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finn2

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chapter 8

Risk & Return

Thu 18 Jul

- Expected Return - Actual Return
 - Beta
 - Standard deviation
- } → Risk Cost

$$\text{\$ Return} = \text{Selling price} - \text{purchase price} \Rightarrow \text{\$ Amount}$$

$CF_1 \quad - \quad CF_0$

$$\%R = \frac{\text{Selling} - \text{Purchase} + \text{Yield}}{\text{purchase price}} \Rightarrow \begin{matrix} \text{Div} \\ \text{Bond interest} \end{matrix}$$

Finn 2

Sat. 20 Jul 2024

* Variance في خطر ليس ما يعرفه حرجي

Chapter 8, Second Lec

Using Prob.

stocks	Return	Prob
A	.10	.30
	.15	.15
	.30	.55

To Calculate Average return * $Avr = \sum R \times Prob$

$$(0.1 \times 0.3) + (0.15 \times 0.15) + (0.3 \times 0.55) = 0.2175 = Avr(A)$$

Standard deviation * $Sd = \sqrt{(R - Avr)^2 \times Prob} \rightarrow Sd = \sqrt{\text{Variance}}$

1 * بنوع Avr لا Stock ليعطى بنوع Avr من كل R على حدة

2 * بنوع كل قيمة من (R - Avr)

R	Avr	R - Avr	(R - Avr) ²	$\frac{(R - Avr)^2 \times Prob}{\text{Variance}}$
.1	.2175	-.1175	.01380625	.00414875
.15	.2175	-.0675	.00455625	.0006834375
.3	.2175	.0825	.00680625	.0037434375

$\Sigma = \text{Variance}$

$$\text{Var} = .008575625$$

$$\rightarrow Sd = \sqrt{\text{Variance}} \rightarrow Sd = \sqrt{.008575625}$$

$$\rightarrow .092604671 = Sd \rightarrow \text{Percent انحراف 9\%}$$

Stocks	Return	Prob
B	.5	30%

-3%	15%
12%	55%

ما يتغير عنان

أفتر انكاف

$$Avr = (.05 \times 0.3) + (-0.03 \times 0.15) + (.12 \times 0.55)$$

$$Avr(B) = .0765$$

R	Avr	R - Avr	(R - Avr) ²	$(R - Avr)^2 \times Prob$
.05	.0765	-.0265	.00072225	.000210675
-.03	.0765	-.1065	.01134225	.0017013375
.12	.0765	.0432	.00189225	.0010473375

$$\text{var} = .0029654625$$

$$Sd = \sqrt{\text{var}} \rightarrow Sd = \sqrt{.0029654625} \rightarrow Sd = .0544339212$$

(1)

$$Sd(A) = .092567543$$

$$= 9\%$$

$$Sd(B) = .054339212$$

$$= 5\%$$

which one is more risky? stock A is more risky.

* Coefficient of Variation = $\frac{Sd}{Avr}$ trade of risk & return
 Coefficient of Variation $> 1 \rightarrow$ good, because risk less than return.

Risk preference ✓

1. Risk Averse

هو الذي يوجه لأب استثمارات ترجح

* يطلب مقابل لا Risk يتيقن في.

بـ Return تخفي أو Risk يتيقن

* The higher the risk \rightarrow higher return

2. Risk Neutral

* ما يتطلع على أو Risk ليس يتطلع

على أو Return (أو) Return

رفض النظر عن أو Risk.

3. Risk seeking (Lovers, Gamblers)

* يتطلع على أعلى Risk

مستعد أن Risk أكثر

من أو Return مثل المقامرين.

Risk single asset:

1. Sd

2. Beta

3. Unexpected return - actual return

4. The range

Range = Subtracting optimistic return - pessimistic return (Return - Return)

"you can't calculate the risk without Return."

Covariance & Correlation

- Statistical measure of the relation between 2 Assets.
- both measure the relationship between 2 Assets.

- * Covariance: the type of the relation, if the relation is pos or neg.
- * Correlation: measure the strength of the relation.

"I Can't Calculate the Correlation without the Covariance"

$$* \text{Covariance} = \frac{\sum (r - \text{avr}(\text{Asset A})) \times (r - \text{avr}(\text{Asset B}))}{(n-1)} \quad , \text{without Prob}$$

$$* \text{Covariance} = \sum (r - \text{avr}(\text{Asset A})) \times (r - \text{avr}(\text{Asset B})) \times \text{Prob} \quad \text{with Prob}$$

$$\begin{aligned} \text{Covariance} &= \sum (r - \text{avr}_{(A)}) \times (r - \text{avr}_{(B)}) \times \text{Prob} \quad \rightarrow \quad \text{There is prob in calculations} \\ &= (-.1175 \times -.0265 \times .3) + (-.0675 \times -.1065 \times .15) + (.0875 \times .0432 \times .55) \\ &= .000934125 \quad + .0010783125 \quad + .0019602 \end{aligned}$$

$$\text{Covariance} = .0039726375 \quad \text{positive relation ship.}$$

$$* \text{Correlation} = \frac{\text{Covariance}}{\text{Sd}_A \times \text{Sd}_B}$$

$$\text{Correlation} = \frac{.0039726375}{.092604671 \times .054339212} = .7894646867 \quad \text{Strong}^{\text{pos}} \text{ relation}$$

Correlation is calculated

no relation

0

"Correlation $\geq .5 \rightarrow$ Strong relation."

"Correlation $\leq .5 \rightarrow$ weak relation."

Correlation -1

perfect neg correlation

[A \uparrow 40%] \rightarrow [B \downarrow 40%]

1

perfect pos correlation

[A \uparrow 10%] \rightarrow [B \uparrow 10%]

Mon 22 Jul 24

A	B
R	
10%	15%
17%	-3%
22%	9%

Avr sd Var Correlation Cov

$$Avr = \frac{.1 + .17 + .22}{3} = .1633$$

$$Avr_B = \frac{.15 + (-.03) + .09}{3} = .0367$$

$R - \bar{R}$	$(R - \bar{R})^2$
$.1 - .1633$	$.003969$
$.17 - .1633$	$.000489$
$.22 - .1633$	$.00321489$

$$Var = \frac{.007669}{2} = .0038345$$

$$sd = \sqrt{.0038345} = .06192$$

Cov = $-.00231 \rightarrow$ negative relation.
Correlation = $-.526 \rightarrow$ Semireal (semiweak/semistrong)

W	
A	1.60
B	1.40

$$\sqrt{.00131 + .0013 + -.0034} = 3.6\%$$

Standard Deviation : 3

$$Variance = 3^2$$

How to Calculate Risk, Return 2 Asset Portfolio?

Weight always = 100%

$$* R_p = (w_a \times \bar{R}_a) + (w_b \times \bar{R}_b) + \dots \dots (w_n \times \bar{R}_n)$$

$$SD = \sqrt{w_a^2 \times \sigma_a^2 + w_b^2 \times \sigma_b^2 + 2w_a w_b \times \text{Cov}}$$

Correlation $\times \sigma_a \times \sigma_b$

- Beta

مقياس المخاطرة السوقية

- Security Marketable

- total risk = Systematic + Unsystematic
 Market diversifiable
 undiversified controllable
 non controllable Unique (firm risk)

CAPM

$$K = R_F + \text{Beta} \times \text{Premium} (MR - MF)$$

σ^2 $\frac{\text{Cov}}{\text{variance market}}$ علاقة السوق مع السوق

- Beta RF = Zero
 - Beta Market = 1

Beta RF = zero
 " Market = 1

Beta
 Security Marketline

Total Risk = 2

Stock, T.Bill
 Beta: Beta

CAPM = $(K) = (R_F) + \text{Beta} (MR - R_F)$

$W_S \times \text{Beta}_{\text{stock}} + W_{TF} \times \text{Beta}_{TF}$
 zero

σ^2 $\frac{\text{Cov}_{a,n}}{\text{variance market}}$ $\frac{.0028}{.0038} = .73$

كلما Beta زادت فكمية المخاطرة السوقية تزيد \rightarrow كلما Risk

Beta \propto Risk

Market Return: return

$$* \text{Beta}_p = w_a \times \text{Beta}_a + w_b \times \text{Beta}_b$$

Q:		R		R
	Prob	A		B
	55%	5%		22%
	15%	12%		-7%
	30%	4%		30%

$$\text{AvR}_A = .55 \times .05 + .15 \times .12 + .3 \times .04 = .0575 = \bar{R}_A$$

$(R - \bar{R})^2_A$	$(R - \bar{R})^2_A \cdot \text{Prob}_A$	$(R - \bar{R})^2_B$	$(R - \bar{R})^2_B \cdot \text{Prob}_B$
.0006	.0003	.0004	.00022
.00391	.00059	.0729	.0094
.00031	.00009	.01	.003

$$\text{Variance}_A = .00071$$

$$\sigma_B^2 = .01416$$

$$(\text{standard dev}) \sigma = \sqrt{.00071} \rightarrow \sigma = 2.66\%$$

$$\sigma_B = 11.9\%$$

$$\text{AvR}_B = 20\%$$

$$\begin{aligned} \text{Cov} &= \sum R - \bar{R}_A \times R - \bar{R}_B \times \text{Prob} \\ &= .00008 + -.00253 + -.00053 \\ \text{Cov} &= .00298 \end{aligned}$$

$$\text{Correlation} = \frac{\text{Cov}}{SD_A \times SD_B} = \frac{.00298}{20\% \times 11.9\%} = .96$$

$$\boxed{RP = w_a \times \bar{R}_a + w_b \times \bar{R}_b}$$

return portfolio

$$= .7 \times .0575 + .3 \times .2 = 10.25\%$$

$$\sigma^2 = w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2 w_a w_b \text{Cov}$$

$$\sigma^2 = .0003$$

$$\sigma = 4.8\%$$

$$CV = \frac{\sigma}{\Sigma R} = \frac{2.68\%}{5.57}$$

$$\begin{aligned} \text{Cov } m, a &= -.005 \\ m, b &= -.003 \end{aligned}$$

$$\sigma_m = 44\%$$

$$\text{Beta}_A = \frac{\text{Cov}}{\sigma_m^2} = \frac{-.005}{.0196} = -.255$$

$$\text{Beta}_B = -.0153$$

$$\text{Beta}_p = w_A \times \text{Beta}_A + w_B \times \text{Beta}_B$$

$$\text{Beta}_{\text{port}} = .7 \times (-.255) + .3 \times (-.0153)$$

Bond Valuation

- Price Bond
- Current yield
- yield to Maturity
- yield to call

Time Value of money (TMV)				
PV (÷)				FV (X)
↓ Annuity	Single amount	Perpetuity	Mix stream	
$PMT \times \left(\frac{1}{(1+i)^n} \right)$	$\frac{FV}{(1+i)^n}$	$\frac{FV}{i}$	$\frac{FV}{(1+i)^1} + \frac{FV}{(1+i)^2} + \dots + \frac{FV^n}{(1+i)^n}$	
i		PV		

stated interest (yield to maturity)

$$\text{Price of the Bond} = \frac{PMT \times \left(1 - \frac{1}{(1+i)^n} \right)}{i} + \frac{1000}{(1+i)^n}$$

$$PMT = \text{Coupon Rate} \times \text{Face Value}$$

الإدارة بالوقت (الوقت بالمال)

- face value always = 1000
- Maturity = 15

- yield to Maturity < coupon rate → Bond Premium → Price > 1000
- YTM > coupon rate → Bond discount → Price < 1000
- YTM = coupon rate → face value → = 1000

$$\frac{50 \times \left(1 - \frac{1}{(1+0.07)^{15}} \right)}{0.07} + \frac{1000}{(1+0.07)^{15}} = 817.85$$

→

لازم يطلع أقل من 1000

n (الوقت بالمال) → Quarterly for ex → n x 4
• zero prices PMT, i

Ex : Face Value 1000
Maturity after (n) 30 years

Interest (Coupon Rate) 10%

Market (i) yield to Maturity 8%

Semi annually $\rightarrow \frac{PMT}{2}, \frac{i}{2}, n \times 2$

* Bond Price?

$$\text{Price of the Bond} = \frac{PMT}{i} \times \left(1 - \frac{1}{(1+i)^n}\right) + \frac{1000}{(1+i)^n}$$

$PMT = \text{Coupon Rate} \times \text{Face Value}$

$$= 10\% \times 1000 = 100$$

$$\text{Price of the Bond} = \frac{\left(\frac{100}{2}\right) \times \left(1 - \frac{1}{\left(1 + \frac{.08}{2}\right)^{60}}\right)}{\frac{.08}{2}} + \frac{1000}{(1 + .04)^{60}}$$

$$= \frac{50 \times (.905)}{.04} + \frac{1000}{10.52}$$

$$= \underline{4226.23} \text{ Premium because it's more than 1000}$$

When $YTM \leq \text{coupon rate} \rightarrow \text{Bond Premium} \rightarrow \text{Price} > 1000$

$$YTM = \frac{\text{Coupon Payment} + \frac{(\text{Face Value} - MV)}{\# \text{ of Maturity}}}{\left(\frac{\text{Face} + MV}{2} \right)}$$

Ex: Price 900 \$
Maturity 10 years
Coupon 7%

$$= \frac{70 + \frac{1000 - 900}{10}}{\frac{1000}{2}} = \frac{80}{950} = 8.4\% \rightarrow$$

$$\frac{PMT}{2}, \frac{\# \text{ of Maturity}}{2} \rightarrow \text{Cib} \rightarrow \frac{\text{السعر}}{2} \quad \text{Semi} \quad \text{السعر 1/2}$$

$$\text{Current Yield} = \frac{\text{Coupon Payment}}{\text{bond Price}}$$

6-11

outline

$$\begin{array}{l}
 \text{Coupon Payment} + \frac{\text{Face value} - MV}{\text{# of maturities}} \\
 \hline
 \frac{\text{Face} + MV}{2} \\
 50 + \frac{1000 - 810.34}{10} = 7.62\% \\
 \hline
 \frac{1810.34}{2} \\
 \left(\frac{50}{4}\right) + \frac{1000 - 810.34}{10 \times 4} = 1.91\% \times 4 \\
 \hline
 \frac{1810.34}{2} = .01904 = 7.62\%
 \end{array}$$

6.2%

Outline 6-15

100 par value
coupon rate 8%
Interest annually

par value : Face Value

i, $y = 12$ year
YTM = 4%

$$\text{par Value} \times \text{coupon rate} = 100 \times .08 = 8$$

سعر السهم بالأسواق المالية

$$P = \frac{\text{PMT} \times \left(1 - \frac{1}{(1+i)^n}\right)}{i} + \frac{\text{Face Value}}{(1+i)^n}$$

$$= 137.54 \rightarrow \text{premium because } > \text{YTM}$$

C. YTM = 10%

6-15

Face value = 100
Coupon rate = 8% $8\% \times 100 = 8$
 $y = 12$
YTM = 4%
(10%)

$$P = \frac{\text{PMT} \times \left(1 - \frac{1}{(1+i)^n}\right)}{i} + \frac{\text{Face value}}{(1+i)^n}$$
$$= \frac{8 \left(1 - \frac{1}{(1+.1)^{12}}\right)}{.1} + \frac{100}{(1+.1)^{12}}$$

Stock Valuation

• Debt → Bond

Borrower creditor relationship has a time when the Debt end the relationship between them end

- There is Maturity
- Interest

حافل ربح وخلاف الشركة

• Equity

- No Maturity
- Dividend

Preferred stock, common stock

no voting right

voting right

حافل ربح وخلاف الشركة

Equity Risker than Debt

إذا الشركة أفست
أنا بفلس

إذا أرباح ما دفعت لا تجز
على أرباح ما بفلس

Authorized Shares :

Issued → Sold to Shareholder

outstanding could be = Issued → if there is no Treasury stocks

outstanding = Issued - Treasury stocks

Types of shares:

- Voting shares → Common stock
- Sober share → مستحق الأسهم بأجر
- non-voting → Preferred

Common stocks

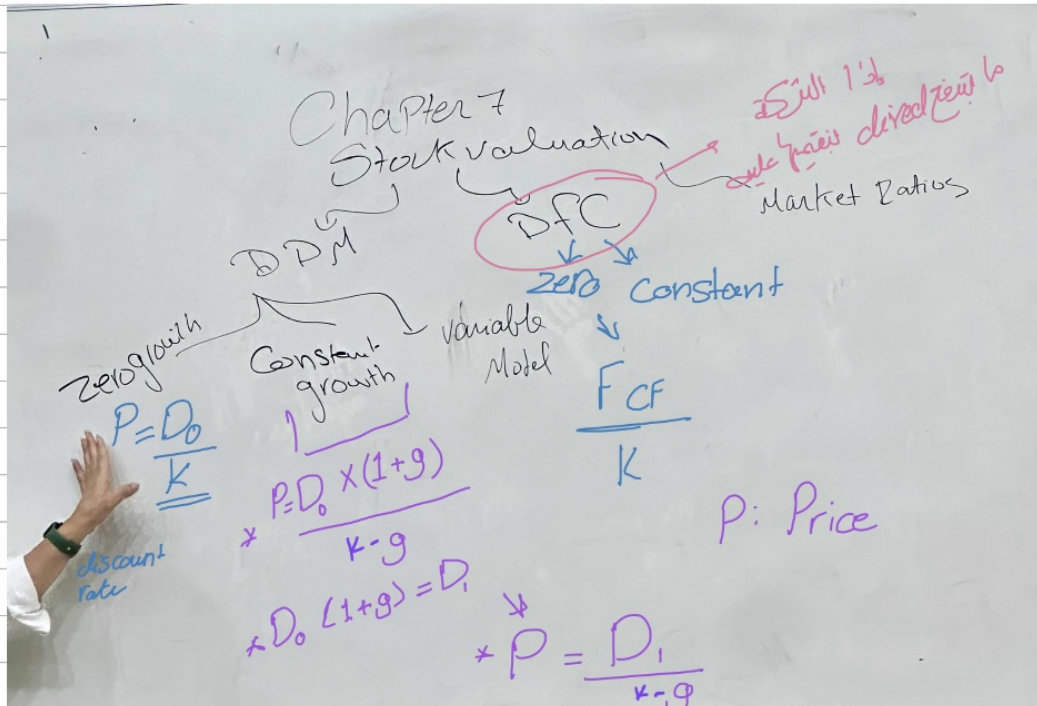
- ADR: American deposit receipt → شهادات إيداع أمريكية
listed in America
- GDR: Global
2.5 stock → شهادات عالمية
- CDR: China

Par Value → داء الاسهم الراف

* When you split # of stocks increase
price of stocks decreases

Preemptive right → ما يقرر الشركة أني بالاسهم لي أنا مستحق
فني على من اجها نسبة الاسهم لي أنا مستحق
ما يتغير له من ما أنا أقدر اذا الشركة لم يبيع
نسبة أسهمها

Commons ۲۹ آفرین ۲۰۲۱



preferred stock \rightarrow perpetuity ??

Free Cash Flow = operating cash flow - Investment Capital Exp

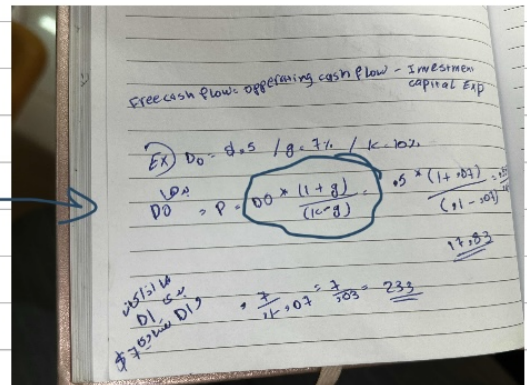
g : growth

- The higher the growth \rightarrow the higher the price

- The higher the discount rate the lower the Price

$$\begin{aligned} D_0 &= \$3 \\ g &= 5\% \\ k &= 12\% \end{aligned}$$

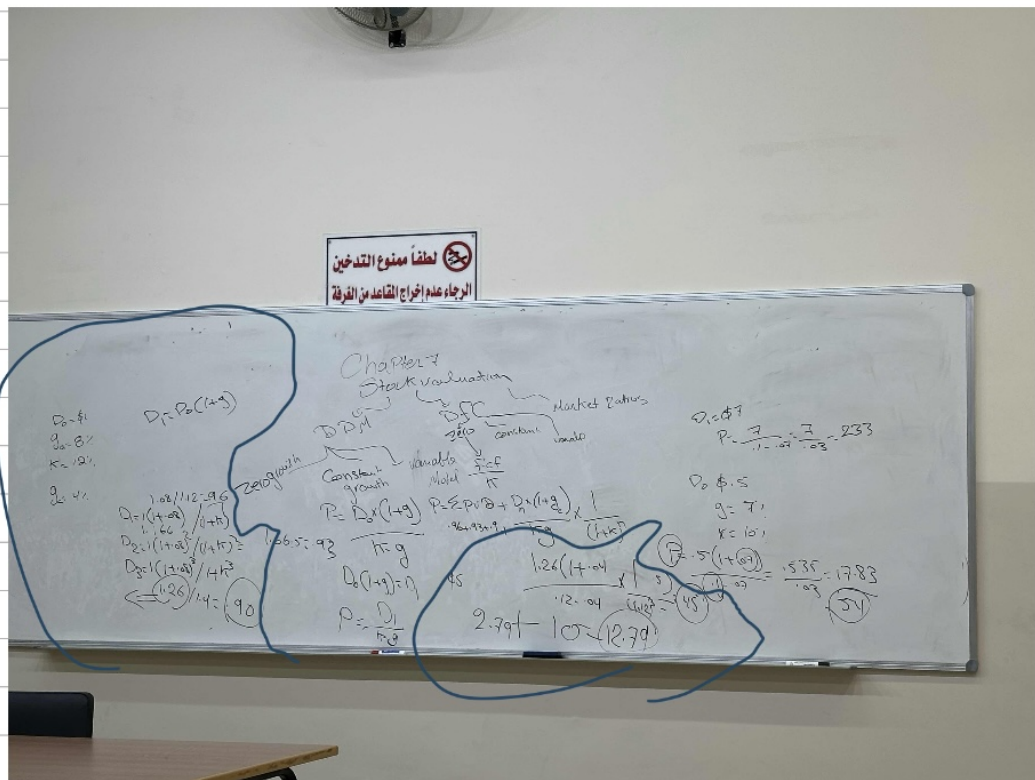
$$P = \frac{3 \times (1.05)}{.12 - .05} = 45$$



$$P = \sum PVD + \frac{(D_n \times (1+g))}{K-g} \times \frac{1}{(1+K)^n} \rightarrow 2 \text{ growth عند } n$$

D_n : Dividend n \rightarrow

Future Value

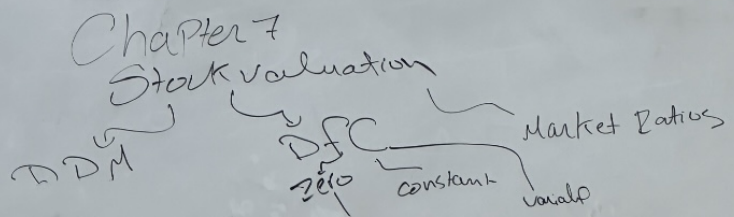


Find Free Cash Flow?

$$\begin{array}{l} 1 \quad fcf \\ 1 \quad 10,000,000 \quad (1+0.17)^1 = 8,547,008 \\ 2 \quad 20,000,000 \quad (1.17)^2 = 14,610,271 \\ 3 \quad 30,000,000 \quad (1.17)^3 = 18,731,116 \end{array} \quad \left. \begin{array}{l} \text{step 1} \\ \rightarrow \Sigma \end{array} \right\}$$

$$g = 10\%$$

$$r = 17\%$$



step 3

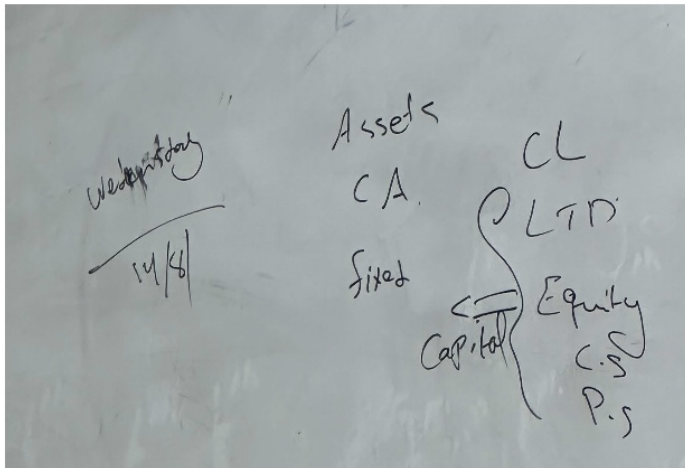
Σ

$$+ 30,000,000 \left(\frac{1}{1.17 \cdot 1} \right) \times \left(\frac{1}{(1.17)^3} \right)$$

Final result = $\boxed{336,237,504}$ \rightarrow Value of the firm
 stock 23

Common Stocks

$$CS = \text{Value of the firm} - MV \text{ of the Bond} - MV \text{ of PS}$$



$$P = \frac{D_0}{K} \rightarrow \text{cost P.S.}$$

$$K \times P = \frac{D_0}{P}$$

$$K = \frac{D_0}{P}$$

$$P = \frac{D_1}{K - g}$$

$$\frac{P \times (K - g)}{P} = \frac{D_1}{P}$$

$$K - g = \frac{D_1}{P}$$

$$K = \frac{D_1}{P} + g$$

$$\text{Bond} \rightarrow \text{YTM} = \frac{\text{PMT} + \left(\frac{\text{Face Value} - \text{MV}}{\text{of Maturities}} \right)}{\left(\frac{\text{Face Value} + \text{MV}}{2} \right)}$$

replace MV with net proceeds

* Net proceeds = MV - Flotation Amount

* Flotation amount = Flotation Cost X Face Value

after finding net proceed

$$YTM = \frac{PMT + \left(\frac{\text{Face Value} - NP}{\text{of Maturities}} \right)}{\left(\frac{\text{Face Value} + NP}{2} \right)} \times (1 - \text{tax})$$

NP: Net proceeds.

إذا بيعتونا بـ 100 : بفوق 100 \$

• Cost P.S = $K = \frac{D_0}{P} \rightarrow \left(K = \frac{D_0}{NP} \right)$

NP : $\frac{\text{المبلغ الذي سترد في قسيمة من 100}}{\text{أعلى قيمة}}$

↓
Come from → 1. Plotation
2. Under Valuation

over Valuation → replace the (-) with (+)

Cost of C.S

1. $\frac{D_1}{NP} + g$

2. $K = RF + \text{Beta (Premium)}$
 $= RF + B (MR - RF)$

* Internal ($\frac{\text{المبلغ الذي سترد في قسيمة من 100}}{\text{أعلى قيمة}}$)
There is no NP
There is Price

Cost of R.E = $\frac{D_1}{P} + g$

Ex : Face Value 1000\$
 Coupon Rate 5% → PMT = 50
 Price (Premium) 1200\$
 Flotation Cost 3%
 Maturity 30
 Tax rate 40%
 Interest Semi annually → $\frac{50}{2} \rightarrow 25 = PMT$
 YTM? Y Maturity = 30 × 2

* Net proceeds = MV - Flotation Amount

* Flotation amount = Flotation Cost × Face Value

$$\text{Flotation Cost} = 3\% \times 1000 = 30$$

$$\text{Net proceeds} = 1200 - 30 = \underline{1170}$$

$$YTM = \frac{PMT + \left(\frac{\text{Face Value} - NP}{\text{of Maturities}} \right)}{\left(\frac{\text{Face Value} + NP}{2} \right)} \times (1 - \text{tax})$$

$$= \frac{25 + \left(\frac{1000 - 1170}{30} \right)}{\left(\frac{1000 + 1170}{2} \right)} \times (1 - .4)$$

$$\frac{25 + (-2.8)}{(1085)} \times .6 = \underline{1.23\%}$$

↓

برجع لجزية ب 2 لانو Semi annual

Handwritten calculation for YTM:

$$YTM = \frac{\left(\frac{50}{2} + \frac{1000 - 1170}{30 \times 2} \right)}{\left(\frac{1000 + 1170}{2} \right)} \times (1 - .4) \times 2$$

net proceeds: 1200 - 30 = 1170
 Flotation = 1000 × 3% = 30

حل الدکتویہ السؤال →

Preferred stock $d = 5\%$
 par value 100\$
 Undervalued by 5\$ for par
 flotation cost 2%
 What is price of P.S

$$K_{PS} = \frac{D}{P} \rightarrow \frac{5}{93} = 5.38\%$$

$$100 - 5 = 95$$

$$NP = 100 - 5 - 2 = 93$$

Common Stock Price = 10\$ flotation 2\$ $NP = 10 - 2 = 8$

$$CS = \frac{D_1}{NP} + g$$

معنى تسمى بحقوق الملكية العادية

$$= \frac{3}{8} + 29.41\%$$

$$= 67\% \text{ Cost of Common stock}$$

if its internal $\rightarrow NP = \text{Price without flotation}$
 $10 + 29.41\%$

$$\begin{aligned} 1 & C D_1 3 \\ 2 & C D_2 5 \\ 3 & C D_3 2 \\ & D_4 65 \end{aligned}$$

$$g = \left(\frac{6.5}{3} \right)^{\frac{1}{3}} = 29.41\%$$

Weighted Average Cost of Capital

$$WACC = (W_{bond} \times YTM) + (W_{PS} \times \text{Cost PS}) + (W_{CS} \times \text{Cost CS})$$

Two ways to find weight [I] MV way

$$WACC = W_B \times YTM + W_{PS} \times \text{Cost PS} + W_{CS} \times \text{Cost CS}$$

Item	MP	Value	Weight	Cost
Bond	500	1200	600,000	76%
CS	10,000	\$10	100,000	12.6%
P.S	3,000	\$30	90,000	11.4%
Total			790,000	

$76\% \times 2.28 + 11.4\% \times 9.9 + 12.6\% \times 67\%$
 $\frac{600,000}{790,000} = 76\%$
 $\frac{100,000}{790,000} = 12.6\%$
 $\frac{90,000}{790,000} = 11.4\%$

$D_1 3$
 $D_2 5$
 $D_3 2$
 $D_4 65$

21 Book Value

نسبة المديونية إلى إجمالي ممتلكات

Chapter 9
Cost of Capital

$$WACC = W_B \times r_B + W_{P.S.} \times \text{Cost } P.S. + W_{C.S.} \times \text{Cost } C.S.$$

$$76\% \times 2.28\% + 11.4\% \times 9\% + 12.6\% \times 6.7\%$$

Cost	Value	Weight	Weighted Cost
Bond	500	1000	500,000
C.S.	10,000	5	50,000
P.S.	3,000	10	30,000
Total			580,000

$$\frac{500,000}{790,000} = 76\%$$

$$\frac{100,000}{790,000} = 12.6\%$$

$$\frac{30,000}{790,000} = 11.4\%$$

$$g = \frac{6.5}{3} = 2.17$$

$$g = \left(\frac{6.5}{3} \right)^{\frac{1}{3}} - 1 = 2.17\%$$

11 Aug 2024

Bond Coupon rate = 12%
Semi annually
Maturity 10 years
discount 30\$
 flotation cost 10\$
tax rate 30% 300 Bond
Cost Bond?

P.S	C.S
D 2\$	RF = 3%
Value 95\$	B = 1.2
flotation cost 5%	MR = 14%
Par Value 100\$	Par value = 10\$
# of stocks = 5 000	# of stocks = 20 000

Find weighted Average Cost of Capital

→ common stock

risk free = 3%

Beta = 1,2

MR = 14%

par value = 10

20,000 common stock

what WACC?

Bond:- $NP = 1000 - 30 - 10 = 960$

$$YTM = 1000 \times 0,06 + \left(\frac{1000 - 960}{20} \right) \times (1 - 30\%) = 0,0885$$
$$\left(\frac{1000 - 960}{20} \right)$$

$$WB = 300 \times 1000 = 300,000 / 1,000,000 = 0,3$$

preferred stock $NP = 95 - (0,05 \times 100) = 90$

$$\text{cost p.s} = \frac{D}{NP} = \frac{5}{90} = 0,0222$$

$$WP.S = \frac{500,000}{1,000,000} = 0,5$$

common stock

$$\text{cost c.s} = R = RF + \text{Beta} (MR - RF)$$

$$= 3\% + 1,2 (14\% - 3\%) = 0,162$$

$$WC.S = 20,000 \times 10 = 200,000 / 1,000,000 = 0,2$$

$$WACC = (0,3 \times 0,0885) + (0,5 \times 0,0222) + (0,2 \times 0,162) = 0,07$$

P9-19

LG 3 LG 4
LG 5 LG 6

P9-19 Calculation of individual costs and WACC Lang Enterprises is interested in measuring its overall cost of capital. Current investigation has gathered the following data. The firm is in the 40% tax bracket.

Debt The firm can raise debt by selling \$1,000-par-value, 8% coupon interest rate, 20-year bonds on which quarter interest payments will be made. To sell the issue, an average discount of \$30 per bond would have to be given. The firm also must pay flotation costs of \$30 per bond.

Preferred stock The firm can sell 8% preferred stock at its \$95-per-share par value. The cost of issuing and selling the preferred stock is expected to be \$5 per share. Preferred stock can be sold under these terms.

Common stock The firm's common stock is currently selling for \$90 per share. The firm expects to pay cash dividends of \$7 per share next year. The firm's dividends have been growing at an annual rate of 6%, and this growth is expected to continue into the future. The stock must be underpriced by \$7 per share, and flotation costs are expected to amount to \$5 per share. The firm can sell new common stock under these terms.

Retained earnings When measuring this cost, the firm does not concern itself with the tax bracket or brokerage fees of owners. It expects to have available

Interest quarterly
Find interest YTM after/before tax

CHAPTER 9 The Cost of Capital 435

\$100,000 of retained earnings in the coming year; once these retained earnings are exhausted, the firm will use new common stock as the form of common stock equity financing.

- Calculate the after-tax cost of debt.
- Calculate the cost of preferred stock.
- Calculate the cost of common stock.
- Calculate the firm's weighted average cost of capital using the capital structure weights shown in the following table. (Round answer to the nearest 0.1%.)

$\text{Tax } 21\%$
 $\text{Coupon Payment } \frac{80}{4} = 20$
 $\text{Years } 20 \times 4 = 80$
 $1000 - 30 - 30 = 940 \rightarrow NP$
 $YTM = 20 + \frac{1000 - 940}{80} = 20.75$
 $\frac{1940}{2} = 970$
 $\frac{970}{940} = 1.0319$
 $1.0319^{80} = 8.56$
 $8.56 \times 20 = 171.2$
 $171.2 \times (1 - 0.21) = 134.1$
 $134.1 / 1000 = 13.41\%$
 $CD = 8\%$
 $8\% \times 100 = 8$
 $CP = \frac{8}{95.5} = \frac{8}{10} = 8.4\%$
 $CS = \frac{7}{90} + 6\% = 13.7\%$
 $\frac{7}{90} + 6\% = 13.7\%$
 Cost R.E.
 $6.76 \times 90\% + 20.1 \times 8\% + 5.2 \times 15\%$

Source of capital	Weight
Long-term debt	35%
Preferred stock	12
Common stock equity	53

The tax rate of the firm is currently 40%. The needed financial information and data are as follows:

Debt Nova can raise debt by selling \$1,000-par-value, 6.5% coupon interest rate, 10-year bonds on which annual interest payments will be made. To sell the issue, an average discount of \$20 per bond needs to be given. There is an associated flotation cost of 2% of par value.

Preferred stock Preferred stock can be sold under the following terms: The security has a par value of \$100 per share, the annual dividend rate is 6% of the par value, and the flotation cost is expected to be \$4 per share. The preferred stock is expected to sell for \$102 before cost considerations.

Common stock The current price of Nova's common stock is \$35 per share. The cash dividend is expected to be \$3.25 per share next year. The firm's dividends have grown at an annual rate of 5%, and it is expected that the dividend will continue at this rate for the foreseeable future. The flotation costs are expected to be approximately \$2 per share. Nova can sell new common stock under these terms.

Retained earnings The firm expects to have available \$100,000 of retained earnings in the coming year. Once these retained earnings are exhausted, the firm will use new common stock as the form of common stock equity financing. (Note: When measuring this cost, the firm does not concern itself with the tax bracket or brokerage fees of owners.)

TO DO

Create a spreadsheet to answer the following questions:

- Calculate the after-tax cost of debt.
- Calculate the cost of preferred stock.
- Calculate the cost of retained earnings.
- Calculate the cost of new common stock.
- Calculate the firm's weighted average cost of capital using retained earnings and the capital structure weights shown in the table above.
- Calculate the firm's weighted average cost of capital using new common stock and the capital structure weights shown in the table above.

Preferred

Handwritten calculations on a piece of paper:

- Left side notes:
 - sell 35%
 - P.S 12%
 - C.S 53%
 - Tax 21% Cou
 - Coupon 6.5%
 - Bond 10y
 - Discounted by 20 = 1000 - 20 = 980
 - Flotation 2%
- Center calculation for after-tax cost of debt:

$$YTM = \frac{65 + \frac{1000 - 960}{10}}{\frac{1960}{2}} = 0.0704$$
- Right side calculation for WACC:

$$6.76\% \times 35\% + 20\% \times 6.9\% + 50\% \times$$

فانچس قوانین chapter 8

$$* \% R = \frac{(\text{Selling Price} - \text{Purchase Price}) + \text{Yield}}{\text{Purchase Price}}$$

$$* \text{Avr}(\bar{R}) = \frac{\sum R}{n}$$

no Prob, equal prob

$$* \text{Avr}(\bar{R}) = \sum r \times \text{Prob}$$

there is Prob.

$$* \text{Sd (standard deviation)} = \sqrt{\text{Variance}} = \sqrt{(r - \bar{r})^2 \times \text{Prob}} \quad \text{there is Prob}$$

- σ^2 : Variance

- σ : standard deviation

$$* \text{Sd} = \sqrt{\frac{\sum (r - \bar{r})^2}{n-1}}$$

no Prob, equal Prob

$$* \text{Coefficient of Variation} = \frac{\text{Sd}}{\text{Avr}} \left(\frac{\sigma}{\bar{r}} \right)$$

$$* \text{Covariance} = \frac{\sum (r - \bar{r}_a) \times (r - \bar{r}_b)}{n-1}$$

no prob, equal Prob.

type of relation

$$* \text{Covariance} = \sum (r - \bar{r}_a) \times (r - \bar{r}_b) \times \text{prob}$$

there is Prob.

$$* \text{Correlation} = \frac{\text{Covariance}}{\text{Sd}_a \times \text{Sd}_b}$$

strength of relation

- $W_p = 100\%$ always

$$* R_p = \sum r \times W \rightarrow \text{return}_p = (w_a \bar{r}_a) + (w_b \bar{r}_b) + \dots + (w_n \bar{r}_n)$$

$$\sigma_p = \sqrt{w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2w_a w_b \text{Cov}}$$

↓
* Cov = correlation $\sigma_a \sigma_b$

6 % Variances 1.900 % to 10

* Total risk = Systematic + Unsystematic.
 Market. Unique (Firm risk).
 undiversifiable. diversifiable
 non Controllable. Controllable.

$$* \text{CAPM} = R_F + \text{Beta} \frac{(\text{MR} - \text{MF})}{\text{Premium}}$$

MR - MF = Risk Premium.

MR: Market return

MF: Market free

RF: Risk free rate (rate on treasury bills.)

$$* \text{Beta} = \frac{\text{Cov}}{\text{Var}}$$

- Beta RF = 0

- Beta Market = 1

Yield to Maturity (YTM):

- Yield to Maturity $\begin{cases} < \end{cases}$ Coupon rate \rightarrow Bond Premium \rightarrow Price > 1000
- YTM $\begin{cases} = \end{cases}$ Coupon rate \rightarrow Bond Discount \rightarrow Price < 1000
- YTM $\begin{cases} = \end{cases}$ Coupon rate \rightarrow Face Value $= 1000$

Same meanings:

- Interest rate : required rate of return : Cost of Money
- Nominal interest rate : Actual interest rate
- Coupon rate : interest
- Market (i) : Yield to Maturity Bond Price قانون
- Price : MV YTM قانون
- Coupon Bond : PMT
- YTM : Priced to Yield.

Chapter (6)

ماكين القوانين

$$* \text{Real Interest Rate} = \left(\frac{(1 + \text{nominal rate})}{(1 + \text{inflation})} \right) - 1$$

nominal rate \rightarrow Actual rate

$$\text{Coupon Payment} = \frac{\text{PMT}}{\text{Coupon rate}} \times \text{Face value}$$

usually 1000 for the Bond

$$* \text{Bond Price} = \frac{\text{PMT} \times \left(1 - \left(\frac{1}{(1+i)^n} \right) \right)}{i} + \frac{1000}{(1+i)^n}$$

-when it Semi annual $\rightarrow \left(\frac{\text{PMT}}{2} \right), \left(\frac{i}{2} \right), (n \times 2)$.

-when it quarterly $\rightarrow \left(\frac{\text{PMT}}{4} \right), \left(\frac{i}{4} \right), (n \times 4)$.

$$\text{YTM} = \frac{\left(\text{PMT} + \left(\frac{\text{Face value} - \text{Market value}}{n} \right) \right)}{\left(\frac{\text{Face value} + \text{Market value}}{2} \right)}$$

n : number of Maturity

MV : Bond Price

-when it Semi annual $\rightarrow \left(\frac{\text{PMT}}{2} \right), \left(\frac{\# \text{ of Maturity}}{2} \right)$ also the $\left(\frac{\text{final result}}{2} \right)$

-when it quarterly $\rightarrow \left(\frac{\text{PMT}}{4} \right), \left(\frac{\# \text{ of Maturity}}{4} \right)$ & the $\left(\frac{\text{final result}}{4} \right)$

$$* \text{Current Yield} = \frac{\text{Coupon Payment}}{\text{Bond Price}}$$

h 7

تکلیف: قوانین

* Out-Standing = Issued - Treasury Stocks

Preferred Stock

$$P = \frac{D}{K}$$

P = Price K : cost of P.S , required rate of return

$$K = RF + B (MR - RF)$$

Perpetuity : discount rate forever.

Common Stock Valuation

DDM :

• Zero growth rate $P = \frac{D_0}{K}$
Price Discount rate

• Constant growth

$$P = \frac{D_1}{(K-g)}$$

g : growth

$$D_1 = D_0 \times (1+g)$$

$$P = \frac{(D_0 \times (1+g))}{(K-g)}$$

The higher the g → the higher the P.

The higher the k → the lower the P.

• Variable Model

2 growths

$$P = \sum P_v D + \left(\frac{(D_n \times (1+g_c))}{K-g} \times \frac{1}{(1+K)^n} \right)$$

Value of the firm

$$PVD = \frac{D_n}{(1+K)^n}$$

• Price of stocks = $\frac{\text{Value of the firm}}{\text{number of stocks}}$

• Price of C.S = Value of the firm - MV(Bond) - MV(PS)

$D_1 = D_0 (1+g)$ / first way
 $D_2 = D_1 (1+g)$ / way
 $D_3 = D_2 (1+g)$
 or
 $D_1 = D_0 (1+g)^1$
 $D_2 = D_0 (1+g)^2$ / sec way
 $D_3 = D_0 (1+g)^3$

DFC:

Dividend لا يتوزع
و لا يتغير

1. Zero growth

$$\frac{FCF}{k} \rightarrow \frac{\text{Free Cash Flow}}{\text{Discount rate}}$$

2. Constant

$$\text{Free Cash Flow} = \text{Operating cash Flow} - \text{Investment Capital Expense.}$$

Book Value (Historical Cost) القيمة التاريخية

$$\text{Market ratio} = \frac{\text{Price}}{\text{Book Value}}$$

$$\text{Book Value of the firm} = \text{Total Assets} - \text{total liabilities} \rightarrow \text{Book Value} = \text{equity}$$

$$\text{Earning Per share} = \frac{(\text{net Income} - \text{Dividends PS})}{\# \text{ of shares}}$$

$$\text{Liquidity Value (MV)} = \text{Market Value of total Assets} - \text{MV of total liabilities}$$

القيمة السائلة

$$\frac{\text{Price Per share}}{\text{BV Per share}} \rightarrow \text{Industry} \text{ أو (التأجير)}$$

$$\frac{\text{Price Per share}}{\text{EPS}} \rightarrow \text{PE ration}$$

$$\frac{\text{Price Per share}}{\text{Liquidation Value Per share}}$$

How to Calculate Growth

(with Constant/Variable)

$$\textcircled{1} G = 1 - \frac{D}{E} \times \text{ROE}$$

$$G = \text{retention ratio} \times \text{ROE}$$

$$\text{retention ratio} = 1 - \text{payout ratio}$$

$$\text{payout ratio} = \frac{D}{E} \rightarrow \text{earning}$$

$$\textcircled{2} \left(\frac{\text{Ending } D}{\text{Beginning } D} \right)^{\frac{1}{n}} - 1$$

"Chapter 9"

* Bond $\rightarrow YTM = \frac{PMT + \left(\frac{\text{Face} - NP}{\text{number of Maturity}} \right)}{\left(\frac{\text{Face Value} + NP}{2} \right)} \times (1 - tax)$

* Cost P.S $K = \frac{D_0}{NP}$

* Cost of C.S $K = \frac{D_1}{NP} + g$

• $NP = MV - \text{Flotation amount}$

• $\text{Flotation amount} = \text{Flotation Cost} \times \text{Face}$

$K = RF + \text{Beta} (MR - RF)$ over valuation $\rightarrow +$ under valuation $\rightarrow -$

* Cost of RE $= \frac{D_1}{P} + g$ (C.S) الشقة أمست أسهم كالتالي
ما نستطيع جدا في P من NP (Internal)

• $WACC = (YTM \times w_{\text{bond}}) + (\text{Cost P.S} \times w_{\text{PS}}) + (\text{Cost}_{\text{CS}} \times w_{\text{CS}})$

$w_{\text{bond}} + w_{\text{CS}} + w_{\text{PS}} = 1$ or 100%

, Bond \rightarrow Debt

• C.S, PS \rightarrow Equity

Ch 10

1] Payback period

كم الفترة لي تسترد فلوسك بعد ما
تقبل بي بتجيب المصاري اشغ

2] Discount payback period

$$= \frac{\text{Investment}}{(1+k)^n}$$

3] Discount operation CF = Σ Discount Payback Period

4] $NPV = - \text{Initial Investment} + \text{discount operation CF}$
↓
net Present value

5] $PJ = \frac{\text{discount operation CF}}{\text{Initial Investment}} = \frac{\Sigma \text{Discount payback}}{\text{Initial Investment}}$
Profitability index

* NPV (-) → reject Project

* NPV (+) → Accept , take higher value.

$PJ > 1$ → Accept , take higher value.