 13 I if X, y are S. Indep, find Mxy (covariance), ER Covariance = E[xx] - My My = E[x]. E[y] - My My = 0 0k = ax 8x + ay 6+ +0 =(4)(4) + (-3)(4) = 25STUDENTS-HUB.com

Two Continuous Random Variable: let X and y be two Random variable with the following joint p.d.f fx,y(X,y) = K, o \$x \$1,0 \$ y \$3 ٥ , ٥.ω ويجب أن يساوع (١) a) determine the value of the Constant R Imethod 1 * one integration gives Area. $\int \int f_{xy}(x_{y}) dy dx = 1$ 3 dx 3 + double integration gives volume JR dydx = 1 م أول إشب تللمل التكامل الد اخلي $\int 3k \, dx = 1$ ع المحا وأ $3R = 1 \rightarrow K = \frac{1}{2}$ 2 method 2. $\int \int f_{xy}(x,y) \, dx \, dy = 1$ 3 Fax Jkdxdy =1 R dy 3K=1 -> K=1 6) p(0xx < 0.5, 0 x x 1) $\iint_{3} dy dx = \iint_{3} dx = \frac{1}{6}$ volume c) p(x < y) method 1 8- $\int \int \frac{1}{3} dy dx = \int \frac{1}{3} (3-x) dx = (x - \frac{x^2}{6}) \Big|_{0}^{1} = 1 - \frac{1}{6} = \frac{5}{6}$ ن بغر ماريه م × 9 method 28-STUDENTS-HUB.com

d)
$$P(X \neq x|) \rightarrow y = \frac{1}{14}$$

 $= \frac{1}{14} \frac{1}{2} \frac{$

note that is
$$f_{X}(i)$$
, $f_{Y}(y) = f_{Y}(x, y)$ -since they are indep.
 $f_{Y_{X}}(x)$ $f_{Y}(y) = \begin{cases} \frac{1}{2} \\ \frac{$