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FINN2

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Chapter 8

Risk & Return

Thu 18 Jul

- Expected Return - Actual Return
  - Beta
  - Standard deviation
- } → Risk Cost

$$\text{\$ Return} = \text{Selling price} - \text{purchase price} \Rightarrow \text{\$ Amount}$$

$CF_1 - CF_0$

$$\% R = \frac{\text{Selling} - \text{Purchase} + \text{yield}}{\text{purchase price}} \rightarrow \begin{matrix} \text{Div} \\ \text{Bond intence} \end{matrix}$$

Finn 2

Sat. 20 Jul 2024

\* Variance في خطر ليس ما يعرفه جميعاً

Chapter 8, Second Lec

Using Prob

stocks	Return	Prob
A	.10	.30
	.15	.15
	.30	.55

To Calculate Average return \*  $Avr = \sum R \times Prob$

$$(.1 \times .3) + (.15 \times .15) + (.3 \times .55) = 0.2175 = Avr(A)$$

Standard deviation \*  $Sd = \sqrt{(R - Avr)^2 \times Prob} \rightarrow Sd = \sqrt{\text{Variance}}$

1 \* بتوسط Avr ل Stock ليعطى بفتح Avr من كل R على حدة  
 2 \* بفتح كل قيمة من (R - Avr)

R	Avr	R - Avr	(R - Avr) <sup>2</sup>	$(R - Avr)^2 \times Prob$	Variance
.1	.2175	-.1175	.01380625	.00414875	Σ = Variance
.15	.2175	-.0675	.00455625	.0006834375	
.3	.2175	.0825	.00680625	.0037434375	

$$\text{Var} = .008575625$$

$$\rightarrow Sd = \sqrt{\text{Variance}} \rightarrow Sd = \sqrt{.008575625} \rightarrow .092604671 = Sd \rightarrow \text{Percent انصبه 9\%}$$

Stocks	Return	Prob
B	.5	30%

	-3%	15%
	12%	55%

ما بتغير عنان  $Avr = (.05 \times .3) + (-.03 \times .15) + (.12 \times .55)$   
 انتر ارقام  $Avr(B) = .0765$

R	Avr	R - Avr	(R - Avr) <sup>2</sup>	(R - Avr) <sup>2</sup> x Prob
.05	.0765	-.0265	.00072225	.000210675
-.03	.0765	-.1065	.01134225	.0017013375
.12	.0765	.0432	.00189225	.0010473375

$$\text{var} = .0029654625$$

$$Sd = \sqrt{\text{var}} \rightarrow Sd = \sqrt{.0029654625} \rightarrow Sd = .0544339212$$

(1)

$$Sd(A) = .092567543$$

$$= 9\%$$

$$Sd(B) = .054339212$$

$$= 5\%$$

which one is more risky? stock A is more risky.

\* Coefficient of variation =  $\frac{Sd}{AVr}$  trade of <sup>مقياس</sup> between risk & return  
 Coefficient of variation  $> 1$  → good, because risk less than return.

### Risk preference ✓

1. Risk Averse

هو الذي يوجهك لأي استثمار كنت تروح.

\* يطلب مقابل لا Risk يعني يتقبله.

يعني Return أعلى أو Risk يعني الدنيا

The higher the risk → higher return

2. Risk Neutral

\* ما يتطلع على أو Risk يعني يتطلع

على أو Return (أعلى) Return

رفض النظر عن أو Risk.

3. Risk seeking (Lovers, Gamblers)

\* يتطلع على أعلى Risk

مستعد بال Risk أكثر

من أو Return مثل الاستثمارين.

### Risk single asset:

1. Sd

2. Beta

3. Unexpected return - actual return

4. The range

Range = Subtracting optimistic return - pessimishing return (Return - Return)

"you can't calculate the risk without... Return."

## Covariance & Correlation

- Statistical measure of the relation between 2 Assets.

- both measure the relationship between 2 Assets.

\* Covariance: the type of the relation, if the relation is pos or neg.

\* Correlation: measure the strength of the relation.

"I can't calculate the Correlation without the Covariance"

$$* \text{Covariance} = \frac{\sum (r - \text{avr Asset A}) \times (r - \text{avr Asset B})}{(n-1)} \quad , \text{without Prob}$$

$$* \text{Covariance} = \sum (r - \text{avr Asset A}) \times (r - \text{avr Asset B}) \times \text{Prob} \quad \text{with Prob}$$

$$\begin{aligned} \text{Covariance} &= \sum (r - \text{avr}_{(A)}) \times (r - \text{avr}_{(B)}) \times \text{Prob} \quad \rightarrow \text{There is prob in calculations} \\ &= (-.1175 \times -.0265 \times .3) + (-.0675 \times -.1065 \times .15) + (.0875 \times .0432 \times .55) \\ &= .000934125 \quad + .0010783125 \quad + .0019602 \end{aligned}$$

$$\text{Covariance} = .0039726375 \quad \text{positive relationship.}$$

$$* \text{Correlation} = \frac{\text{Covariance}}{\text{Sd}_A \times \text{Sd}_B}$$

$$\text{Correlation} = \frac{.0039726375}{.092604671 \times .054339212} = .7894646867 \quad \text{Strong}^{\text{pos}} \text{ relation}$$

جذب أو دفع الأصول

no relation

0

"Correlation > .5 → Strong relation."

Correlation < .5 → weak relation.

Correlation -1  
↓  
perfect neg correlation

[A ↑ 40%] → [B ↓ 40%]

1  
↓  
perfect pos correlation

[A ↑ 10%] → [B ↑ 10%]

A	B
10%	15%
17%	-3%
22%	9%

Avr sd Var Correlation Cov

$$Avr = \frac{.1 + .17 + .22}{3} = .1633$$

$$Avr_B = \frac{Var_B = .00515}{Sd_B = 9.03\%}$$

$R - \bar{R}$	$(R - \bar{R})^2$
.1 - .1633	.003969
.17 - .1633	.000489
.22 - .1633	.00321484

$$Var = \frac{.007279}{2} = .0036395$$

$$sd = \sqrt{.0036395} = .060329$$

Cov = -.00231 → negative relation.  
 Correlation = -.526 → Semireal (semiweak/semistrong)

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W	
A	1.60
B	1.40

$$\sqrt{.00131 + .0013 + -.00134} = 3.6\%$$

Standard Deviation : 3

$$Variance = 3^2$$

How to Calculate Risk, Return 2 Asset Portfolio?

Weight always = 100%

$$* R_p = (w_a \times \bar{R}_a) + (w_b \times \bar{R}_b) + \dots + (w_n \times \bar{R}_n)$$

$$SD = \sqrt{w_a^2 \times \sigma_a^2 + w_b^2 \times \sigma_b^2 + 2w_a w_b \times \text{Cov}}$$

↓  
Correlation  $\times$   $\sigma_a \times \sigma_b$

- Beta

مقياس المخاطرة السوقية

- Security Marketable

- total risk = Systematic + Unsystematic  
 Market diversifiable  
 undiversified controllable  
 non controllable Unique (firm risk)

CAPM  

$$k = R_f + \text{Beta} \left( \frac{\text{Premium}}{MR - MF} \right)$$
 علة المخاطرة السوقية  
 $\sigma^2$  variance market

- Beta RF = zero
- Beta Market = 1

Beta RF = zero  
 " Market = 1

Beta  
 Security Marketline

Total Risk =  $\sigma^2$

Stock, T.Bill  
 Beta: Beta

CAPM =  $(R_f) + \text{Beta} (MR - R_f)$

$\sigma^2$  Variance Stock

$\text{COV}_{a,n} = \frac{.0028}{.0038} = .73$

$W_s \times \text{Beta}_{stock} + W_{T.Bill} \times \text{Beta}_{T.Bill}$

المخاطرة السوقية ← المخاطرة الكلية التي يتحملها المستثمر في Beta المخاطرة الكلية

Beta  $\propto$  Risk

Market Return: return

$$* \text{Beta}_p = w_a \times \text{Beta}_a + w_b \times \text{Beta}_b$$

Q:	Prob	R A	R B
	55%	5%	22%
	15%	12%	-7%
	30%	4%	30%

$$\text{AVR}_A = .55 \times .05 + .15 \times .12 + .3 \times .04 = .0575 = \bar{R}_A$$

$(R - \bar{R})_A^2$	$(R - \bar{R})_A^2 \cdot \text{Prob}_A$	$(R - \bar{R})_B^2$	$(R - \bar{R})_B^2 \cdot \text{Prob}_B$
.00006	.00003	.0004	.00022
.00391	.00059	.0729	.01094
.00031	.00009	.01	.003

$$\text{Variance}_A = .00071$$

$$\sigma_B^2 = .01416$$

(standard dev)  $\sigma = \sqrt{.00071} \rightarrow \sigma = 2.66\%$

$$\sigma_B = 11.9\%$$

$$\text{AVR}_B = 20\%$$

$$\begin{aligned} \text{Cov} &= \sum R - \bar{R}_A \times R - \bar{R}_B \times \text{Prob} \\ &= .00008 + -.00253 + -.00053 \\ \text{Cov} &= .00298 \end{aligned}$$

$$\text{Correlation} = \frac{\text{Cov}}{\text{SD}_A \times \text{SD}_B} = \frac{.00298}{20\% \times 11.9\%} = .96$$

$$\text{RP} = w_a \times \bar{R}_a + w_b \times \bar{R}_b$$

return portfolio

$$= .7 \times .0575 + .3 \times .2 = 10.25\%$$

$$\sigma^2 = w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2w_a w_b \text{Cov}$$

$$\sigma^2 = .0003$$

$$\sigma = 4.8\%$$

$$CV = \frac{\sigma}{\Sigma P} = \frac{2.68\%}{5.57}$$

$$\begin{array}{l} \text{Cov} \quad m, a = -.005 \\ \quad \quad m, b = -.003 \end{array}$$

$$\sigma_m = 44\%$$

$$\text{Beta}_A = \frac{\text{Cov}}{\sigma_m^2} = \frac{-.005}{.0196} = -.255$$

$$\text{Beta}_B = -.0153$$

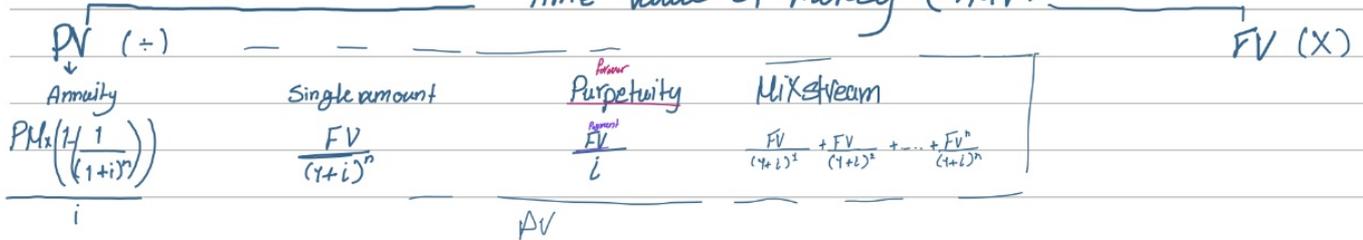
$$\text{Beta}_p = W_A \times \text{Beta}_A + W_B \times \text{Beta}_B$$

$$\text{Beta}_{\text{port}} = .7 \times (-.255) + .3 \times (-.0153)$$

Bond Valuation

- Price Bond
- Current yield
- yield to Maturity
- yield to call

Time Value of money (TMV)



stated interest (yield to maturity)

- Price of the Bond =  $\frac{PMT \times \left( 1 - \frac{1}{(1+i)^n} \right)}{i} + \frac{1000}{(1+i)^n}$

$PMT = \text{Coupon Rate} \times \text{Face Value}$

الأداة بالوقت الصافي بالمالين

- face value always = 1000
- Maturity = 15

- yield to Maturity < coupon rate → Bond Premium → Price > 1000
- YTM > coupon rate → Bond discount → Price < 1000
- YTM = coupon rate → face value → = 1000

$$\frac{50 \times \left( 1 - \frac{1}{(1+0.07)^{15}} \right)}{0.07} + \frac{1000}{(1+0.07)^{15}}$$

$$455.4 + 362.45 = \boxed{817.85}$$

لا يزال يظل أقل من 1000

n → Quarterly for ex → n x 4  
 . zero prices PMT, i

Ex : Face Value 1000  
Maturity after (n) 30 years

Interest (Coupon Rate) 10%

Market (i) yield to Mat 8%

Semi annually  $\rightarrow \frac{PMT}{2}, \frac{i}{2}, n \times 2$

\* Bond Price?

$$\text{Price of the Bond} = \frac{PMT}{i} \left( 1 - \frac{1}{(1+i)^n} \right) + \frac{1000}{(1+i)^n}$$

$$PMT = \text{Coupon Rate} \times \text{Face Value}$$

$$= 10\% \times 1000 = 100$$

$$\text{Price of the Bond} = \frac{(100) \times \left( 1 - \frac{1}{(1 + \frac{.08}{2})^{60}} \right)}{\frac{.08}{2}} + \frac{1000}{(1 + .04)^{60}}$$

$$= \frac{50 \times (.905)}{.04} + \frac{1000}{10.52}$$

$$= \underline{4226.23} \text{ Premium because it's more than 1000}$$

When YTM  $\leq$  coupon rate  $\rightarrow$  Bond Premium  $\rightarrow$  Price  $\geq$  1000

$$YTM = \frac{\text{Coupon Payment} + \frac{(\text{Face Value} - MV)}{\# \text{ of Maturity}}}{\left(\frac{\text{Face} + MV}{2}\right)}$$

Ex: Price 900 \$  
 Maturity 10 years  
 Coupon 7%

$$= \frac{70 + \frac{1000 - 900}{10}}{\frac{1000}{2}} = \frac{80}{950} = 8.4\% \rightarrow$$

$$\frac{PMT}{2}, \frac{\# \text{ of Maturity}}{2} \rightarrow \text{القسمة} \rightarrow \frac{\text{النتيجة}}{2} \quad \text{semi} \quad \text{القسمة}$$

$$\text{Current Yield} = \frac{\text{Coupon Payment}}{\text{bond Price}}$$

6-11

outline

$$\begin{array}{l}
 \text{Coupon Payment} + \frac{\text{Face Value} - MV}{\text{# of months}} \\
 \hline
 \frac{\text{Face} + MV}{2} \\
 50 + \frac{1000 - 810.34}{10} = 7.62\% \\
 \hline
 \frac{1810.34}{2} \\
 \left(\frac{50}{4}\right) + \frac{1000 - 810.34}{10 \times 4} = 1.91\% \times 4 \\
 \hline
 \frac{1810.34}{2} = .01904 = 7.62\%
 \end{array}$$

6.2%

Outline 6-15

100 par value  
coupon rate 8%  
interest annually

$i, y = 12$  year  
YTM = 4%

par value : Face Value

$$\text{par value} \times \text{coupon rate} = 100 \times .08 = 8$$

$$P = \frac{\text{PMT} \times \left(1 - \frac{1}{(1+i)^n}\right)}{i} + \frac{\text{Face Value}}{(1+i)^n}$$

$$= 137.54 \rightarrow \text{premium because } > \text{YTM}$$

C. YTM = 10%

6-15

Face value = 100  
Coupon rate = (8%)  $8\% \times 100 = 8$   
 $Y = 12$   
YTM = (4%)  
(10%)

$$P = \frac{\text{PMT} \times \left(1 - \frac{1}{(1+i)^n}\right)}{i} + \frac{\text{Face value}}{(1+i)^n}$$
$$8 \left(1 - \frac{1}{(1+.1)^{12}}\right) + \frac{100}{(1+.1)^{12}}$$

Stock Valuation

• Debt → Bond

Borrower creditor relationship has a time when the Debt end the relationship between them end

- There is Maturity
- Interest

حامل ربح وخسارة الشركة

• Equity

- No Maturity
- Dividend

Preferred stock, common stock  
no voting right, voting right

حامل ربح وخسارة الشركة

Equity Risker than Debt

إذا الشركة أفلسنا  
أنا نفلس

إذا أرباحنا ما ربحنا لا نجز  
على أرباحنا ما نفلس

Authorized Shares :

Issued → Sold to Shareholder

- outstanding could be = Issued → if there is no Treasury stocks

- outstanding = Issued - Treasury stocks



Preferred Stocks (preferred financial asset)  
 Convertible Feature  $\leftarrow$  Bond  $\downarrow$  بيان حصة من الـ Bond  
 Commons  $\text{\textcircled{2}}$  كمن أجرة

PS

required rate of return

zero growth dividend

$$P = \frac{D}{K}$$

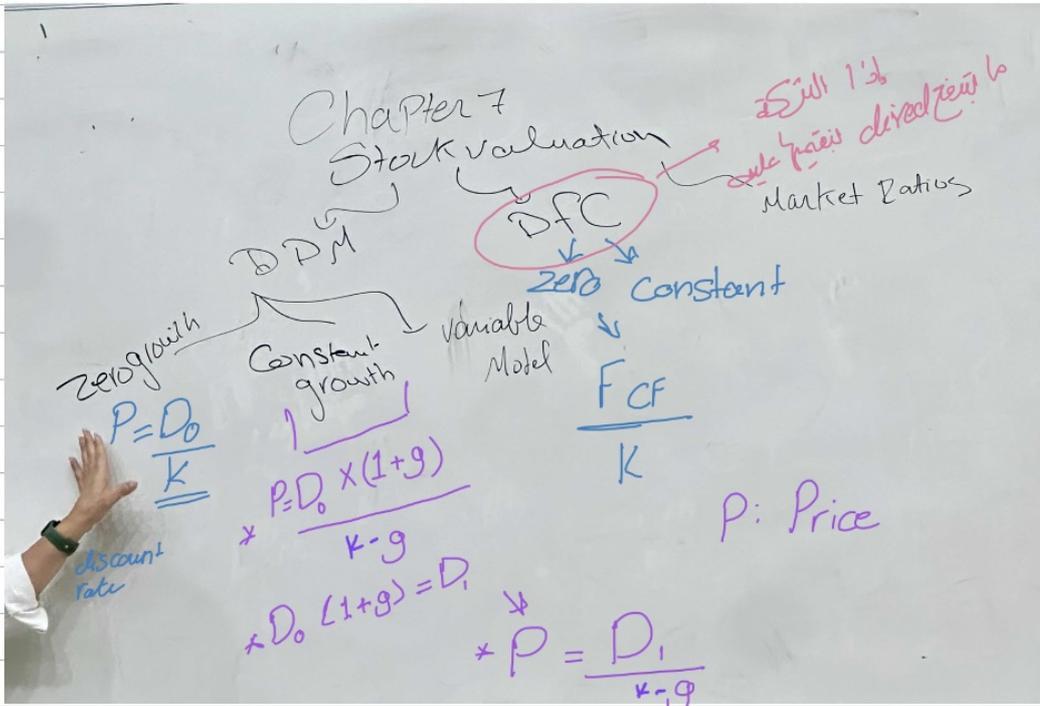
zero growth model

$K \leq R_F + B$  (Premium)

Perpetuity  $\rightarrow$  بـسـة فـلـوـجـة  
 discount rate

# Valuation C.S

Tue, 6 Aug



preferred stock  $\rightarrow$  perpetuity??

Free Cash Flow = operating cash flow - Investment Capital Exp

$g$ : growth

- The higher the growth  $\rightarrow$  the higher the price

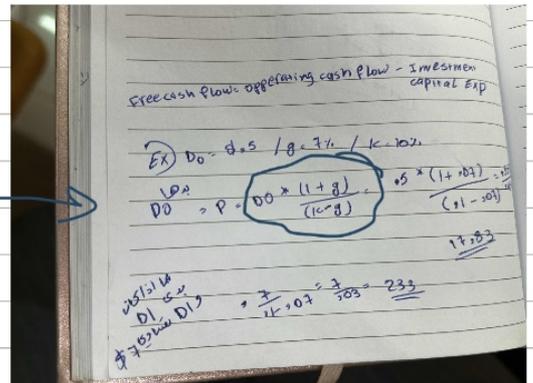
- The higher the discount rate the lower the Price

$$D_0 = 3\$$$

$$g = 5\%$$

$$k = 12\%$$

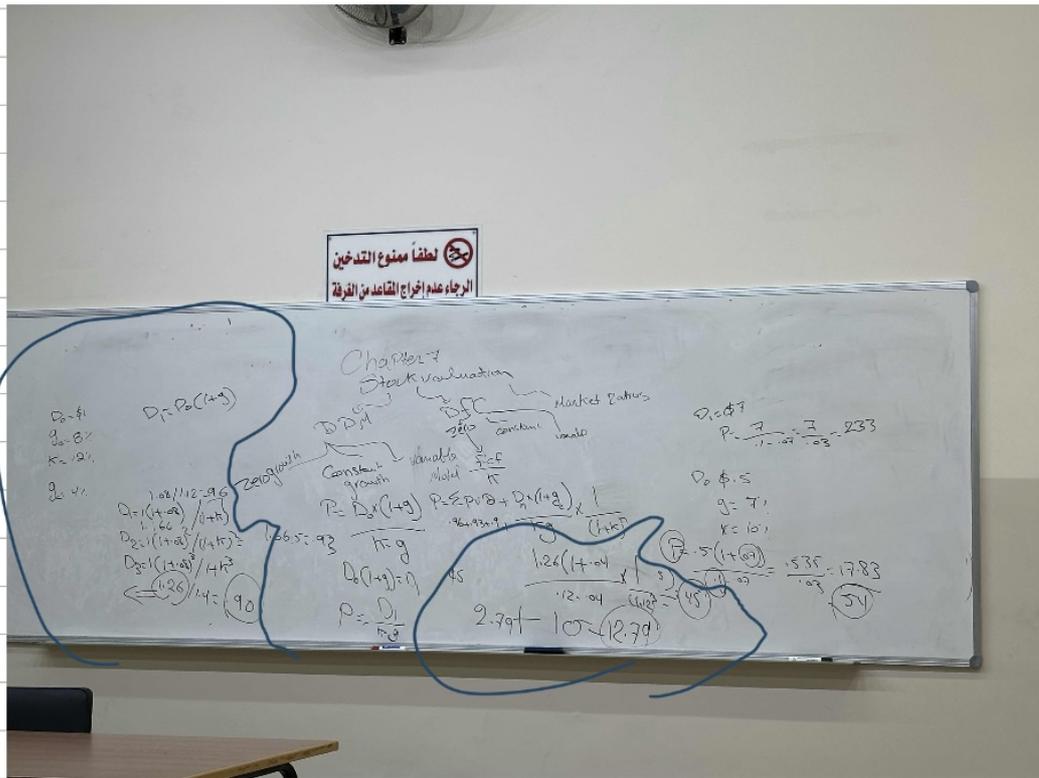
$$P = \frac{3 \times (1.05)}{.12 - .05} = 45$$



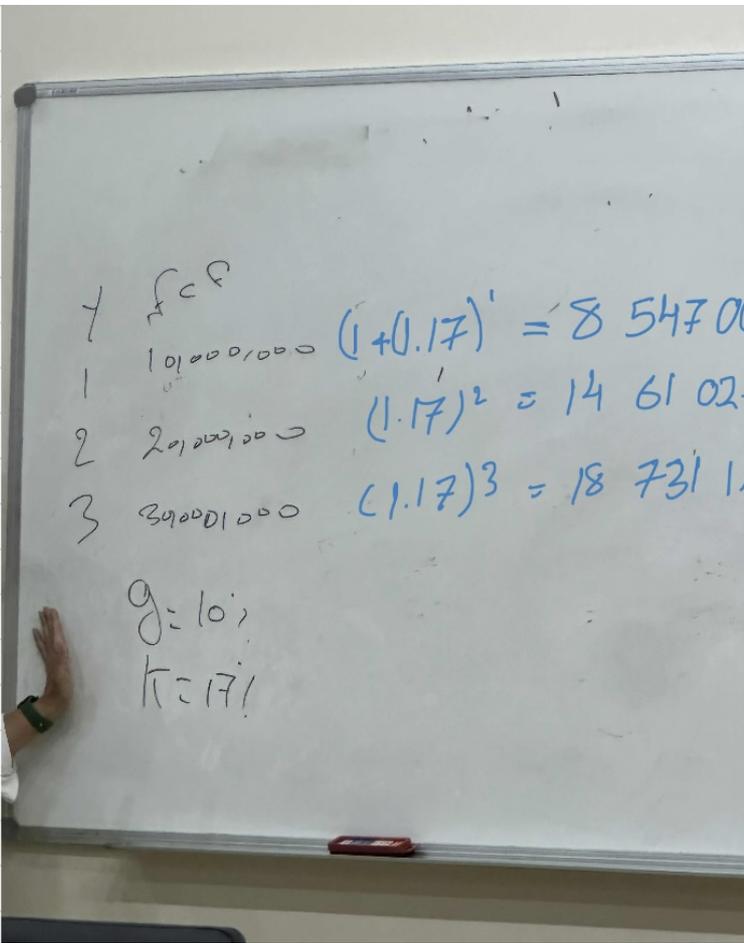
$$P = \sum PV D + \frac{(D_0 \times (1+g)^n)}{K-g} \times \frac{1}{(1+K)^n} \rightarrow 2 \text{ growth عندنا}$$

$D_n$  : Dividend  $n$

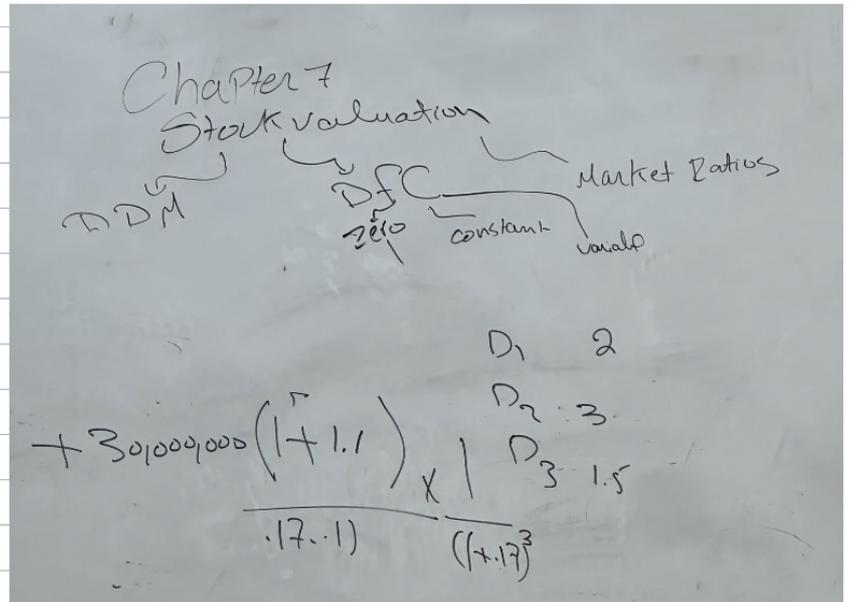
future value



Find free cash flow?



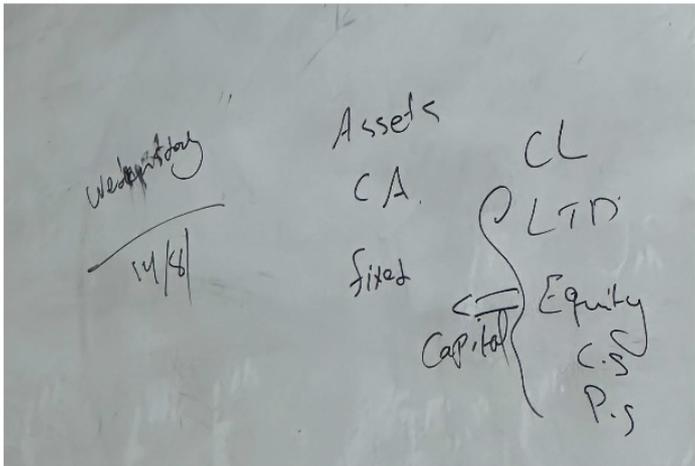
step ①  
→ Σ



Final result =  $\frac{\text{value of the firm}}{336,237,500}$  →  $\frac{\text{القيمة السوقية للشركة}}{\text{عدد الأسهم}} = \text{سعر السهم}$   
 Stock price =  $\frac{\text{value of the firm}}{\text{number of shares}}$

Common Stocks

$CS = \text{value of the firm} - MV \text{ of the Bond} - MV \text{ of PS}$



$$P = \frac{D_0}{k} \rightarrow \text{cost P.S.}$$

$$k \times P = \frac{D_0}{P}$$

$$k = \frac{D_0}{P}$$

$$P = \frac{D_1}{k-g}$$

$$\frac{P \times (k-g)}{P} = \frac{D_1}{P}$$

$$k-g = \frac{D_1}{P}$$

$$k = \frac{D_1}{P} + g$$

Bond  $\rightarrow$  YTM =  $\frac{PMT + \left( \frac{\text{Face Value} - \boxed{MV}}{\text{of Maturities}} \right)}{\left( \frac{1 \text{ Face Value} + MV}{2} \right)}$

replace MV with net proceeds

\* Net proceeds = MV - Flotation Amount

\* Flotation amount = Flotation Cost  $\times$  Face Value

after finding net proceed

$$YTM = \frac{PMT + \left( \frac{\text{Face Value} - NP}{\text{# of Maturities}} \right)}{\left( \frac{\text{Face Value} + NP}{2} \right)} \times (1 - \text{tax})$$

NP: Net proceeds.

إذا بيعت بالمال : بقولها \$

• Cost P.S =  $K = \frac{D_0}{P} \rightarrow \left( K = \frac{D_0}{NP} \right)$

NP : ابلغك في سؤلتي و قيسه من اقل في اقل

↓  
Come from → 1. Plotation  
2. Under Valuation

over Valuation → replace the (-) with (+)

Cost of C.S

1.  $\frac{D_1}{NP} + g$

2.  $K = RF + \text{Beta (Premium)}$   
 $= RF + B (MR - RF)$

\* Interrial ( اصدت اسما كالم في بين ما تسعين اذونك في )  
There is no NP  
There is Price

Cost of R.E =  $\frac{D_1}{P} + g$

Ex : Face Value 1000\$  
 Copon rate 5% → PMT = 50  
 Price (Premium) 1200\$  
 Flotation Cost 3%  
 Maturity 30  
 Tax rate 40%  
 Interest Semi annually →  $\frac{50}{2} \rightarrow \frac{125 = PMT}{2}$   
 YTM? Y Maturity = 30 x 2

\* Net proceeds = MV - Flotation Amount  
 \* Flotation amount = Flotation Cost x Face Value

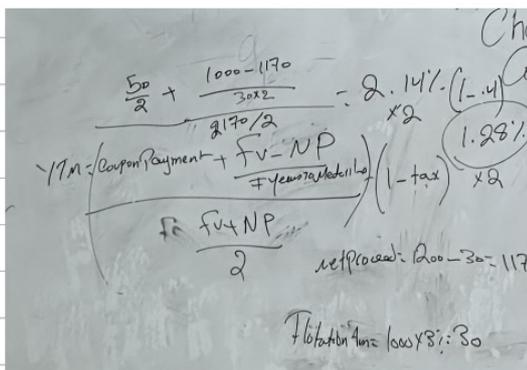
Flotation Cost = 3% x 1000 = 30  
 Net proceeds = 1200 - 30 = 1170

$$YTM = \frac{PMT + \left( \frac{\text{Face Value} - NP}{\text{# of Maturities}} \right) \times (1 - tax)}{\left( \frac{\text{Face Value} + NP}{2} \right)}$$

$$= \frac{25 + \left( \frac{1000 - 1170}{30} \right) \times (1 - .4)}{\left( \frac{1000 + 1170}{2} \right)}$$

$$\frac{25 + (-2.8)}{(1085)} \times .6 = \underline{1.23\%}$$

↓  
 يرجع لجزءه بـ 2 لانو Semi annual



حل اللى فوق السؤال →

Preferred stock  $d = 5\%$   
 par value 100\$  
 undervalued by 5\$ for par  
 flotation cost 2%  
 what is price of P.S

$$K_{PS} = \frac{D}{P} \rightarrow \frac{5}{93} = 5.38\%$$

$$100 - 5 = 95$$

$$NP = 100 - 5 - 2 = 93$$

Common Stock Price = 10\$ flotation 2\$ NP = 10 - 2 = 8

$$C.S. = \frac{D_1}{NP} + g$$

$$= \frac{3}{8} + 29.41\%$$

= 67% Cost of Common stock

if its internal  $\rightarrow$  NP = Price without flotation  
 10 + 29.41%  $\leftarrow$

1 C D<sub>1</sub> 3  
 2 C D<sub>2</sub> 5  
 3 C D<sub>3</sub> 2  
 3 C D<sub>4</sub> 65

$$g = \left(\frac{6.5}{3}\right)^{\frac{1}{3}} = \underline{\underline{29.41\%}}$$

## Weighted Average Cost of Capital

$$\bullet WACC = (w_{bond} \times YTM) + (w_{PS} \times \text{Cost PS}) + (w_{CS} \times \text{Cost CS})$$

Two ways to find weight [I] MV way

WACC =  $w_B \times YTM + w_{PS} \times \text{Cost PS} + w_{CS} \times \text{Cost CS}$

$.76 \times 2.25 + 11.4\% \times 9.9 + 12.6\% \times 67\%$

Bond	500	1200	600,000	$\frac{600,000}{790,000} = 76\%$
CS	10,000	10	100,000	$\frac{100,000}{790,000} = 12.6\%$
P.S	3000	30	90,000	$\frac{90,000}{790,000} = 11.4\%$
			790,000	

D<sub>1</sub> 3  
 D<sub>2</sub> 5  
 D<sub>3</sub> 2  
 D<sub>4</sub> 65

## 2 | Book Value

نتیجہ طریقہ ایک بیچلر میں بالامقار

Chapter 9  
Cost of Capital

$$WACC = W_B \times r_B + W_{P.S} \times \text{Cost P.S} + W_{C.S} \times \text{Cost C.S}$$

Bank	500	1000	500,000	$\frac{600,000}{790,000} = 76\%$
C.S	10,000	5	50,000	$\frac{100,000}{790,000} = 12.6\%$
P.S	3000	10	30,000	$\frac{90,000}{790,000} = 11.4\%$
			580,000	

$r = \left(\frac{6.5}{3}\right)^{\frac{1}{3}} - 1 = 29.4\%$

$r_1 = 3$   
 $r_2 = 5$   
 $r_3 = 7$   
 $r_4 = 6.5$

11 Aug 2024

Bond Coupon rate = 12%  
Semi annually  
Maturity 10 years  
discount 30\$  
 flotation cost 10\$  
tax rate 30% 300 Bond  
Cost Bond?

P.S		C.S	
D	2\$	RF	= 3%
Value	95\$	B	= 1.2
flotation cost	5%	MR	= 14%
Par Value	100\$	Par value	= 10\$
# of stocks	= 5 000	# of stocks	= 20 000

find wighted AVarage Cost of Capital

→ common stock

risk free = 3%

Beta = 1,2

MR = 14%

par value = 10

20,000 common stock

what WACC?

$$\text{Bond: } NP = 1000 - 30 - 10 = 960$$

$$YTM = \frac{1000 \times 0,06 + \left( \frac{1000 - 960}{20} \right) \times (1 - 30\%)}{\left( \frac{1000 + 960}{2} \right)} = 0,0885$$

$$WB = 300 \times 1000 = 300,000 / 1,000,000 = 0,3$$

$$\text{preferred stock } NP = 95 - (0,05 \times 100) = 90$$

$$\text{cost p.s.} = \frac{D}{NP} = \frac{5}{90} = 0,0222$$

$$WP.S = \frac{500 \times 100}{1,000,000} = 0,5$$

common stock

$$\begin{aligned} \text{cost c.s.} = R &= R_f + \text{Beta} (MR - R_f) \\ &= 3\% + 1,2 (14\% - 3\%) = 0,162 \end{aligned}$$

$$WC.S = 20,000 \times 10 = 200,000 / 1,000,000 = 0,2$$

$$WACC = (0,3 \times 0,0885) + (0,5 \times 0,0222) + (0,2 \times 0,162) = 0,07$$

P9-19

LG 3 LG 4  
LG 5 LG 6

**P9-19** Calculation of individual costs and WACC Lang Enterprises is interested in measuring its overall cost of capital. Current investigation has gathered the following data. The firm is in the 40% tax bracket.

**Debt** The firm can raise debt by selling \$1,000-par-value, 8% coupon interest rate, 20-year bonds on which quarterly interest payments will be made. To sell the issue, an average discount of \$30 per bond would have to be given. The firm also must pay flotation costs of \$30 per bond.

**Preferred stock** The firm can sell 8% preferred stock at its \$95-per-share par value. The cost of issuing and selling the preferred stock is expected to be \$5 per share. Preferred stock can be sold under these terms.

**Common stock** The firm's common stock is currently selling for \$90 per share. The firm expects to pay cash dividends of \$7 per share next year. The firm's dividends have been growing at an annual rate of 6%, and this growth is expected to continue into the future. The stock must be underpriced by \$7 per share, and flotation costs are expected to amount to \$5 per share. The firm can sell new common stock under these terms.

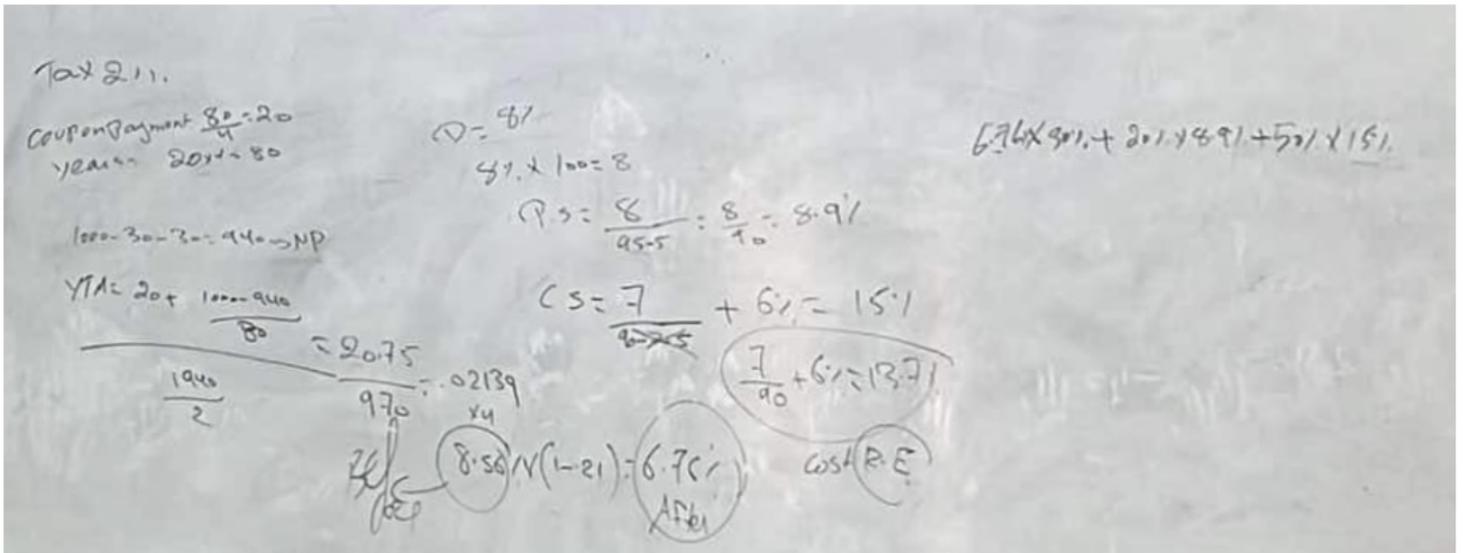
**Retained earnings** When measuring this cost, the firm does not concern itself with the tax bracket or brokerage fees of owners. It expects to have available

Interest quarterly  
Find interest YTM after/before tax

CHAPTER 9 The Cost of Capital 435

\$100,000 of retained earnings in the coming year; once these retained earnings are exhausted, the firm will use new common stock as the form of common stock equity financing.

- Calculate the after-tax cost of debt.
- Calculate the cost of preferred stock.
- Calculate the cost of common stock.
- Calculate the firm's weighted average cost of capital using the capital structure weights shown in the following table. (Round answer to the nearest 0.1%.)



Source of capital	Weight
Long-term debt	35%
Preferred stock	12
Common stock equity	53

The tax rate of the firm is currently 40%. The needed financial information and data are as follows:

**Debt** Nova can raise debt by selling \$1,000-par-value, 6.5% coupon interest rate, 10-year bonds on which annual interest payments will be made. To sell the issue, an average discount of \$20 per bond needs to be given. There is an associated flotation cost of 2% of par value.

**Preferred stock** Preferred stock can be sold under the following terms: The security has a par value of \$100 per share, the annual dividend rate is 6% of the par value, and the flotation cost is expected to be \$4 per share. The preferred stock is expected to sell for \$102 before cost considerations.

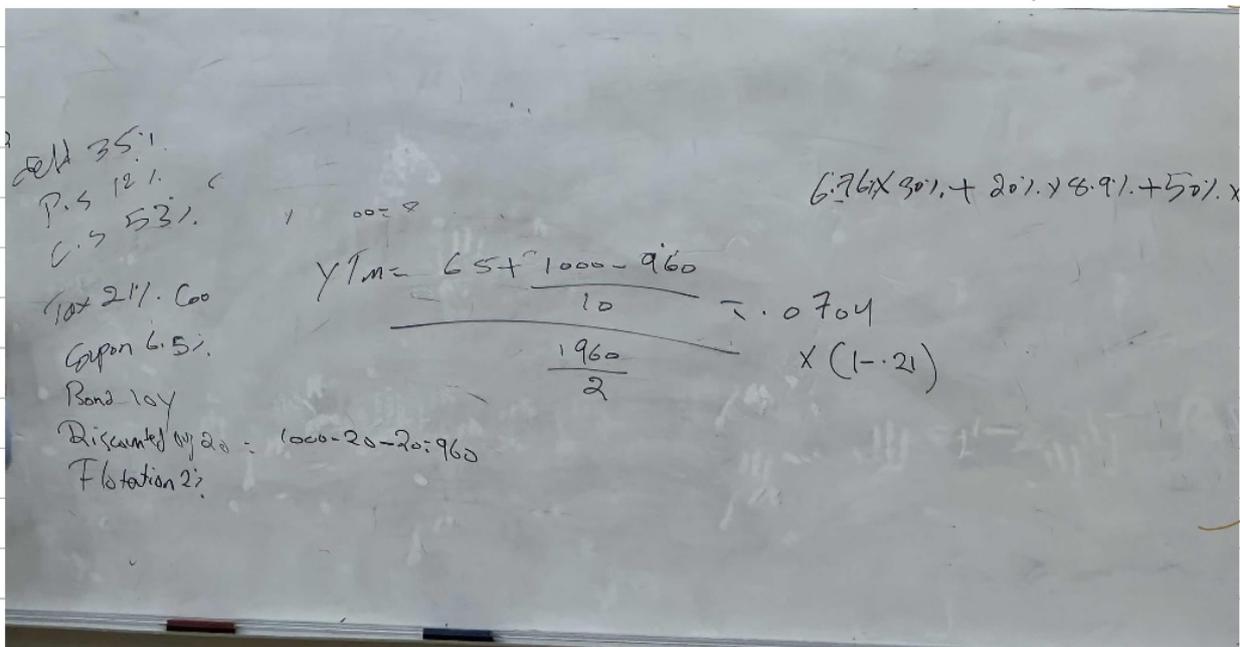
**Common stock** The current price of Nova's common stock is \$35 per share. The cash dividend is expected to be \$3.25 per share next year. The firm's dividends have grown at an annual rate of 5%, and it is expected that the dividend will continue at this rate for the foreseeable future. The flotation costs are expected to be approximately \$2 per share. Nova can sell new common stock under these terms.

**Retained earnings** The firm expects to have available \$100,000 of retained earnings in the coming year. Once these retained earnings are exhausted, the firm will use new common stock as the form of common stock equity financing. (Note: When measuring this cost, the firm does not concern itself with the tax bracket or brokerage fees of owners.)

**TO DO**

Create a spreadsheet to answer the following questions:

- Calculate the after-tax cost of debt.
- Calculate the cost of preferred stock.
- Calculate the cost of retained earnings.
- Calculate the cost of new common stock.
- Calculate the firm's weighted average cost of capital using retained earnings and the capital structure weights shown in the table above.
- Calculate the firm's weighted average cost of capital using new common stock and the capital structure weights shown in the table above.



$$* \% R = \frac{(\text{Selling Price} - \text{Purchase Price}) + \text{Yield}}{\text{Purchase Price}}$$

$$* \text{Avr}(\bar{R}) = \frac{\sum R}{n}$$

no Prob, equal prob

$$* \text{Avr}(\bar{R}) = \sum r \times \text{Prob}$$

there is Prob.

$$* \text{Sd (standard deviation)} = \sqrt{\text{Variance}} = \sqrt{(r - \bar{r})^2 \times \text{Prob}} \quad \text{there is Prob}$$

-  $\sigma^2$  : Variance

-  $\sigma$  : standard deviation

$$* \text{Sd} = \sqrt{\frac{\sum (r - \bar{r})^2}{n-1}}$$

no Prob, equal Prob

$$* \text{Coefficient of Variation} = \frac{\text{Sd}}{\text{Avr}} \left( \frac{\sigma}{\bar{r}} \right)$$

$$* \text{Covariance} = \frac{\sum (r - \bar{r}_a) \times (r - \bar{r}_b)}{n-1}$$

no prob, equal Prob.

type of relation

$$* \text{Covariance} = \sum (r - \bar{r}_a) \times (r - \bar{r}_b) \times \text{prob}$$

there is Prob.

$$* \text{Correlation} = \frac{\text{Covariance}}{\text{Sd}_a \times \text{Sd}_b}$$

strength of relation

-  $w_p = 100\%$  always

$$* R_p = \sum r \times w \rightarrow \text{return}_p = (w_a \bar{r}_a) + (w_b \bar{r}_b) + \dots + (w_n \bar{r}_n)$$

$$* \text{Std } p = \sqrt{w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2w_a w_b \frac{\text{Cov}}{\sigma_a \sigma_b}}$$

\*  $\text{Cov} = \text{Correlation } \sigma_a \sigma_b$

• 6 % Variance 1.90 %

\* Total risk = Systematic + Unsystematic.  
 Market. Unique (firm risk).  
 undiversifiable. diversifiable  
 non Controllable. Controllable.

$$* \text{CAPM} = \text{RF} + \text{Beta} \frac{\text{MR} - \text{MF}}{\text{Premium}}$$

MR - MF = Risk Premium.

MR: Market Return

MF: Market Free

RF: Risk Free Rate (rate on treasury bills.)

$$* \text{Beta} = \frac{\text{Cov}}{\text{Var}}$$

- Beta RF = 0

- Beta Market = 1

Yield to Maturity (YTM):

- Yield to Maturity  $\left[ \begin{array}{|l} < \\ \hline \end{array} \right]$  Coupon rate  $\rightarrow$  Bond Premium  $\rightarrow$  Price  $> 1000$
- YTM  $\left[ \begin{array}{|l} > \\ \hline \end{array} \right]$  Coupon rate  $\rightarrow$  Bond Discount  $\rightarrow$  Price  $< 1000$
- YTM  $\left[ \begin{array}{|l} = \\ \hline \end{array} \right]$  Coupon rate  $\rightarrow$  Face Value = 1000

Same meanings:

- Interest rate : required rate of return : Cost of Money

- Nominal interest rate : Actual interest rate

- Coupon rate : interest

- Market (i) : Yield to Maturity

Bond Price قانون

- Price : MV

YTM

قانون

- Coupon Bond : PMT

- YTM : Priced to Yield.

# Chapter (6)

ماكين القوانين

$$\text{Real Interest Rate} = \left( \frac{1 + \text{nominal rate}}{1 + \text{inflation}} \right) - 1$$

nominal rate : Actual rate

$$\text{PMT} = \text{Coupon rate} \times \text{Face value}$$

usually 1000 for the Bond

$$\text{Bond Price} = \frac{\text{PMT} \times \left( 1 - \left( \frac{1}{(1+i)^n} \right) \right)}{i} + \frac{1000}{(1+i)^n}$$

-when it Semi annual  $\rightarrow \left( \frac{\text{PMT}}{2}, \left( \frac{i}{2} \right), (n \times 2) \right)$

-when it quarterly  $\rightarrow \left( \frac{\text{PMT}}{4}, \left( \frac{i}{4} \right), (n \times 4) \right)$

$$\text{YTM} = \frac{\left( \text{PMT} + \left( \frac{\text{Face value} - \text{Market value}}{n} \right) \right)}{\left( \frac{\text{Face value} + \text{Market value}}{2} \right)}$$

n : number of Maturity

MV : Bond Price

-when it Semi annual  $\rightarrow \left( \frac{\text{PMT}}{2}, \left( \frac{\# \text{ of Maturity}}{2} \right) \right)$  also the  $\left( \frac{\text{final result}}{2} \right)$

-when it quarterly  $\rightarrow \left( \frac{\text{PMT}}{4}, \left( \frac{\# \text{ of Maturity}}{4} \right) \right)$  & the  $\left( \frac{\text{final result}}{4} \right)$

$$\text{Current Yield} = \frac{\text{Coupon Payment}}{\text{Bond Price}}$$

\* out-standing = Issued - Treasury Stocks

Preferred Stock

$P = \frac{D}{K}$

P = Price, K : cost of P.S, required rate of return

$K = RF + B(MR - RF)$

Perpetuity : discount rate forever.

Common Stock Valuation

DDM :

• Zero growth rate  $P = \frac{D_0}{K}$   
Price Discount rate

• Constant growth

$P = \frac{D_1}{(K-g)}$

g: growth

$D_1 = D_0 \times (1+g)$

$P = \frac{(D_0 \times (1+g))}{(K-g)}$

The higher the g → the higher the P.

The higher the k → the lower the P.

• Variable Model

$P = \sum P_v D + \left( \frac{(D_n \times (1+g_c))}{K-g} \times \frac{1}{(1+K)^n} \right)$

Value of the firm

2 growths

$PVD = \frac{D_n}{(1+K)^n}$

• Price of stocks =  $\frac{\text{Value of the firm}}{\text{number of stocks}}$

• Price of C.S = Value of the firm - MV(Bond) - MV(PS)

$D_1 = D_0(1+g)$  | first way |  
 $D_2 = D_1(1+g)$  | |  
 $D_3 = D_2(1+g)$  | |  
 or  
 $D_1 = D_0(1+g)^1$  | sec way |  
 $D_2 = D_0(1+g)^2$  | |  
 $D_3 = D_0(1+g)^3$  | |

# DFC:

Dividend لا يتوزع إلا على المساهمين  
و لا يمكن توزيعه على الموظفين

1. Zero growth

$$\frac{FCF}{k} \rightarrow \frac{\text{Free Cash Flow}}{\text{Discount rate}}$$

2. Constant

$$\text{Free Cash Flow} = \text{Operating Cash Flow} - \text{Investment Capital Expense.}$$

Book Value (Historical Cost) القيمة التاريخية

$$\text{Market ratio} = \frac{\text{Price}}{\text{Book Value}}$$

$$\text{Book Value of the firm} = \text{Total Assets} - \text{total liabilities} \rightarrow \text{Book Value} = \text{equity!}$$

$$\text{Earning Per share} = \frac{(\text{net income} - \text{Dividends PS})}{\# \text{ of shares}}$$

$$\text{Liquidity Value (MV)} = \text{Market Value of total Assets} - \text{MV of total liabilities}$$

مزاينة مالية

$$\frac{\text{Price Per share}}{\text{BV Per share}} \rightarrow \text{Industry} \text{ الارتفاع في الصناعة}$$

$$\frac{\text{Price Per share}}{\text{EPS}} \rightarrow \text{PE ration}$$

$$\frac{\text{Price Per share}}{\text{Liquidation Value per share}}$$

How to Calculate Growth

(with Constant/Variable)

$$\textcircled{1} G = 1 - \frac{D}{E} \times \text{ROE}$$

$$G = \text{retention ratio} \times \text{ROE}$$

$$\text{retention ratio} = 1 - \text{payout ratio}$$

$$\text{payout ratio} = \frac{D}{E} \rightarrow \text{earning}$$

$$\textcircled{2} \left( \frac{\text{Ending } D}{\text{Beginning } D} \right)^{\frac{1}{n}} - 1$$

« Chapter 9 »

\* Bond  $\rightarrow$  
$$YTM = PMT + \left( \frac{\text{Face} - NP}{\text{number of Maturity}} \right) \times (1 - tax)$$
  
$$\left( \frac{\text{Face Value} + NP}{2} \right)$$

\* Cost P.S  $K = \frac{D_0}{NP}$

\* Cost of C.S  $K = \frac{D_1}{NP} + g$

•  $NP = MV - \text{Flotation amount}$

•  $\text{Flotation amount} = \text{Flotation Cost} \times \text{Face}$

$K = RF + \text{Beta} (MR - RF)$  over valuation  $\rightarrow$  + under valuation  $\rightarrow$

\* Cost of RE =  $\frac{D_1}{P} + g$  (C.S) الشركة أصدرت أسهمًا بالبايوت  
ما تستحقه في P من NP (Internal)

•  $WACC = (YTM \times w_{\text{bond}}) + (\text{Cost P.S} \times w_{\text{PS}}) + (\text{Cost}_{\text{CS}} \times w_{\text{CS}})$

$w_{\text{bond}} + w_{\text{CS}} + w_{\text{PS}} = 1$  or 100%

, Bond  $\rightarrow$  Debt

• C.S, PS  $\rightarrow$  Equity

Ch 10

1] Payback period

كم الفترة التي تسترد فلوسها  
تقبل على بتجيب الاستثمار أسرع

2] Discount payback period

$$= \frac{\text{Investment}}{(1+k)^n}$$

3] Discount operation CF =  $\Sigma$  Discount Payback Period

4] NPV = - Initial Investment + discount operation CF  
net Present value

5]  $PJ = \frac{\text{discount operation CF}}{\text{Initial Investment}} = \frac{\Sigma \text{ Discount payback}}{\text{Initial Investment}}$   
Profitability index

\* NPV (-) → reject Project  
\* NPV (+) → Accept, take higher value.

$PJ > 1$  → Accept, take higher value.